



# Gateway Classes

**Semester -I & II****Common to All Branches****BEE101/201: FUNDAMENTALS OF ELECTRICAL ENGG.**

## **UNIT-1 ONE SHOT : DC Circuits**



## **Gateway Series for Engineering**

- Topic Wise Entire Syllabus**
- Long - Short Questions Covered**
- AKTU PYQs Covered**
- DPP**
- Result Oriented Content**

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# Gateway Classes



**BEE101 / BEE201: FUNDAMENTALS OF ELECTRICAL ENGINEERING**

## **Unit-1 Introduction to DC Circuits Syllabus**

**Electrical circuit elements (R, L and C), Concept of active and passive elements, voltage and current sources, concept of linearity, unilateral and bilateral elements. Kirchhoff's laws, Mesh and nodal methods of analysis.**



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# AKTU



## Electrical Engg

# One Shot

## UNIT - I



Source Conv.

Star-Delta  
Equivalent Resistance  
Theorem

# Syllabus BEE-201/101

## Unit -1: (DC Circuits )

- Electrical circuit elements (R, L and C),
- Concept of active and passive elements,
- voltage and current sources,
- concept of linearity,
- unilateral and bilateral elements.
- Kirchhoff's laws,
- Mesh and nodal methods of analysis.

No Num.

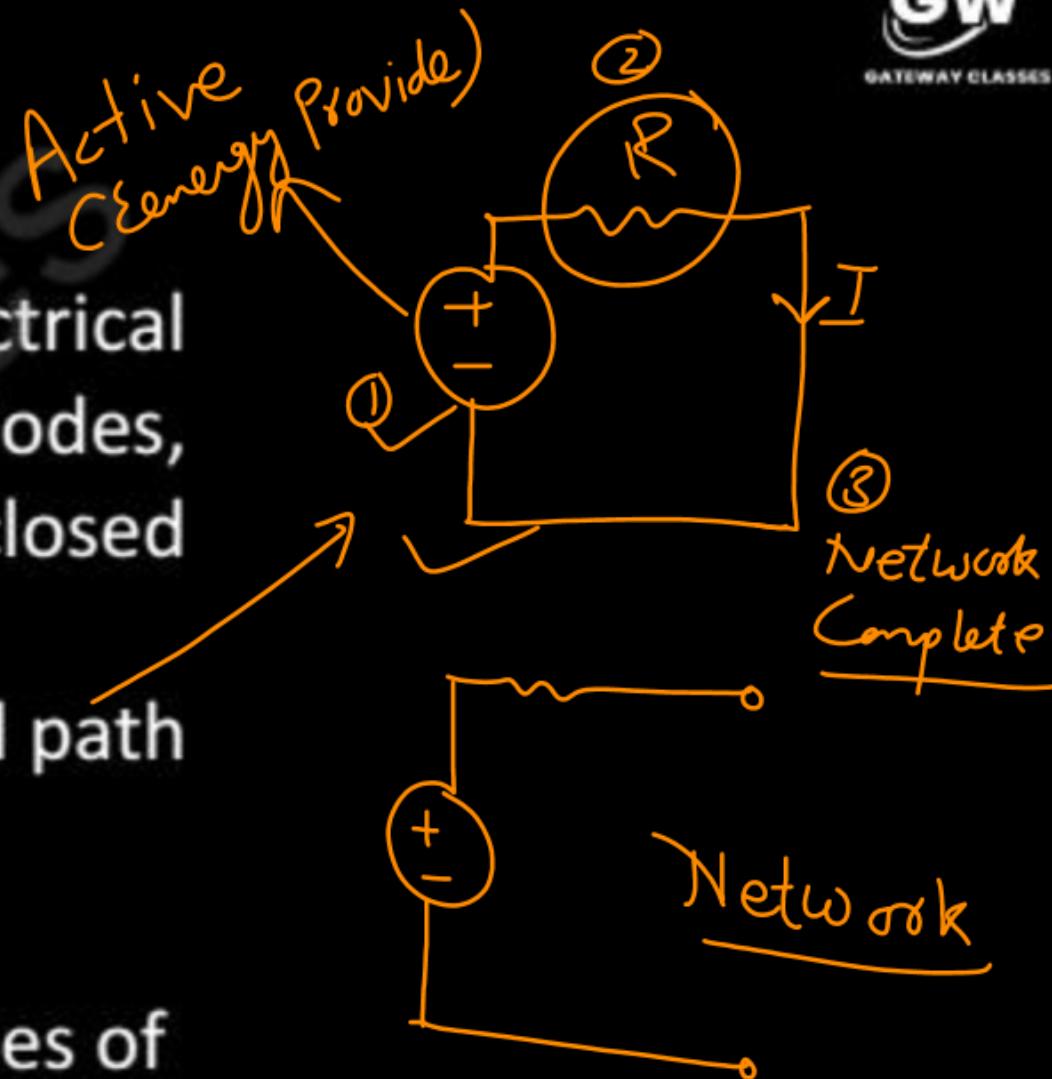
# Basics of DC Circuits

## Electric Circuit and Electrical Network:-

- An electrical network is an interconnection of electrical components (like sources, resistors, inductors, capacitors, diodes, transistors etc.). An electrical network need not contain a closed path for the flow of electric current.
- An electric circuit is, an electric network that contains a closed path for the flow of electric current.

**Passive Network** – A passive network does not contain any sources of energy. They consist only passive circuit elements like resistors, inductors and capacitors etc.

**Active Network** – An active network contains one or more sources of energy (like voltage source or current source), they can supply energy to the network indefinitely. **An active network is also termed as electric circuit.**

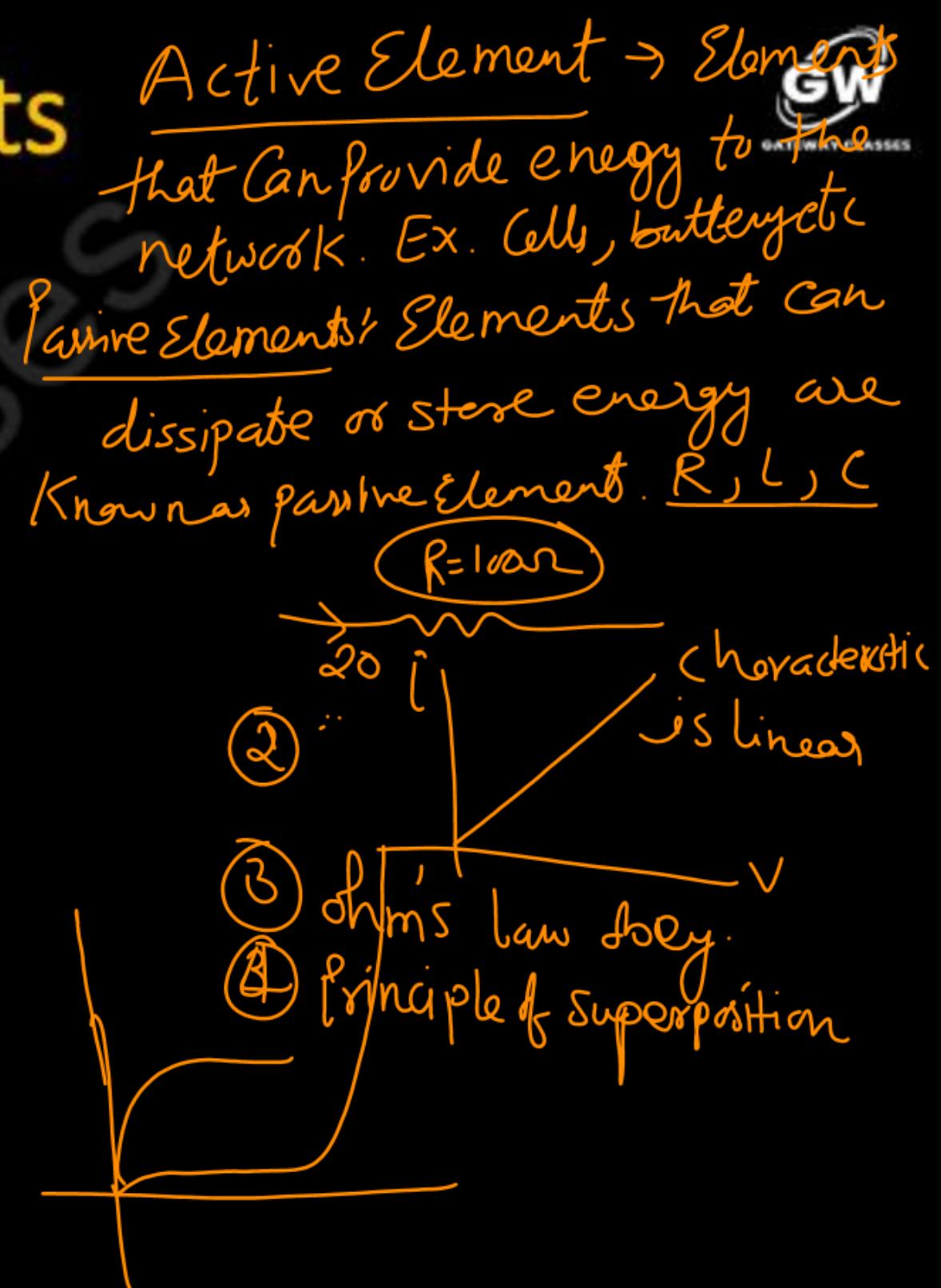


# Basics of DC Circuits

Linear & Non Linear Network - A network is said to be **linear**, if it consists of the circuit elements that obeys the principle of homogeneity and superposition, Otherwise networks is known as **Non-Linear Network**. Ex- Resistive network (Linear), Network having diodes etc. (Non-Linear).

Lumped Network:-A network in which all the network elements are physically separable is known as a lumped network. (Ex.- R,L,C Network etc.)

Distributed Network - A network in which network elements can not be physically separable is known as **Distributed network** like Transmission Line.



# Basics of DC Circuits

Loop = ABCDEF  $\rightarrow$  A-B-C-D, A-D-E-F  
① Mesh =

**Loop And Mesh:-** Any Closed path is known as loop. Any Shortest Closed Path is Known as Mesh.

**Note:-** Every Mesh will be a loop but it is not necessary that every loop will be a mesh.

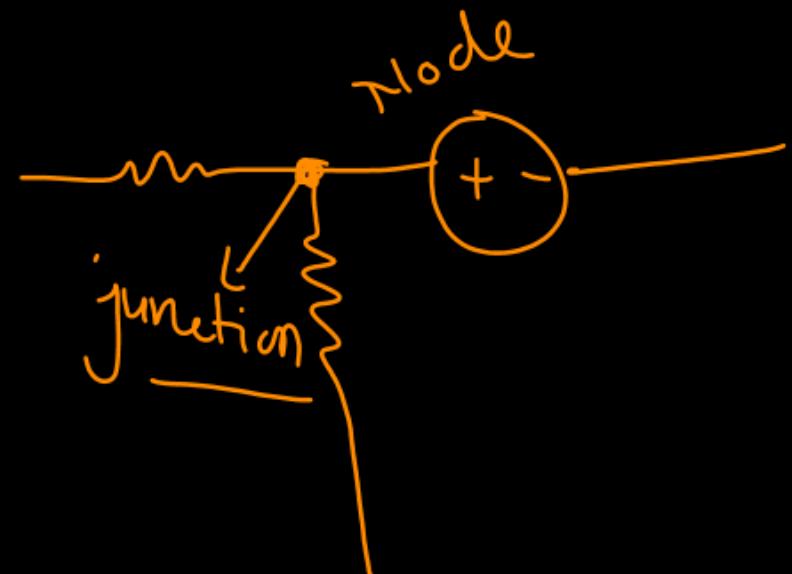
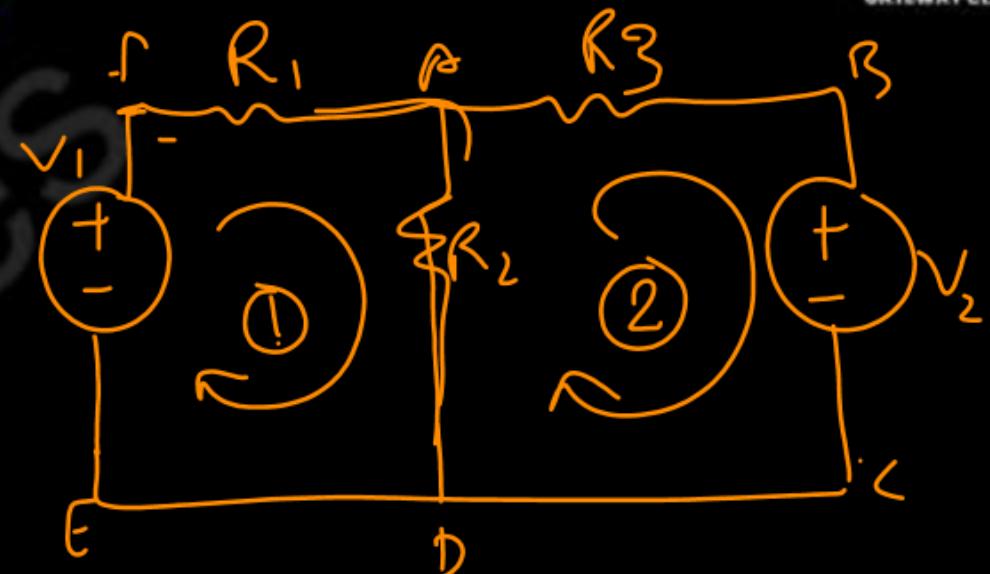
→ A mesh does not contain any other loop in it.



**Node and Junction:-** Node is a point where two or more elements meets.

Junction is a point where three or more elements meets.

**Note:-** Every Junction will be a node but it is not necessary that every node will be a Junction.



# Basics of DC Circuits

Bi → two

**Active Elements**:- Elements that can provide energy to the networks. Ex. Voltage Source & Current Source

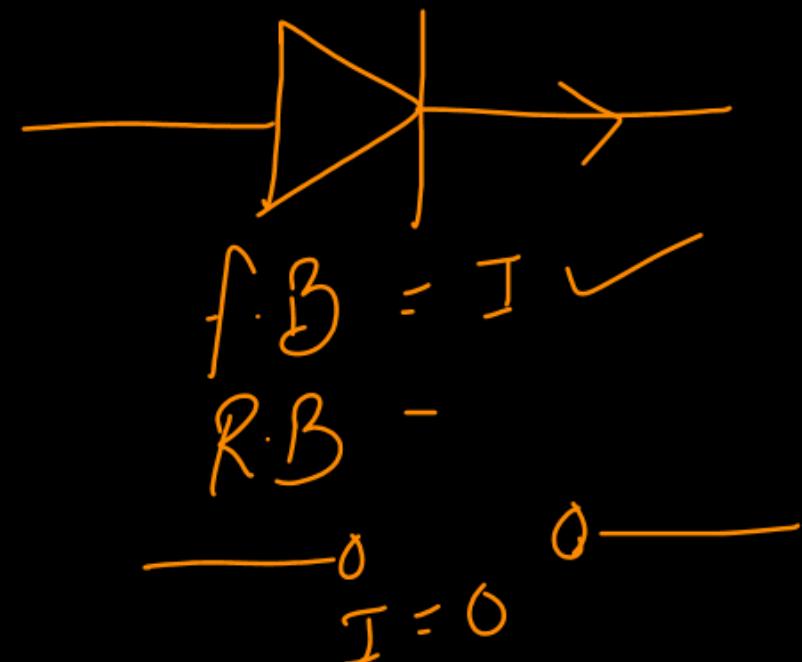
**Passive Elements**:- Elements that can only receive energy, which it can either dissipate, absorb or store it in an electric field or a magnetic field. Ex. R,L,C

**Bilateral Element**:- Elements which allows current to flow from both directions are known as Bilateral Element.

(Ex- Resistance).

**Unilateral Element**:- Elements which allows current to flow only from one direction are known as Unilateral Element.

(Ex- Diode)

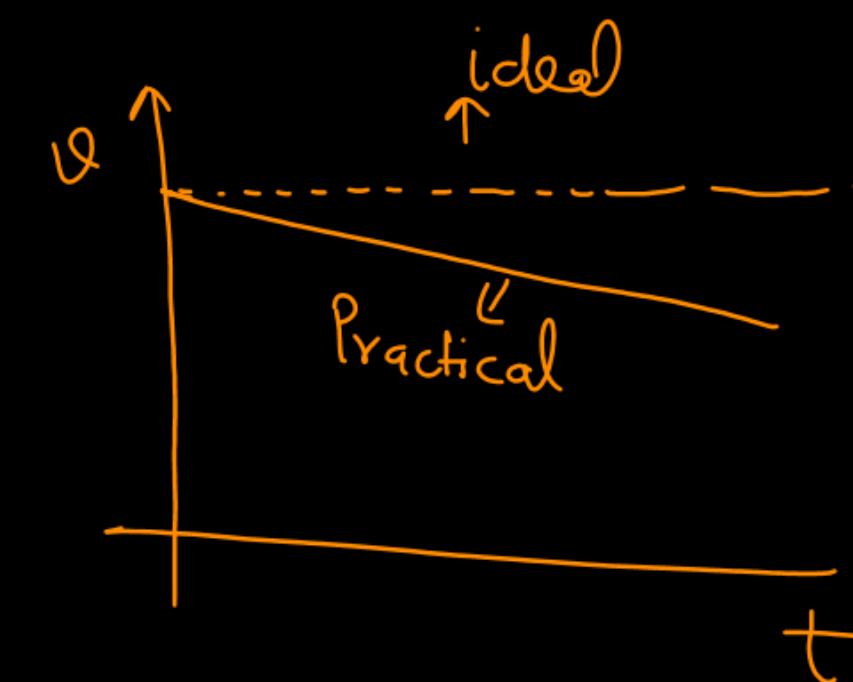
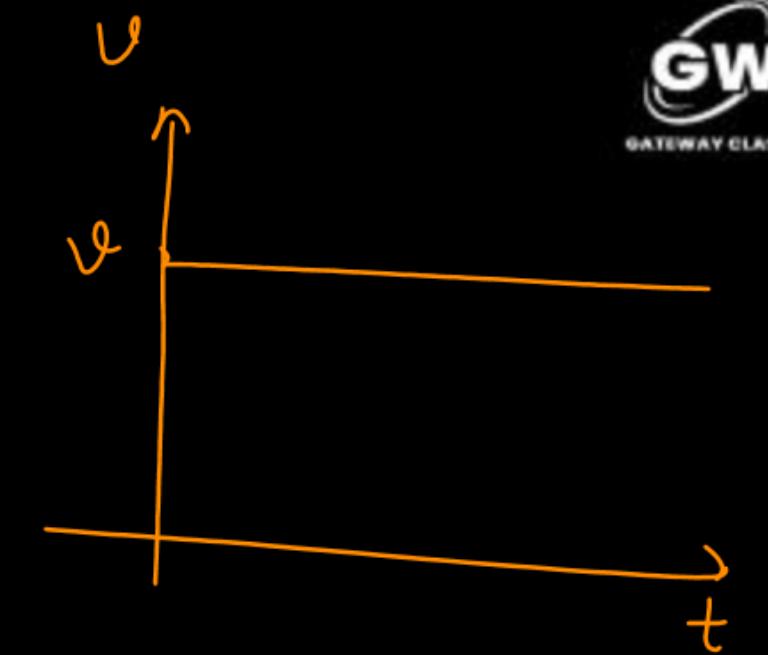
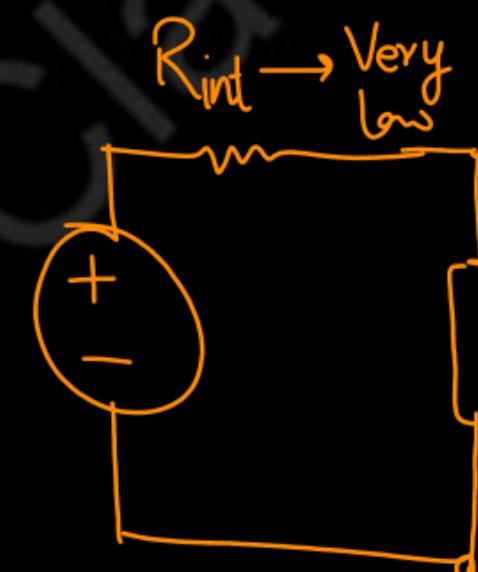
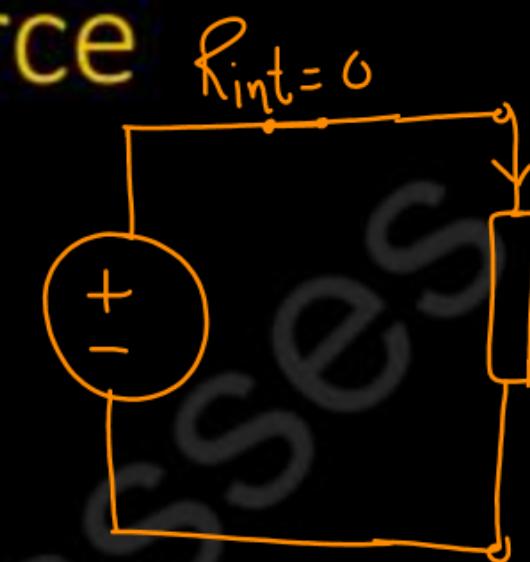


# Voltage Source

**Ideal Voltage source:-** Energy Source which provide constant voltage across its terminals irrespective of current drawn through its terminals.

It has Zero Internal Resistance

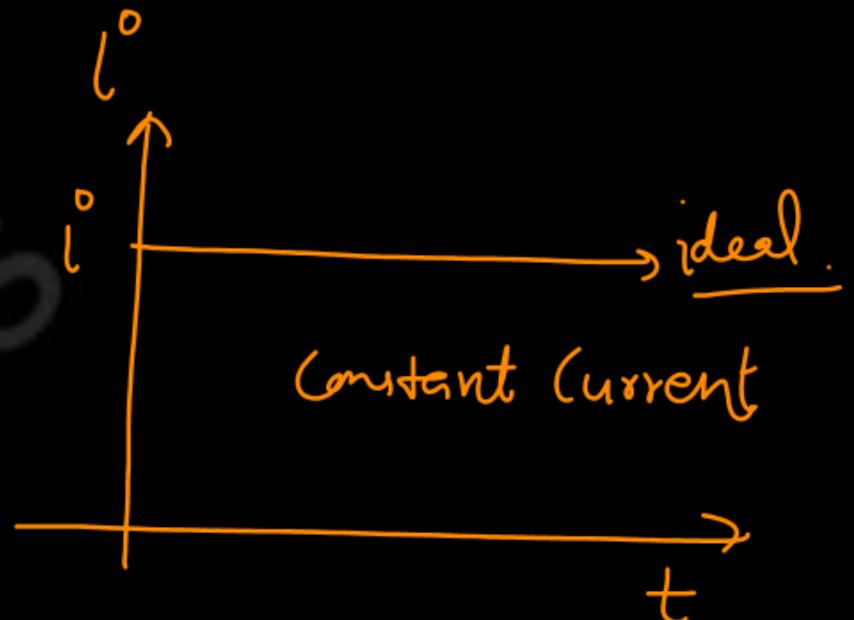
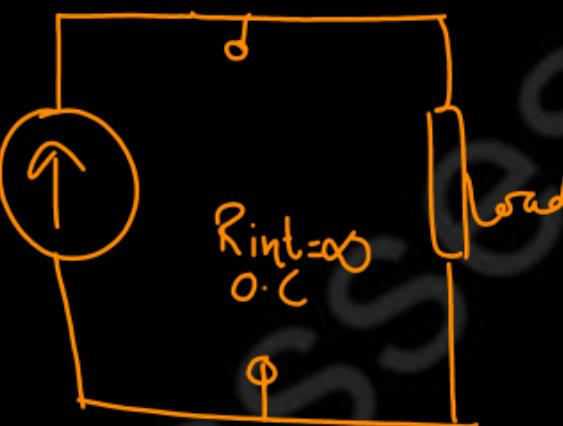
**Practical Voltage Source:-** A practical voltage source has small internal resistance due to which voltage across terminals decrease slightly with increase in current.



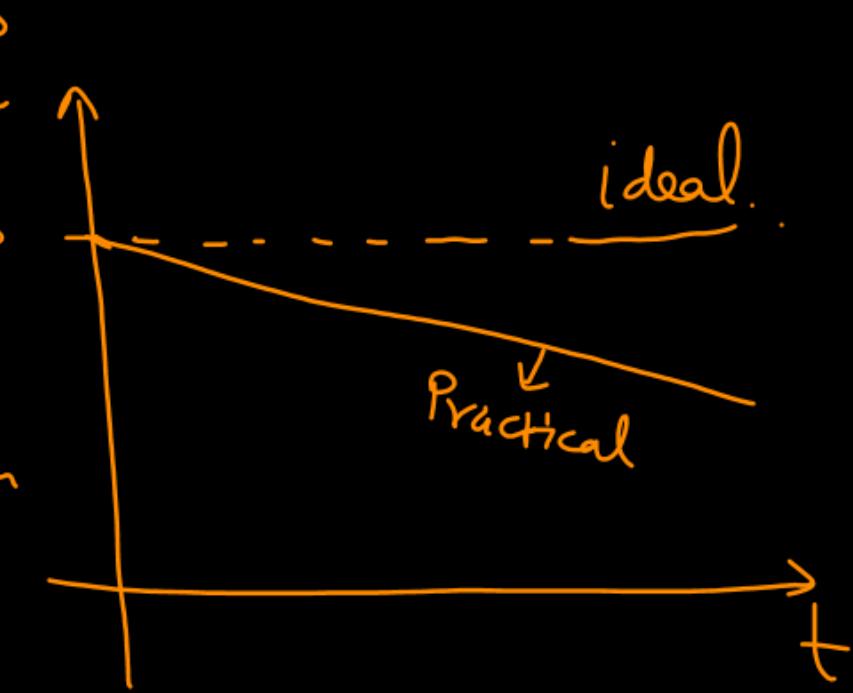
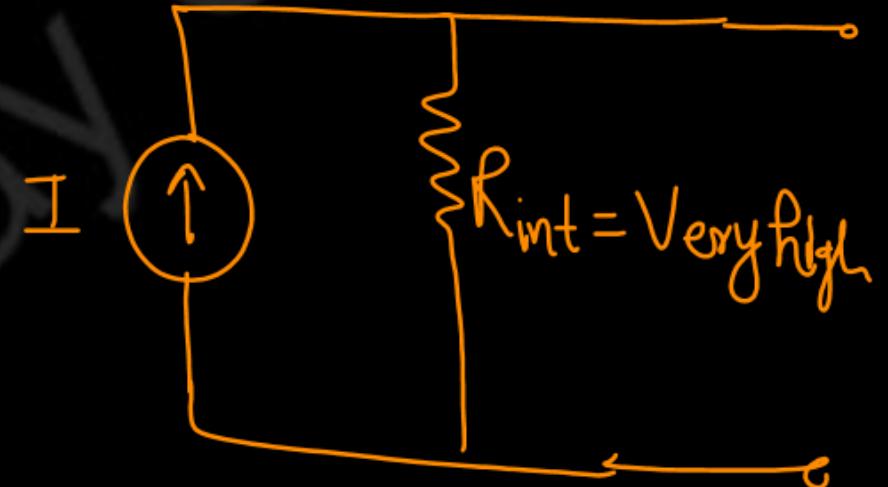
# Current Source

**Ideal Current source**:- Energy Source which provide constant Current across its terminals irrespective of current drawn through its terminals.

It has infinite Internal Resistance



**Practical Current Source**:- A practical Current source has very high internal resistance due to which Current across terminals decrease slightly with increase in voltage.



# Elements of Electric Circuit (Resistance)



**Resistance:-** Opposition to the flow of current is known as resistance.

**Formula:-**

$$R = \rho \frac{l}{a} \rightarrow \text{length of Conductor}$$

area of Conductor

Specific resistance

Resistivity

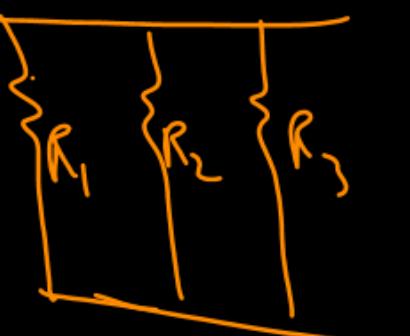
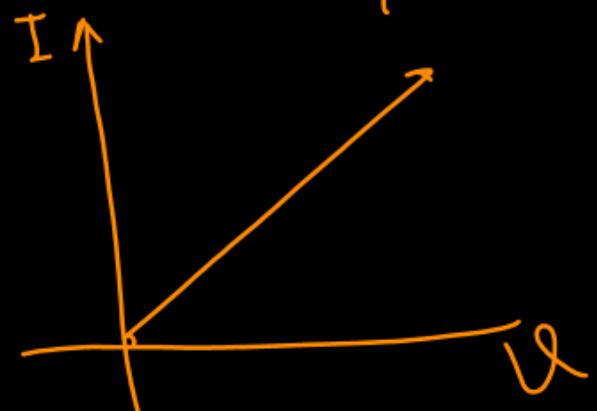
static Element.

Memory less element

$$R = \frac{V}{I}$$

Series  $\rightarrow R_{eq} = R_1 + R_2 + R_3 + \dots$

Parallel  $\rightarrow \frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$



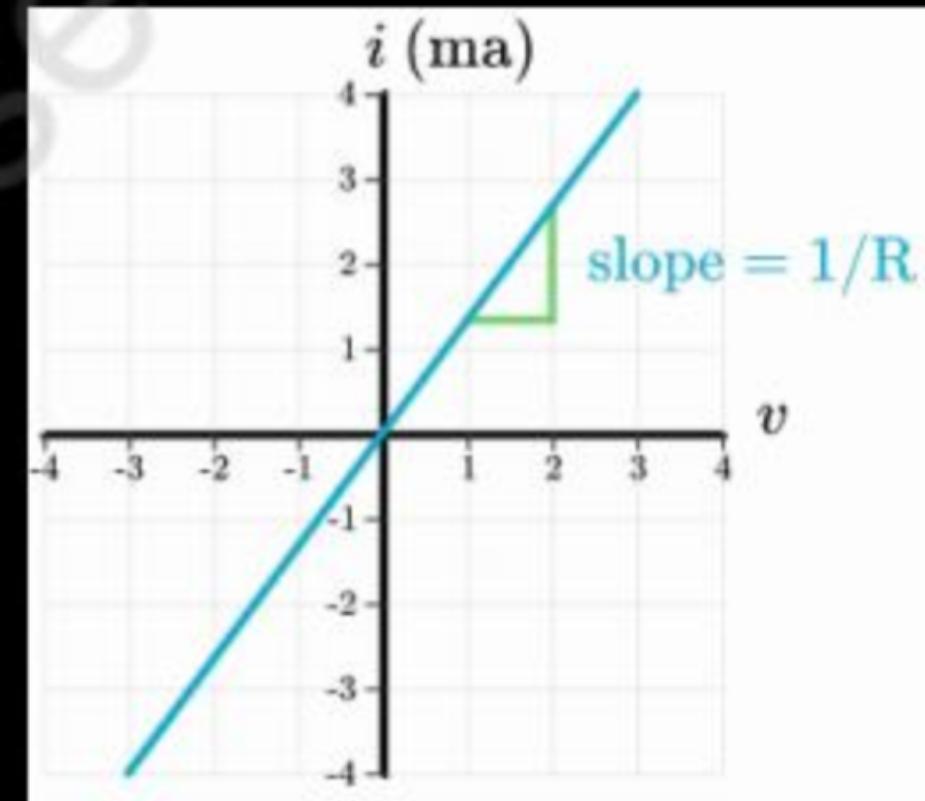
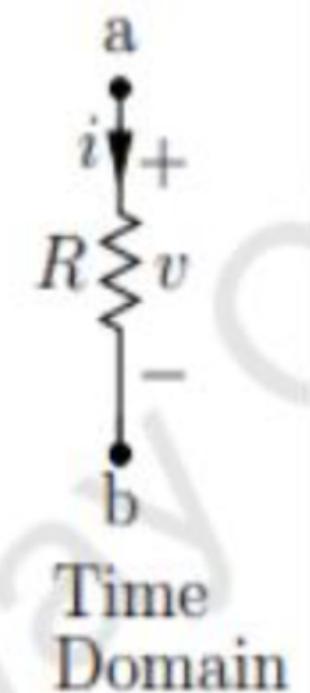
# Elements of Electric Circuit (Resistance)

## Resistance:

Time domain:

$$v(t) = Ri(t)$$

$$i(t) = \frac{v(t)}{R}$$



Resistance is a static element in the sense  $v(t)$  versus  $i(t)$  relationship is instantaneous.

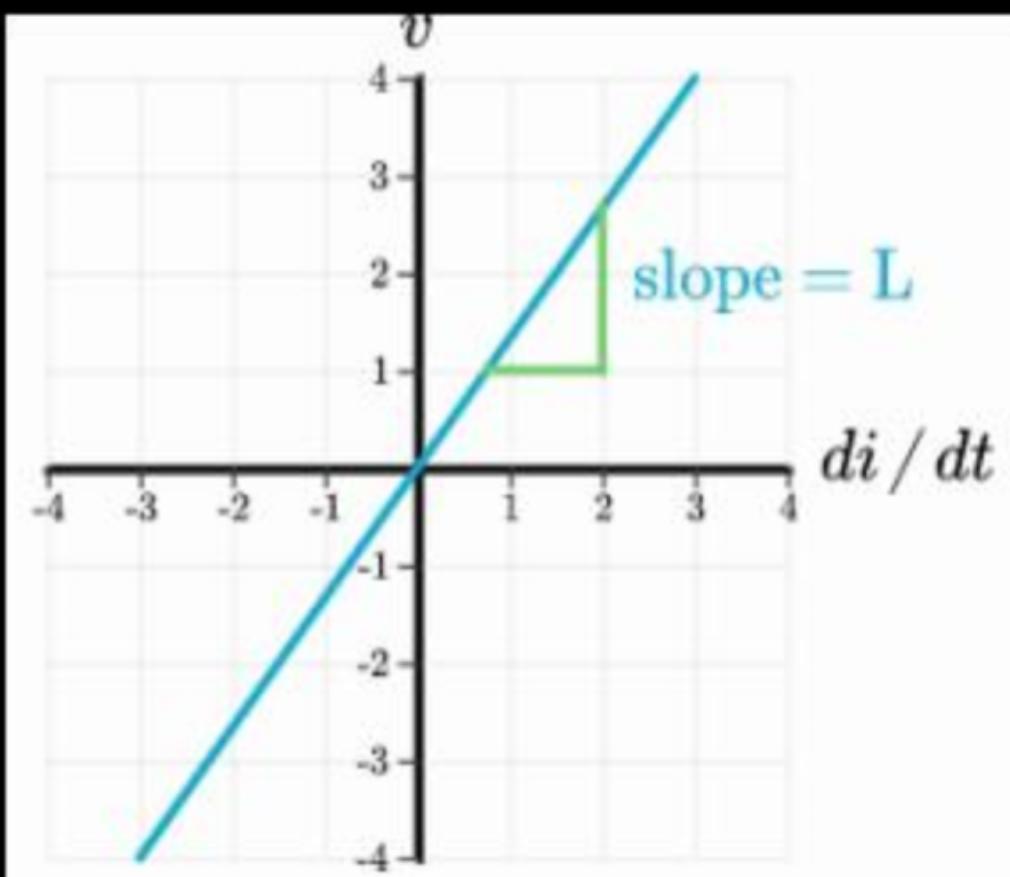
- Example:- let  $v(t)$  at time  $t = 2$  seconds simply depends only on  $i(t)$  at  $t = 2$  seconds and nothing else. This implies that the resistance does not know what happened in the past, in other words it does not store any energy unlike other elements C and L as we see soon.

# (Inductance)

$$V = L \frac{di}{dt}$$

## Inductor: -

- It is a passive component that store energy in the form of magnetic energy when electricity is applied to it.
- An inductor is simply a coil of wire.
- Inductance (L) is a property of an inductor that opposes any change in magnitude or direction of current flowing through it.
- Inductance is the ration of flux linkage ( $N\phi$ ) to the current I.
- Inductance is a dynamic element. What happened in the past influences the present behavior

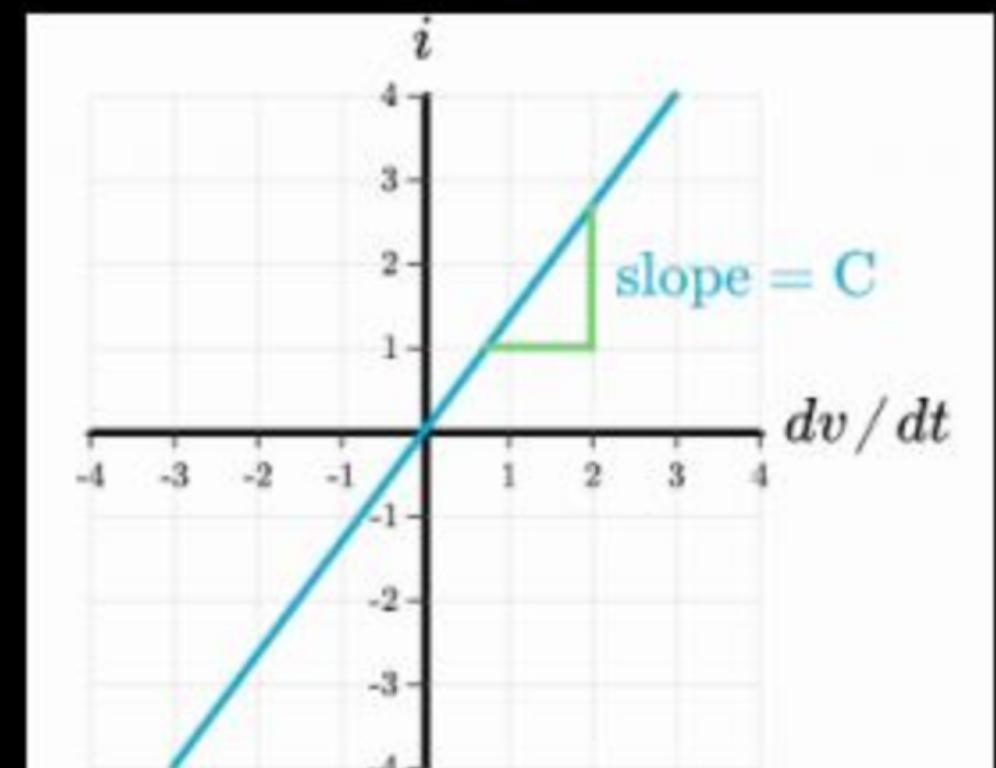
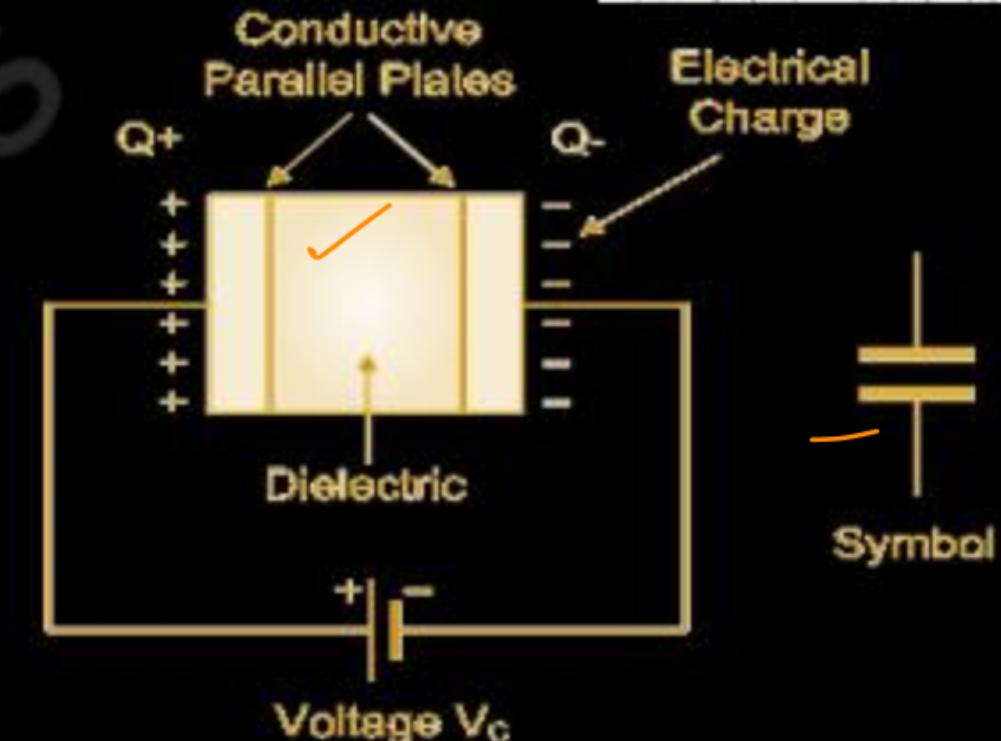


$$\textcircled{P} \quad C \left( \frac{dV}{dt} \right)$$

# (Capacitance)



- The capacitor is a component which has the ability or **“capacity” to store energy** in the form of an electrical charge producing a potential difference (*Static Voltage*) across its plates, much like a small rechargeable battery.
- A capacitor consists of two or more parallel conductive (metal) plates electrically separated either by air or by some form of a good insulating material.
- This insulating material could be waxed paper, mica, ceramic, plastic or some form of a liquid gel as used in electrolytic capacitors.
- Insulating layer between a capacitors plates is commonly called the **Dielectric**.
- What happened in the past influences the present behavior. This implies that the capacitance is **a dynamic element**.



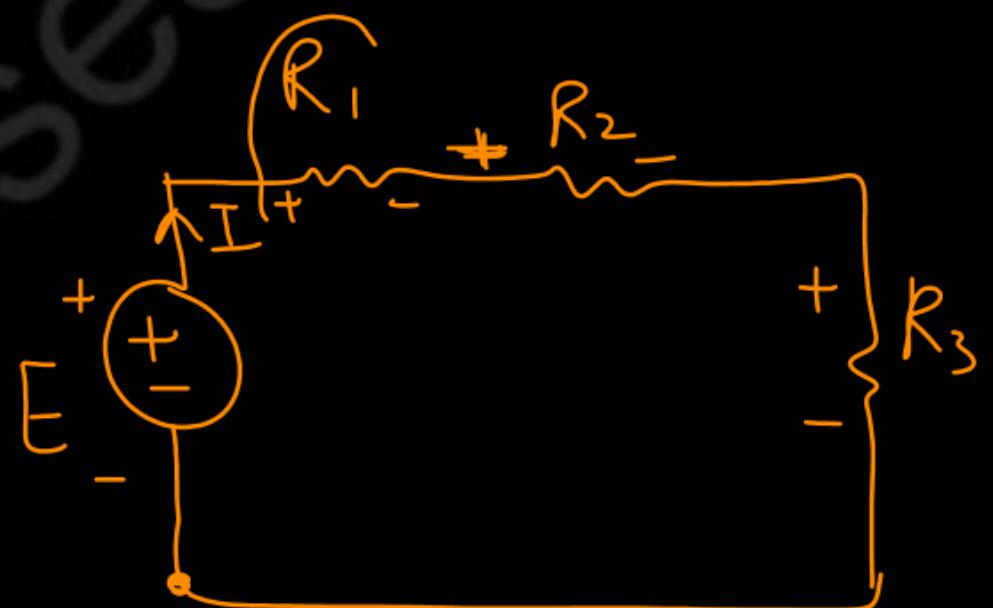


# Kirchhoff's Voltage Law (KVL)

**Kirchhoff's Voltage Law (KVL);-** According to KVL “algebraic sum of all the voltages around any closed loop in a circuit is equal to zero”.

$$\sum(\vec{E} + \vec{I}\vec{R}) = 0$$

$$-\underbrace{E}_{-E} + \underbrace{IR_1}_{V_1} + \underbrace{IR_2}_{V_2} + \underbrace{IR_3}_{V_3} = 0$$



Current int Reris =  $\alpha$ 

# Mesh Analysis(KVL)

① find mesh  
mode  $\rightarrow$  Equ  $\rightarrow$  Q

**Methods for solving electric Network Using KVL (Mesh Analysis )**

**Ex.- Using Mesh Analysis Find Current in all branches.**

## 1. Loop Current Method $\rightarrow$

Apply KVL in loop ①

$$+3I_1 + 4(I_1 - I_2) - 20 = 0$$

$$7I_1 - 4I_2 = 20 \quad \text{---} ①$$

Apply KVL in mesh ②,

$$+5I_2 + 5(I_2 - 1) + 4(I_2 - I_1) = 0$$

$$-4I_1 + 14I_2 = 5 \quad \text{---} ②$$

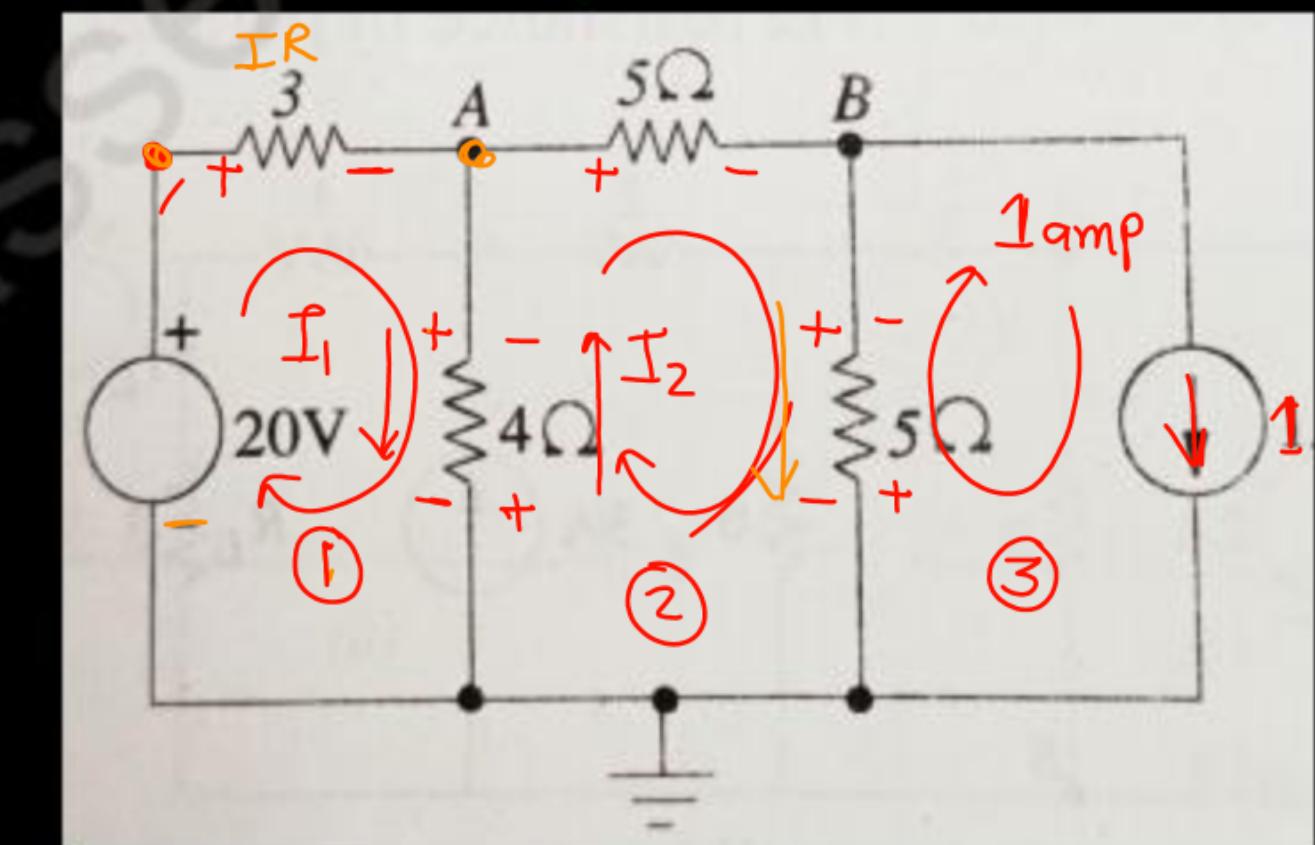
Solv Equ ① & ②

$$I_1 = 3.65 \text{ amp}$$

$$I_2 = 1.40 \text{ amp}$$

$$I_{4\Omega} = I_1 - I_2$$

$$\begin{aligned} &= 3.65 - 1.40 \\ &= 2.25 \text{ amp} \downarrow \end{aligned}$$



mesh

Similar question in AKTU- 2021-22

# Kirchhoff's Voltage Law (KVL)

Ex.- Using Mesh Analysis Find Current in all branches.

## 1. Branch Current Method

Apply KVL in Loop ①

$$I = 3.65$$

$$+3I + 4(I - I_1) - 20 = 0 \quad I_1 = 1.40$$

$$7I - 4I_1 = 20 \quad \text{---} ①$$

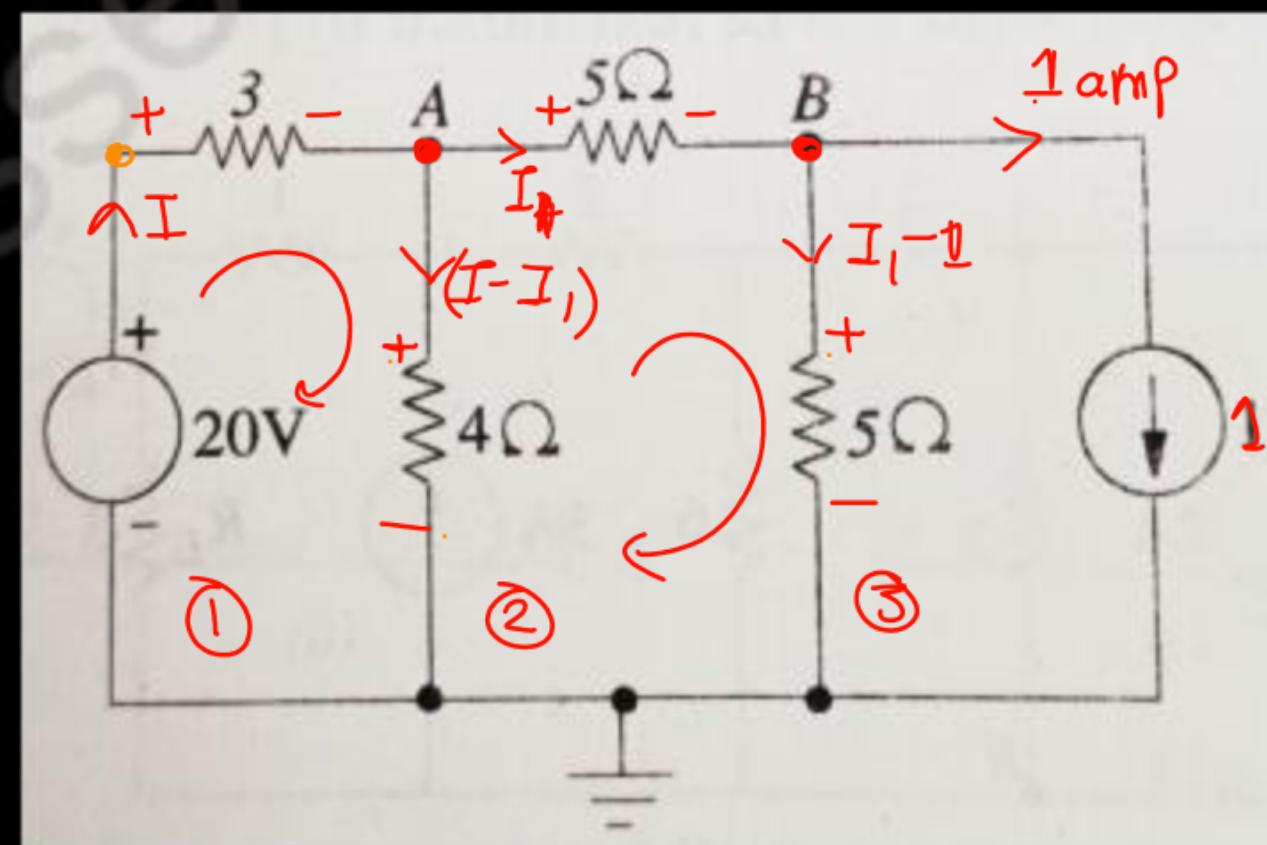
Apply KVL in Mesh ②,

$$I_4 = I - I_1$$

$$5I_1 + 5(I_1 - 1) - 4(I - I_1) = 0 \quad = 3.65 - 1.40 \\ -4I + 14I_1 = 5 \quad \text{---} ② \quad = 2.25 \text{ amp}$$

Solve Eq ① & ②

Similar question in AKTU- 2021-22



# Mesh Analysis (Concept of Super Mesh)

Ex.- Using Mesh Analysis Find Current in 5 Ohm.

AKTU- 2021-22 C.O., 2019-20, 2018-19

If any Current Source is Common b/w two mesh. Then  
These two meshes are combined and known as Super mesh.

Apply KVL in Loop ①

$$+4I_1 + 2(I_1 - I_2) - 15 = 0$$

$$6I_1 - 2I_2 = 15 \quad \text{---} \textcircled{1}$$

Apply KVL in Supermesh,

$$+3(I_2 + 6) + 5(I_2 + 6) + 2(I_2 - I_1) = 0$$

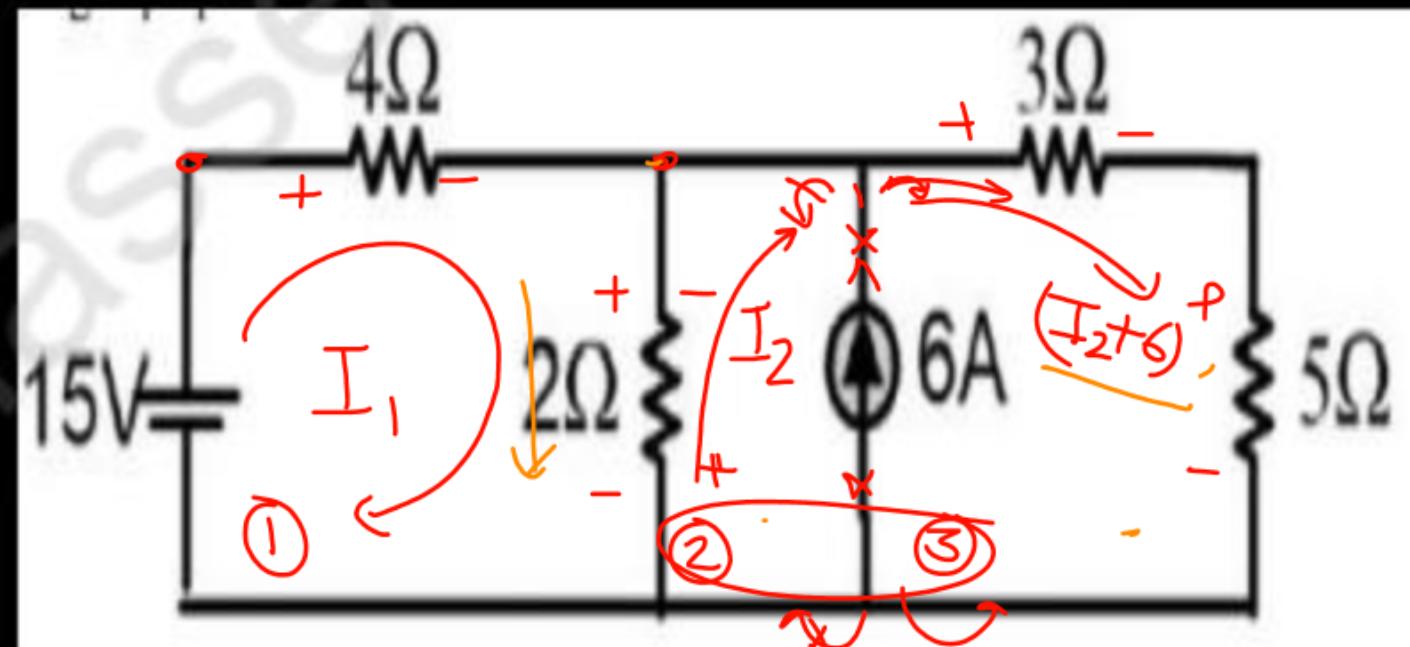
$$-2I_1 + 10I_2 = -48 \quad \text{---} \textcircled{2}$$

Solve Eqn ① & ②

$$I_1 = 0.96 \text{ amp}$$

$$I_2 = -4.6 \text{ amp}$$

$$I_{5\Omega} = I_2 + 6 \\ = -4.6 + 6 = 1.4 \text{ amp}$$



# Mesh Analysis

**Ques.** Find Current in 1 ohm Resistance using Mesh Analysis.

AKTU 2021-22

Apply KVL in loop ①

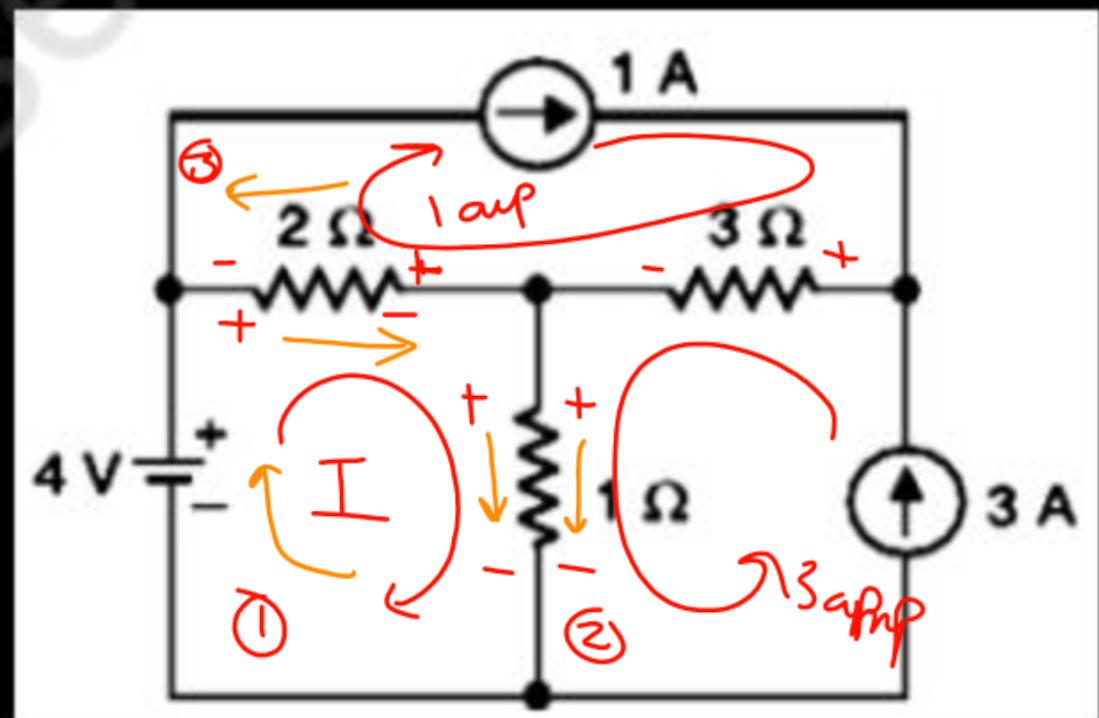
$$+2(I-1) + 1(I+3) - 4 = 0$$

$$3I - 2 + 3 - 4 = 0$$

$$3I = 3$$

$$\boxed{I = 1 \text{ amp}}$$

$$\begin{aligned} I_{1\Omega} &= I + 3 \\ &= 1 + 3 = 4 \text{ amp} \end{aligned}$$



# Mesh Analysis

**Ex. Using Mesh Analysis Find Current in 12 ohm Resistance.**

AKTU- 2018-19.

Apply KVL in mesh ②

$$+8(I_1 + 20) - 40 + 4(I_1 + I_2) + 5(I_1) = 0$$

$$17I_1 + 4I_2 = -12 \quad \textcircled{1}$$

Apply KVL in mesh ③

$$+12(I_2) - 40 + 4(I_2 + I_1) = 0$$

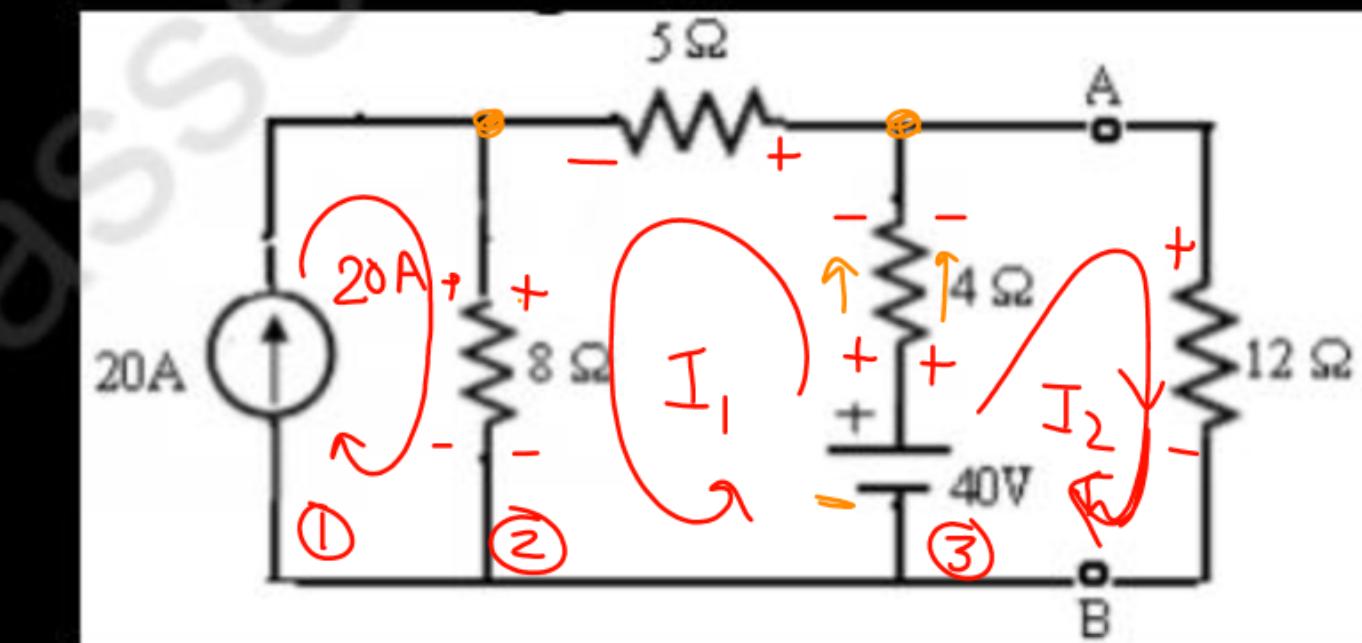
$$4I_1 + 16I_2 = 40 \quad \textcircled{2}$$

Solve Eqn ① & ②

$$I_1 = \cancel{-20} - 8 \cdot \cancel{125}$$

$$I_2 = \cancel{-03} 4.53$$

$$\left| \begin{array}{l} I_{12\Omega} = I_2 \\ = 4.53 \end{array} \right.$$



Ave

# Mesh Analysis

Ex.- Using Mesh Analysis Find Current in 6 Ohm. AKTU- 2021-22 C.O.

Apply KVL in mesh ①

$$2I_1 + 6(I_1 - I_2) + 6 + 4(I_1) - 10 = 0$$

$$12I_1 - 6I_2 = 4 \quad \text{--- } ①$$

Apply KVL in mesh ②

$$3I_2 + 2 + 5(I_2) - 6 + 6(I_2 - I_1) = 0$$

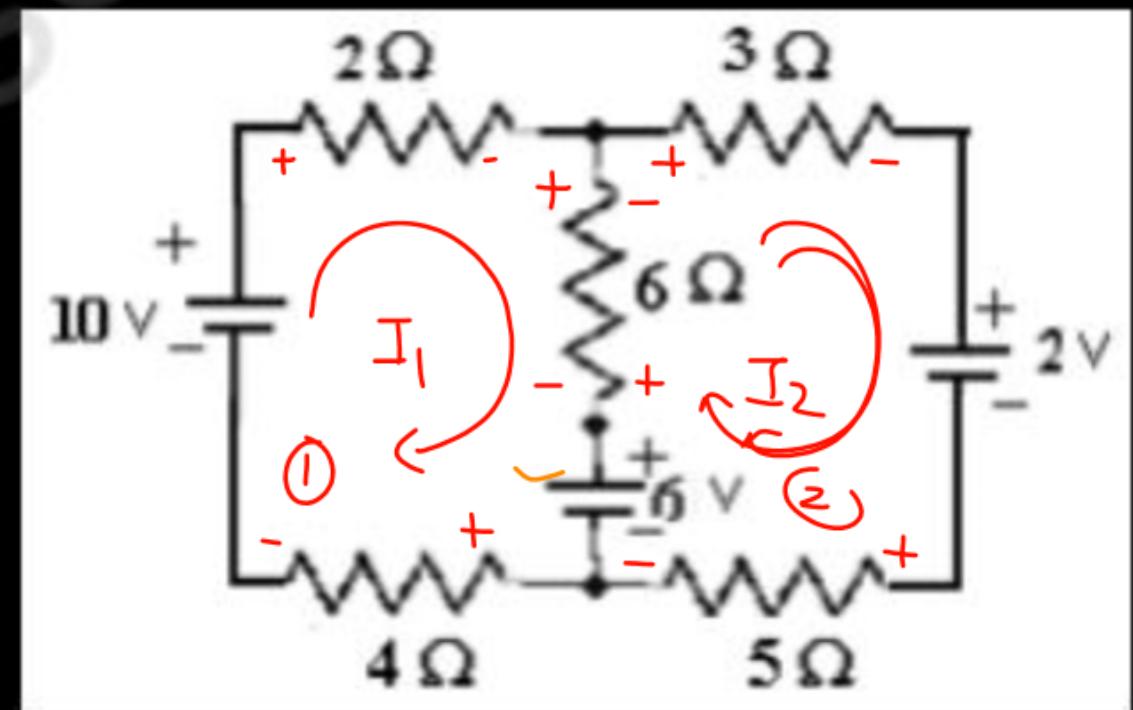
$$-6I_1 + 14I_2 = 4 \quad \text{--- } ②$$

Solve Eqn ① & ②

$$I_1 = 0.6 \text{ A}$$

$$I_2 = 0.54 \text{ A}$$

$$\begin{aligned} I_6 &= I_1 - I_2 \\ &= 0.6 - 0.54 \\ &= 0.06 \text{ A} \end{aligned}$$



# Mesh Analysis

Ex. Using Mesh Analysis Find Current in  $3\Omega$  Resistance.

Apply KVL in Supermesh.

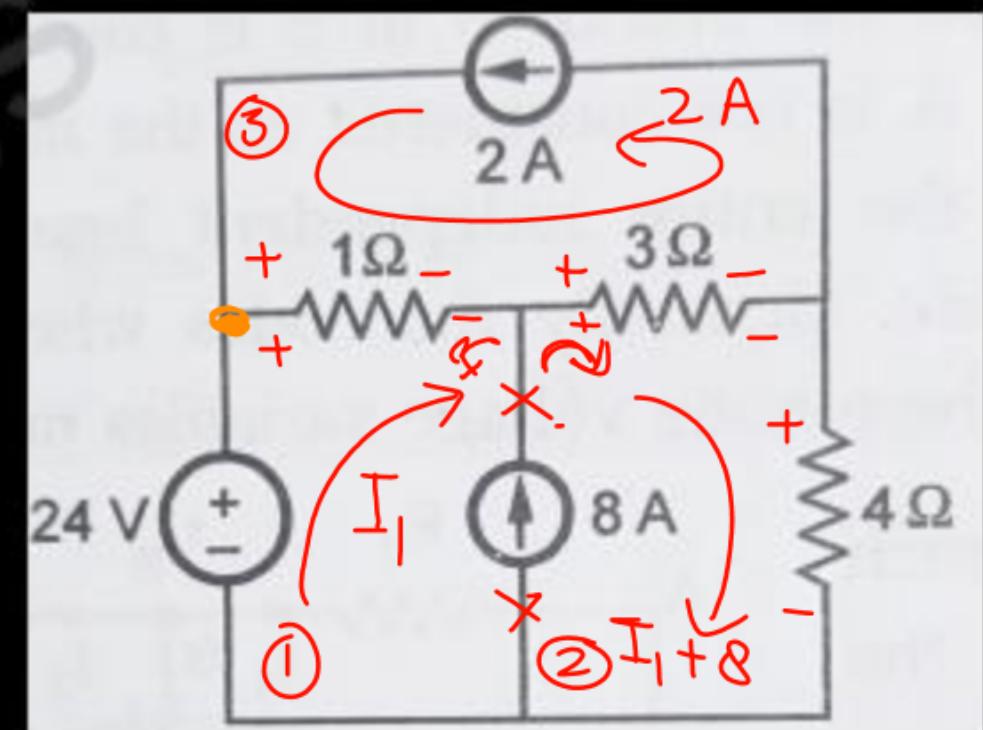
$$1(I_1 + 2) + 3(I_1 + 8 + 2) + 4(I_1 + 8) - 24 = 0$$

$$I_1 + 2 + 3I_1 + 30 + 4I_1 + 32 - 24 = 0$$

$$8I_1 = -40$$

$$\boxed{I_1 = -5 \text{ A}}$$

$$\begin{aligned} I_{3\Omega} &= I_1 + 8 + 2 \\ &= -5 + 8 + 2 \\ &= +5 \text{ A} \end{aligned}$$

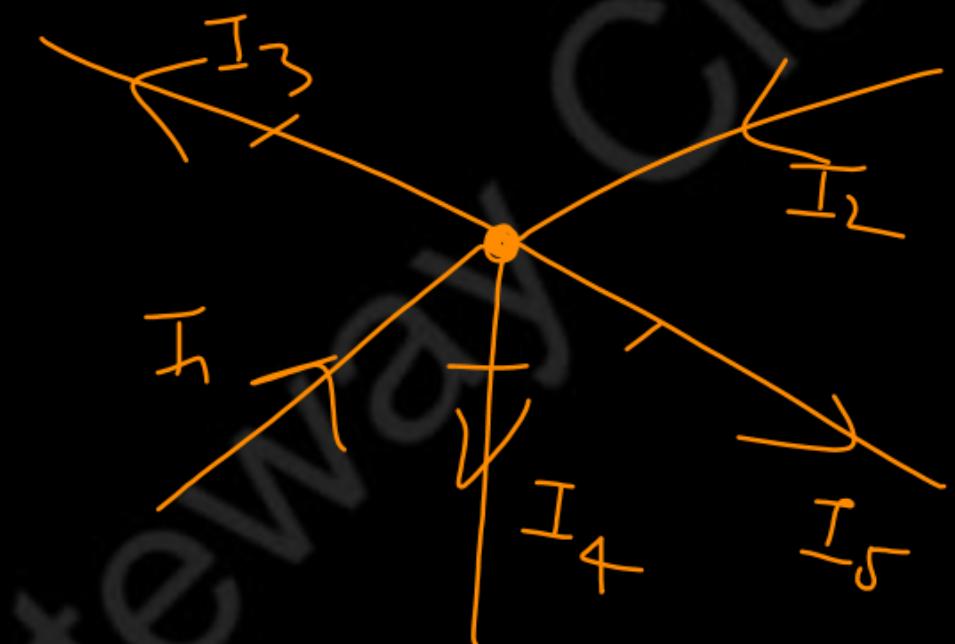


# Kirchhoff's Current Law (KCL)

**Kirchhoff's Current Law (KCL):-** According to KCL "Algebraic sum of all the Current at a node is always equal to zero"

Or

*"Sum of incoming current at a node is always equal to the sum of outgoing currents from that node."*



$$I_1 + I_2 = I_3 + I_4 + I_5$$

# Nodal Analysis

**Examples:-Using Nodal Analysis Find Current in 8 ohm**

Resistance.

$$I_1 = \frac{0-V+2}{6} = \frac{2-V}{6}$$

$$I_2 = \frac{V-0}{8} = \frac{V}{8}$$

Apply KCL at Node

$$2+I = I_2$$

$$2 = I_2 - I = \frac{V}{8} - \frac{2-V}{6} = \frac{3V-8+4V}{24}$$

$$7V-8 = 48$$

$$7V = 56$$

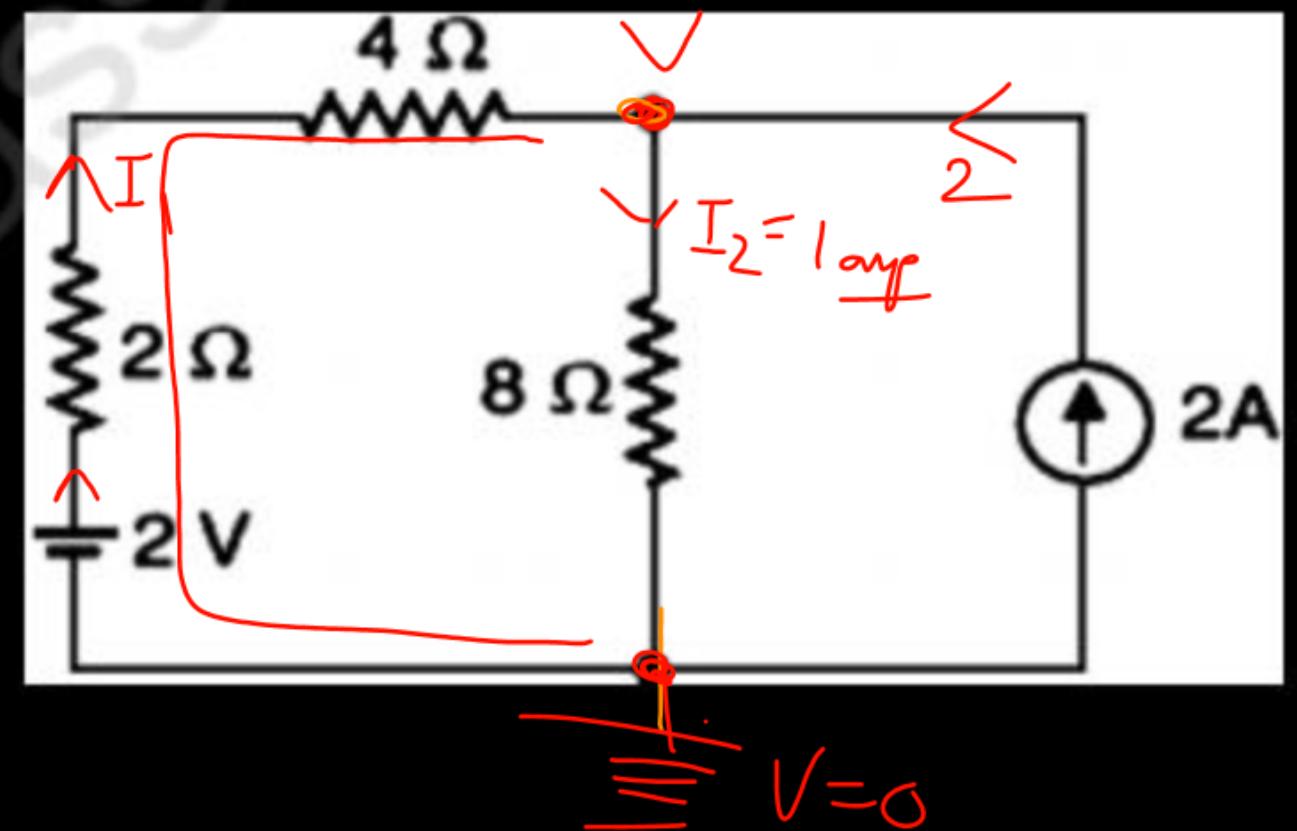
$$V = \frac{56}{7} \Omega = 8 \text{ Volt.}$$

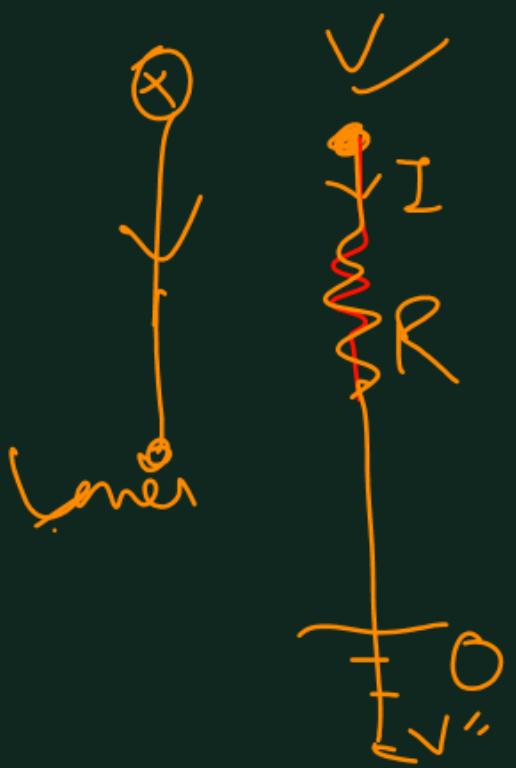
$$I_8 = I_2 = \frac{V}{8} = \frac{8}{8} = 1 \text{ amp}$$

find Junction Current divide)

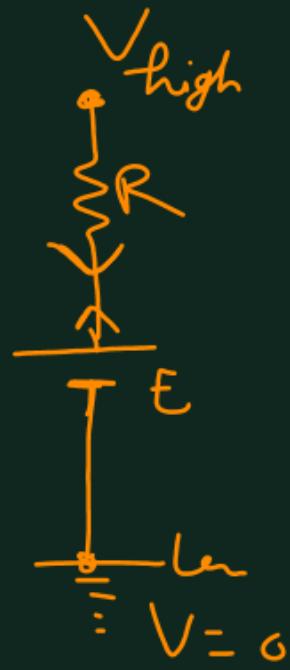
- Consider Ref Node

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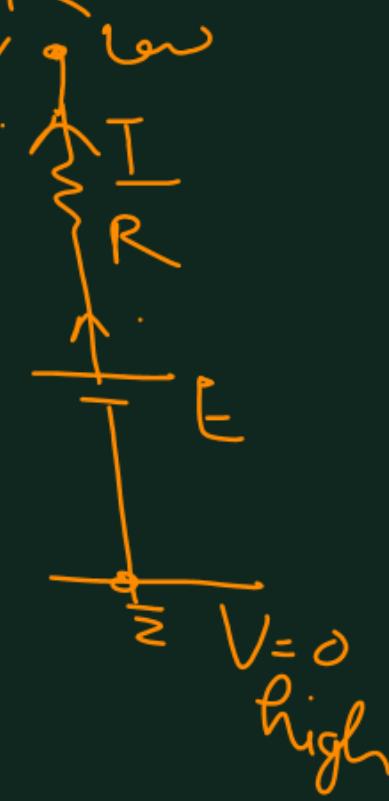




$$= I = \frac{V - O}{R}$$



$$\frac{V - O - E}{R}$$



$$\frac{O - V + E}{R}$$

# Concept of Super Node

**Ex. Using Nodal Analysis Find Current in 2 ohm Resistance.**

$$3 = I_1 + I_3 + 2$$

$$3 = \left(\frac{V_1 - 0}{2}\right) + \left(\frac{V_2 - 0}{1}\right) + 2$$

$$3 = \frac{V_1}{2} + V_2 + 2$$

$$3 = \frac{V_1 + 2V_2 + 4}{2}$$

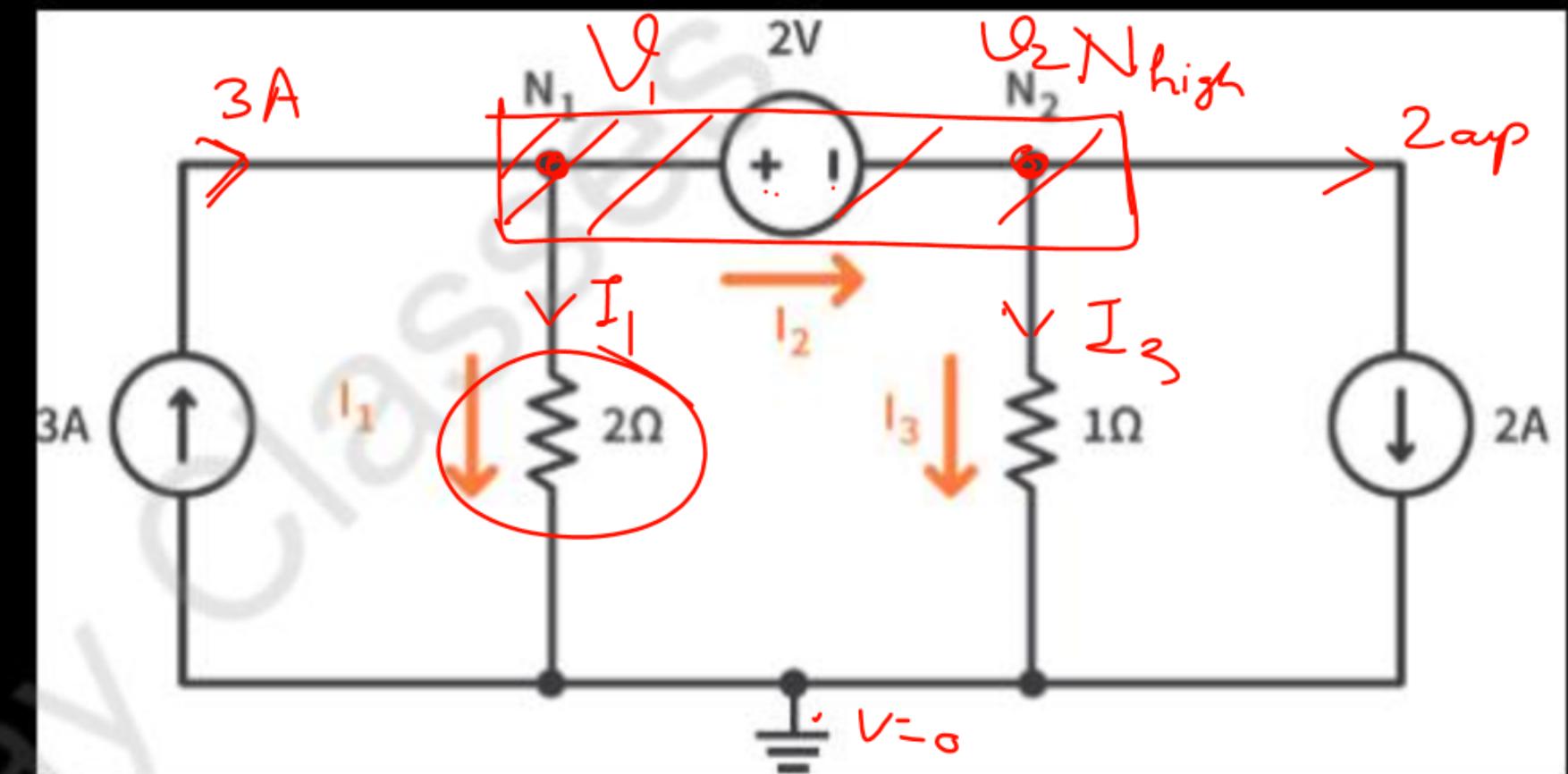
$$\boxed{\begin{aligned} V_1 + 2V_2 &= 6 - 4 = 2 \\ \boxed{V_1 + 2V_2 &= 2} \end{aligned}}$$

$$V_1 - V_2 = 2 - ②$$

$$V_1 = 2$$

$$V_2 = 0$$

$$I_1 = \frac{V_1}{2} = \frac{2}{2} = 1 \text{ amp}$$



# Nodal Analysis

Ex.- Using Nodal Analysis Find Current in all branches. AKTU- 2021-22

Apply KCL at ①

$$15 = I_1 + I_2$$

$$V_1 + V_1 - V_0 = 15$$

$$2V_1 - V_0 = 15 \quad \text{---} ①$$

Apply KCL at ②

$$I_2 = I_3 + I_4$$

$$V_1 - V_0 = \frac{V_0}{4} + \frac{V_0 - 10}{4}$$

$$4(V_1 - V_0) = 2V_0 - 10$$

$$4V_1 - 6V_0 = -10 \quad \text{---} ②$$

Solve  $\Sigma$  ① & ②

$$V_1 = 12.5 \text{ V}$$

$$V_0 = 10 \text{ V}$$

$$I_1 = \frac{V_1 - 0}{1} = V_1 = 12.5 \text{ A}$$

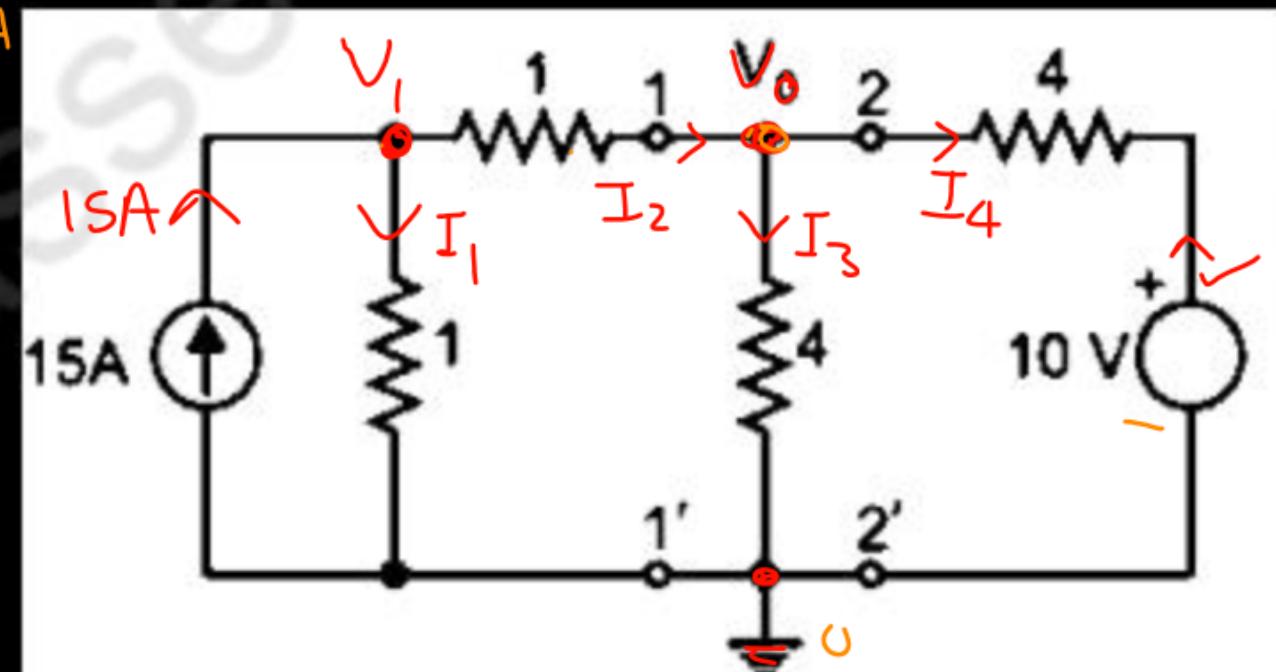
$$I_2 = \frac{V_1 - V_0}{1} = 2.5$$

$$I_3 = \frac{V_0}{4} = \frac{10}{4} = 2.5$$

$$I_4 = \frac{V_0 - 0 - 10}{4}$$

$$= \frac{V_0 - 10}{4}$$

$$\boxed{I_4 = 0}$$



## Nodal Analysis

Ex.- Using Nodal Analysis Find Current in 50 ohm. AKTU- 2021-22

$$I_1 + I_2 + 120 + 40 = 0$$

$$I_1 + I_2 = -160$$

$$\frac{V_1}{50} + \frac{V_2}{150} = -160 \quad \text{--- } ①$$

from Supernode

$$V_2 - V_1 = 10 \quad \text{--- } ②$$

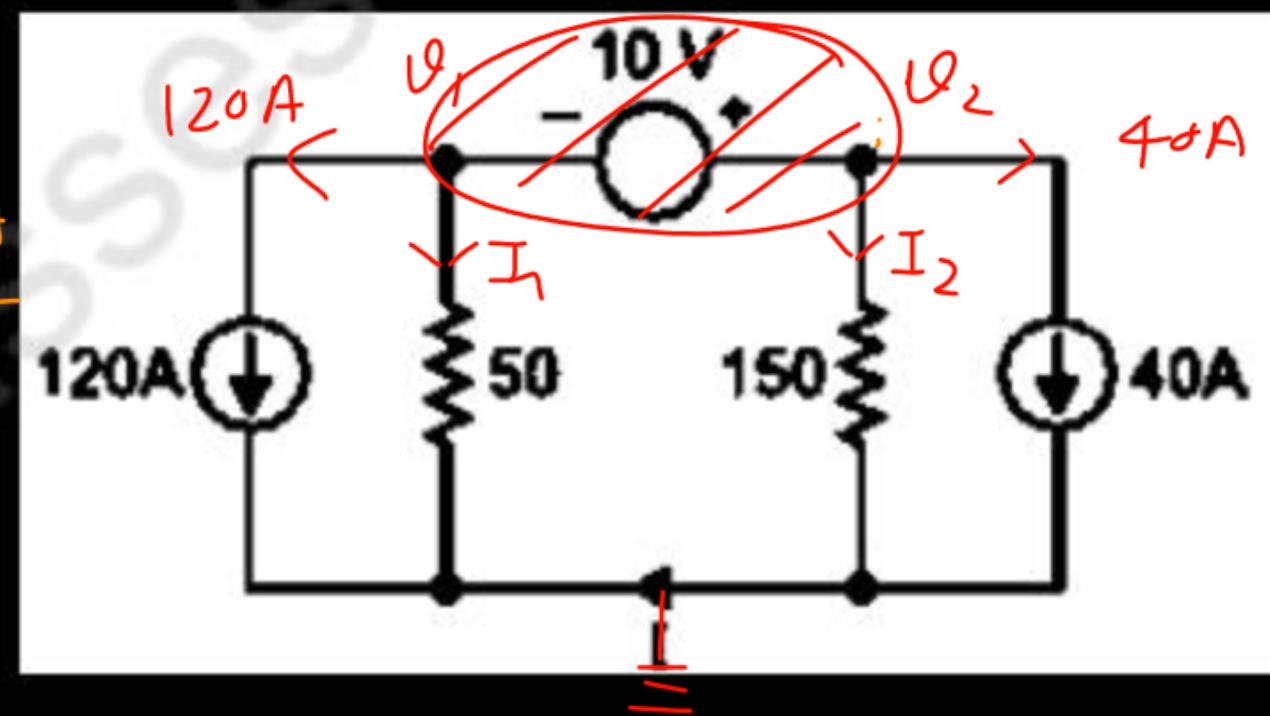
$$V_1 = -6002.5 \text{ V}$$

$$V_2 = -5992.5 \text{ V}$$

$$I_1 = \frac{V_1}{50} = -\frac{6002.5}{50} = -120.05 \text{ A}$$

*Ans*

$$I_2 = \frac{V_2}{150}$$



## Nodal Analysis

Ex. Using Nodal Analysis Find Current in 8 ohm Resistance. AKTU-2021-22

$$I_1 + I_2 + I_3 + 2 = 0$$

$$\frac{90 - V_1}{20} + \frac{60 - V_1}{12} - \frac{V_1}{8} = -2$$

$$\frac{90}{20} - \frac{V_1}{20} + \frac{60}{12} - \frac{V_1}{12} - \frac{V_1}{8} = -2$$

$$-\frac{V_1}{20} - \frac{V_1}{12} - \frac{V_1}{8} = -2 - 9.5$$

$$+0.258 V_1 = -11.5$$

$$V_1 = 44.51 \text{ Volt}$$

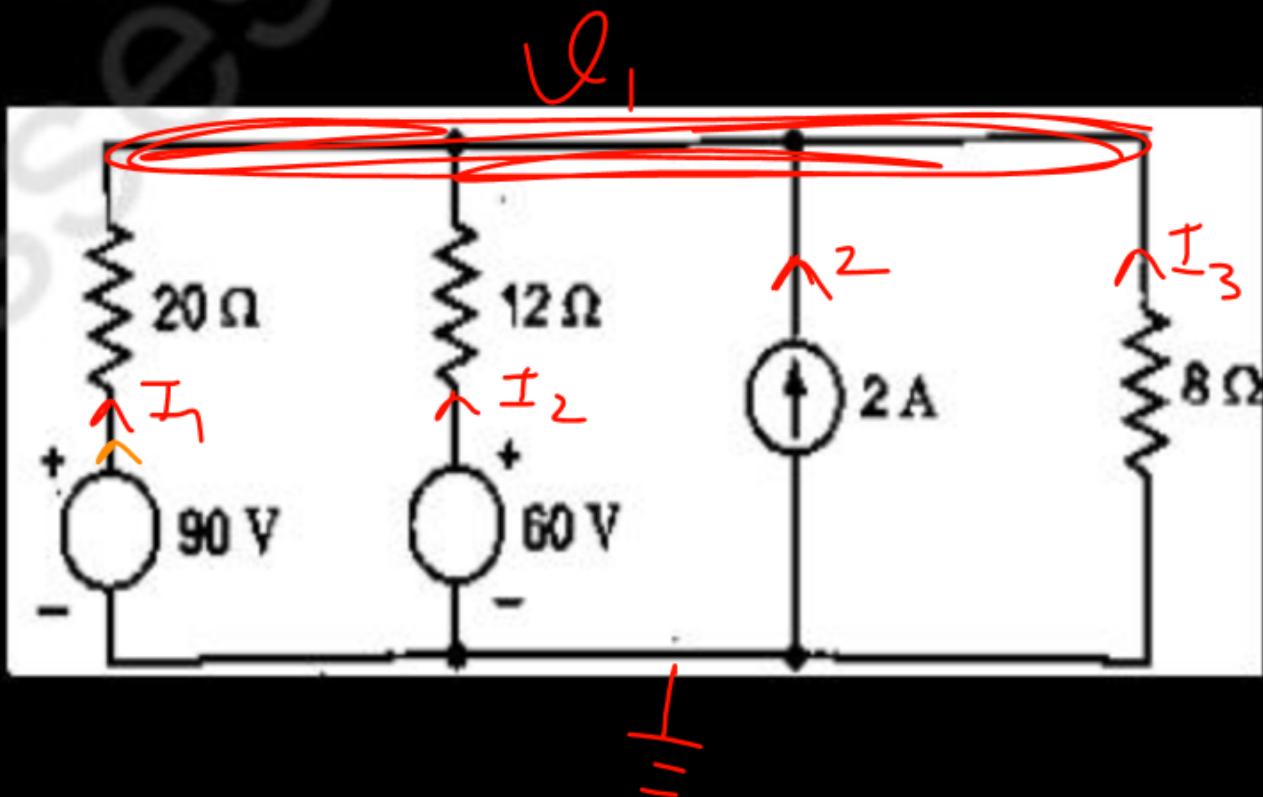
$$I_1 = \frac{0 - V_1 + 90}{20} = \frac{90 - V_1}{20}$$

$$I_2 = \frac{60 - V_1}{12}$$

$$I_3 = -\frac{V_1}{8} = -\frac{44.51}{8}$$

$$= -5.56 \text{ A}$$

Ans



## Nodal Analysis

Ex. Using Nodal Analysis Find Current in  $r_2$  Resistance.

AKTU- 2021-22

$$I_1 = I_2 + I_3 + I_4$$

$$\frac{50 - V_1}{20} = \frac{V_1}{100} + \frac{V_1}{120} + \frac{V_1 - 20}{30}$$

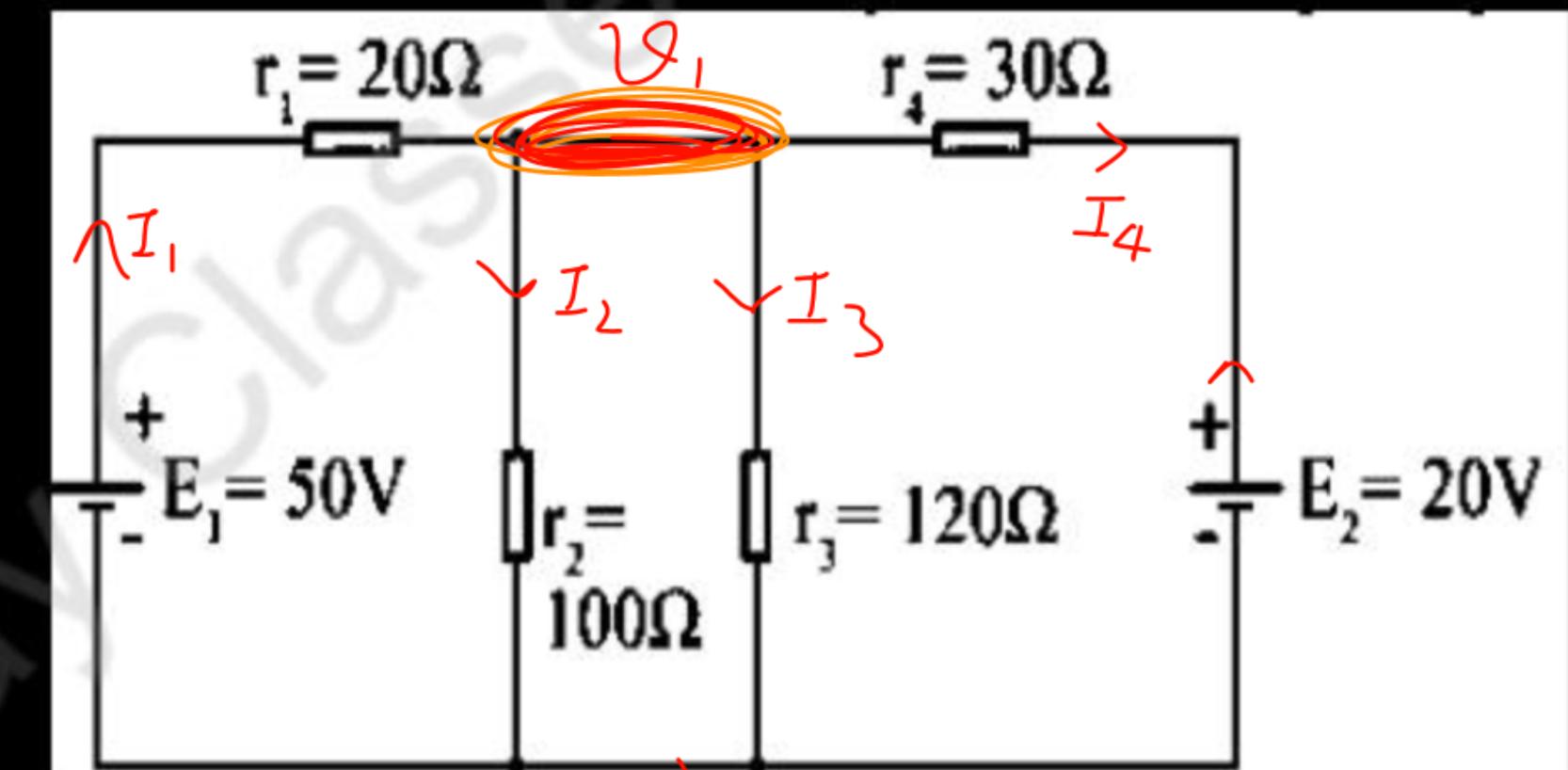
$$V_1 = ?$$

$$I_1 = \frac{50 - V_1}{20}$$

$$I_2 = \frac{V_1}{100}$$

$$I_3 = \frac{V_1}{120}$$

$$I_4 = \frac{V_1 - 20}{30}$$



Q.1 What Is E.M.F? **(AKTU-2021-22)**

Q.2 Differentiate between EMF and Potential Difference.? **(AKTU-2021-22)**

Q.3 Why Linearity is important? **(AKTU-2021-22)**

Q.4 Can we apply KVL in a loop containing a current source? Give answer with reason. **(AKTU-2018-19)**

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# Thank You



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