

**Exercise 1.4.9:** Give a formula to predict the running time of a program for a problem of size  $N$  when doubling experiments have shown that the doubling factor is  $2^b$  and the running time for problems of size  $N_0$  is  $T$ .

**Solution: Example below:** Recall  $\log_2 N$  is usually used anytime when search interval is halving or doubling by 2. If going down by number  $n$ , then becomes  $\log_n N$

- $T(2) = T(1) * 2^b$
- $T(4) = T(2) * 2^b$
- $T(8) = T(4) * 2^b$
- $T(16) = T(8) * 2^b$  OR  $T(16) = T(1) * 2^b * 2^b * 2^b * 2^b$
- $T(N) = T(N/2) * 2^b$
- Therefore,  $T(N) = T * 2^{b \log N}$