Name	Anand Tiwari
UID no.	2021700068
Experiment No.	5

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AIM:
                   Dynamic Programming - Matrix Chain Multiplication
                                          Program
                   Apply the concept of dynamic programming to solve the problem of
PROBLEM
STATEMENT:
                   finding the minimum cost i.e. multiplications required to perform Matrix
                   Chain Multiplications
PROGRAMME
                   #include inits.h>
                   #include <stdio.h>
                   #include <stdlib.h>
                   #include <string.h>
                   void print parentheses(int s[][5], int i, int j)
                   if (i == j)
                   printf("A%d", i);
                   return;
                   printf("(");
                   print parentheses(s, i, s[i][j]);
                   print_parentheses(s, s[i][j] + 1, j);
                   printf(")");
                   int matrixmin(int p[], int n)
                   int m[n][n];
                   int s[n][n];
                   memset(m, 0, sizeof(m[0][0]) * n * n);
                   int i, j, k, L, q;
                   for (L = 2; L < n; L++)
                   for (i = 1; i < n - L + 1; i++)
                   j = i + L - 1;
                   m[i][j] = INT MAX;
                   for (k = i; k \le j - 1; k++)
                   q = m[i][k] + m[k + 1][j] + p[i - 1] * p[k] * p[j];
                   if (q < m[i][j])
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m[i][j] = q;
s[i][j] = k;
printf("m Table:\n");
for (int i = 1; i < n; i++)
printf("\t%d", i);
printf("\n\n");
for (i = 1; i < n; i++)
for (j = 1; j < n; j++)
if (j == 1)
printf("%d", i);
printf("\t%d", m[i][j]);
printf("\n\n");
printf("s Table:\n");
for (i = 1; i < n - 1; i++)
for (j = 2; j < n; j++)
if (i \le j)
printf("%d ", s[i][j]);
else
printf(" ");
printf("\n");
printf("Multiplication Order: ");
print_parentheses(s, 1, n - 1);
printf("\n");
return m[1][n - 1];
int main()
printf("Length of matix chain: ");
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int n;
scanf("%d", &n);
int arr[n];
printf("Dimensions of the matrices: ");
for (int i = 0; i < n; i++)
{
    scanf("%d", &arr[i]);
}
printf("min cost is %d\n", matrixmin(arr, n));
return 0;
}</pre>
```

Matrix Chain Multiplication can be solved using dynamic programming. Theory: We can define the minimum number of scalar multiplications needed to iteratively compute the product of a chain of matrices. We start with sub chains of length 1 and then compute the minimum cost for sub chains of increasing length until we have the minimum cost for the entire chain. The time complexity of this algorithm is $O(n^3)$, where n is the number of matrices in the chain. Algorithm: 1. Define the subproblem: Find the minimum number of scalar multiplications needed to compute the product of a chain of matrices. 2. Find the recurrence relation: Let M[i,j] be the minimum number of scalar multiplications needed to compute the product of the chain of matrices from matrix i to matrix j. We can define M[i,j] recursively as follows: M[i,j] = min(M[i,k] + min(M[i,k])) $M[k+1,j] + a[i-1] \times a[k] \times a[j]$ for $i \le k < j$ 3. Initialize the base case: M[i,i] = 0 for $1 \le i \le j$ n, where n is the number of matrices in the chain. 4. Solve the subproblems: Compute the minimum cost for subchains of increasing length until we have the minimum cost for the entire chain. 5. Return the final answer: The minimum cost for the entire chain is stored in M[1,n], where n is the number of matrices in the chain.

CONCLUSION: | Major | State |