



# Gateway Classes

**Semester -I & II****Common to All Branches****BEE101/201: FUNDAMENTALS OF ELECTRICAL ENGG.**

## **UNIT-3 ONE SHOT : Transformers**



## **Gateway Series for Engineering**

- Topic Wise Entire Syllabus**
- Long - Short Questions Covered**
- AKTU PYQs Covered**
- DPP**
- Result Oriented Content**

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# Gateway Classes



**BEE101 / BEE201: FUNDAMENTALS OF ELECTRICAL ENGINEERING**

**Unit-3**

**Introduction to Transformers**

**Syllabus**

**Magnetic circuits, ideal and practical transformer, equivalent circuit, losses in transformers, regulation and efficiency.**



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# AKTU

## Electrical Engg

# One Shot

## UNIT - III



- Unit-3: (Transformers)

- Magnetic circuits,

- ideal and practical transformer,

- equivalent circuit, → Num.

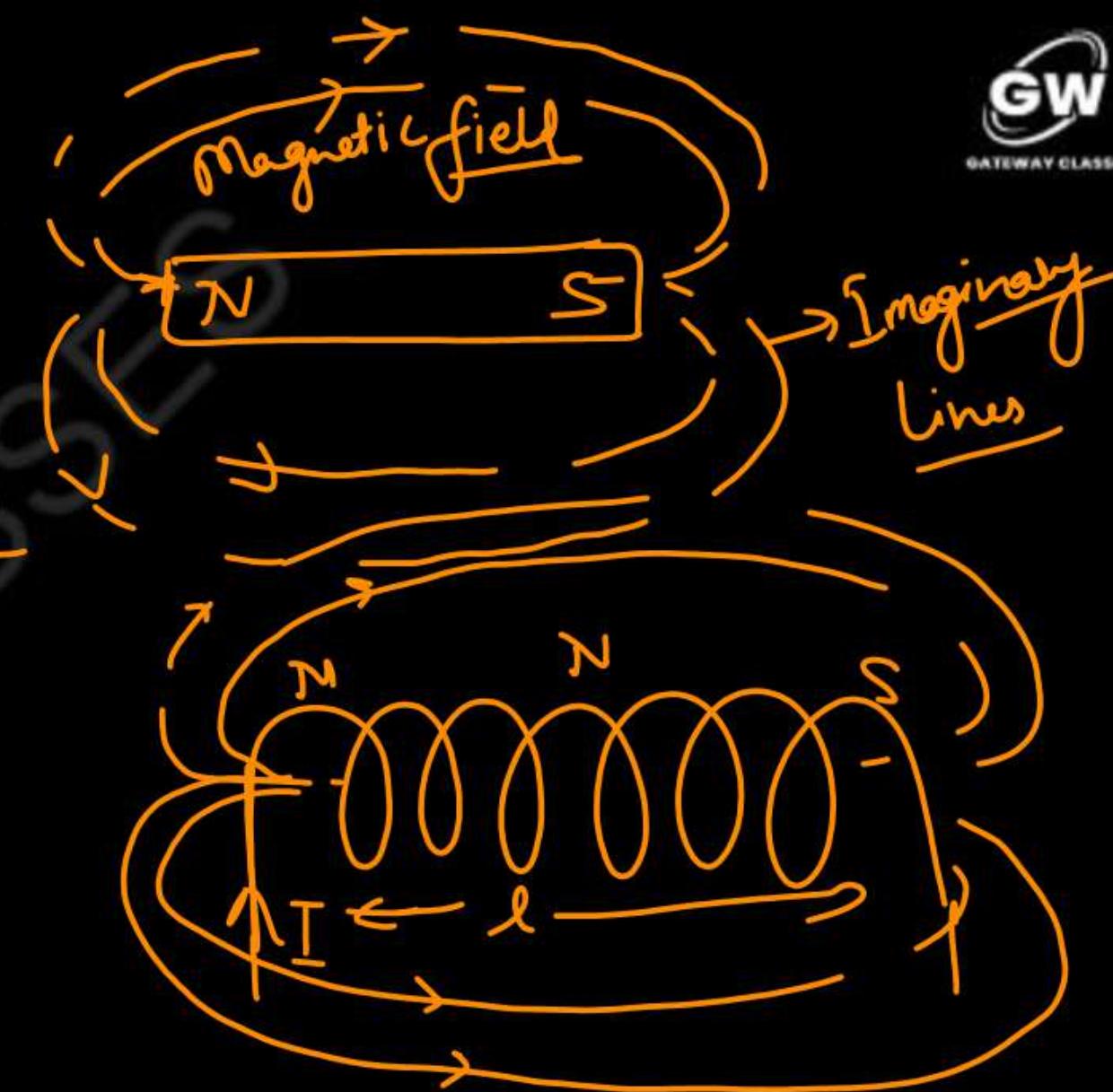
- losses in transformers,

- regulation and efficiency.

→ Ques.

## Basic Definitions

**1. Magnetic Field**:- Area around a magnet within which its influence is perceptible is known as magnetic field.



**2. Magnetic Flux** :- total number of magnetic field lines passing through a given surface. unit of flux is Weber (Wb).  $1 \text{ wb} = 10^8$  line of force

**3. Magnetic Flux density** :- Flux per unit area is known as flux density  $(B) = \frac{\text{flux}}{\text{area}}$

flux  
area

**4. Magnetic field intensity**:- Magnetizing force or Magnetic field intensity or magnetic field strength is the MMF required to magnetize a unit length of the magnetic flux path. The unit of magnetic field intensity is AT/m and is denoted by H.

$$H = \frac{NI}{l}$$

AT/m

$$H = \frac{NI}{l}$$

**5. Magneto-motive force or MMF:-** MMF is the cause for producing the magnetic flux. The MMF in a magnetic circuit depends on the number of turns(N) and the amount of current(I) flowing through it. unit is ampere turns.  $\text{AT}$

$$\text{MMF} = NI$$

**6 Reluctance:-** It is the opposition that the magnetic circuit offers for the flow of magnetic flux. We can also define the reluctance as the ratio of magneto-motive force to the magnetic flux. It is denoted by S and its unit is ampere-turns per weber.

$$\text{Reluctance}(S) = \frac{\text{mmf}}{\text{Flux}} = \frac{NI}{A\mu_0\mu_r} = \frac{I}{\mu A} = \frac{\text{mmf}}{\phi}$$

$$\text{Resistance} = \frac{\psi}{I} = \frac{NI}{R \cdot \mu_0 \mu_r l}$$

**7. Permeance:-** Permeance is the reciprocal of reluctance. The ease with which the flux can pass through the material is known as permeance. Weber/AT is the unit of permeance.

**8. Permeability:-** Permeability is the ability of a material to allow the magnetic flux when the object is placed inside the magnetic field.

$$\mu = \mu_0 \mu_r$$

Where  $\mu_0$  is absolute permeability ( $4\pi \times 10^{-7}$ ) and  $\mu_r = 1$  for air is relative permeability

**Magnetic Circuit:-** The closed path followed by the magnetic flux is magnetic circuit.

*The laws of magnetic circuits are quite similar to the electric circuits.*

A **magnetic circuit** is made up of magnetic materials having high permeability such as iron, soft steel, etc. Consider a solenoid having  $N$  turns wound on an iron core. The magnetic flux of  $\phi$  Weber sets up in the core when the current of  $I$  ampere is passed through a solenoid.

Let,  $l$  = mean length of the magnetic circuit,  $A$  = cross-sectional area of the core

$\mu_r$  = relative permeability of the core

Now the Field Strength is given by

$$H = \frac{NI}{l} \text{ AT/m}$$

$$B = \mu_0 \mu_r H = \frac{\mu_0 \mu_r NI}{l} \text{ Wb/m}^2 \text{ Wb}$$

$$\text{Total Flux } \phi = B \times A = \frac{\mu_0 \mu_r NIA}{l} = \frac{NI}{\frac{l}{A\mu_0 \mu_r}} \text{ Wb.}$$

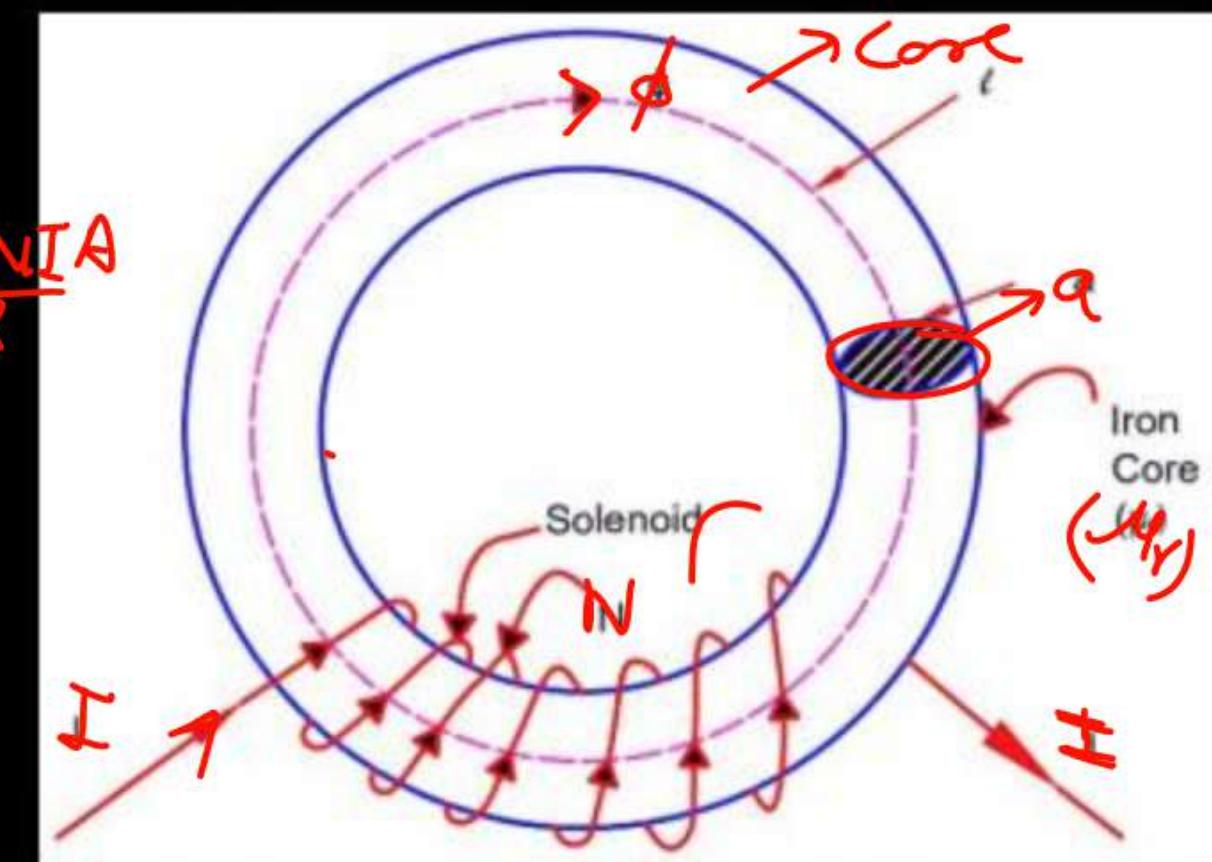
$$\begin{aligned} B &= \mu_r H \\ &= \mu_0 \mu_r \cdot H \\ \phi &= B \times A = \frac{\mu_0 \mu_r \cdot H \cdot A}{l} = \frac{\mu_0 \mu_r NIA}{l} \end{aligned}$$

The denominator  $\frac{l}{A\mu_0 \mu_r}$  is called reluctance of the circuit

and  $NI$  is called mmf .

$$\phi = \frac{\text{mmf}}{\text{reluctance}} \text{ Wb}$$

this relation is similar to electric circuit  $I = V/R$



# Similarities between Magnetic Circuit & Electric Circuit

## Similarities

Analogies

1. The closed path for magnetic flux is called a magnetic circuit.

2. Flux,  $\phi = \frac{\text{m.m.f.}}{\text{reluctance}}$

3. m.m.f. (ampere-turns)

4. Reluctance,  $S = \frac{l}{a\mu_0\mu_r}$

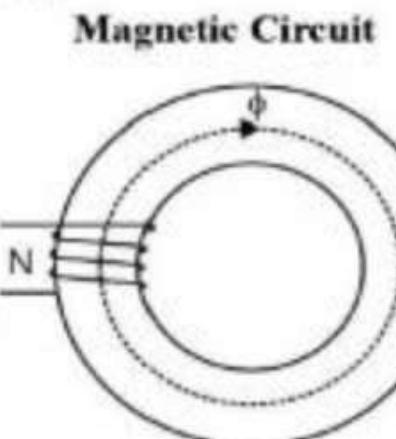
5. Flux density,  $B = \frac{\phi}{a} \text{ Wb/m}^2$

6. m.m.f. drop =  $\phi S$

7. Magnetic intensity,  $H = N I / l$

8. Permeance

9. Permeability



1. The closed path for electric current is called an electric circuit.

2. Current,  $I = \frac{\text{e.m.f.}}{\text{resistance}}$

3. e.m.f. (volts)

4. Resistance,  $R = \rho \frac{l}{a}$

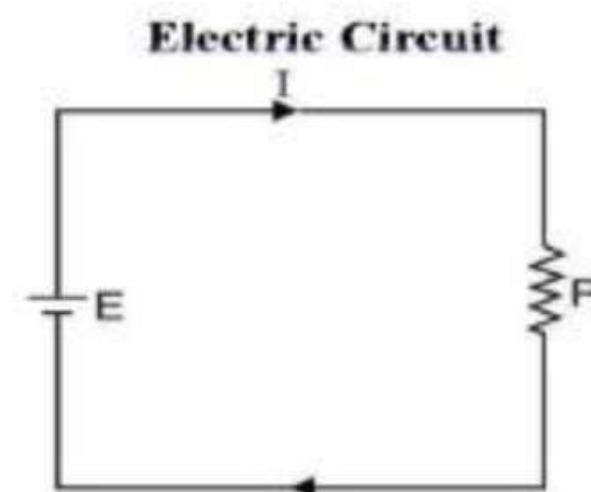
5. Current density,  $J = \frac{I}{a} \text{ A/m}^2$

6. Voltage drop =  $I R$

7. Electric intensity,  $E = V/d$

8. Conductance.

9. Conductivity



# Disimilarities between Magnetic Circuit & Electric Circuit

## Dissimilarities

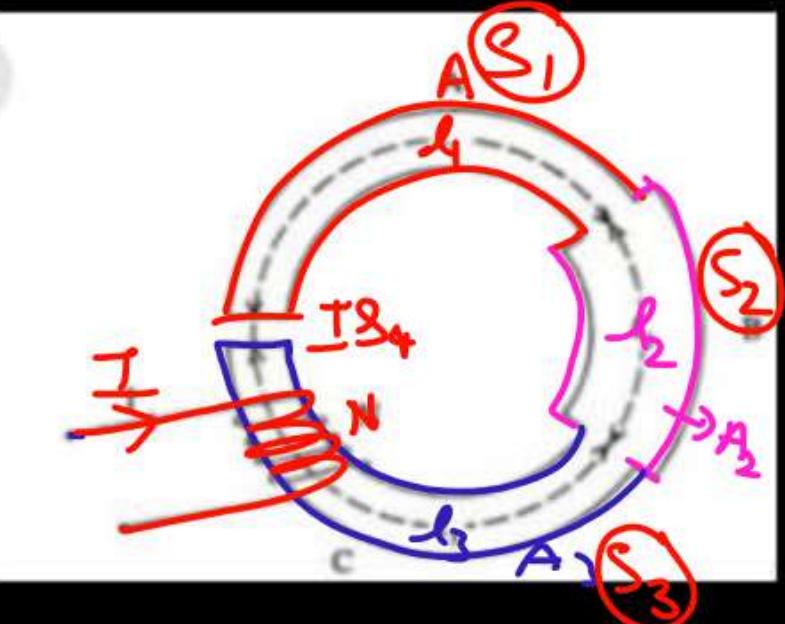


- |  |   |
|--|---|
| <p>1. Truly speaking, magnetic flux does not flow. <i>flux is setup in the Core</i>.</p> <p>2. <u>There is no magnetic insulator.</u> For example, flux can be set up even in air (the best known magnetic insulator) with reasonable m.m.f.</p> <p>3. The value of <math>\mu_r</math> is not constant for a given magnetic material. It varies considerably with flux density (<math>B</math>) in the material. This implies that reluctance of a magnetic circuit is not constant rather it depends upon <math>B</math>.</p> <p>4. <u>No energy is expended in a magnetic circuit.</u> In other words, energy is required in creating the flux, and not in maintaining it.</p> | <p>1. The electric current actually flows in an electric circuit. <del><math>I = 0</math></del></p> <p>2. <u>There are a number of electric insulators.</u> For instance, air is a very good insulator and current cannot pass through it.</p> <p>3. The value of resistivity (<math>\rho</math>) varies very slightly with temperature. Therefore, the resistance of an electric circuit is practically constant. This salient feature calls for different approach to the solution of magnetic and electric circuits.</p> <p>4. When current flows through an electric circuit, energy is expended so long as the current flows. The expended energy is dissipated in the form of heat.</p> |
|--|---|

## Alternating Quantity "Series Magnetic Circuit"

- **Series magnetic circuits** :- consider a circular ring made from different materials of lengths  $l_1, l_2$  and  $l_3$ , cross-sectional areas  $a_1, a_2$  and  $a_3$  and relative permeability  $\mu_{r1}, \mu_{r2}$  and  $\mu_{r3}$  respectively with a cut of length  $l_g$  called air gap. The total reluctance is the arithmetic sum of individual reluctance as they are joined in series.

$$S = \frac{l}{\mu_r A} \quad \text{①}$$



Total reluctance ( $S$ ) =  $\frac{l_1}{\mu_0 \mu_{r1} A_1} + \frac{l_2}{\mu_0 \mu_{r2} A_2} + \frac{l_3}{\mu_0 \mu_{r3} A_3} + \frac{l_g}{\mu_0 A_g}$

Total mmf =  $\phi \times S$

$$= \phi \left[ \frac{l_1}{\mu_0 \mu_{r1} A_1} + \frac{l_2}{\mu_0 \mu_{r2} A_2} + \frac{l_3}{\mu_0 \mu_{r3} A_3} + \frac{l_g}{\mu_0 A_g} \right]$$

or Total ampere – turns required

$$= H_1 l_1 + H_2 l_2 + H_3 l_3 + H_g l_g$$

$$\frac{l_1}{\mu_0 \mu_{r1} A_1} + \dots - \dots - \dots$$

$$R_r = 1$$

## (Parallel Magnetic Ckt)

A magnetic circuit which has more than one path for the magnetic flux is called as **parallel magnetic circuit**.

Consider a coil of  $N$  turns wound on limb BD carries an electric current of  $I$  amperes. The magnetic flux  $\phi$  set up by the coil divides at B into two paths. The magnetic flux  $\phi_2$  passes along the path BCD. The magnetic flux  $\phi_1$  passes along the path BAD.

Therefore, the total flux is,

$$\underline{\Phi = \phi_1 + \phi_2}$$

The path BD and BCD are in parallel and hence form a parallel magnetic circuit. In a parallel magnetic circuit, the MMF required for the whole parallel magnetic circuit is equal to MMF required for any one of the parallel paths.

Let

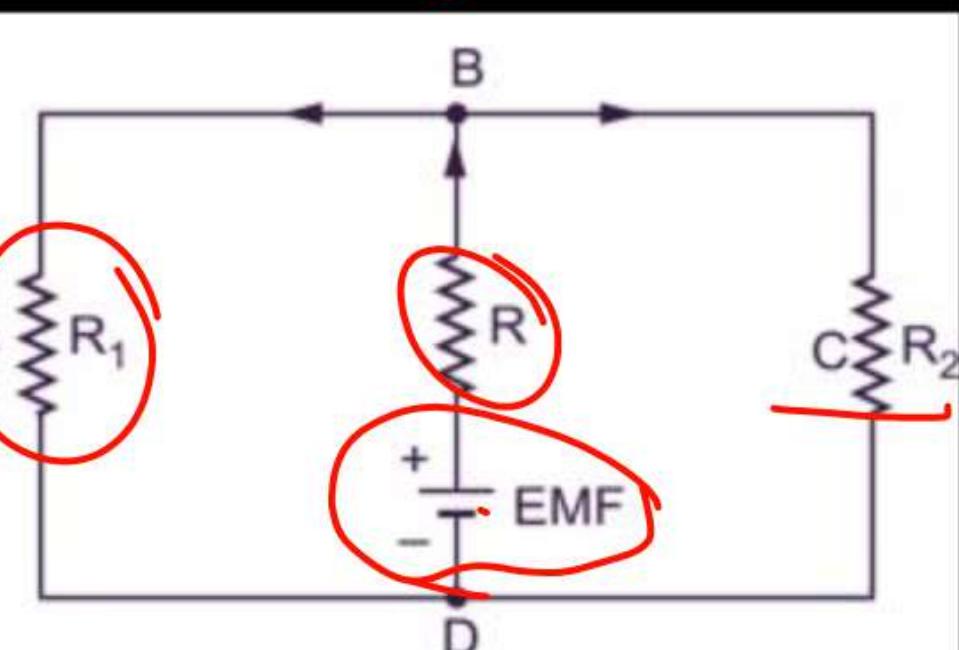
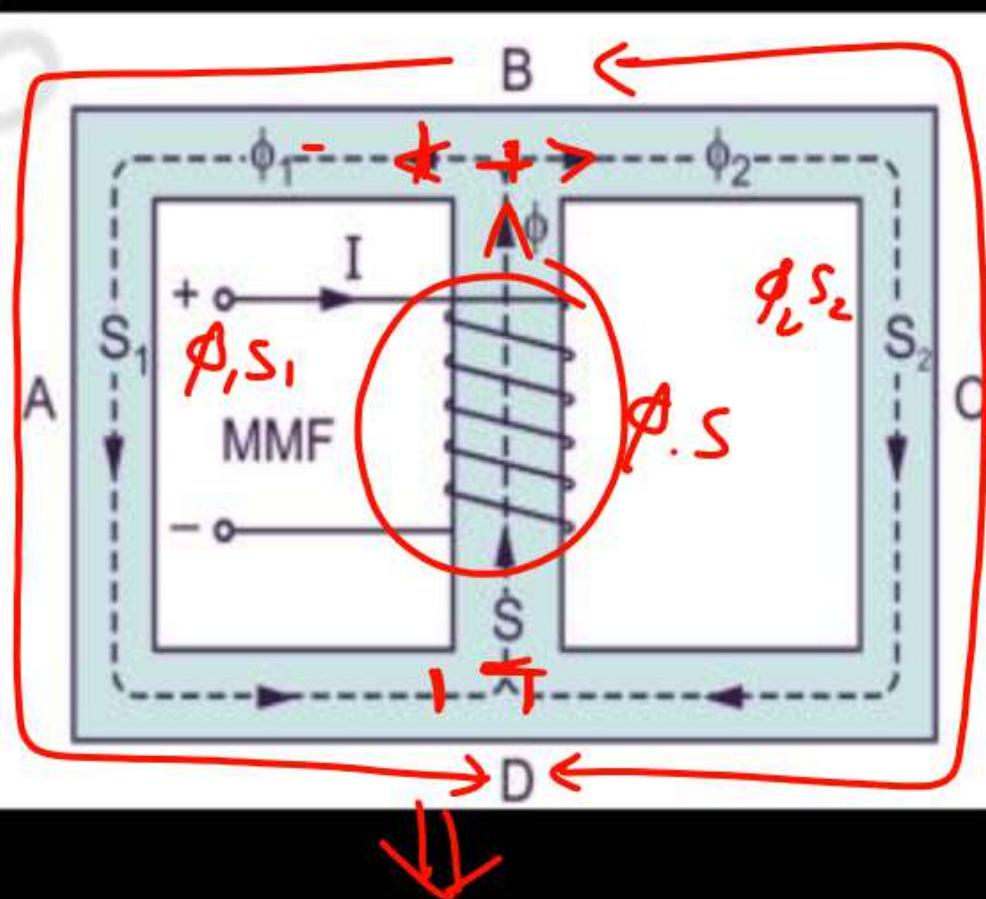
$S$  = Reluctance of magnetic path BD,  $S_1$  = Reluctance of magnetic path BAD

$S_2$  = Reluctance of magnetic path BCD

Therefore,

Total MMF = MMF for path ABD + MMF for path BD or BCD

$$\underline{\text{MMF} = \underline{\underline{\Phi \cdot S}} + \underline{\underline{\Phi_2 \cdot S_2}} = \underline{\underline{\Phi \cdot S}} + \underline{\underline{\Phi_1 \cdot S_1}}}$$



**Leakage Flux:-** The part of magnetic flux that does not follow the desired path in a magnetic circuit is known as *leakage flux*.

Flux can be divided into two main components

- magnetic flux throughout the magnetic circuit including air gap is known as **useful flux ( $\phi_g$ )**
- leakage flux** Link partially with magnetic circuit and complete its path through air.

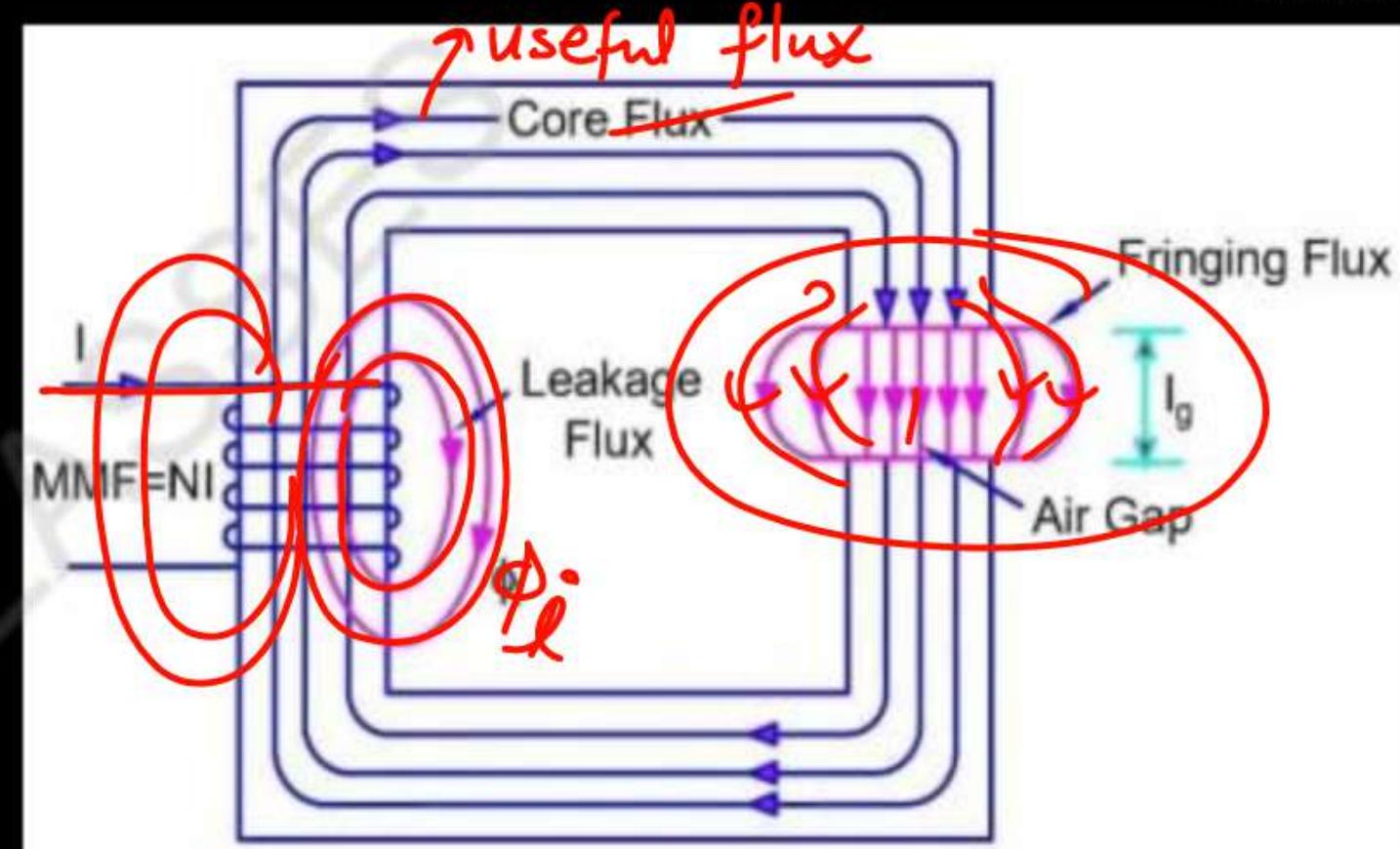
$$\text{Leakage Flux} = \text{Total flux} - \text{useful flux}$$

$$\Phi_{\text{leakage}} = \Phi_i - \Phi_g$$

$$\text{Leakage Coefficient, } \lambda = \frac{\text{Total Magnetic Flux } (\Phi_i)}{\text{Useful Magnetic Flux } (\Phi_g)}$$

**Magnetic Fringing:** When the magnetic field lines pass through an air gap, they tend to bulge out . It is because the magnetic field lines repel each other when passing through the air . This effect is known as *magnetic fringing*.

Due to magnetic fringing, the effective area of the air gap is increased and thus the magnetic flux density is decreased in the air gap. The longer the air gap, the higher is the fringing and *vice-versa*.



Ex.-1 :- A coil of 1000 turns is wound uniformly on an iron ring of mean circumference 50 cm and across sectional area 5 cm<sup>2</sup>. Current 12 Amp is flowing through coil. Relative permeability of the material is 4000. Find (i) MMF (ii) Total flux (iii) Reluctance. 2019-20

$$N = \overline{1000}, l = \overline{50 \text{ cm}}$$

$$a = 5 \text{ cm}^2, I = 12 \text{ amp}$$

$$\mu_r = 4000$$

$$\text{mmf} = NI = 1000 \times 12 = 12000 \text{ AT}$$

$$\phi = \frac{\text{mmf}}{S} = \frac{12000}{1.98 \times 10^{-5}} = 0.06 \text{ wb.}$$

$$S = \frac{1}{\mu_r \mu_0 I} = \frac{50 \times 10^{-2}}{5 \times 10^{-4} \times 4 \pi \times 10^{-7} \times 4000} = 1.98 \times 10^5$$

AS

**Ex-2** An electromagnet is shown in figure whose area of cross section is  $12\text{cm}^2$ . Mean length of iron path is  $50\text{cm}$ . It is excited by two coils each having 400 turns. When the current in the coil is  $1.0\text{ A}$ , the resulting flux density gives a relative permeability of  $1300$ . Calculate (i) reluctance of iron part, air gap and total reluctance.(ii) total flux(iii) flux density in air gap. 2018-19

$$\overline{A} = 12 \text{ cm}^2, l_i = 50 \text{ cm}$$

$$N = 2 \times 400 = 800$$

$$I = 1 \text{ A}, M_r = 1300$$

$$S_i = \frac{l_i}{A_i \cdot 4 \cdot \mu_0} = \frac{0.5}{12 \times 10^{-4} \times 4 \pi \times 10^{-7} \times 1300}$$

$$\boxed{S_i = 2.55 \times 10^5}$$

$$S_g = \frac{0.4 \times 10^{-2}}{12 \times 10^{-4} \times 4 \pi \times 10^{-7}}$$

$$= 2.65 \times 10^5$$

$$\text{Total } S = S_i + S_g$$

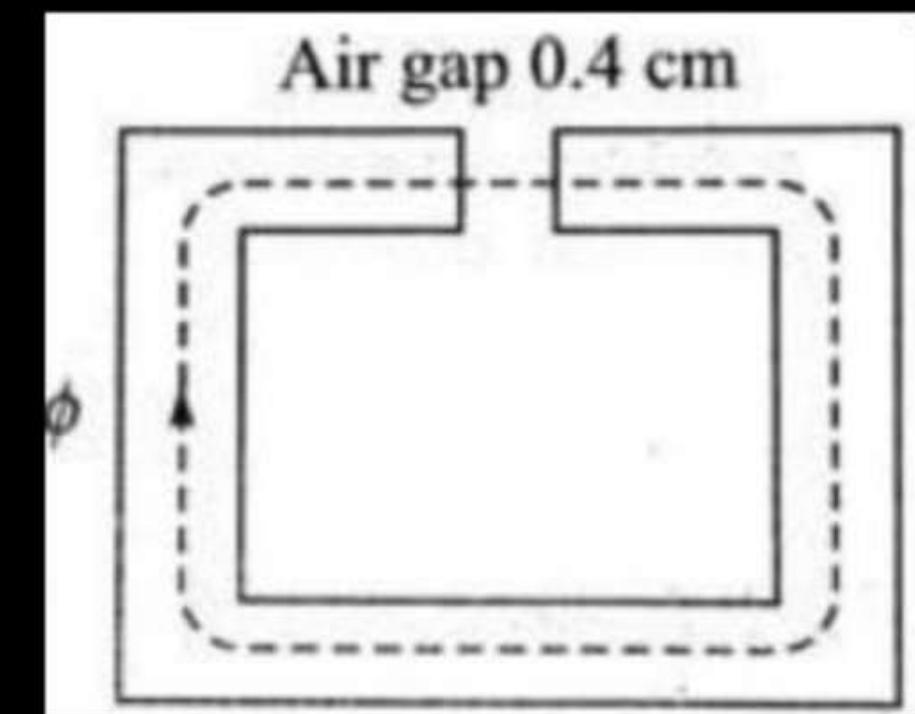
$$\boxed{S = 5.20 \times 10^5}$$

$$\phi = \frac{\text{mmf}}{S} = \frac{NI}{S}$$

$$= \frac{800 \times 1}{5.20 \times 10^5} = 15 \text{ mwb}$$

$$B = \frac{\phi}{A} = \frac{15 \text{ mwb}}{12 \times 10^{-4}}$$

$$= 1.25 \times 10 = 12.5$$



# Numerical Examples Magnetic Circuit

- Ex. 3 :- A cast steel magnetic structure made of a bar of section 8cm x 2 cm is shown in figure . Determine the current that the 500 turn magnetizing coil on the left limb should carry so that a flux of 2 m Wb is produced in the right limb. Take  $\mu_r = 600$  and neglect leakage.

$$A = 16 \text{ cm}^2, N = 500$$

$$\mu_r = 600, I = ?$$

$$\phi_1 S_1 = \phi_2 S_2$$

$$\phi_1 = \phi_2 \frac{S_2}{S_1}$$

$$= \frac{l_2}{\sigma_2 \mu_0 \mu_r} \frac{\sigma_1 \mu_0 \mu_r}{l_1}$$

$$\phi_1 = \phi_2 \frac{l_2}{l_1} = \frac{2 \times 10^{-3} \times 25 \times 10^{-2}}{18 \times 10^{-2}}$$

$$\phi = \frac{10}{3} \times 10^{-3} = 3.33 \times 10^{-3}$$

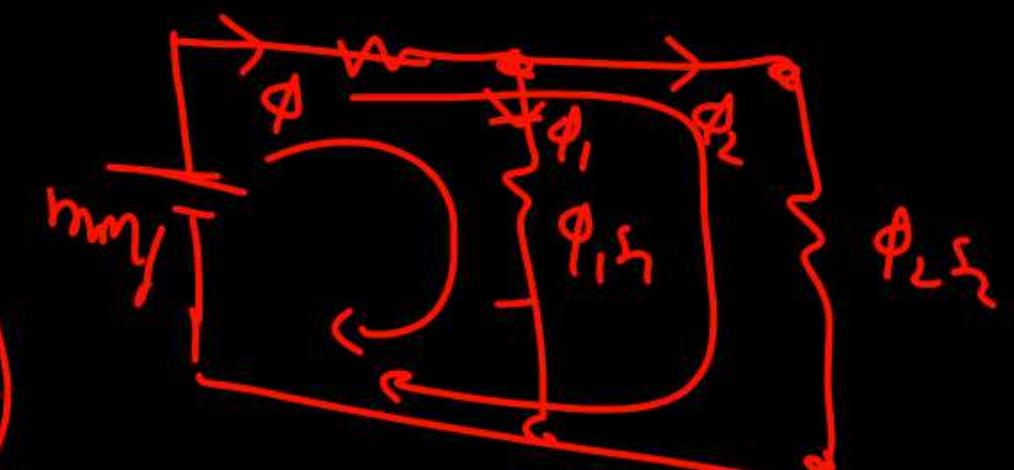
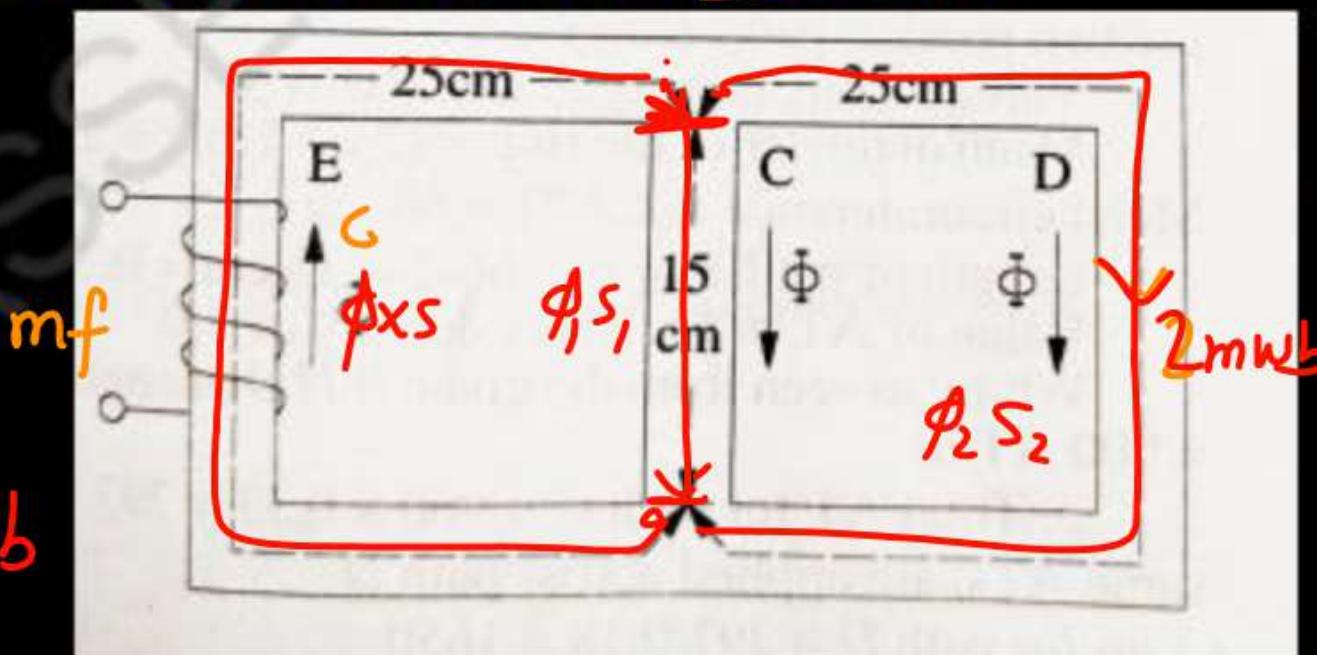
$$\phi = \phi_1 + \phi_2 = 2 + 3.33 = 5.33 \text{ mWb}$$

$$\text{mmf} = \phi \cdot S + \phi_1 S_1$$

$$= 5.33 \times 10^{-3} \left( \frac{l}{\sigma_1 \mu_0 \mu_r} \right) + 3.33 \times 10^{-3}$$

$$\frac{\text{mmf}}{I} = \frac{1508.65}{500} \left( \frac{l_1}{\sigma_1 \mu_0 \mu_r} \right)$$

Any



## Faraday's law of Electromagnetic Induction

**First law:** Whenever a conductor is placed in a varying magnetic field, EMF induces and this emf is called an induced emf and if the conductor is a closed circuit than the induced current flows through it.

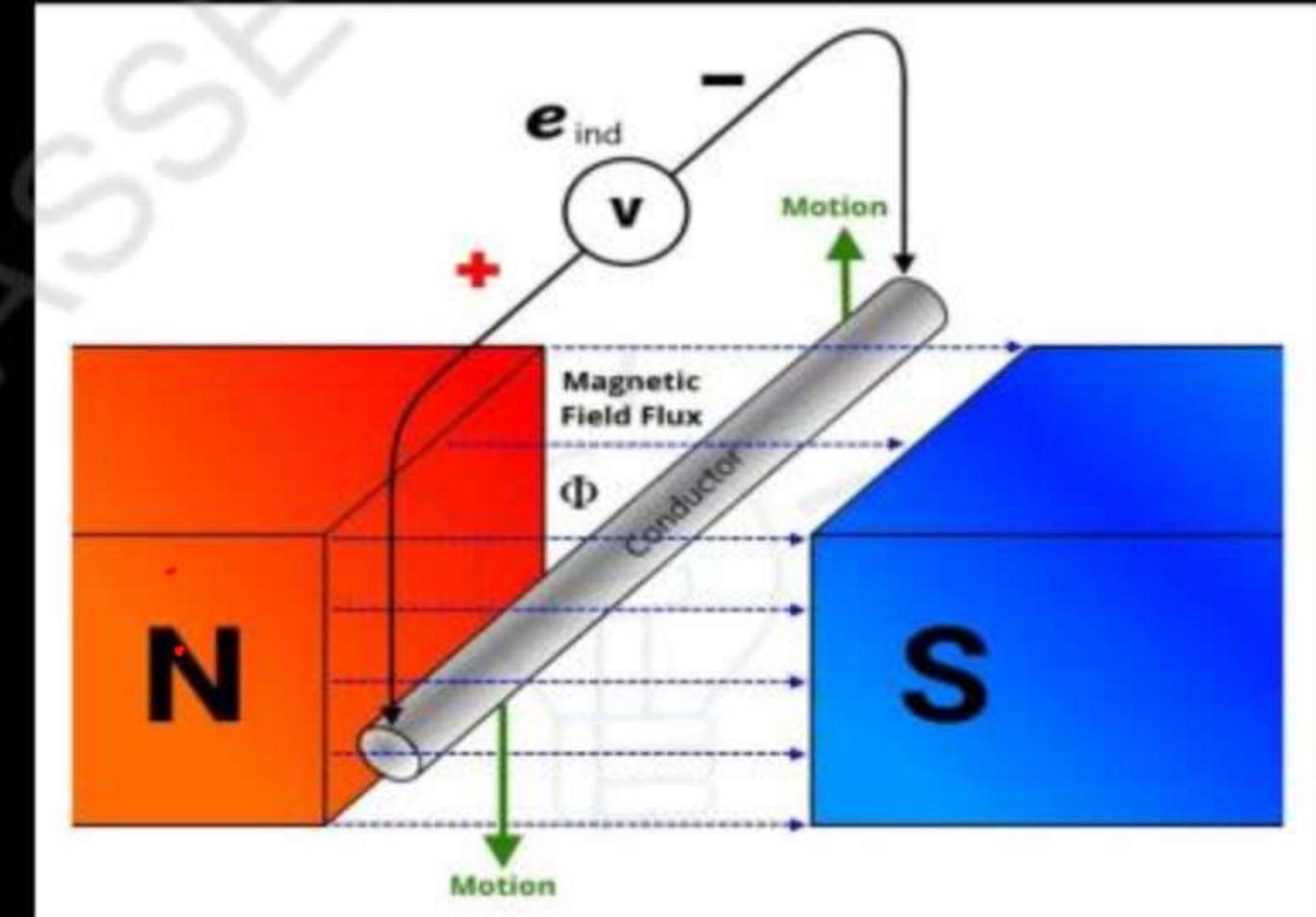
**Second law:** The magnitude of the induced EMF is equal to the rate of change of flux linkages.

Based on his experiments we now have Faraday's law of electromagnetic induction according to which the amount of voltage induced in a coil is proportional to the number of turns and the changing magnetic field of the coil.

So now, the induced voltage is as follows:

$$e = N \times d\Phi / dt$$

## Faraday's Laws of Electromagnetic Induction



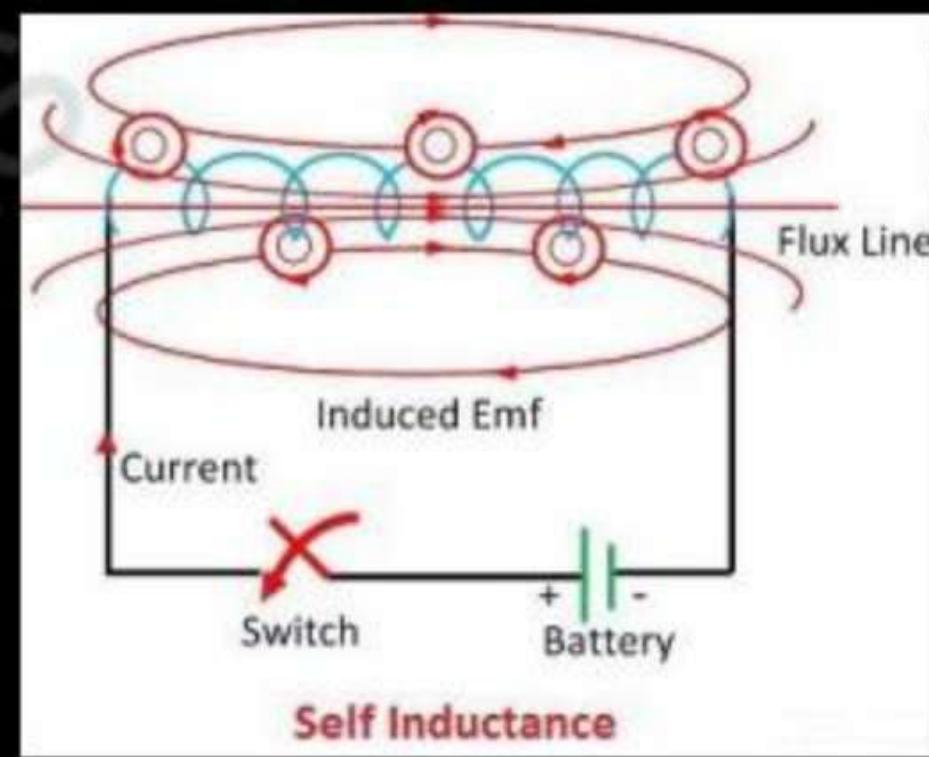
# Self and mutual Inductance

**Self-inductance :-** It is defined as the property of the coil due to which it opposes the change of current flowing through it. Inductance is attained by a coil due to the self-induced emf produced in the coil itself by changing the current flowing through it.

If the current in the coil is increasing, the self-induced emf produced in the coil will oppose the rise of current, that means the direction of the induced emf is opposite to the applied voltage

$$\checkmark e = L \frac{di}{dt}$$

$$L = \frac{e}{di/dt}$$

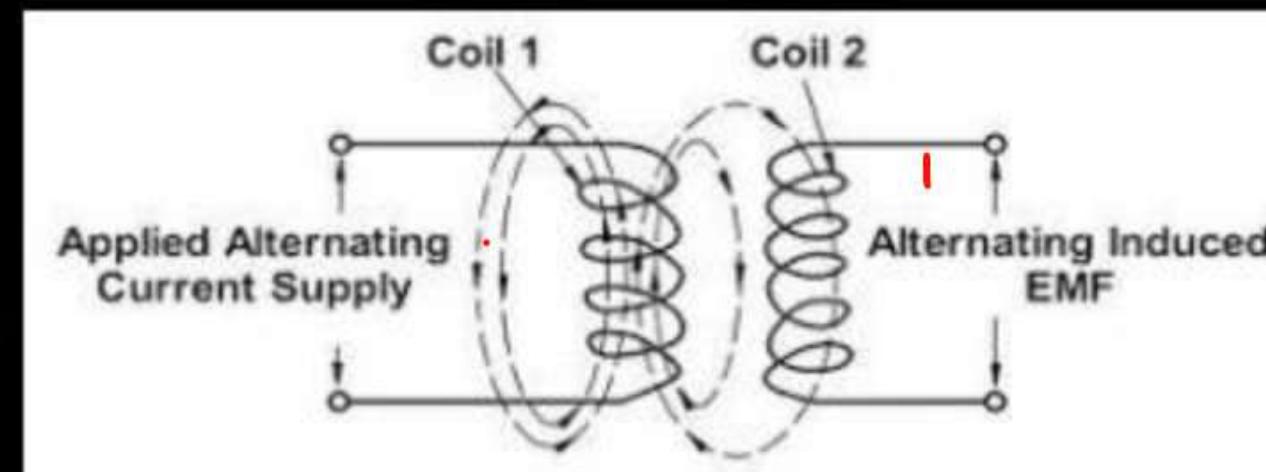


**Mutual Inductance** between the two coils is defined as the property of the coil due to which it opposes the change of current in the other coil, or you can say in the neighboring coil.

When the current in the neighboring coil changes, the flux sets up in the coil and because of this, changing flux emf is induced in the coil called Mutually Induced emf and the phenomenon is known as **Mutual Inductance**.

$$e_m = M \frac{di_1}{dt}$$

$$M = \frac{e_m}{di_1/dt} \dots\dots\dots(1)$$

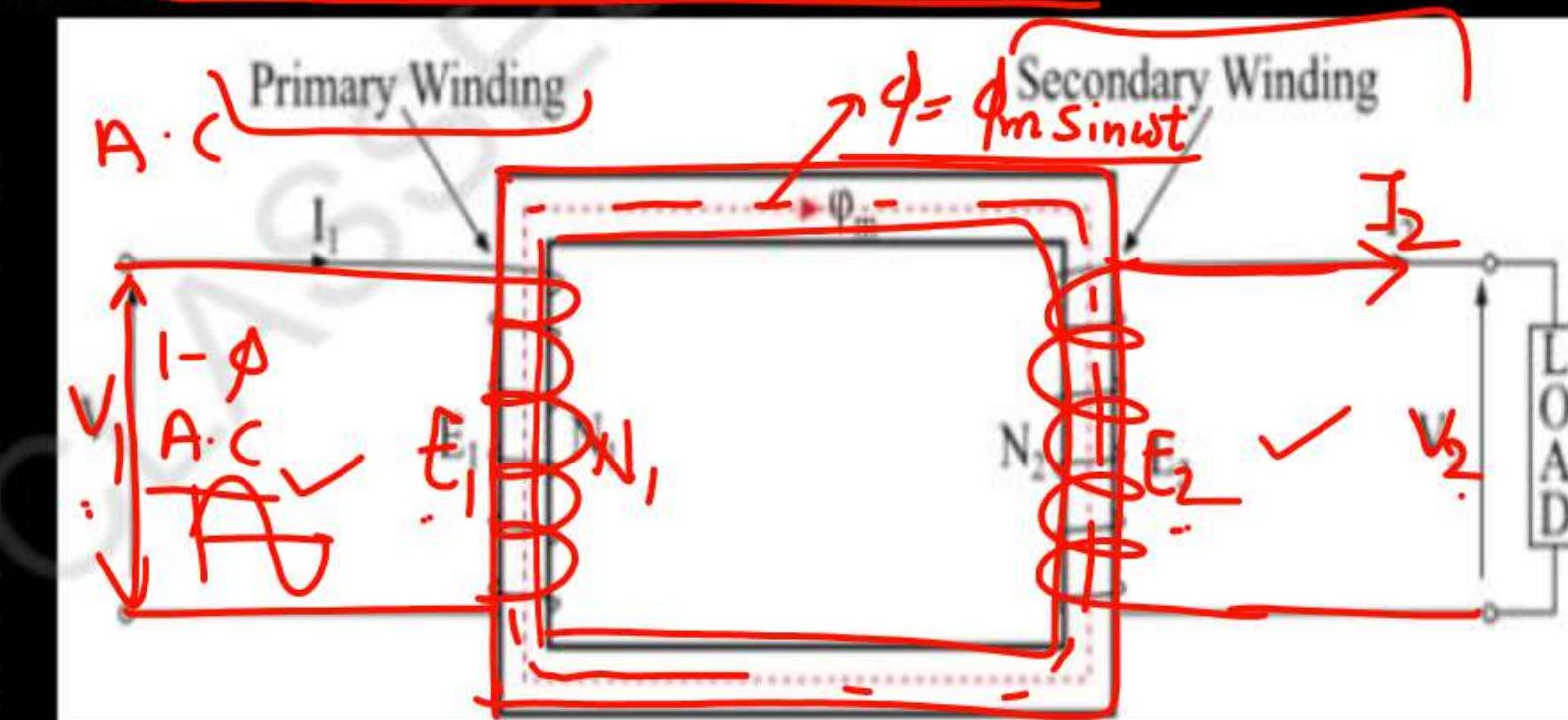


# Transformer

A transformer is a static electrical machine which is used for either increasing or decreasing the voltage level of the AC supply with a corresponding decrease or increase in the current at constant frequency.

## Working Principle of Transformer

- The **basic principle behind working of a transformer** is the phenomenon of mutual induction between two windings linked by common magnetic flux.
- Transformer consists of two inductive coils; primary winding and secondary winding.
- When, primary winding is connected to a source of alternating voltage, alternating magnetic flux is produced around the winding.
- The core provides magnetic path for the flux, to get linked with the secondary winding.
- As the flux produced is alternating, EMF gets induced in the secondary winding according to Faraday's law of electromagnetic induction.
- This emf is called 'mutually induced emf', and the frequency of mutually induced emf is same as that of supplied emf.
- If the secondary winding is closed circuit, then mutually induced current flows through it, and hence the electrical energy is transferred from one circuit (primary) to another circuit (secondary).



# Transformer ( Turns Ratio)

$$E_1 = -N_1 \frac{d\phi_m}{dt}$$

and

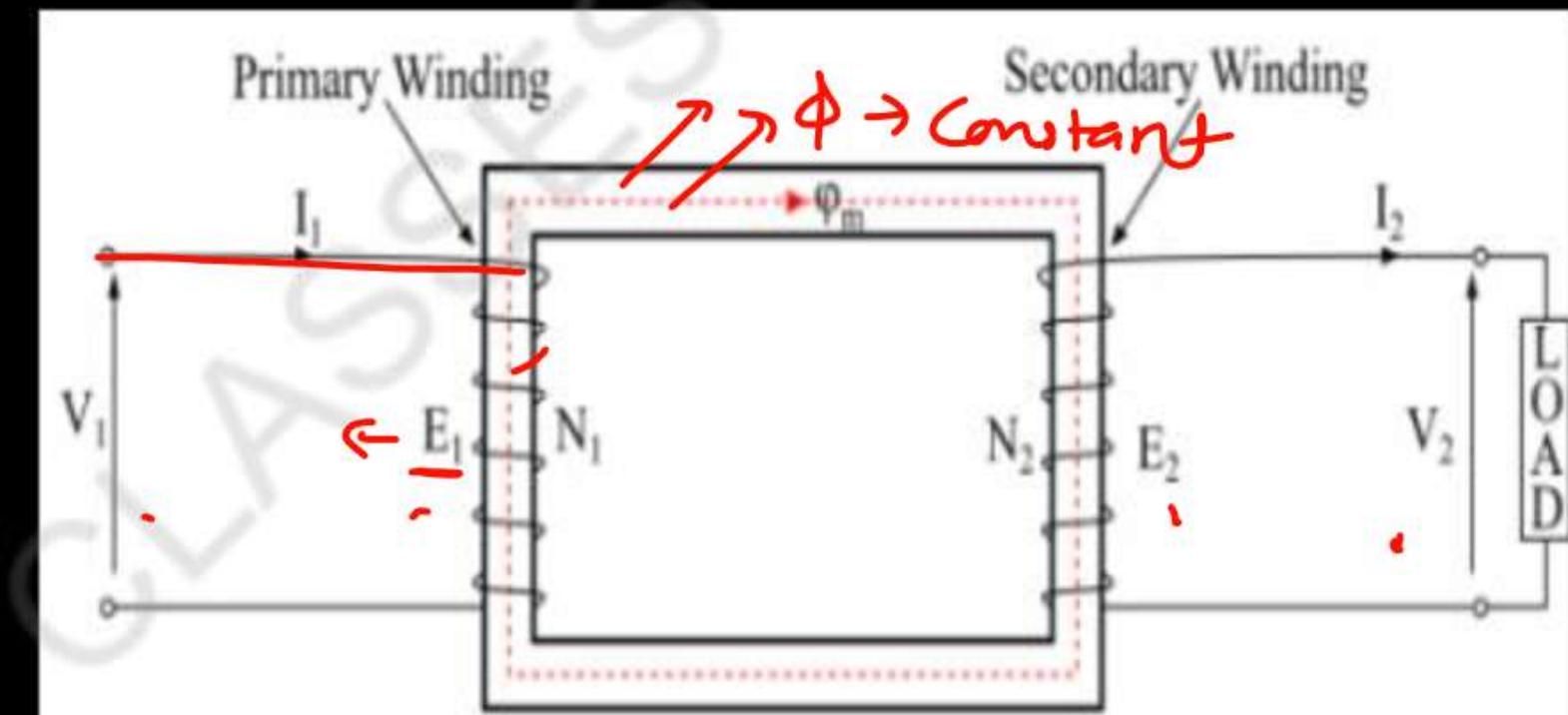
$$E_2 = -N_2 \frac{d\phi_m}{dt}$$

Therefore

$$\frac{E_2}{E_1} = \frac{N_2}{N_1}$$

$$\frac{E_2}{E_1} = \frac{N_2}{N_1} = K$$

$$K = \frac{I_1}{I_2} = \frac{N_2}{N_1}, \frac{V_2}{V_1}, \frac{E_2}{E_1}$$



Imp 2 mark  
Can Transformer work on DC

No

$\Phi = \text{constant}$

$$E = \Phi$$

Transformer will not work.

Transformers can be classified on different basis, like types of construction, types of cooling etc.

On the basis of construction

- Core type
- Shell type

On the basis of their purpose

- Step up  $V_2 > V_1$
- Step down  $V_2 < V_1$

On the basis of type of supply



## Classification of Transformer based on Construction

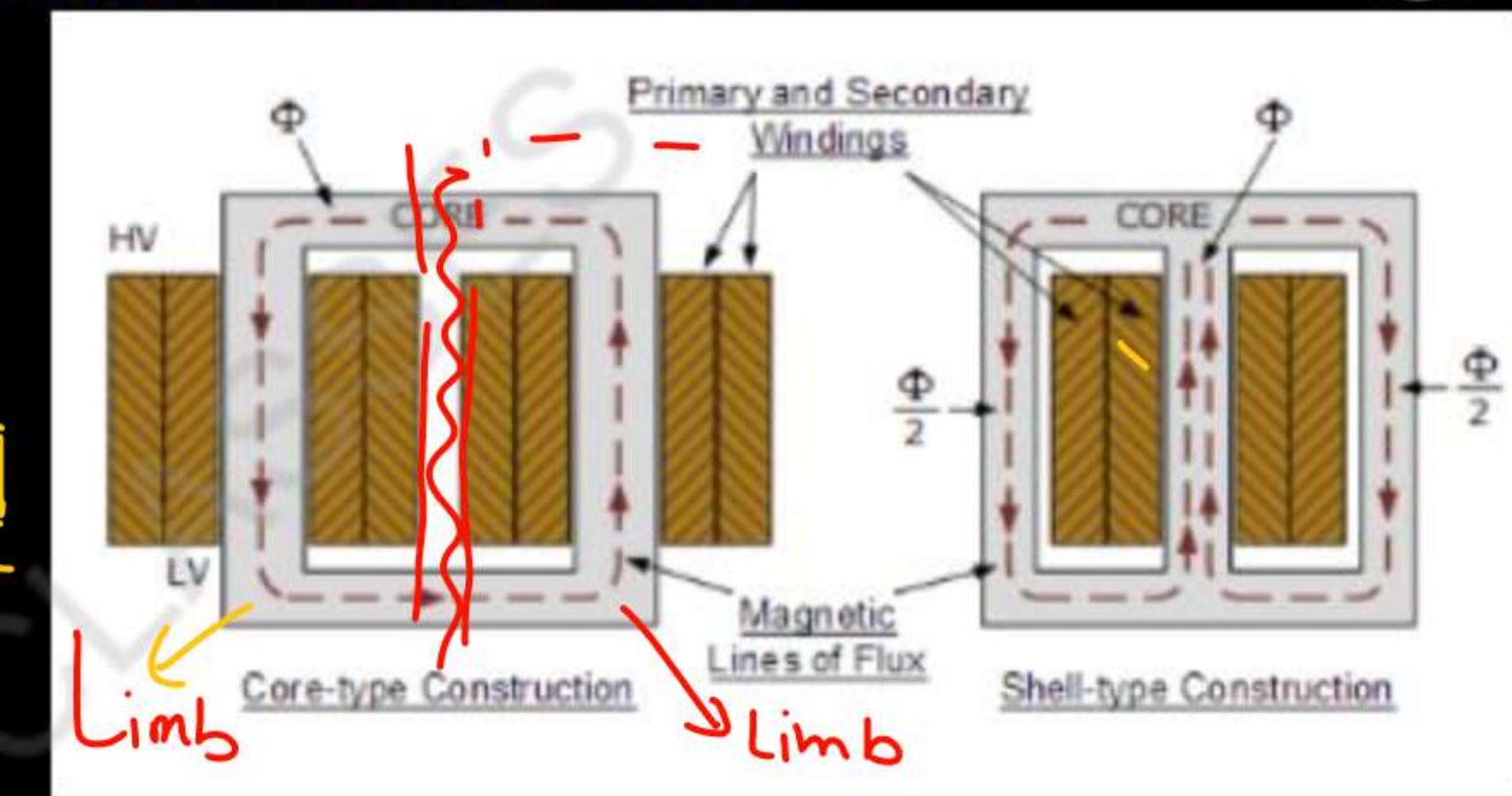
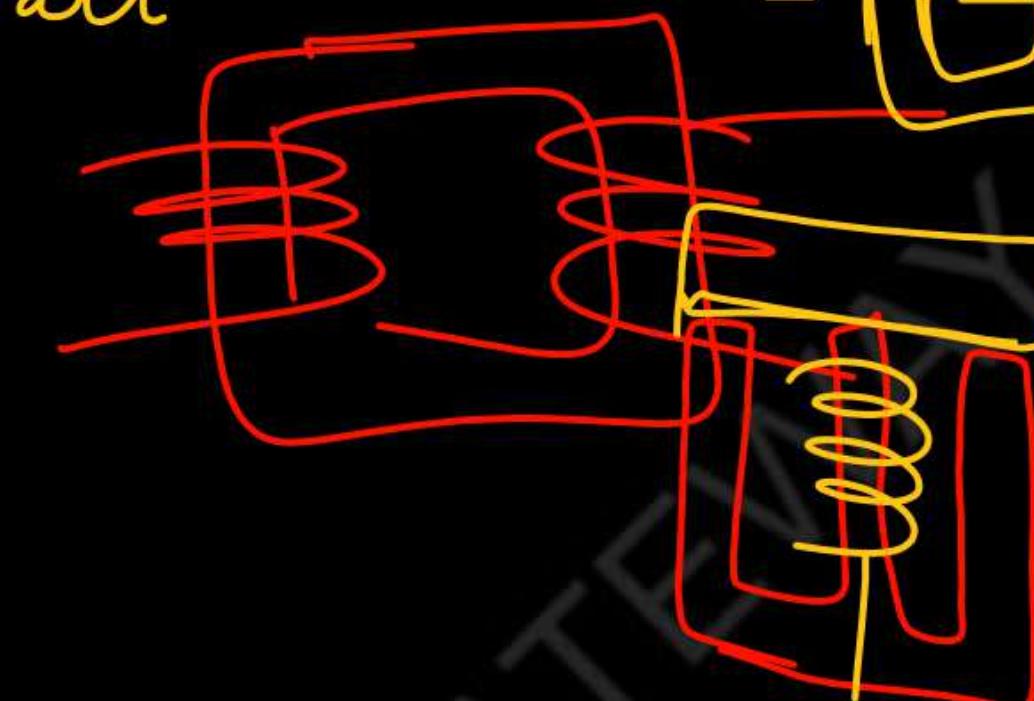
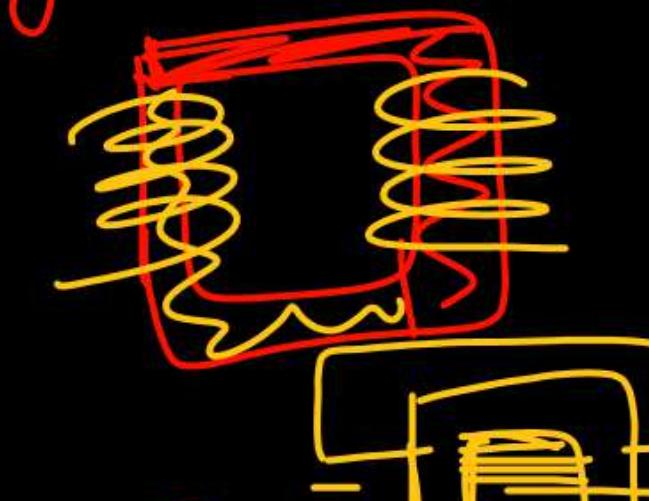
- 1. Core type transformer:

Considerable Part of Core.

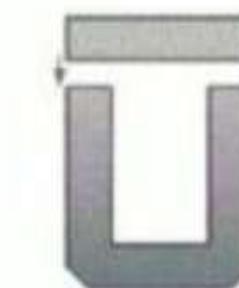
- 2. Shell-type transformer:

Core surrounds a  
Considerable part  
of winding.

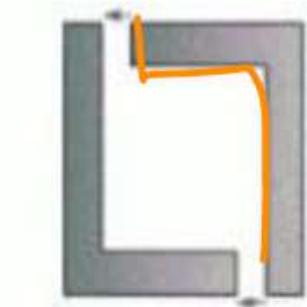
Winding Surrounds a



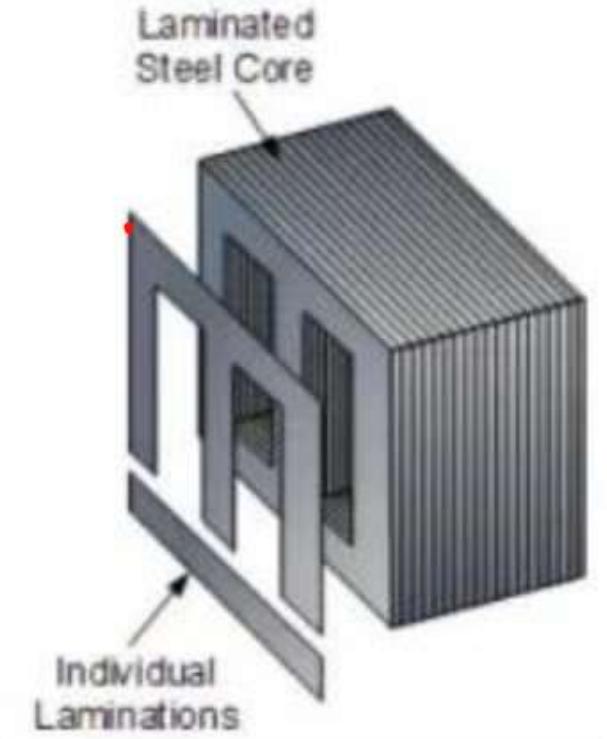
Core type Laminations



"U - I" laminations



"L" laminations



# E.M.F. Equation of Transformer

$$\phi = \phi_m \sin \omega t$$

E.m.f induced

$$E_1 = -N_1 \frac{d\phi}{dt}$$

$$= -N_1 \frac{d}{dt}(\phi_m \sin \omega t)$$

$$= -N_1 \phi_m \omega \cos \omega t$$

$$e_1 = -N_1 \phi_m \omega \sin\left(\omega t - \frac{\pi}{2}\right)$$

$$E_1 = E_m \sin \omega t$$

on comparing

$$E_m = N_1 \phi_m \omega$$

→ Standard Equation

$$E_{1,lm} = \frac{E_m}{\sqrt{2}}$$

$$E_1 = \frac{N_1 \phi_m \omega}{\sqrt{2}}$$

$$= \frac{N_1 \phi_m 2\pi f}{\sqrt{2}}$$

$$E_1 = N_1 \phi_m F \cdot \sqrt{2} \pi$$

$$E_1 = 4.44 N_1 \phi_m f$$

$$E_2 = 4.44 N_2 \phi_m f$$

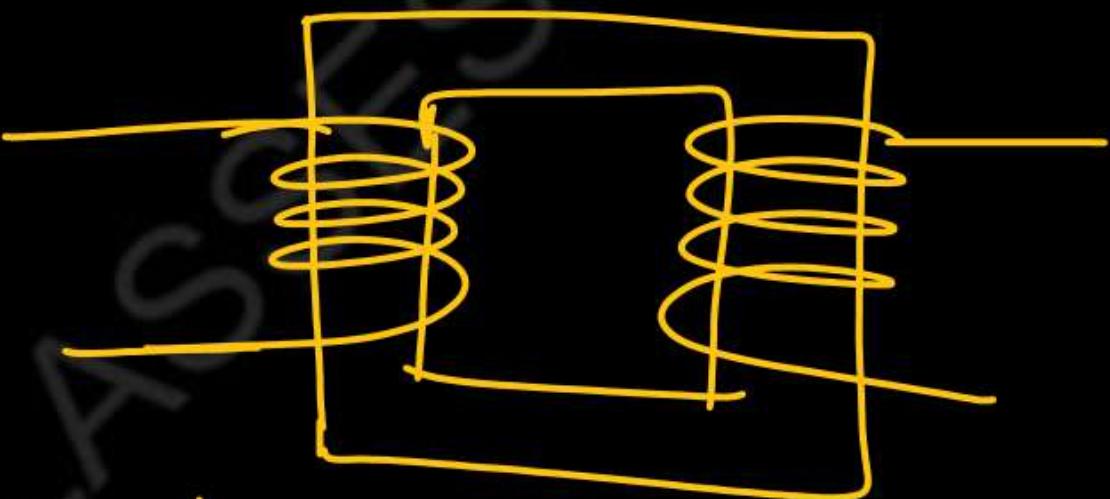
## Rating of Transformer

→ Core loss  $\rightarrow \propto V^2$        $V_{\text{old}}$

→ Copper loss  $\rightarrow I - V_{\text{imp}}$

Rating = KVA

# Ideal and Practical Transformer



Losses = 0

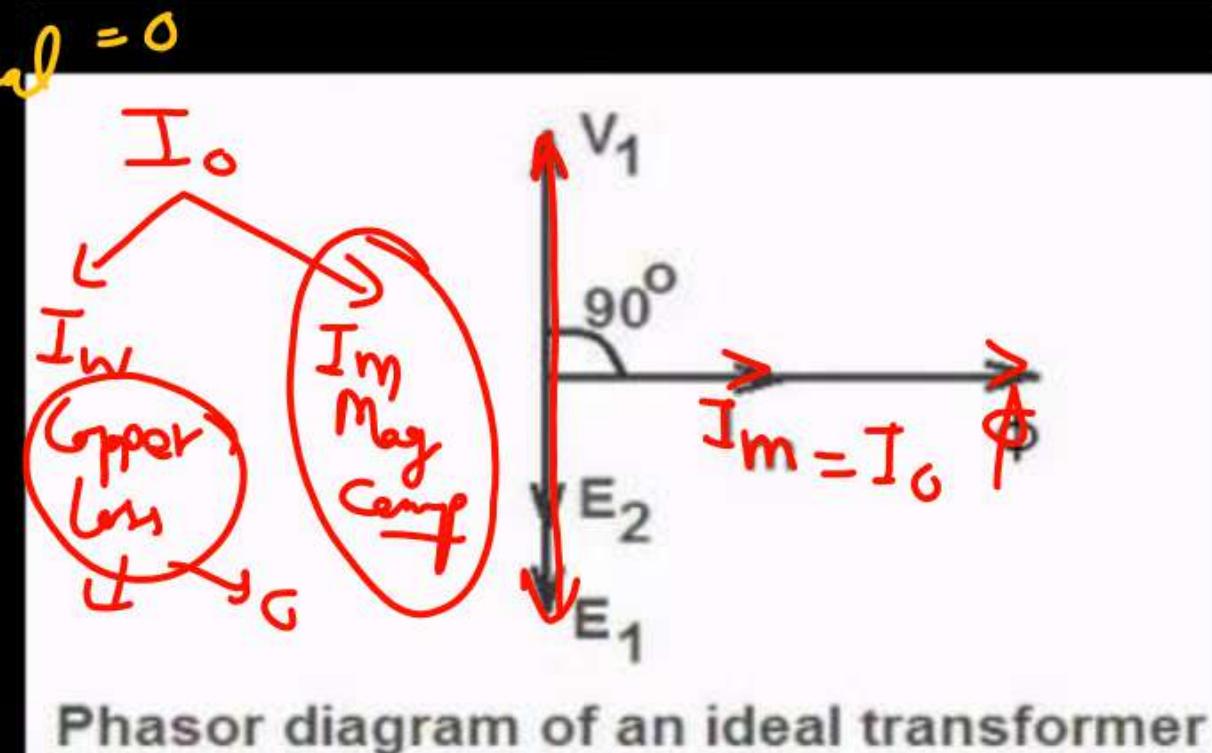
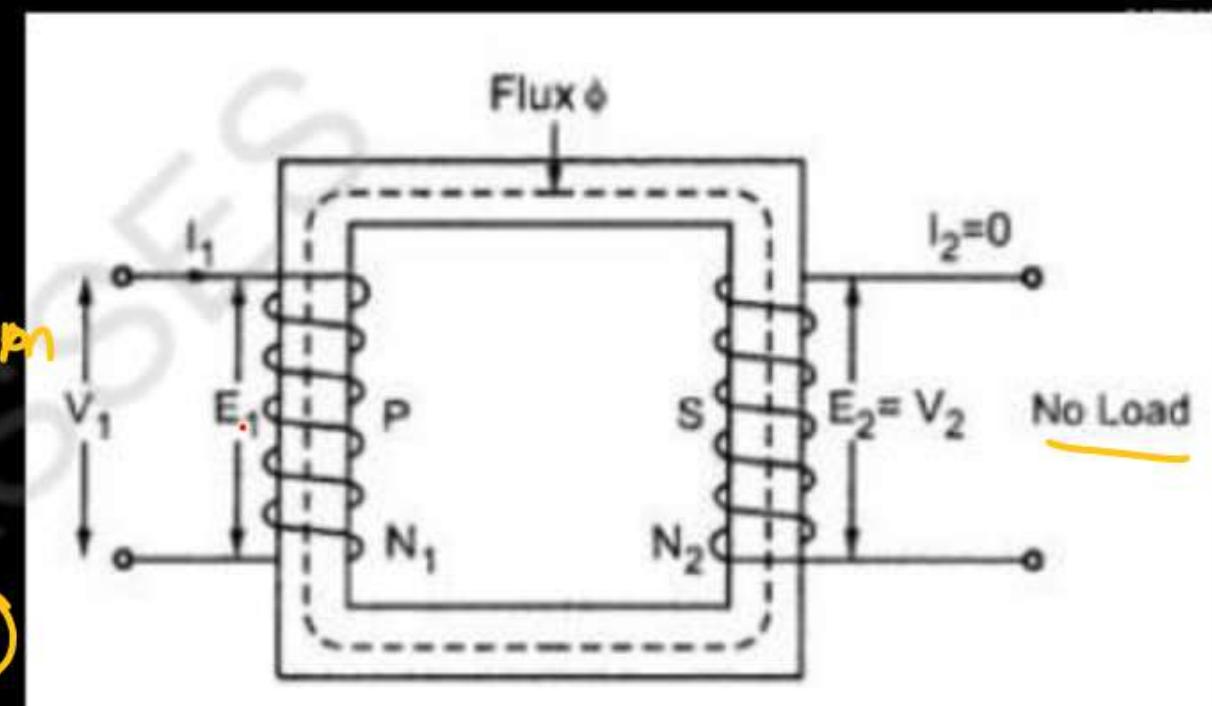
Ideal

Practical  
Losses  $\rightarrow \swarrow$

## Ideal Transformer on no load

- The primary draws a very small current  $I_1$  which is just necessary to produce flux in the core. As it is magnetizing the core, it is called **magnetizing current denoted as  $I_m$** .
- As the transformer is ideal, the winding reactance is zero and it is purely inductive in nature.
- The magnetizing current is very small and lags  $V_1$  by  $90^\circ$  as the winding is purely inductive. This  $I_m$  produces an alternating flux  $\Phi$  which is in phase with  $I_m$ .
- The flux links with both the winding producing the induced  $i_{ideal} = 0$  emf  $E_1$  and  $E_2$ , in the primary and secondary windings respectively.
- According to Lenz's law, the induced emf opposes the cause producing it which is supply voltage  $V_1$ . Hence  $E_1$  is in antiphase with  $V_1$  but equal in magnitude.
- The induced emf  $E_2$  also opposes  $V_1$  hence in antiphase with  $V_1$  but its magnitude depends on  $N_2$ . Thus  $E_1$  and  $E_2$  are in phase.

**No Load Current**



Phasor diagram of an ideal transformer

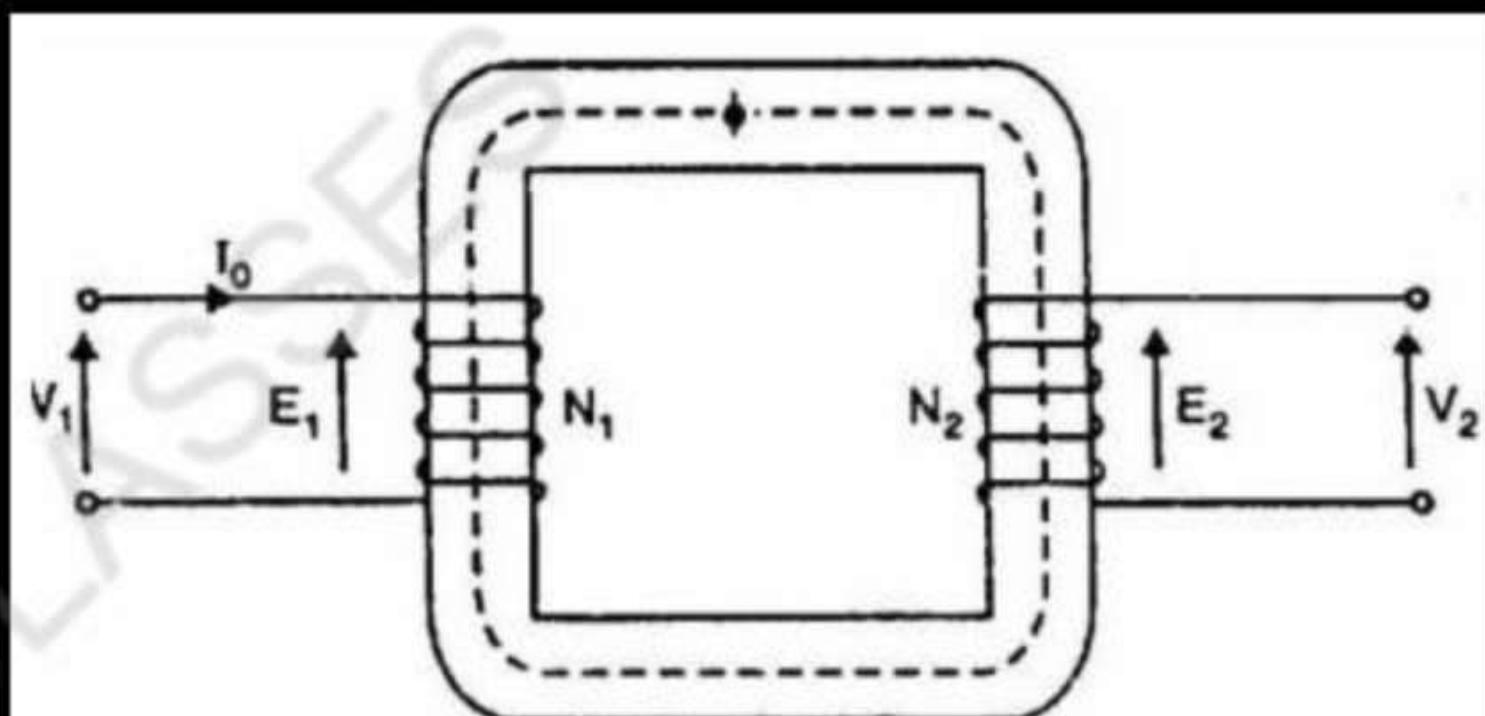
# Practical Transformer on no load

The no-load current consists of two components:

**Reactive or magnetizing component  $I_m$ :**- It produces flux in the core

**Active or power component  $I_w$ :**- It supplies small amount of primary copper loss.

Hence the primary no load current  $I_0$  is not  $90^\circ$  behind the applied voltage  $V_1$  but lags it by an angle  $\Phi_0 < 90^\circ$  as shown in the phasor diagram.



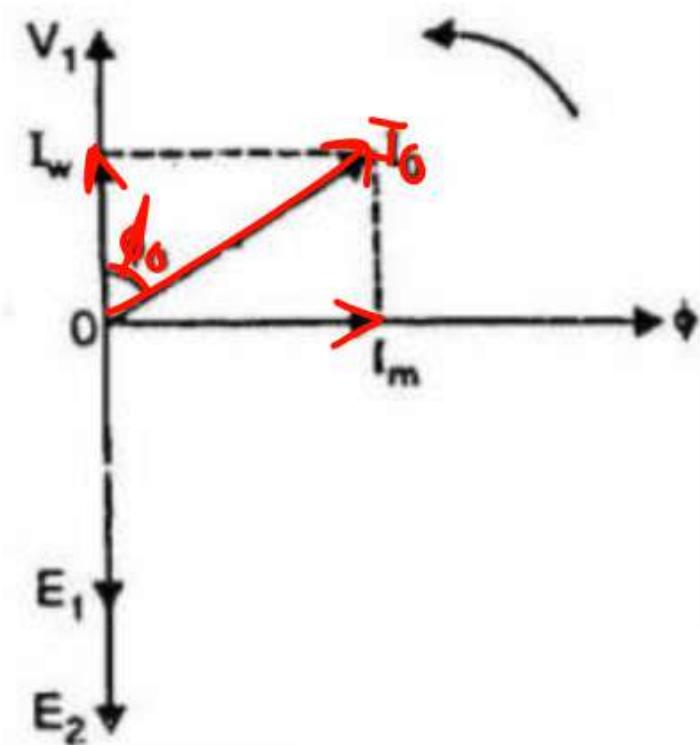
Working component  $I_w = I_0 \cos \varphi_0$

No load current  $I_0 = \sqrt{I_w^2 + I_m^2}$

Magnetizing component  $I_m = I_0 \sin \varphi_0$

Power factor  $\cos \varphi_0 = \frac{I_w}{I_0}$

No load power input  $P_0 = V_1 I_0 \cos \varphi_0$



## Practical Transformer on no load

Ex.1 A 25 KVA, 3300/230V, 50 Hz, 1 phase transformer draws no load current of 15 A when excited on load voltage side and consumes 350 watts. Calculate two components of current . Aktu – 2003-04

$$I_o = 15 \text{ A} \quad , P = 350 \text{ watt}$$

$$P = V_i I_o \cos \phi_o \quad , \quad \cos \phi_o = \frac{P}{V_i I_o}$$

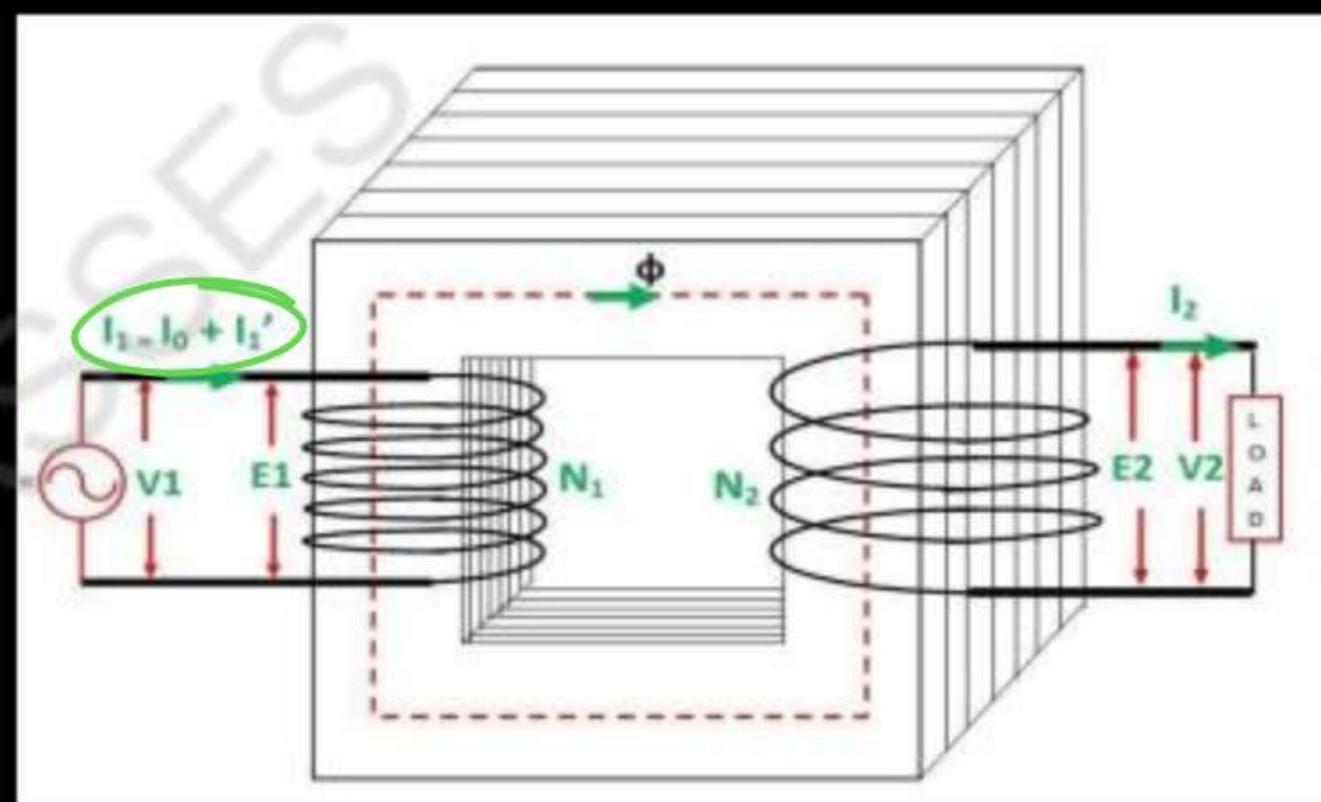
$$\cos \phi_o : \frac{350}{230 \times 15} = 0.1014$$

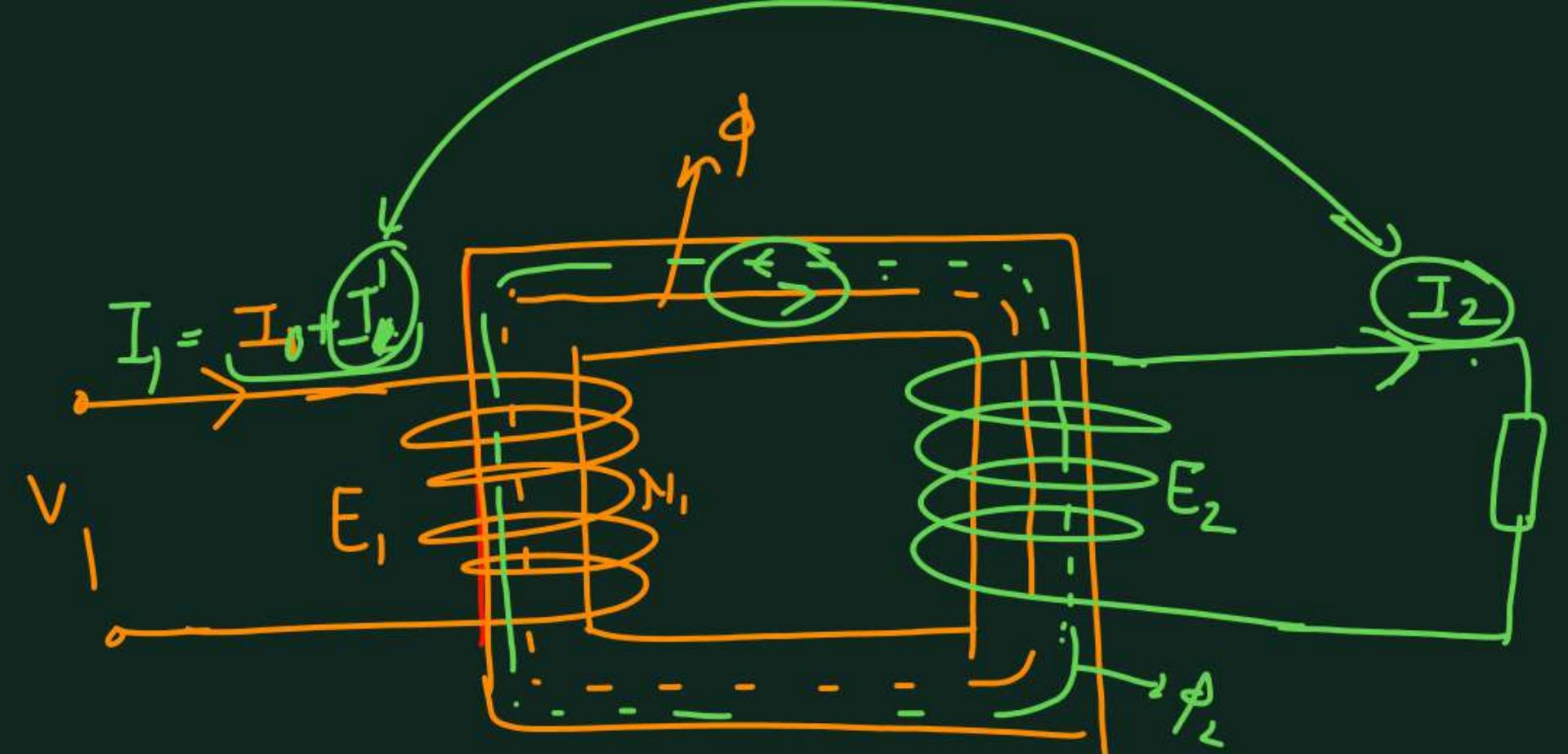
$$I_w = I_o \cos \phi_o = 15 \times 0.1014 =$$

$$I_m = I_o \sin \phi_o = 15 \times 0.9948 =$$

# Transformer on Load

- When the secondary is kept open, it draws the no-load current from the main supply. The no-load current induces the mmf  $N_0I_0$  and this force set up the flux  $\Phi$  in the core.
- When the load is connected to the secondary of the transformer,  $I_2$  current flows through their secondary winding. The secondary current induces the mmf  $N_2I_2$  on the secondary winding of the transformer. This force set up the flux  $\Phi_2$  in the transformer core. The flux  $\Phi_2$  opposes the flux  $\Phi$ , according to Lenz's law.
- flux  $\Phi_2$  opposes the flux  $\Phi$ , the resultant flux of the transformer decreases and this flux reduces the induced EMF  $E_1$ . Thus, the strength of  $V_1$  is more than  $E_1$  and an additional primary current  $I'_1$  drawn from the mains.
- The additional current is used for restoring the original value of the flux in the core of the transformer so that  $V_1 = E_1$ . The primary current  $I'_1$  is in phase opposition with the secondary current  $I_2$ .
- The additional current  $I'_1$  induces the mmf  $N_1I'_1$ . And this force set up the flux  $\Phi'_1$ . The direction of the flux is the same as that of the  $\Phi$  and it cancels the flux  $\Phi_2$  which induces because of the MMF  $N_2I_2$ .





# Transformer on Load

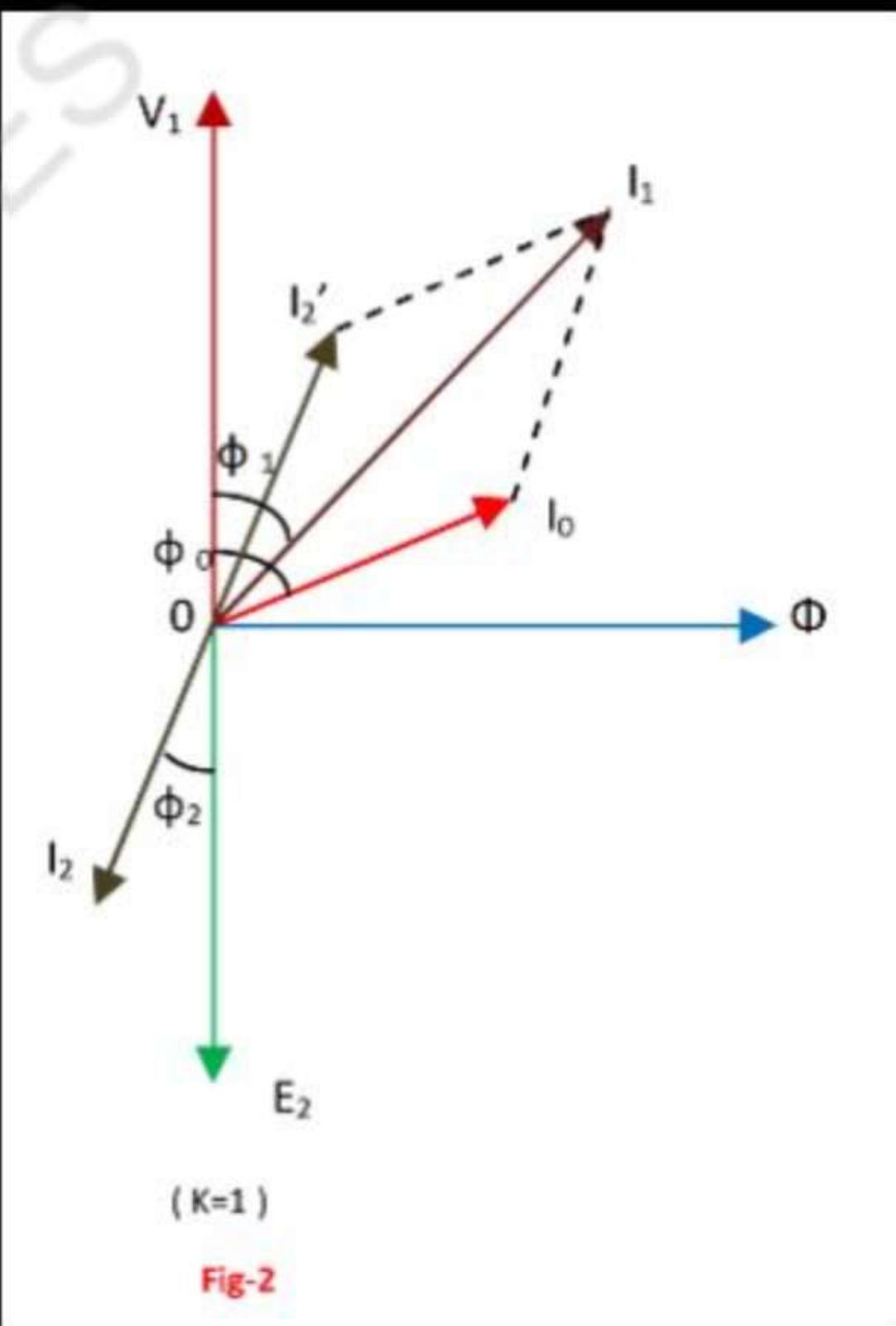
- Now,  $N_1 I_1' = N_2 I_2$

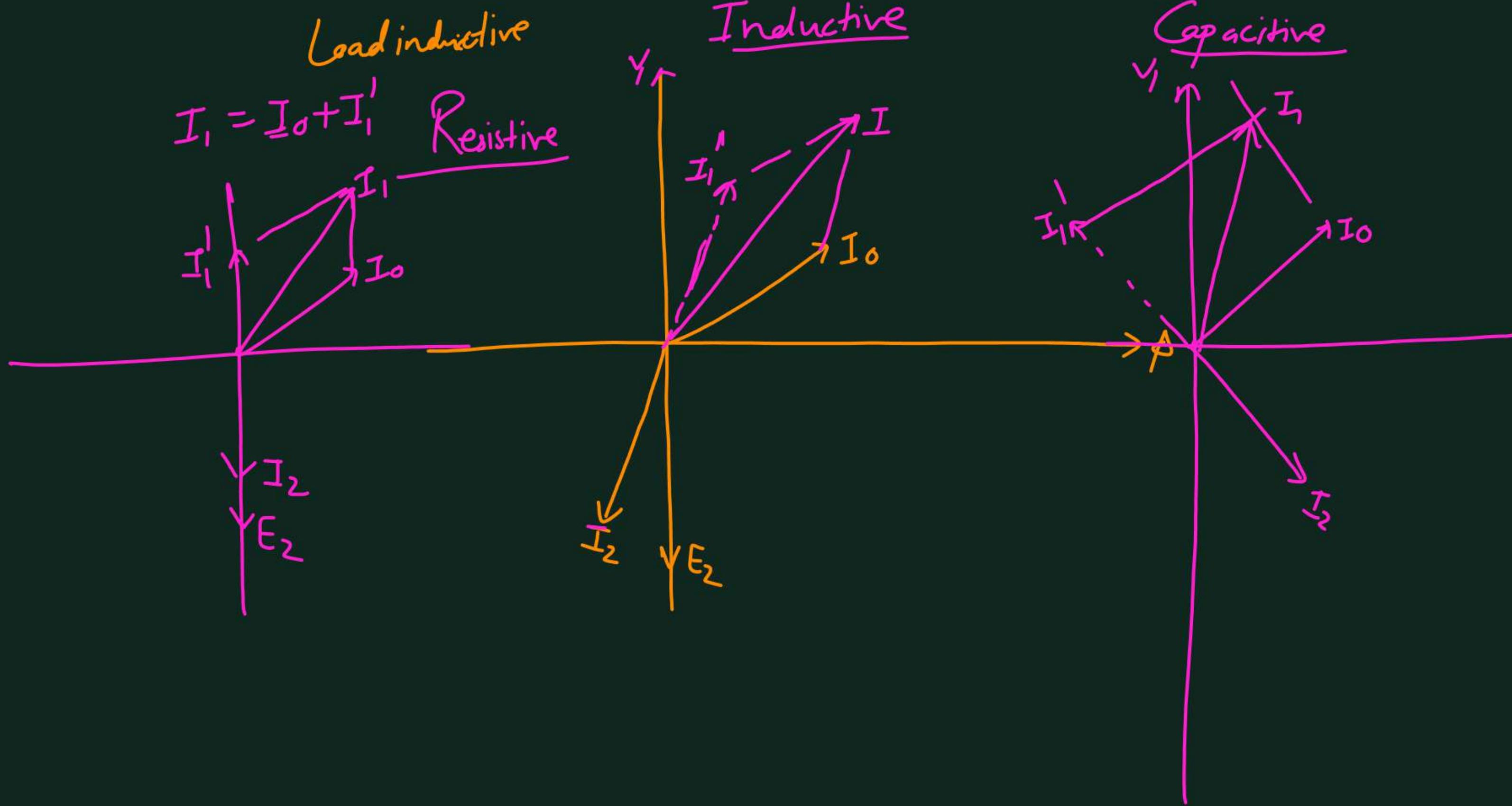
Therefore,

$$I_1' = \left(\frac{N_2}{N_1}\right) I_2 = K I_2$$

- The phase difference between  $V_1$  and  $I_1$  gives the power factor angle  $\phi_1$  of the primary side of the transformer.
- The power factor of the secondary side depends upon the type of load connected to the transformer.
- The total primary current  $I_1$  is the vector sum of the currents  $I_0$  and  $I_1'$ .

$$\bar{I}_1 = \bar{I}_0 + \bar{I}_1'$$



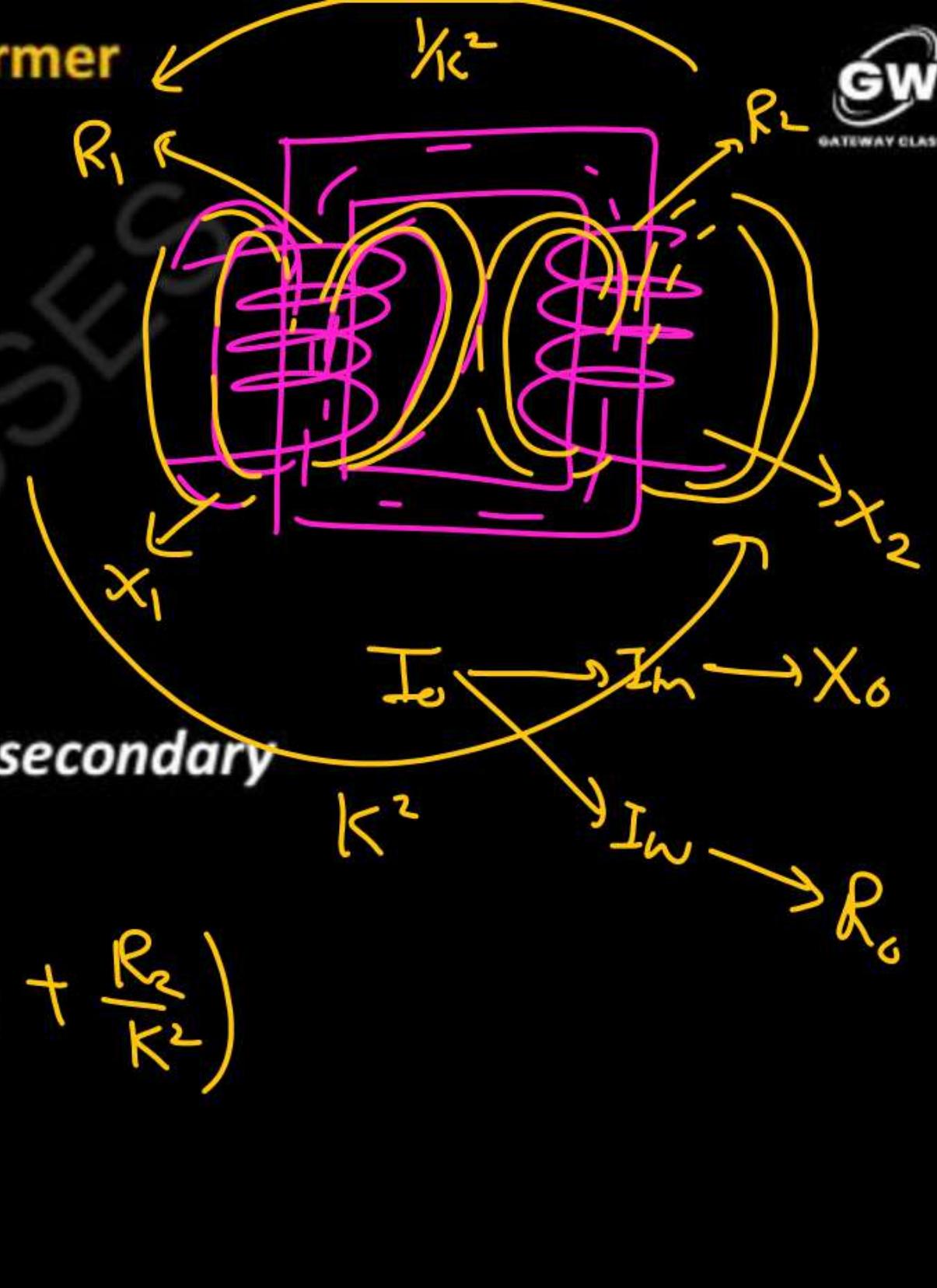


# Equivalent circuit of Transformer

**Concept of Leakage reactance:-**

Primary  
 $R_1 \rightarrow$  Resi  
 $X_1 \rightarrow$  leakage  
 React.

Secondary  
 $R_L =$  Resistance  
 $X_L =$  leakage  
 React.

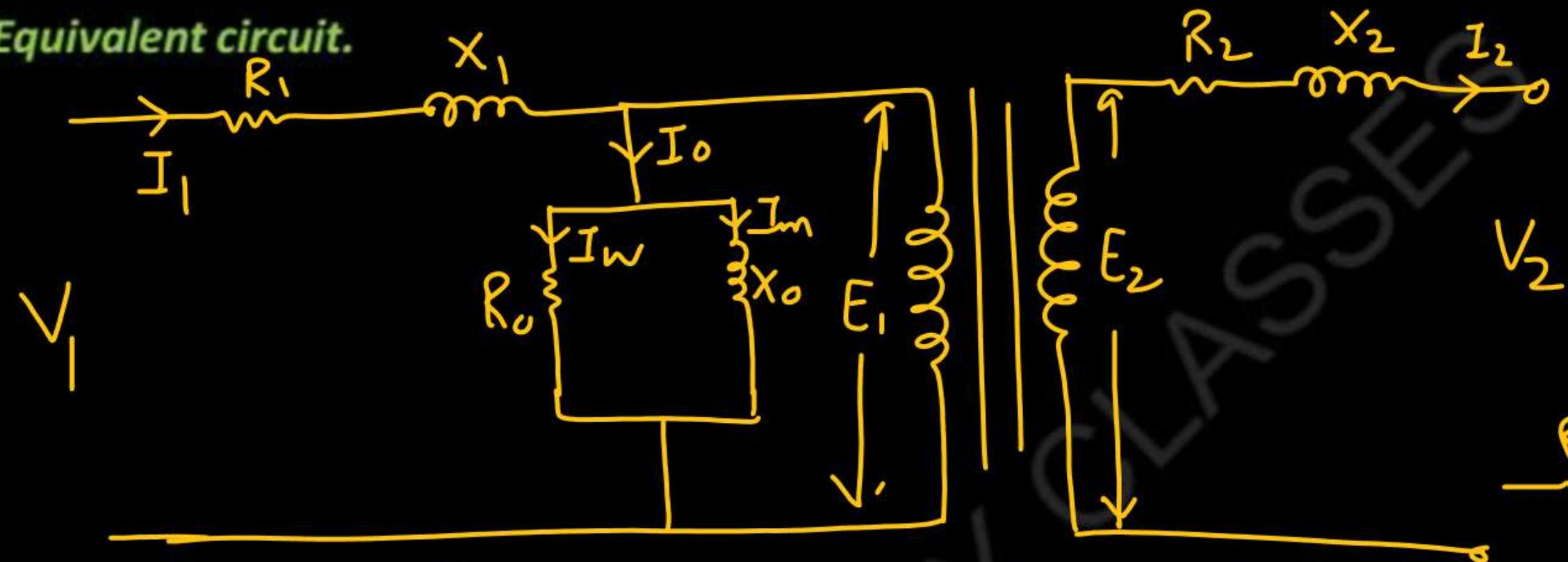


**Concept of equivalent resistance:- referred to primary and secondary**

$$\begin{aligned}
 \text{Total loss} &= I_1^2 R_1 + I_2^2 R_2 \\
 &= I_1^2 \left( R_1 + \left( \frac{I_2}{I_1} \right)^2 R_2 \right) = I_1^2 \left( R_1 + \frac{R_2}{K^2} \right) \\
 &= I_1^2 R_1 + \frac{I_1^2 R_2}{K^2}
 \end{aligned}$$

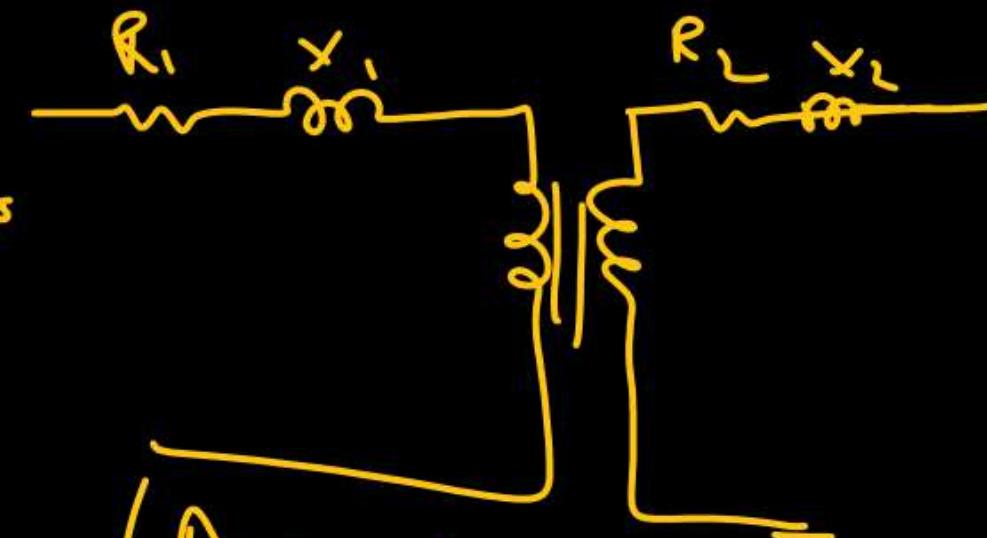
# Equivalent circuit of Transformer

Exact Equivalent circuit.



$R_1, X_1$  = Primary resistance & leakage Reactance

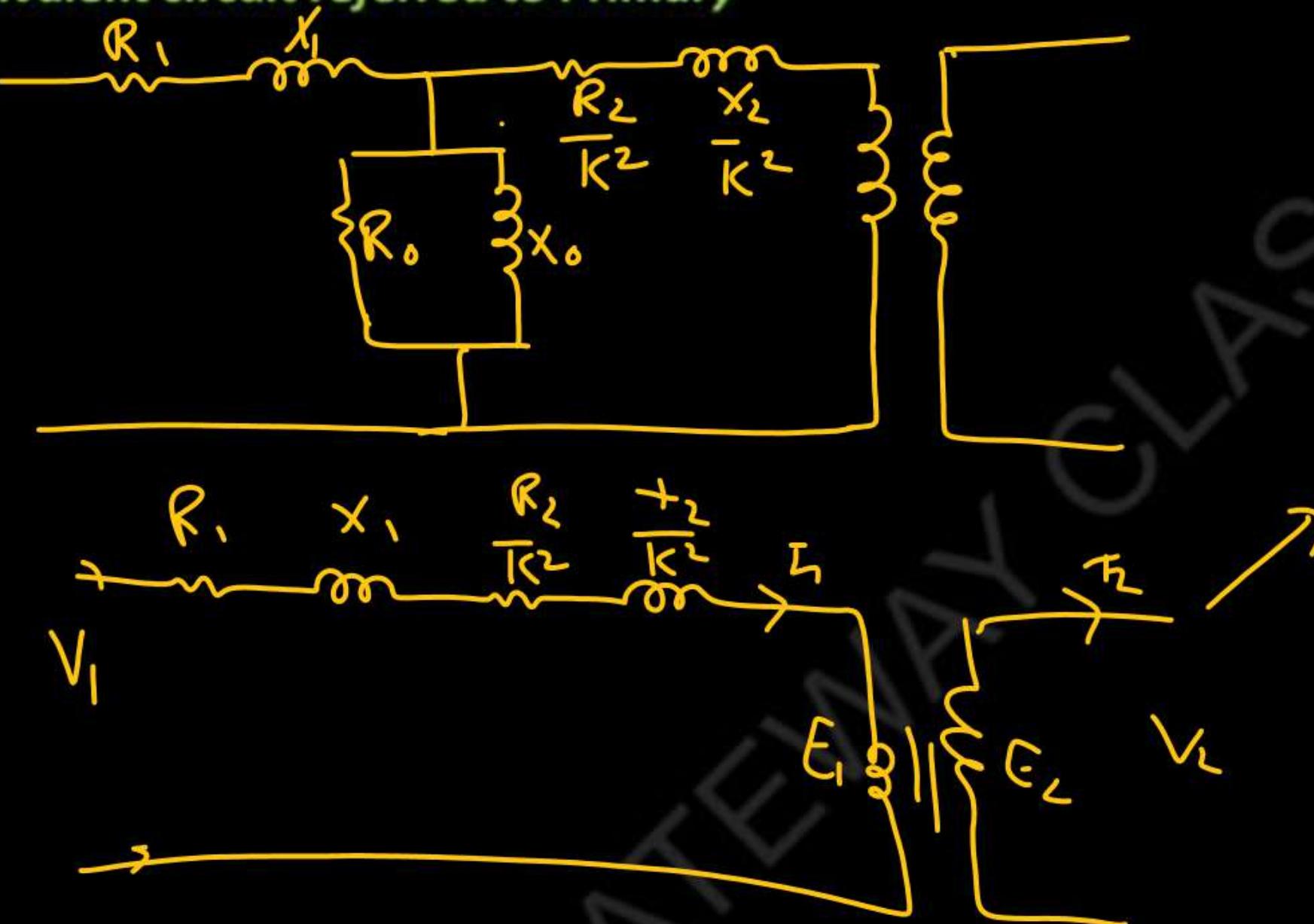
$R_2, X_2$  = Secondary " "



(Approximate  
Equivalent ( $k_f$ )

# Equivalent circuit of Transformer

**Exact Equivalent circuit referred to Primary**



$$R_{01} = R_1 + \frac{R_2}{k^2}$$

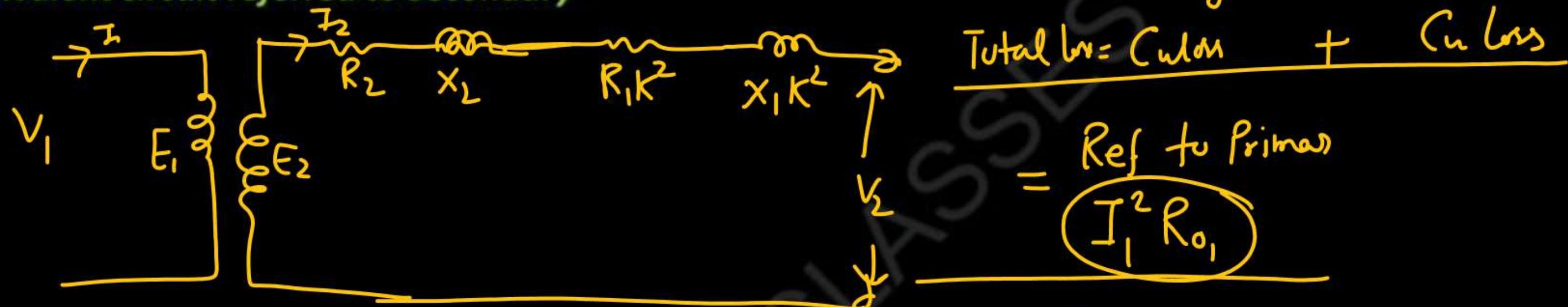
$$X_{01} = X_1 + \frac{X_2}{k^2}$$

$$Z_{01} = \sqrt{R_{01}^2 + X_{01}^2}$$

$$Z_{01} = R_{01} + jX_{01}$$

# Equivalent circuit of Transformer

**Exact Equivalent circuit referred to Secondary**



$$R_{o2} = R_2 + R_1 K^2$$

$$X_{o2} = X_2 + X_1 K^2$$

$$Z_{o2} = R_{o2} + j X_{o2}$$

Ref. to Secondary

Total =  $I_2^2 R_{o2}$

**Ex-1** A 20kVA, 2000V/200V, single-phase, 50 Hz transformer has a primary resistance of  $1.5 \Omega$  and reactance of  $2 \Omega$ . The secondary resistance and reactance are  $0.015 \Omega$  and  $0.02 \Omega$  respectively. The no load current of transformer is 1A at 0.2 power factor. Determine: (i) Equivalent resistance, reactance and impedance referred to primary & Secondary (ii) Supply current (iii) Total copper loss Draw approximate equivalent circuit **2021-22**

$$R_1 = 1.5, X_1 = 2 \Omega$$

$$R_2 = 0.015, X_2 = 0.02 \Omega$$

Ref. to Primary

$$R_{01} = R_1 + \frac{R_2}{K^2} = 1.5 + \frac{0.015}{\frac{1}{100}} = 1.5 + 1.5 = 3 \Omega$$

$$X_{02} = X_1 + \frac{X_2}{K^2} = 2 + \frac{0.02}{\frac{1}{100}} = 2 + 2 = 4 \Omega$$

$$\boxed{Z_{01} = 3 + 4j \Omega}$$

Ref. to Secondary

$$R_{02} = R_2 + R_1 K^2 = 0.015 + 1.5 \times \frac{1}{100} = 0.03 \Omega$$

$$X_{02} = X_2 + X_1 K^2 = 0.02 + 2 \times \frac{1}{100} = 0.04 \Omega$$

$$Z_{02} = 0.03 + 0.04j \text{ ohm}$$

$$P = V_1 I_1 \\ I_1 = \frac{20 \times 10^3}{2000} = 10 \text{ amp}$$

Total -

$$= I_1^2 R_{01} \\ = 10^2 \times 3 \\ = 300 \text{ watt Ans}$$

~~Iron~~

## Losses in a Transformer

- Core Loss/ Iron Loss/ Fixed Loss/ Constant Loss

**① Hysteresis Loss:-** When a magnetic material is subjected to cycle of magnetization , a power loss occurs due to molecular friction in the material Therefore, energy is required in the material to overcome this opposition. This loss being in the form of heat and is termed as *hysteresis loss*.

$$\text{Area of hysteresis loop} \propto B_{\max}^{1.6}$$

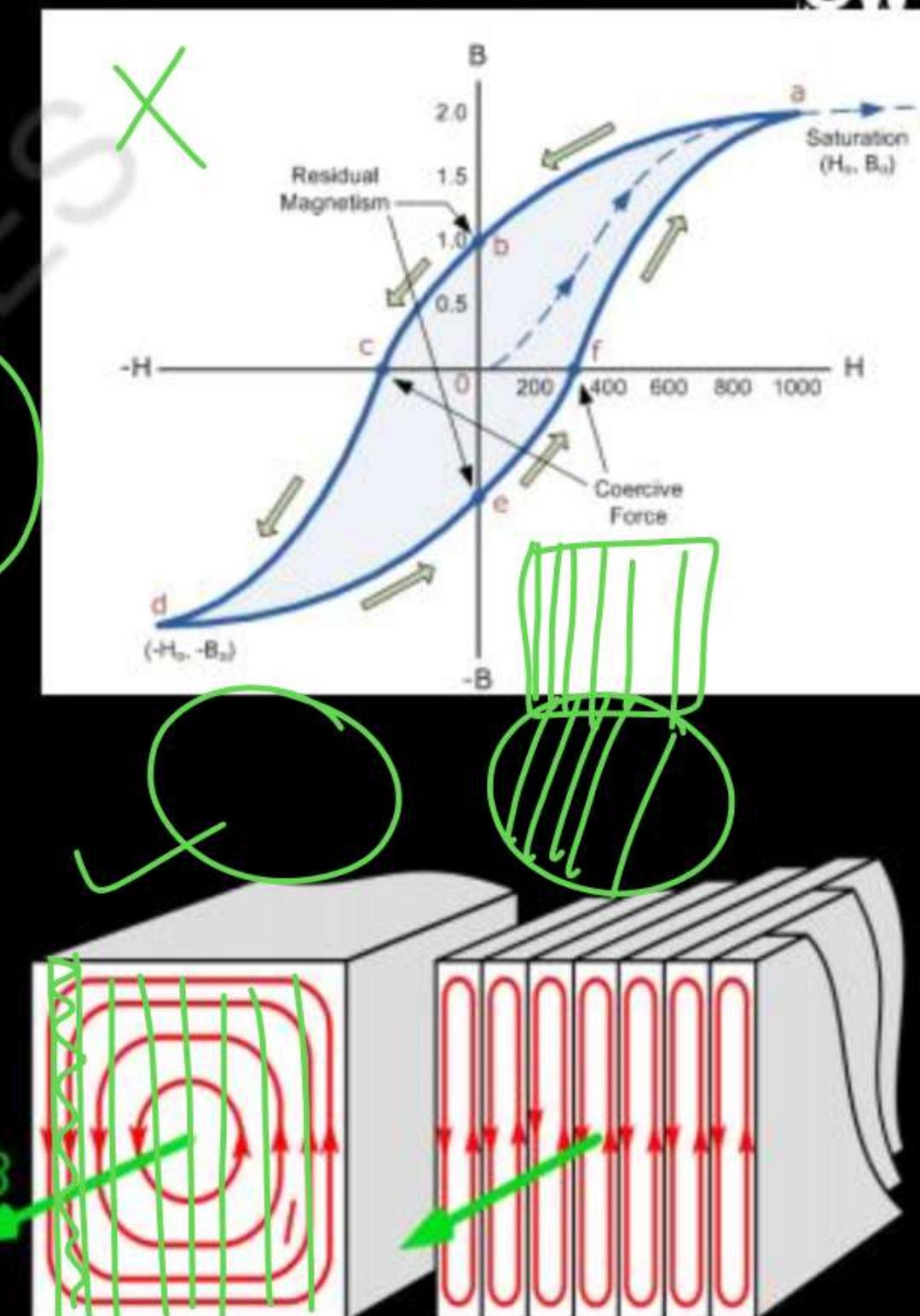


$$\text{Hysteresis power loss, } P_h = \eta B_{\max}^{1.6} f V \text{ Watts}$$

**② Eddy Current Loss:-** When a magnetic material is subjected to a changing magnetic field, a voltage is induced in the material according to Faraday's law of electromagnetic induction. Since the material is conducting, the induced voltage circulates currents within the body of the magnetic material. These circulating currents are known as *eddy currents*. These eddy currents causes  $I^2R$  loss in the material, known as *eddy current loss*.

$$\text{Eddy current power loss, } P_e = K_e B_{\max}^2 f^2 t^2 V \text{ Watts}$$

Where  $K_e$  = Eddy current coefficient,  $B_{\max}$  = Maximum flux density,  $f$  = frequency of magnetization or flux,  $t$  = thickness of lamination, and  $V$  = Volume of magnetic material.



### Copper Loss/ Variable Loss/ $I^2R$ Loss

- Copper Loss:-** The losses occurs due the resistance of primary and secondary winding. These losses depends upon the magnitude of current in winding.

$$P_{cu} \propto I^2$$

$$P_{cu} = I^2 R$$

- Thus for a Transformer Total Losses = Iron Loss + Copper Loss =  $P_i + P_{cu}$

### Methods of reducing Losses in a Transformer

**Iron Loss:-** (i) Choice of Material for Iron Core (steel of high silicon content)

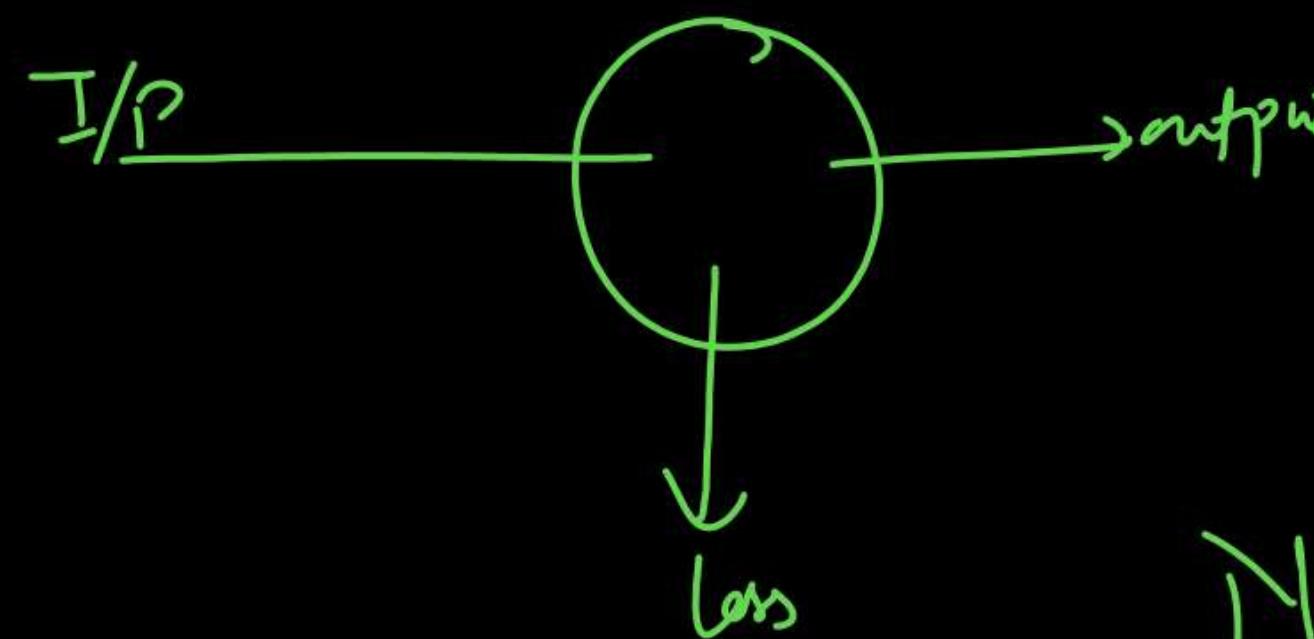
(ii) Use of Thin Laminated Core

### Copper Loss/ Variable Loss/ $I^2R$ Loss

- (i) Reduce resistance of winding (use of thick wire)

# Efficiency of Transformer

- Efficiency of Transformer:-



$$\frac{I}{P} - \text{losses} = \text{output}$$

$$\frac{I}{P} = \frac{\text{output} + \text{losses}}{\text{output}}$$

$$\eta = \frac{\text{output}}{\frac{\text{output} + \text{losses}}{\text{input}}} = \frac{\text{output}}{\text{output} + \text{losses}} = \frac{V_L I_L \cos \phi_2}{V_L I_L \cos \phi_1 + P_{cu}} = \frac{V_L I_L \cos \phi_2}{V_L I_L \cos \phi_1 + I^2 R + P_{cu}}$$

Now loading fraction:  $\chi = 0.5$

$$\boxed{\eta = \frac{\chi V_L I_L \cos \phi}{\chi V_L I_L \cos \phi + R + \chi^2 P_{cu}}}$$

# Efficiency of Transformer

**Condition of Maximum Efficiency of a Transformer:-**

$$\eta = \frac{V_2 I_2 \cos\phi}{V_2 I_2 \cos\phi + P_i + I_2^2 R}$$

$$\frac{d\eta}{dI_2} = 0$$

$$\eta = \frac{\left( V_2 I_2 (\cos\phi + P_i + I_2^2 R) \right) - V_2 I_2 (\cos\phi)}{\left( V_2 I_2 (\cos\phi + P_i + I_2^2 R) \right)^2} = 0$$

$$= (V_2 I_2 \cos\phi + P_i + I_2^2 R) - V_2 I_2 \cos\phi - 2I_2^2 R = 0$$

$$P_i^o - I_2^2 R$$

$$P_i^o = I_2^2 R$$

$$\Rightarrow P_i^o = P_{C4}$$

At any load

$$P_i^o = x^e P_{C4}$$

Load Current at Maximum Efficiency :-

$$I_2^2 R_n = P_i \cdot$$

$$I_2^2 = \frac{P_i}{R_{02}} \Rightarrow I_2 = \sqrt{\frac{P_i}{R_{02}}}$$

$$\frac{I_2}{I_{f.L}} = \frac{1}{I_{f.L}} \sqrt{\frac{P_i}{R_{02}}} = \sqrt{\frac{P_i}{I_{f.L}^2 R_{02}}} \Rightarrow \sqrt{\frac{P_i}{P_{cu.f.L}}}$$

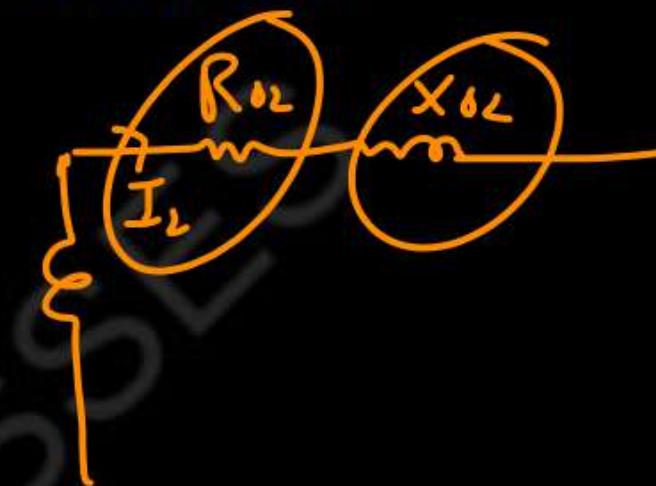
$$I_2 = I_{f.L} \times \sqrt{\frac{P_i}{P_{cu}}}$$

KVA at Maximum Efficiency:

$$KVA = V_2 I_2 = V_2 \cdot I_{f.L} \sqrt{\frac{P_i}{P_{cu}}} \Rightarrow (KVA)_{f.L} \sqrt{\frac{P_i}{P_{cu}}}$$

# Voltage Regulation of a Transformer

$$\begin{aligned} \therefore V \cdot R &= \frac{E_2 - V_2}{V_2} \xrightarrow{\text{lagging}} \\ &= I_2 R_{02} \cos \phi + I_2 X_{02} \sin \phi \end{aligned}$$



$V_2 I_2$ 

Ex-1 A **40 KVA** transformer has iron loss of **450W** and full load copper loss of **850W**. if the power factor of the load is **0.8 lagging**, calculate: (i) Full load efficiency (ii) The load at which the maximum efficiency occurs and (iii) The maximum efficiency. 2021-22

$$P_{I'} = 450 \text{ W}, P_{Cu} = 850 \text{ W}$$

$$\cos \phi = 0.8$$

$$\eta_{FL} = \frac{40 \times 10^3 \times 0.8}{(40 \times 10^3 \times 0.8) + (450 + 850)}$$

$$= 0.96$$

$$\boxed{\sqrt{\eta_{FL}} = 96 \text{ V.}}$$

$$\begin{aligned} P_{I'} &= P_{Cu} \\ &= 2P_{I'} \end{aligned}$$

$$(KVA)_{max.} = KVA_{FL} \sqrt{\frac{P_{I'}}{P_{Cu}}} = 40 \sqrt{\frac{450}{850}} = 2910 \text{ VA.}$$

$$\eta_{max} = \frac{2910 \times 0.8}{(2910 \times 0.8) + 2P_{I'}} = \frac{2328}{2328 + (2 \times 450)} = 96.27\%$$

Ex-2 A 25kVA, 2000/200V transformer has full load copper and iron losses of 1.8kW and 1.5kW respectively. Calculate efficiency at half the rated kVA and at unity power factor, the efficiency at full load and at 0.8 pf lagging and maximum efficiency. 2020-21

$$P_i = 1.5 \text{ kW}, P_{cu} = 1.8 \text{ kW}$$

$$\chi = 0.5$$

$$\eta_{1/2} = \frac{(0.5) \times (25 \times 10^3) \times 1}{(0.5 \times 25 \times 10^3 \times 1) + (15w + \frac{18w}{\chi})}$$

$$\boxed{\eta_{1/2} = 86.5 \%}$$

$$\begin{aligned}\eta_{LL} &= \frac{25 \times 10^3 \times 0.8}{(25 \times 10^3 \times 0.8) + (15w + 18w)} \\ &= 85.83 \%\end{aligned}$$

$$KVA_{max} = 25 \times 10^3 \times \sqrt{\frac{15w}{18w}} = 22821.7 \text{ VA}$$

$$\eta_{max} = \frac{22821.7 \times 0.8}{22821.7 \times 0.8 + (2 \times 15w)} = 85.88 \%$$

Ans

Ex-3 A single phase 100KVA 6.6kv , 230V 50Hz transformer has 90% efficiency at 0.8 lagging power factor both at full load and also at half load. Determine iron and copper loss at full load for the transformer. 2019-20

$$\eta_{f.l} = 90\% = 0.90 \quad \text{COS } \phi = 0.8$$

$$\eta_{h.l.}$$

at full load

$$0.9 = \frac{100 \times 10^3 \times 0.8}{100 \times 10^3 \times 0.8 + (P_i + P_{cu})} \Rightarrow P_i + P_{cu} = 8888.8 \quad \textcircled{1}$$

At half load

$$0.9 = \frac{0.5 \times 100 \times 10^3 \times 0.8}{0.5 \times 100 \times 10^3 \times 0.8 + (P_i + \frac{P_{cu}}{4})} \Rightarrow P_i + \frac{P_{cu}}{4} = 4444.4 \quad \textcircled{2}$$

Solve

$$P_i = 2.916.0$$

$$P_{cu} = 5.952$$

Ans

Ex-4 The maximum efficiency of a 100 KVA, 1100/440 V, 50 Hz transformer is 96%, This occurs at 75% of full load at 0.8 p.f. lagging. Find the efficiency of transformer at 3.4 FL at 0.6 p.f. leading. 2018-19

$$\eta_{max} = .96 \text{ at } \kappa_{load} = ((100 \times 10^3) \times 0.75) = 75 \text{ KVA}$$

$$0.96 = \frac{75 \times 10^3 \times 0.8}{75 \times 10^3 \times 0.8 + 2P_L^o}$$

$$\boxed{P_L^o = 1250 \text{ watt}}$$

$$P_L^o = \kappa^2 P_m$$

$$P_m = \frac{P_o}{\kappa^2} = \frac{1250}{(0.75)^2} = 2222.2 \text{ watt}$$

$$\kappa = \frac{3}{4}, \cos\phi = 0.6$$

$$\eta_{f.L} = \frac{\frac{3}{4} \times 100 \times 10^3 \times 0.6}{\left(\frac{3}{4} \times 100 \times 10^3 \times 0.6\right) + (1250 + \left(\frac{3}{4}\right)^2 2222.2)}$$

$$\eta_{f.L} = 88.33\%.$$

Ans

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# Thank You



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