

1.4.5 Give tilde approximations for the following quantities:

a) $N + 1$ is equivalent to $\sim N$

b) $1 + 1/N$ is equivalent to ~ 1

c) $(1 + 1/N)(1 + 2/N)$ is equivalent to ~ 1 since 1 is dominant after expansion

d) $(2N^3) - (15N^2) + N$ is equivalent to $\sim 2N^3$, since N^3 is dominant

e) $\log(2N)/\log(N)$

$$= \frac{\lg(2) + \lg(N)}{\lg(N)}$$

$$= \frac{\log(2)}{\log(N)} + \frac{\log(N)}{\log(N)}$$

$$= \sim 1$$

f) $\frac{\log(N^2+1)}{\log(N)}$

$$= 2 \frac{\log(N)}{\log(N)} // \text{Used Logarithm power law. Ignore the 1 since log is dominant}$$

$$= \sim 2 \text{ g) } \frac{N^{100}}{2^N}$$

$$= \sim 0 \text{ since limit approaches 0}$$