# UNIT 3

## Formal Languages:

## 1. Derivations and the Language Generated by a Grammar:

o A derivation is a sequence of production rules applied to generate a string in a language. The language generated by a grammar is the set of all strings derivable from the start symbol.

#### 2. Definition of a Grammar:

- o A grammar is a formal set of rules used to define the structure of a language, consisting of:
  - A set of non-terminal symbols (e.g., NNN)
  - A set of terminal symbols (e.g., TTT)
  - A set of production rules (e.g.,  $A \rightarrow BCA \setminus BCA \rightarrow BC$ )
  - A start symbol (e.g., SSS)

### 3. Chomsky Classification of Languages:

- o Type 0 (Recursively Enumerable Languages): Can be recognized by a Turing machine.
- o Type 1 (Context-Sensitive Languages): Can be recognized by a linear-bounded automaton.
- o Type 2 (Context-Free Languages): Can be recognized by a pushdown automaton.
- o Type 3 (Regular Languages): Can be recognized by a finite automaton.

## 4. Languages and their Relation:

The hierarchy shows the inclusion of languages from Type 3 (regular) to Type 0 (recursively enumerable), where every regular language is context-free, every context-free language is context-sensitive, and every context-sensitive language is recursively enumerable.

#### 5. Recursive and Recursively Enumerable Sets:

- Recursive Set: A set for which a decision procedure exists (algorithm to determine membership).
- o **Recursively Enumerable Set**: A set where a Turing machine can enumerate its elements but might not halt for non-members.

#### 6. Languages and Automata:

- o **Automata** are abstract machines used to recognize languages, where:
  - Finite automata recognize regular languages.
  - Pushdown automata recognize context-free languages.
  - Turing machines recognize recursively enumerable languages.

#### 7. Chomsky Hierarchy of Languages:

o Defines a classification of formal languages based on generative power, from regular languages (simplest) to recursively enumerable languages (most powerful).

## **Regular Grammars:**

#### 1. Regular Sets and Regular Grammars:

- o A **regular set** is a set of strings that can be expressed by a regular expression or recognized by a finite automaton.
- o A **regular grammar** is a context-free grammar where the production rules are restricted to right-linear or left-linear form.

## 2. Converting Regular Expressions to Regular Grammars:

o A regular expression can be converted into an equivalent regular grammar using rules based on the structure of the expression (e.g., concatenation, union, and Kleene star).

## 3. Converting Regular Grammars to Regular Expressions:

o A regular grammar can be converted into an equivalent regular expression by applying the reverse process of grammar construction.

## 4. Left Linear and Right Linear Regular Grammars:

- o **Left Linear Grammar**: All production rules are of the form  $A \rightarrow xBA$  \rightarrow  $xBA \rightarrow xB$  or  $A \rightarrow xA$  \rightarrow  $xA \rightarrow x$ , where xxx is a string of terminals and BBB is a non-terminal.
- o **Right Linear Grammar**: All production rules are of the form  $A \rightarrow BxA$  \rightarrow  $BxA \rightarrow Bx$  or  $A \rightarrow xA$  \rightarrow  $xA \rightarrow x$ , where xxx is a string of terminals and BBB is a non-terminal.

## **Important MCQ**

### 1. Which of the following is true about a grammar?

- a) A grammar defines only regular languages
- b) A grammar defines only context-free languages
- c) A grammar defines the structure of a language
- d) A grammar is the same as a regular expression **Answer:** C

## 2. Which of the following is a Type 3 language in the Chomsky hierarchy?

- a) Context-free language
- b) Regular language
- c) Context-sensitive language
- d) Recursively enumerable language **Answer: B**

#### 3. Which automaton is used to recognize regular languages?

- a) Pushdown automaton
- b) Turing machine
- c) Finite automaton
- d) Linear-bounded automaton **Answer:** C

## 4. A context-sensitive language can be recognized by which of the following?

- a) Pushdown automaton
- b) Turing machine
- c) Finite automaton
- d) Linear-bounded automaton

**Answer: D** 

# 5. Which of the following is a valid production rule in a regular grammar?

- a) A→aBA \rightarrow aBA→aB
- b) A→BaA \rightarrow BaA→Ba
- c) A→aBbA \rightarrow aBbA→aBb
- d) A→ABA \rightarrow ABA→AB
  Answer: A

## 6. The language recognized by a Turing machine is:

- a) Context-sensitive
- b) Regular
- c) Context-free
- d) Recursively enumerable

Answer: D

## 7. Which of the following is not a property of regular languages?

- a) They can be recognized by a finite automaton
- b) They can be expressed by regular expressions
- c) They can be recognized by a pushdown automaton
- d) They can be described by regular grammars **Answer:** C

## 8. What is the Chomsky type of the language $L=\{anbn|n\geq 1\}L=\{a^n b^n | n \geq 1\}L=\{anbn|n\geq 1\}$ ?

- a) Type 0
- b) Type 1
- c) Type 2
- d) Type 3

**Answer: C** 

#### 9. Which of the following languages is context-free?

- a)  $\{anbncn|n\geq 1\}\setminus \{a^n b^n c^n | n \geq 1 \setminus \{anbncn|n\geq 1\}$
- b)  $\{anbm|n,m\geq 1\}\setminus \{a^n b^m \mid n, m \geq 1\} \{anbm|n,m\geq 1\}$
- c)  $\{anbn|n\geq 1\}\setminus \{a^n b^n \mid n \neq 1 \} \{anbn|n\geq 1\}$
- d) {anbncn|n≥1}\{ a^n b^n c^n | n \geq 1 \} {anbncn|n≥1}
   Answer: C

#### 10. Which of the following is true about left-linear and right-linear grammars?

- a) Both types generate regular languages
- b) Left-linear grammars generate context-free languages
- c) Right-linear grammars generate context-sensitive languages
- d) Left-linear grammars generate context-sensitive languages **Answer: A**

# 11. Which of the following is a valid regular expression for the language of all strings over the alphabet $\{a,b\}\setminus\{a,b\}$ that contain at least one aaa?

- a) b\*a(b\*a)\*b^\*a(b^\*a)^\*b\*a(b\*a)\*
- b) a\*b\*a^\*b^\*a\*b\*
- c)  $(a|b)*a(a|b)^*a(a|b)*a$
- d) a\*b\*a^\*b^\*a\*b\*

**Answer: C** 

# 12. Which type of automaton recognizes context-free languages?

- a) Finite automaton
- b) Pushdown automaton
- c) Turing machine
- d) Linear-bounded automaton

Answer: B

# 13. The production rule $S \rightarrow aSb|\epsilon S \cdot b|\epsilon S \rightarrow aSb|\epsilon S$

- a) Context-free grammar
- b) Regular grammar
- c) Context-sensitive grammar
- d) Recursive grammar

Answer: A

# 14. Which of the following is not a characteristic of regular expressions?

- a) They can represent all regular languages
- b) They can be converted into finite automata
- c) They can describe context-free languages
- d) They are used to describe regular sets

**Answer: C** 

## 15. Which of the following is an example of a left-linear grammar?

- a) A→aBA \rightarrow aBA→aB
- b) A→BcA \rightarrow BcA→Bc
- c) A→aBbA \rightarrow aBbA→aBb
- d)  $A \rightarrow ABA \land rightarrow ABA \rightarrow AB$

Answer: A

## 16. Which type of language is the set $\{anbn|n\geq 1\}\setminus \{a^n b^n \mid n \geq 1\} \{anbn|n\geq 1\}$ ?

- a) Regular
- b) Context-free
- c) Context-sensitive
- d) Recursively enumerable

**Answer: B** 

## 17. What is the language of the regular expression $(a|b)*(a|b)^*(a|b)*?$

- a) The set of all strings containing at least one aaa or bbb
- b) The set of all strings containing only aaa or bbb
- c) The set of all strings starting with aaa or bbb
- d) The set of all strings containing zero or more aaa's and bbb's
   Answer: D

## 18. What does the Kleene star in a regular expression represent?

- a) Zero or more repetitions of the preceding symbol
- b) One or more repetitions of the preceding symbol
- c) A choice between two options
- d) Concatenation of two symbols

Answer: A

# 19. Which of the following is the correct conversion of the regular expression $(a|b)*(a|b)^**(a|b)*$ to a regular grammar?

- a)  $S \rightarrow aS|bS| \in S \cdot rightarrow aS \mid bS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid bS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid bS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid bS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid bS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS \mid epsilonS \rightarrow aS|bS| \in S \cdot rightarrow aS|bS| \in S \cdot rightarrow aS|bS| = epsilonS \rightarrow aS|bS| = epsilonS|bS| = epsilonS|bS|$
- b) S→aS|bSS \rightarrow aS | bSS→aS|bS
- c) S→Sa|SbS \rightarrow Sa | SbS→Sa|Sb
- d) S→a|bS \rightarrow a | bS→a|b

Answer: A

## 20. A Turing machine can recognize which type of language?

- a) Type 1
- b) Type 2
- c) Type 3
- d) Type 0

Answer: D

## 21. Which of the following is true about a recursive set?

- a) It can be decided algorithmically
- b) It can be recognized by a finite automaton
- c) It can be recognized by a Turing machine that does not halt
- d) It can only be enumerated by a Turing machine **Answer: A**

## 22. Which of the following is not a regular grammar?

- a) A→aBA \rightarrow aBA→aB
- b) A→BaA \rightarrow BaA→Ba
- c) A→aBbA \rightarrow aBbA→aBb
- d) A→aB|bA \rightarrow aB | bA→aB|b Answer: C

## 23. Which of the following is a characteristic of a recursively enumerable set?

- a) It can be recognized by a finite automaton
- b) It can be decided algorithmically
- c) It can be enumerated by a Turing machine but may not halt
- d) It is always a context-sensitive set **Answer:** C

#### 24. Which of the following is an example of a right-linear grammar?

- a) A→aBA \rightarrow aBA→aB
- b)  $A \rightarrow BcA \land BcA \rightarrow Bc$
- c)  $A \rightarrow aB | \epsilon A \setminus aB | \epsilon A \rightarrow aB | \epsilon$
- d) A→bAA \rightarrow bAA→bA
   Answer: A

25. What is the Chomsky type of the language L={anbm| $n\neq m$ }L = \{ a^n b^m | n \neq m \}L={anbm| $n\square=m$ }?

- a) Type 0
- b) Type 1
- c) Type 2
- d) Type 3

Answer: A

## 26. Which of the following languages is regular?

- a)  $\{anbn|n\geq 1\}\setminus \{a^n b^n \mid n \geq 1\} \{anbn|n\geq 1\}$
- b)  $\{anbm|n\neq m\}\setminus \{a^n b^m \mid n \neq m \setminus \{anbm|n = m\}$
- c)  $\{anbm|n,m\geq 1\}\setminus \{a^n b^m \mid n, m \geq 1\} \{anbm|n,m\geq 1\}$
- d) {anbncn|n≥1}\{ a^n b^n c^n | n \geq 1 \} {anbncn|n≥1}
   Answer: C

## 27. Which of the following statements is true about regular languages?

- a) They are always context-sensitive
- b) They can be recognized by a finite automaton
- c) They can be described by context-free grammars
- d) They cannot be described by regular expressions
   Answer: B

# 28. What is the regular expression for the language of all strings over $\{a,b\}\setminus\{a,b\setminus\}\{a,b\}$ that end with aaa?

- a)  $(a|b)*a(a|b)^*a(a|b)*a$
- b)  $a*(a|b)*a^*(a|b)^*a*(a|b)*$
- c) a\*b\*aa^\*b^\*aa\*b\*a
- d)  $(a|b)+a(a|b)^++a(a|b)+a$

Answer: A

# 29. What is the primary difference between regular languages and context-free languages?

- a) Regular languages can be recognized by finite automata, while context-free languages require a pushdown automaton
- b) Context-free languages are more complex than regular languages
- c) Regular languages use grammars only with terminal symbols
- d) Context-free languages use grammars with recursive rules
   Answer: A

## 30. What is the key feature of a regular grammar?

- a) It can have recursive production rules
- b) It generates non-context-free languages
- c) Its rules consist of a terminal symbol followed by a non-terminal symbol
- d) It is used for context-sensitive languages

Answer: C