

A faint, light blue background pattern consisting of a network of interconnected circular nodes and straight lines, resembling a molecular structure or a data network.

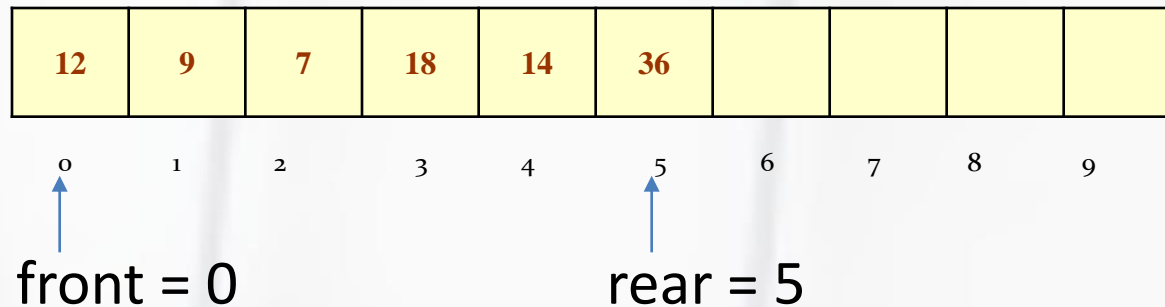
# Queues

# Introduction

- Queue is an important data structure which stores its elements in an ordered manner.
- We can explain the concept of queues using the following analogy:  
*People moving on an escalator. The people who got on the escalator first will be the first one to step out of it.*
- A queue is a FIFO (First-In, First-Out) data structure in which the element that is inserted first is the first one to be taken out.
- The elements in a queue are added at one end called the *rear* and removed from the other one end called the *front*.

# Array Representation of Queues

- Queues can be easily represented using linear arrays.
- Every queue has front and rear variables that point to the position from where deletions and insertions can be done, respectively.
- Consider the queue shown in figure

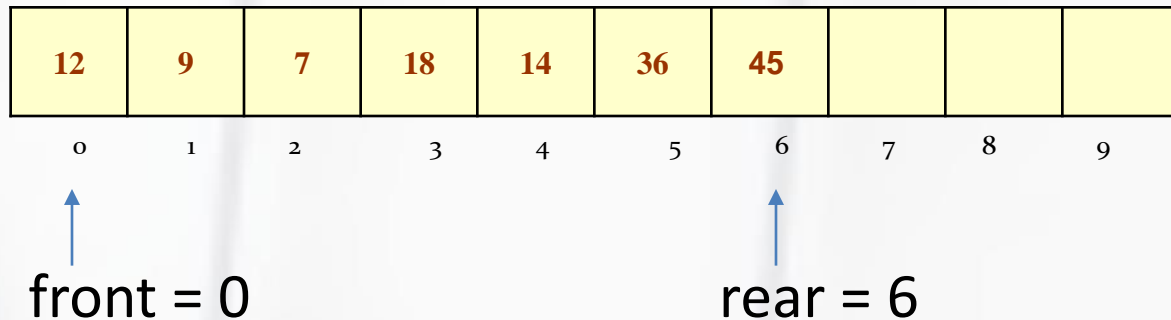


- Here, front = 0 and rear = 5.

0 1 2 3 4 5 6 7 8 9

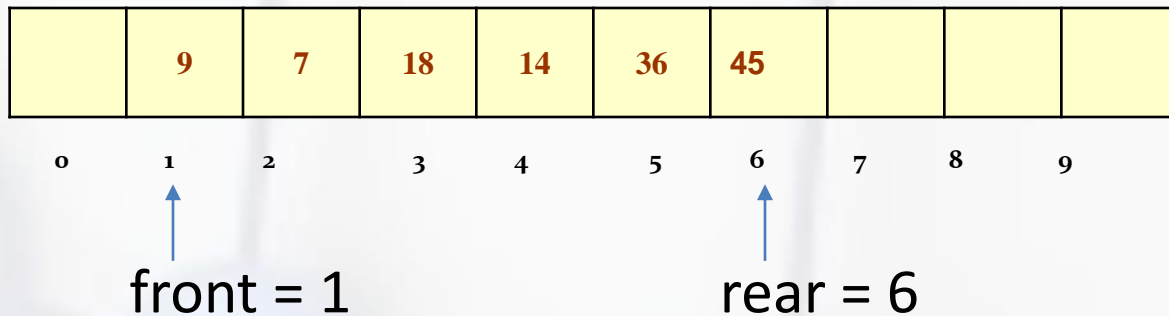
# Array Representation of Queues

- If we want to add one more value in the list say with value 45, then rear would be incremented by 1 and the value would be stored at the position pointed by rear.



# Array Representation of Queues

- Now,  $\text{front} = 0$  and  $\text{rear} = 6$ . Every time a new element has to be added, we will repeat the same procedure.
- Now, if we want to delete an element from the queue, then the value of  $\text{front}$  will be incremented. Deletions are done from only this end of the queue.



- Now,  $\text{front} = 1$  and  $\text{rear} = 6$ .

# Array Representation of Queues

- Before inserting an element in the queue we must check for **overflow** conditions.
- An **overflow** occurs when we try to insert an element into a queue that is already full, i.e. when **rear = MAX – 1**, where MAX specifies the maximum number of elements that the queue can hold.
- Similarly, before deleting an element from the queue, we must check for **underflow** condition.
- An **underflow** occurs when we try to delete an element from a queue that is already empty. If **front = -1** and **rear = -1**, this means there is no element in the queue.

# Algorithm for Insertion Operation

Algorithm to insert an element in a queue

Step 1: IF REAR=MAX-1, then;

    Write OVERFLOW

    Goto Step 4

    [END OF IF]

Step 2: IF FRONT == -1 and REAR = -1, then

    SET FRONT = REAR = 0

ELSE

    SET REAR = REAR + 1

    [END OF IF]

Step 3: SET QUEUE[REAR] = NUM

Step 4: Exit

# Algorithm for Deletion Operation

Algorithm to delete an element from a queue

Step 1: IF FRONT = -1 OR FRONT > REAR, then

Write UNDERFLOW

Goto Step 2

ELSE

SET VAL = QUEUE[FRONT]

SET FRONT = FRONT + 1

[END OF IF]

Step 2: Exit



# Circular Queues

		7	18	14	36	45	21	99	72
0	1	2	3	4	5	6	7	8	9

- We will explain the concept of circular queues using an example.
- In this queue, front = 2 and rear = 9.
- Now, if you want to insert a new element, it cannot be done because the space is available only at the left of the queue.
- If  $\text{rear} = \text{MAX} - 1$ , then OVERFLOW condition exists.
- This is the major drawback of a linear queue. Even if space is available, no insertions can be done once rear is equal to  $\text{MAX} - 1$ .
- This leads to wastage of space. In order to overcome this problem, we use circular queues.
- In a circular queue, the first index comes right after the last index.
- A circular queue is full, only when  $\text{front} = 0$  and  $\text{rear} = \text{Max} - 1$ .

# Inserting an Element in a Circular Queue

- For insertion we check for three conditions which are as follows:
  - If  $\text{front}=0$  and  $\text{rear}=\text{MAX}-1$ , then the circular queue is full.

90	49	7	18	14	36	45	21	99	72
front=0	1	2	3	4	5	6	7	8	rear = 9

- If  $\text{Rear}+1 = \text{Front}$ , then also the circular queue is full.

90	49	7	18	14	36	45	21	99	72
0	1	2	3	rear=4	front =5	6	7	8	9

# Inserting an Element in a Circular Queue

- For insertion we check for three conditions which are as follows:
  - If  $\text{front}=0$  and  $\text{rear}=\text{MAX}-1$ , then the circular queue is full.

90	49	7	18	14	36	45	21	99	72
front=0	1	2	3	4	5	6	7	8	rear = 9

- If  $\text{rear} \neq \text{MAX}-1$ , then the rear will be incremented and value will be inserted

90	49	7	18	14	36	45	21	99	
front=0	1	2	3	4	5	6	7	rear=8	9

- If  $\text{front} \neq 0$  and  $\text{rear}=\text{MAX}-1$ , then it means that the queue is not full. So, set  $\text{rear} = 0$  and insert the new element.

	49	7	18	14	36	45	21	99	72
front=1	2	3	4	5	6	7	8	rear=9	

# Algorithm to Insert an Element in a Circular Queue

Step 1: IF (FRONT = 0 and REAR = MAX - 1) or (REAR + 1 = FRONT), then

Write "OVERFLOW"

Goto Step 4

[END OF IF]

Step 2: IF FRONT = -1 and REAR = -1, then;

SET FRONT = REAR = 0

ELSE IF REAR = MAX - 1

SET REAR = 0

ELSE

SET REAR = REAR + 1

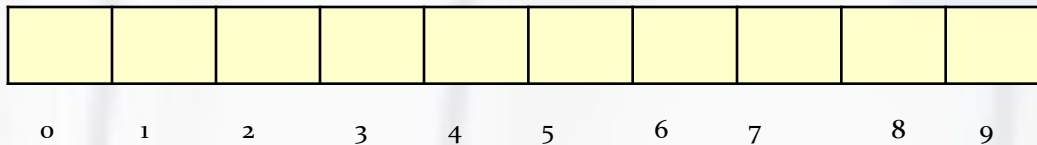
[END OF IF]

Step 3: SET QUEUE[REAR] = VAL

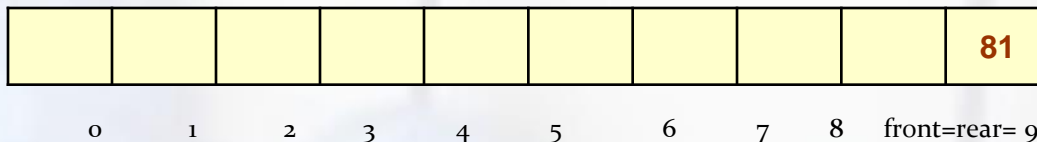
Step 4: Exit

# Deleting an Element from a Circular Queue

- To delete an element again we will check for three conditions:
  - If  $\text{front} = -1$ , then it means there are no elements in the queue. So an underflow condition will be reported.

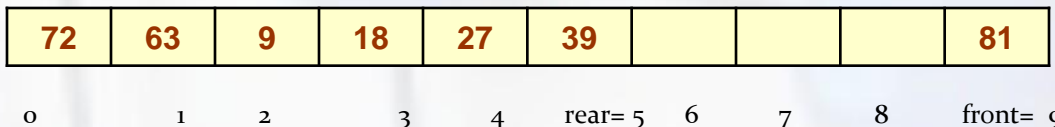


- If the queue is not empty and after returning the value on front, if  $\text{front} = \text{rear}$ , then it means now the queue has become empty and so front and rear are set to -1.



Delete this element and set  
 $\text{rear} = \text{front} = -1$

- If the queue is not empty and after returning the value on front, if  $\text{front} = \text{MAX} - 1$ , then front is set to 0.

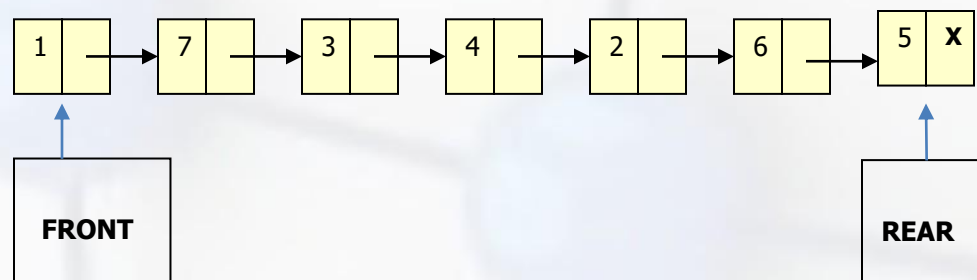


# Algorithm to Delete an Element from a Circular Queue

```
Step 1: IF FRONT = -1, then
        Write "Underflow"
        Goto Step 4
    [END OF IF]
Step 2: SET VAL = QUEUE[FRONT]
Step 3: IF FRONT = REAR
        SET FRONT = REAR = -1
    ELSE
        IF FRONT = MAX - 1
            SET FRONT = 0
        ELSE
            SET FRONT = FRONT + 1
        [END OF IF]
    [END OF IF]
Step 4: EXIT
```

# Linked Representation of Queues

- In a linked queue, every element has two parts: one that stores data and the other that stores the address of the next element.
- The START pointer of the linked list is used as FRONT.
- We will also use another pointer called REAR which will store the address of the last element in the queue.
- All insertions will be done at the rear end and all the deletions will be done at the front end.
- If  $\text{FRONT} = \text{REAR} = \text{NULL}$ , then it indicates that the queue is empty.



# Inserting an Element in a Linked Queue

Algorithm to insert an element in a linked queue

Step 1: Allocate memory for the new node and name it as PTR

Step 2: SET PTR->DATA = VAL

Step 3: IF FRONT = NULL, then

    SET FRONT = REAR = PTR

    SET FRONT->NEXT = REAR->NEXT = NULL

ELSE

    SET REAR->NEXT = PTR

    SET REAR = PTR

    SET REAR->NEXT = NULL

    [END OF IF]

Step 4: END



# Deleting an Element from a Linked Queue

Algorithm to delete an element from a linked queue

Step 1: IF FRONT = NULL, then  
          Write "Underflow"  
          Go to Step 5

          [END OF IF]

Step 2: SET PTR = FRONT

Step 3: FRONT = FRONT->NEXT

Step 4: FREE PTR

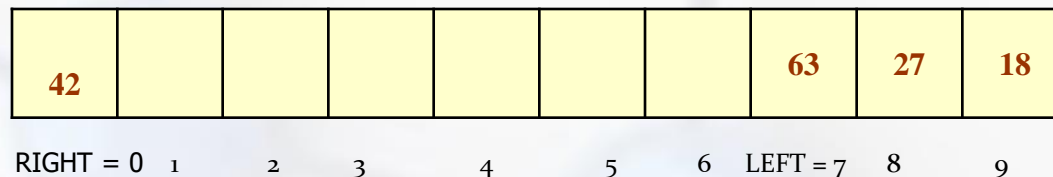
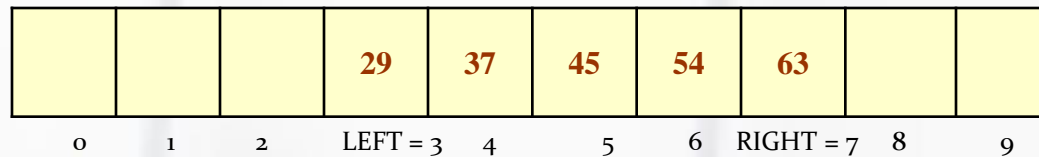
Step 5: END

# Dequeues

- **Deque or Double Ended Queue** is a **generalized version of Queue** data structure that allows insert and delete at both ends.
- A deque can be implemented either using a circular array or a circular doubly linked list.
- Linked list implementation of deque also known as a **head-tail linked** list because elements can be added to or removed from the front (head) or back (tail).

# Dequeues

- In a deque, two pointers are maintained, LEFT and RIGHT which point to either end of the deque.
- The elements in a deque stretch from LEFT end to the RIGHT and since it is circular, Dequeue[MAX-1] is followed by Dequeue[0].



# Dequeues

- **Operations on Deque:**

Mainly the following four basic operations are performed on queue:

- ***insertFront()***: Adds an item at the front of Deque.  
***insertRear()***: Adds an item at the rear of Deque.  
***deleteFront()***: Deletes an item from front of Deque.  
***deleteRear()***: Deletes an item from rear of Deque.
- A deque is a generalized data structure that can be used as regular ***queue*** or ***stack***.
- As a Queue: Use only ***deleteFront()*** and ***insertRear()*** operations.
- As a stack: Use only ***insertRear()*** and ***deleteRear()*** operations.

# Dequeues

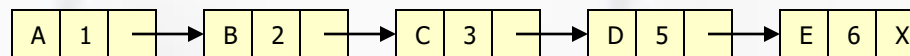
- There are two variants of a double-ended queue:
  - ***Input restricted deque***: In this dequeue insertions can be done only at one of the ends while deletions can be done from both the ends.
  - ***Output restricted deque***: In this dequeue deletions can be done only at one of the ends while insertions can be done on both the ends.

# Priority Queues

- A **priority queue** is a queue in which each element is assigned a priority.
- The priority of elements is used to determine the order in which these elements will be processed.
- The general rule of processing elements of a priority queue can be given as:
  - An element with higher priority is processed before an element with lower priority.
  - Two elements with same priority are processed on a **first come first served** (FCFS) basis.
- Priority queues are widely used in **operating systems** to execute the highest priority process first.
- In computer's memory, priority queues can be represented using arrays or linked lists.

# Linked Representation of Priority Queues

- When a priority queue is implemented using a linked list, then every node of the list contains three parts: (i) the information or data part, (ii) the priority number of the element, (iii) and address of the next element.
- If we are using a sorted linked list, then element having higher priority will appear before the element with lower priority.

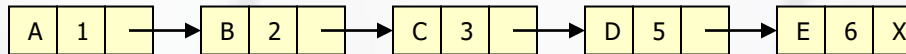


- **Note:** Assumes lower the priority field value, higher the priority.

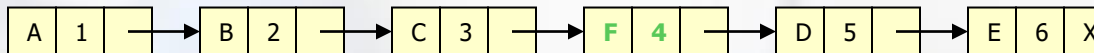
# Linked Representation of Priority Queues

## Insertion into a priority queue:

- Traverse the list until we find a node that has a priority lower than that of the new element.
- The new node is inserted before the node with the lower priority.



Priority queue after insertion of a new node F with priority 4.

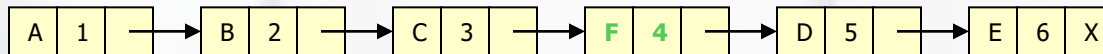




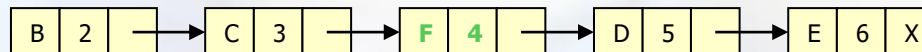
# Linked Representation of Priority Queues

## Deletion a priority queue:

- From a priority queue, element with highest priority is removed first.
- In this case, elements are stored in descending order of priority. Hence the first element is removed.



Priority queue after deletion of a highest priority element.



# Array Representation of Priority Queues

- When arrays are used to implement a priority queue, then a separate queue for each priority number is maintained.
- Each of these queues will be implemented as circular queues. Every individual queue will have its own FRONT and REAR pointers.
- We can use a two-dimensional array for this purpose where each queue will be allocated same amount of space.
- Given the front and rear values of each queue, a two- dimensional matrix can be formed.

# Array Representation of Priority Queues

FRONT	REAR
3	3
1	3
4	5
4	1

	1	2	3	4	5
1			A		
2	B	C	D		
3				E	F
4	I			G	H

**Figure 8.29** Priority queue matrix

FRONT	REAR
3	3
1	3
4	1
4	1

	1	2	3	4	5
1			A		
2	B	C	D		
3	R			E	F
4	I			G	H

**Figure 8.30** Priority queue matrix after insertion of a new element

# Applications of Queues

- Queues are widely used as waiting lists for a single resource like printer, disk, CPU etc. shared by many user agents.
- Queues are used to transfer data asynchronously between different applications/processes running in a system(e.g., IPC mechanism pipes, sockets use queues).
- Queues are used as buffers on devices MP3 players and portable CD players, iPod playlist.
- Queues are used in Playlist for music player apps to add songs to the end, play from the front of the list.