

Shri G.S. Institute of Technology and Science, Indore
Department of Computer Engineering
CO2453: Discrete Structures
Session: Jan.-May 2016

Instructor: Mahima Agrawal

Tutorial 02

State whether the following propositions are equivalent

1. $(\neg p \wedge (\neg q \wedge r)) \vee (q \wedge r) \vee (p \wedge r) \equiv r$
2. $p \rightarrow (q \rightarrow p) \equiv \neg p \rightarrow (p \rightarrow q)$
3. $p \rightarrow (q \vee r) \equiv (p \rightarrow q) \vee (p \rightarrow r)$
4. $(p \rightarrow q) \wedge (r \rightarrow q) \equiv (p \vee r) \rightarrow q$
5. $[d \rightarrow ((\neg a) \wedge b) \wedge c] \equiv \neg[(a \vee (\neg(b \wedge c)))] \wedge d]$
6. $\neg(p \vee (\neg p \wedge q)) \equiv \neg p \wedge \neg q$
7. $(p \rightarrow q) \rightarrow r \equiv p \rightarrow (q \rightarrow r)$

Simplify using algebraic laws of proposition

1. $(p \wedge q) \vee p$
2. $(p \wedge q) \wedge \neg p$
3. $\neg(\neg p \wedge q) \wedge (\neg p \vee q) \wedge (p \vee q)$
4. $(p \vee q) \wedge \neg p$
5. $p \vee (p \wedge q)$
6. $\neg(p \vee q) \vee (\neg p \wedge q)$
7. $(p \vee q) \wedge \neg p$
8. $\neg(p \vee q) \vee (\neg p \vee q)$

Obtain the pcnf of the following

1. $\neg p \vee q$
2. $(p \wedge q) \vee (q \wedge r)$
3. $(\neg p \rightarrow r) \wedge (q \leftrightarrow p)$, and hence find pdnf from pcnf.
4. $(p \wedge q) \vee (\neg p \wedge q) \vee (p \wedge \neg q)$
5. $(p \wedge q) \vee (\neg p \wedge q \wedge r)$
6. $(\neg s \wedge \neg p \wedge r \wedge q) \vee (s \wedge p \wedge \neg r \wedge \neg q) \vee (\neg s \wedge p \wedge r \wedge \neg q) \vee (q \wedge \neg p \wedge \neg r \wedge s) \vee (p \wedge \neg s \wedge \neg r \wedge q)$
7. $\neg(p \vee q)$
8. $\neg(p \rightarrow q)$
9. $(p \wedge q \wedge r) \vee (\neg p \wedge r \wedge q) \vee (\neg p \wedge \neg q \wedge \neg r)$
10. $p \vee (\neg p \rightarrow (q \vee (\neg q \rightarrow r)))$
11. $p \rightarrow (p \wedge (q \rightarrow p))$
12. $p \rightarrow ((p \rightarrow q) \wedge \neg(\neg q \vee \neg p))$

"Every Accomplishment Starts With The Decision To Try".

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Obtain the pdnf of the following

1. $\neg p \vee q$
2. $(p \wedge q) \vee (q \wedge r)$
3. $p \rightarrow ((p \rightarrow q) \wedge \neg (\neg q \vee \neg p))$
4. $\neg((p \vee q) \wedge r) \wedge (p \vee r)$
5. $p \vee (p \wedge q) \equiv p$
6. $p \vee (\neg p \wedge q) \equiv p \vee q$
7. $p \vee (\neg p \rightarrow (q \vee (\neg q \rightarrow r)))$

Obtain the pdnf, pcnf for the following and which of the formulas are tautology

1. $q \wedge (p \vee \neg q)$
2. $(q \rightarrow p) \wedge (\neg p \wedge q)$