

## Classification Problem :-

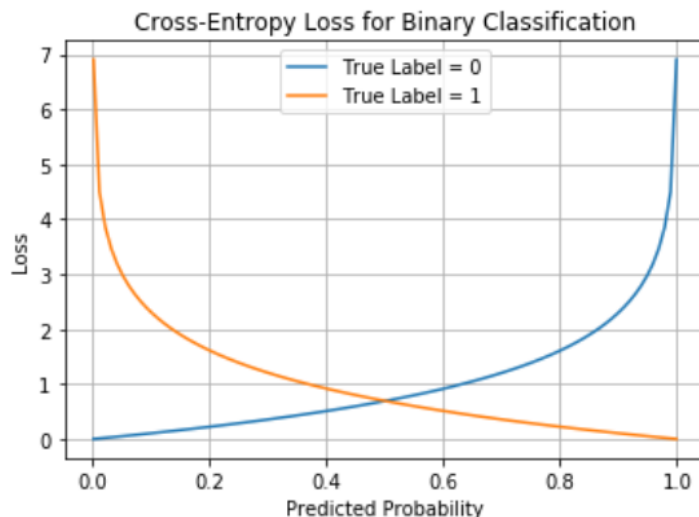
Let's take a look at binary cross entropy loss function,

$$L_{BCE} = -\frac{1}{n} \sum_{i=1}^n (Y_i \cdot \log \hat{Y}_i + (1 - Y_i) \cdot \log (1 - \hat{Y}_i))$$

Here  $Y_i$  is the ground truth and  $\hat{Y}_i$  is the predicted label.

If  $Y_i = 1$ , then  $L_{BCE} = -\frac{1}{n} \sum_{i=1}^n \log \hat{Y}_i$

If  $Y_i = 0$ , then  $L_{BCE} = -\frac{1}{n} \sum_{i=1}^n \log (1 - \hat{Y}_i)$



## This can be inferred from the graph above:-

When **True Label = 0** if we predict 1 we get a very large loss and if we predict 0 we get 0 loss.

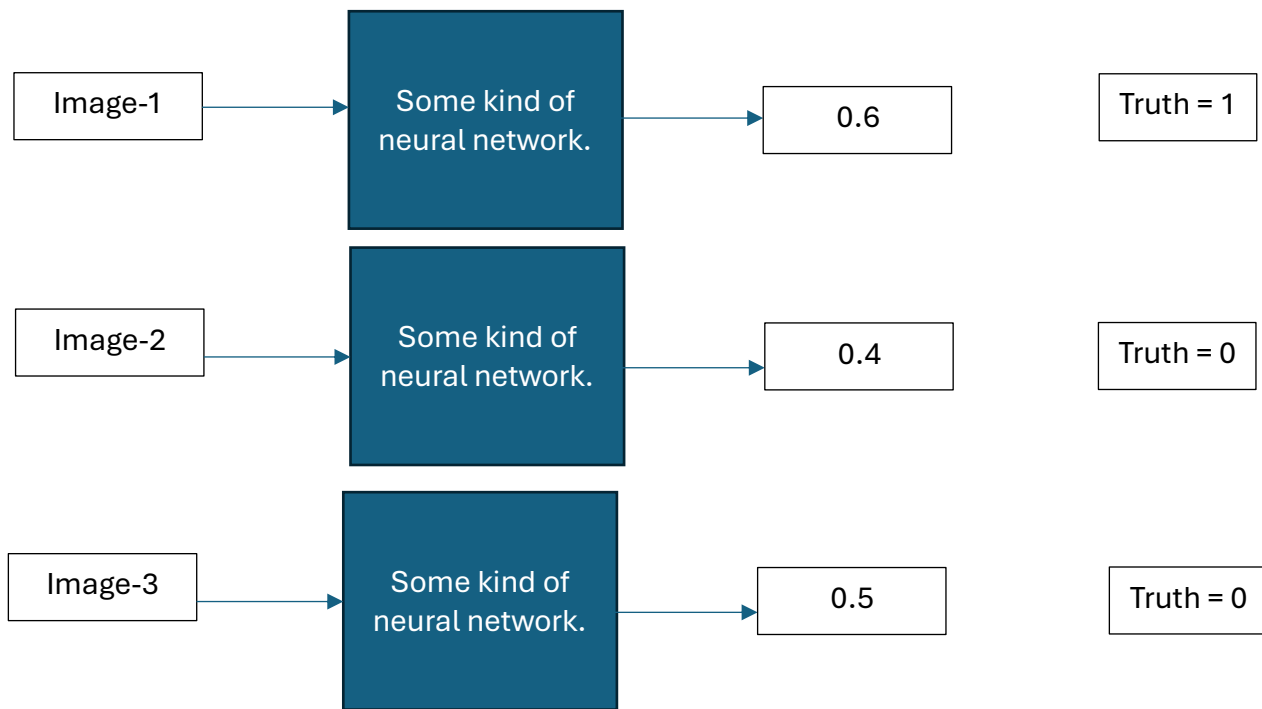
When **True Label = 1** if we predict 1 we get a 0 loss and if we predict 1 we get a very large loss.

**Let's say we are classifying whether image is fake or real,**

Data looks something like this

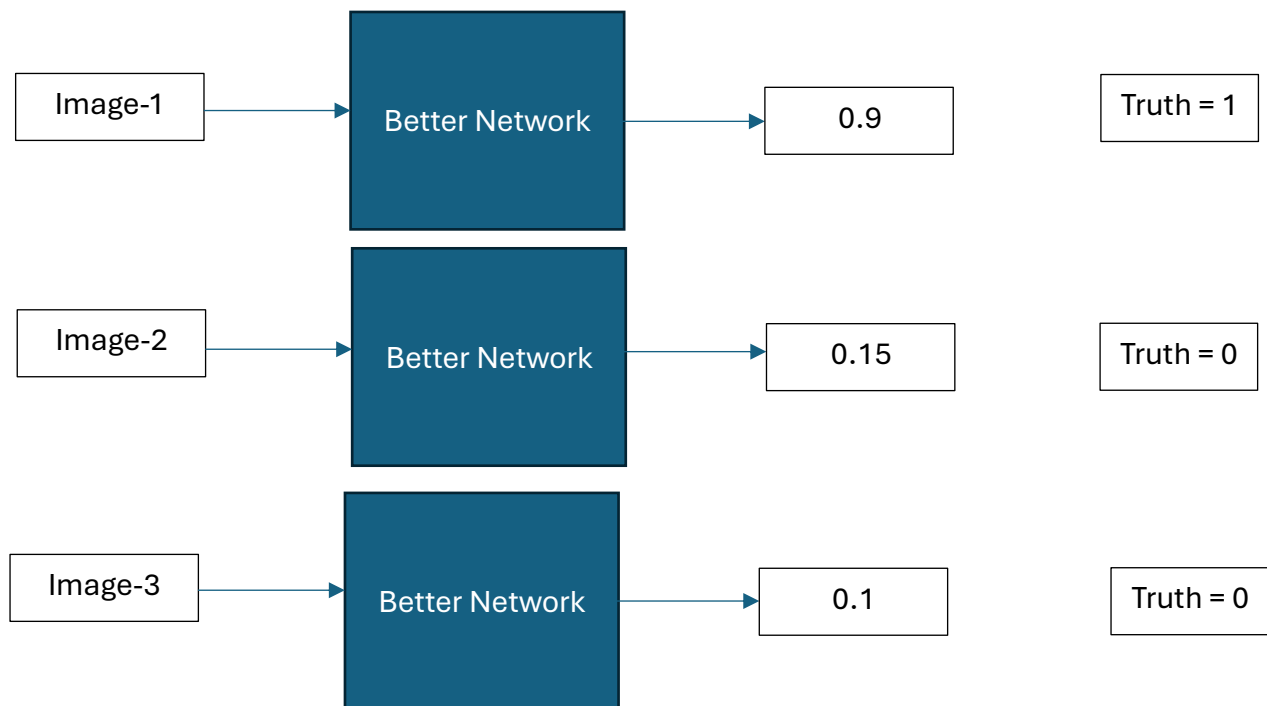
Data	Label
Image-1	1
Image-2	0
Image-3	0

Let's feed images into our imaginary network initially as you can see the output is not that good:-



$$\text{BCE (initially)} = -\frac{1}{3}((1 * \log(0.6) + 0 * \log(0.4) + 0 * \log(0.3) + (0 * \log(1 - 0.6) + 1 * \log(1 - 0.4) + 1 * \log(1 - 0.3))) = 0.199$$

**For a better classifier :-**



$$\text{BCE (for this better network)} = -\frac{1}{3}((1 * \log(0.9) + 0 * \log(0.15) + 0 * \log(0.1) + (0 * \log(1 - 0.9) + 1 * \log(1 - 0.15) + 1 * \log(1 - 0.1))) = 0.054$$

**BCE decreases for better network , so while training the weights and biases changes to decrease our BCE hence giving better classification.**