

COMPARISON OF PARAMETRE BETWEEN

AVL ,BST AND TREAP

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- Five text files are generated using test case generator program.
- In each text file 10,000 key values are present which is randomly generated.
- In every text file the range of numbers is different.
- Now we will run AVL, BST and TREAP using these text files and compare parameters.

Output of AVL code:

Insert: 70%	Delete: 30%	file1.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
AVL:	11	2253	94376	2.32258
Insert: 75%	Delete: 25%	file2.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
AVL:	13	2733	107487	2.31755
Insert: 65%	Delete: 35%	file3.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
AVL:	12	2577	102046	2.3353
Insert: 60%	Delete: 40%	file4.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
AVL:	13	3198	110589	2.32092
Insert: 80%	Delete: 20%	file5.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
AVL:	14	3073	110876	2.32516

Insertion and deletion percentage is different for every file.

We can see final tree height, number of rotations, key comparisons and avg. node height for each text file.

Now we are going to compare these parameters with BST and TREAP.

Output of BST code:

Insert: 70%	Delete: 30%	file1.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
BST:	19	0	101719	3.27165
Insert: 75%	Delete: 25%	file2.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
BST:	23	0	135163	3.29938
Insert: 65%	Delete: 35%	file3.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
BST:	22	0	115139	3.19003
Insert: 60%	Delete: 40%	file4.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
BST:	23	0	127633	3.32805
Insert: 80%	Delete: 20%	file5.txt		
File	Tree_height	Rotations	key_comparisons	Avg_node_height
BST:	27	0	129955	3.39769

Output of TREAP code:

Insert: 70%	Delete: 30%	file1.txt		
DS	Tree_height	Rotations	key_comparisons	Avg_node_height
Treap:	23	6518	104325	3.56706
Insert: 75%	Delete: 25%	file2.txt		
DS	Tree_height	Rotations	key_comparisons	Avg_node_height
Treap:	23	8083	126806	3.45863
Insert: 65%	Delete: 35%	file3.txt		
DS	Tree_height	Rotations	key_comparisons	Avg_node_height
Treap:	21	7970	118065	3.46706
Insert: 60%	Delete: 40%	file4.txt		
DS	Tree_height	Rotations	key_comparisons	Avg_node_height
Treap:	33	9244	132633	3.5733
Insert: 80%	Delete: 20%	file5.txt		
DS	Tree_height	Rotations	key_comparisons	Avg_node_height
Treap:	27	8661	129392	3.43728

(1) HEIGHT OF THE FINAL TREE :

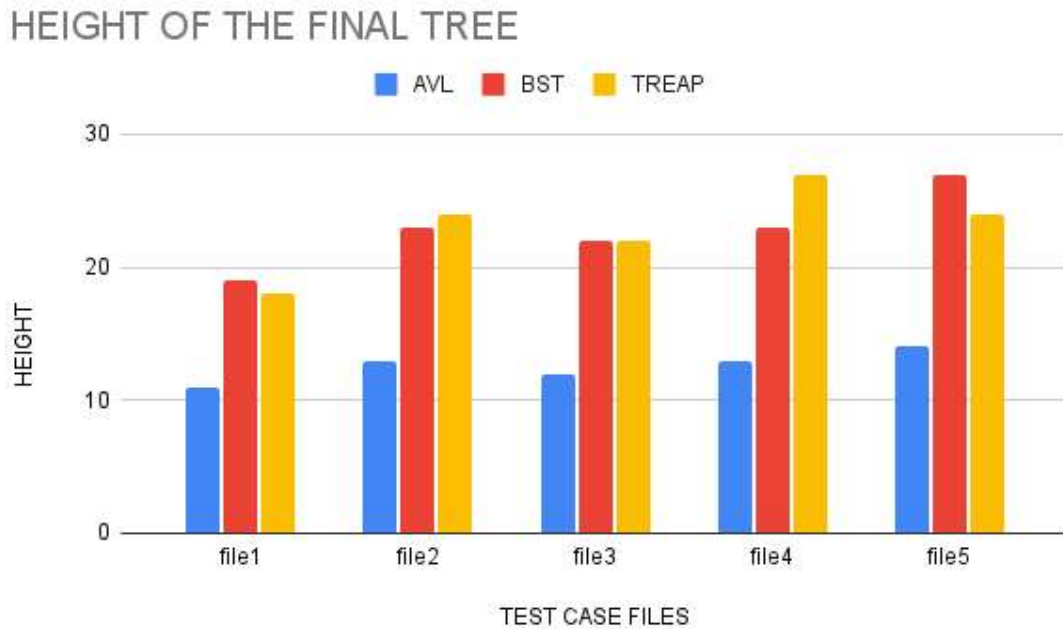


Chart of final tree height comparison

- Height of AVL tree is $\log(n)$. We can see the heights are in range 11-14 for 10,000 key values. Which makes it same as theoretical.
 - BST and TREAP height will be in between $\log(n)$ and n . ($n=10,000$)
 - AVL gives best performance here. Here we can see that height of AVL tree is less than BST and TREAP.
 - Height of TREAP depends on its priority values, which is random. So we cannot compare the height of TREAP with BST. It will be more sometimes and less sometimes.
 - Final height of AVL and BST is constant for these 5 test case files.
 - Final height of TREAP is not constant for these 5 test case files because of the priority values.
 - Priority values are randomly generated that's why height will change each time you will run the program.
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(2) NUMBER OF ROTATIONS OF THE FINAL TREE :

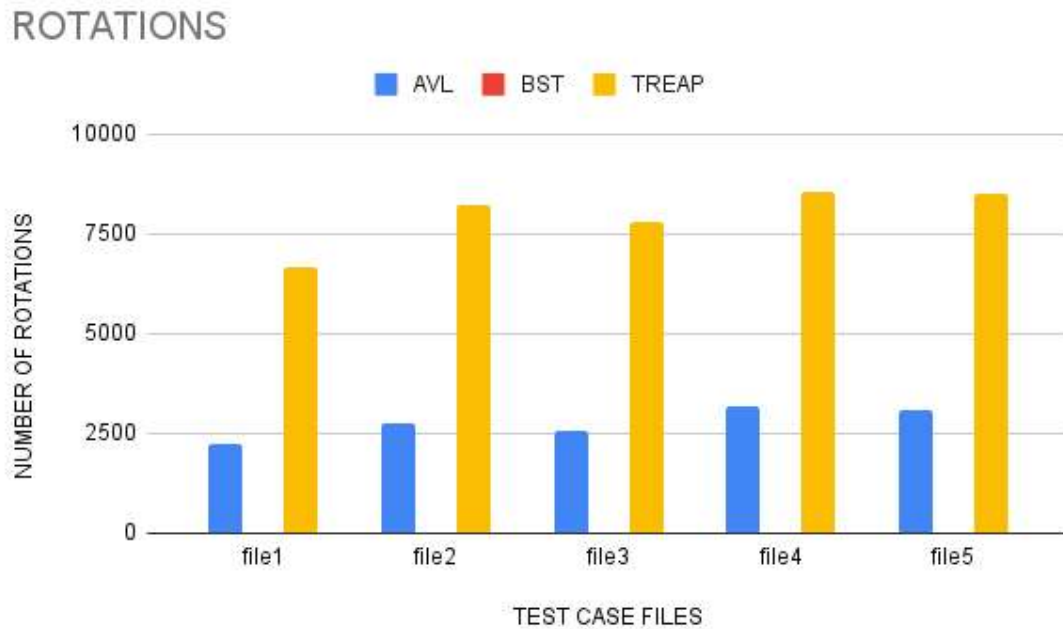


Chart of rotations(insertion + deletion) comparison

- There are no rotations in BST. Therefore values are zero in all five files.
 - As the height of the AVL tree is always less than or equal to TREAP, the rotations takes place in AVL will also be less than or equal to TREAP.
 - Rotations depends on input key value for AVL.
 - Rotations depends on priority value for TREAP.
 - As priority values are randomly generated the number of rotations are not fix for given test case files.
 - Every time we run the program we will get new number of rotations.
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(3) NUMBER OF KEY COMPARISONS OF THE FINAL TREE :

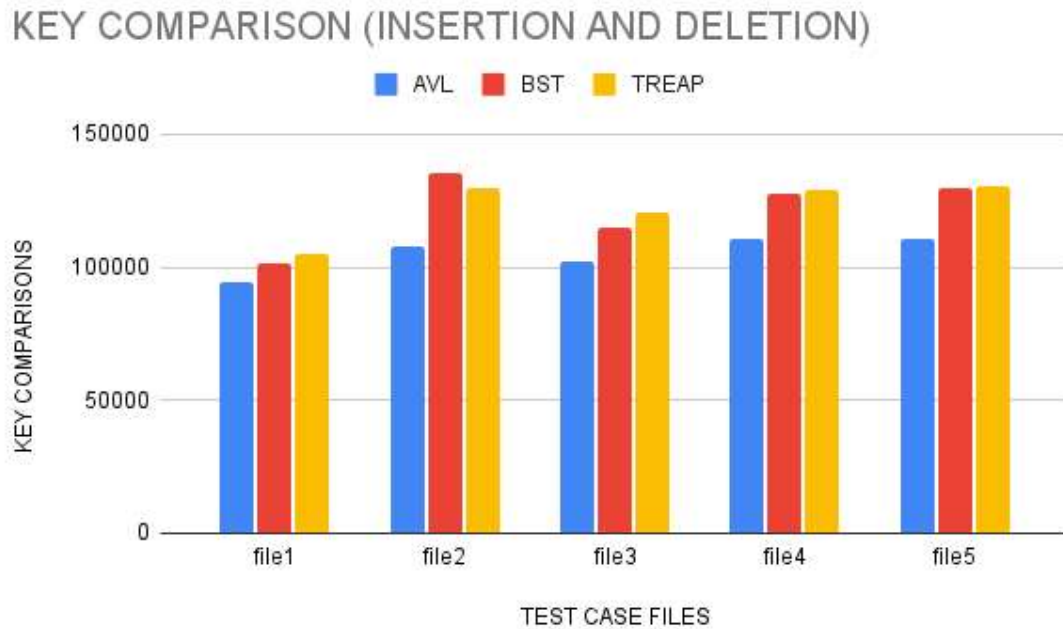


Chart of key(insertion + deletion) comparison

- Key comparisons totally depends on height of the tree.
 - Key comparison = $n \cdot \log(n) = 10,000 \cdot \log(10,000)$
 - Key comparison values are not exactly the same but the difference is not very big.
 - AVL tree is always balanced. So the number of comparisons will be little lesser than other Data structures.
 - As height of the TREAP totally depends on priority values, we cannot compare it with BST.
 - BST height totally depends on input key values. Therefore we cannot compare it with TREAP.
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(4) AVERAGE NODE HEIGHT OF THE FINAL TREE :

AVERAGE HEIGHT OF NODE

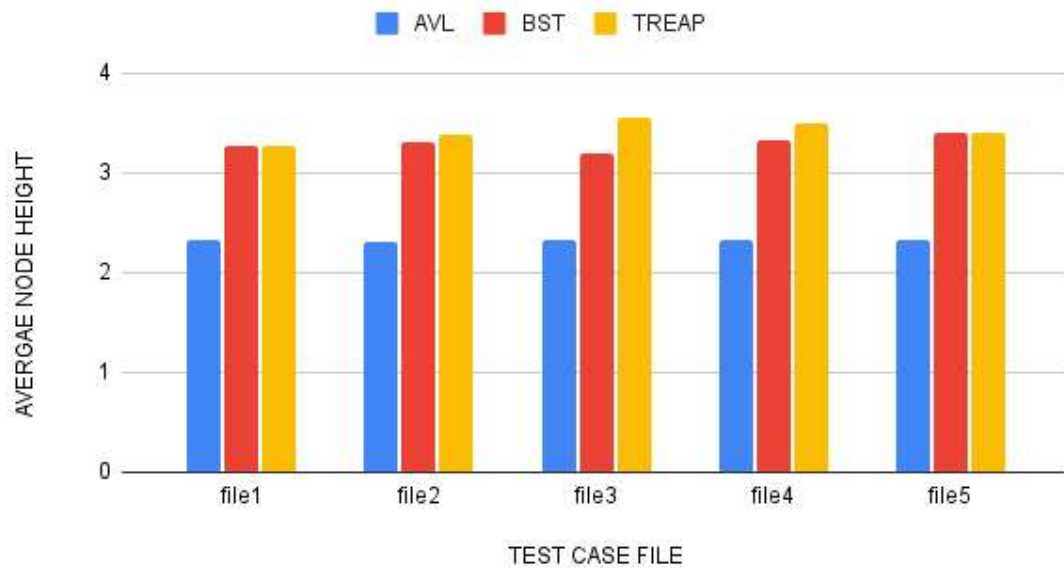


Chart of average node height comparison

- AVL tree is always balanced. So the height will always be little lesser than other Data structures.
- Height of leaf node = 1.
- Height of root = longest path distance from root to node.
- Therefore AVL average node height is always less.
- BST average node height is less here than TREAP. It is not necessarily true for all other test files.
- In some cases average node height of TREAP can be less than BST.
