

# Project Calculations



## 1. Rover Base & Structure

- **10cm Wheels:**  $83 \text{ g} \times 2 = 166 \text{ g}$
- **Base Plates (3D Printed PETG):**
  - Volume:  $110 \text{ cm}^3$
  - Infill: 40%
  - Density:  $1.3 \text{ gm/cm}^3$
  - Weight per Plate:  $110 \times 0.4 \times 1.3 = 57.2 \text{ g}$
  - Total (3 Plates):  $57.2 \text{ g} \times 3 = 171.6 \text{ g}$
- **Rods & Brackets:**
  - 15cm Threaded Rods (M5):  $17.33 \text{ g} \times 4 = 69.32 \text{ g}$
  - Brackets:  $5.724 \text{ g} \times 2 = 11.448 \text{ g}$
  - Subtotal (Rods & Brackets): **80.768g**

## 2. Rover Electronics

- **ESP 32:** 15 grams
- **L298N (Motor Driver):** 40g
- **MPU (Sensor):** 3g
- **12v 200 rpm Johnson motors :**  $165 \text{ g} \times 2 = 330 \text{ g}$
- **Wires:** 20g
- **Total (Wheel Electronics):** 421 g

### 3. Drone Components

- **F450 Frame:** 415g
- **Pixhawk (Flight Controller):** 15.5g
- **3S Lipo Battery:** 288g
- **Emax MT2213 Motors:**  $53\text{g} \times 4 = 212\text{g}$
- **SimonK 30A ESCs:**  $3.2\text{g} \times 4 = 12.8\text{g}$
- **Receiver:** 2.5g
- **PDB (PTB XT60):** 12g

### 4. Fasteners & Buffer

- **Bracket to Motor Screws (M3 7mm x 4):** 4g
- **Bracket to Base Plate (M3 15mm x 12 screws/bolts):** 16.8g
- **M5 Nuts (x24):**  $1.36\text{g} \times 24 = 32.64\text{g}$
- **M5 Washers (x24):**  $0.3\text{g} \times 24 = 7.2\text{g}$
- **Fastener Total:**  $4 + 16.8 + 32.64 + 7.2 = 60.64\text{g}$
- **Buffer:** 100g
- **Net Total (Fasteners & Buffer):** 160.64g

### 5. Final Weight & Thrust Summary

- **Full Weight Calculation:**  
 $166 + 80.76 + 171.6 + 421 + 1235 + 160.64 = 2235\text{ g}$
- **Total Weight:** 2.235 kg
- **Motor Thrust:** 860g per motor (Emax)
- **Net Thrust:**  $860\text{g} \times 4 = 3440\text{g}$
- **Thrust-to-Weight Ratio:** 1.53
- **Motor Size:** 2208 - 2216
- **Propeller Size:** 1045 / 945

# Wheel Torque Estimation

The **main equation** for calculating the **torque required** for a self-balancing robot (to keep it upright or recover from tilt) is:

$$\tau = mgL \sin(\theta)$$

Where:

- $\tau$  = torque required (N·m)
- $m$  = mass of the robot (kg)
- $g$  = acceleration due to gravity (9.81 m/s<sup>2</sup>)
- $L$  = distance from wheel axle to the robot's center of mass (m)
- $\theta$  = tilt angle from vertical (radians or degrees)

If you also want to include forward motion (accelerating or climbing), add the **drive torque** term:

$$\tau = r (ma + mg \sin(\alpha) + C_{rr}mg \cos(\alpha))$$

Where:

- $r$  = wheel radius (m)
- $a$  = desired linear acceleration (m/s<sup>2</sup>)
- $\alpha$  = slope angle (radians or degrees)
- $C_{rr}$  = rolling resistance coefficient ( $\approx 0.01$ – $0.02$  for small rubber wheels)

## Torques at different lean angles and wheel sizes

| Wheel Ø | 15°                    | 20°                    | 30°                    |
|---------|------------------------|------------------------|------------------------|
| 7 cm    | 0.229 N·m (2.34 kg·cm) | 0.293 N·m (2.98 kg·cm) | 0.413 N·m (4.21 kg·cm) |
| 10 cm   | 0.243 N·m (2.48 kg·cm) | 0.306 N·m (3.12 kg·cm) | 0.426 N·m (4.35 kg·cm) |

## RPM at different wheel sizes

| Wheel Diameter | Radius<br>r (m) | Speed<br>$v = 1 \text{ m/s}$ | Wheel RPM                 |
|----------------|-----------------|------------------------------|---------------------------|
| 7 cm           | 0.035           | 1.0                          | $\approx 273 \text{ rpm}$ |
| 10 cm          | 0.05            | 1.0                          | $\approx 191 \text{ rpm}$ |