

## Assignment 2

### Q1) Computer Staffing Centre

#### 1) Assuming that there are full time workers in 3 shifts $s_1, s_2, s_3$

Number of full-time employees in 8am – 4 pm =  $s_1$

Number of full-time employees in 12pm -8pm =  $s_2$

Number of full-time employees in 4pm-12 am =  $s_3$

#### 2) Assuming the part time employees for the shifts are $x_1, x_2, x_3, x_4$

Number of full-time employees in 8am-12 pm =  $x_1$

Number of full-time employees in 12pm-4pm =  $x_2$

Number of full-time employees in 4pm -8 =  $x_3$

Number of full-time employees in 8-12 am =  $x_4$

#### 3) Constraints:

8-12 am  $\geq 4$ , i.e.  $s_1 + x_1 \geq 4$

12pm-4pm  $\geq 8$ , i.e.  $s_1 + s_2 + x_2 \geq 8$

4pm -8  $\geq 10$ , i.e.  $s_2 + s_3 + x_3 \geq 8$

8-12 am  $\geq 6$ , i.e.  $s_3 + x_4 \geq 6$

One full time should be there with part time during a shift

$s_1, s_2, s_3, x_1, x_2, x_3, x_4 \geq 0$

Min :  $112 S_1 + 112 S_2 + 112 S_3 + 48 X_1 + 48 X_2 + 48 X_3 + 48 X_4$

st:

$s_1 + x_1 \geq 4$

$s_1 + s_2 + x_2 \geq 8$

$s_2 + s_3 + x_3 \geq 8$

$$s_3 + x_4 \geq 6$$

$$s_1 \geq x_1 \text{ for 1}^{\text{st}} \text{ shift}$$

$$s_1 + s_2 \geq x_2 \text{ for 2}^{\text{nd}} \text{ shift}$$

$$s_2 + s_3 \geq x_3 \text{ for 3}^{\text{rd}} \text{ shift}$$

$$s_3 \geq x_4 \text{ for 4}^{\text{th}} \text{ shift}$$

Minimum number of employees required are = **28**

Time required to complete the work is 4, total number of fulltime = **28/4=7**  
and remaining **14** are parttime

Given Fulltime employees are paid 14 \$/hr and for 8 hrs = **14 \* 8 = 112**,  
Therefore 7 FT salary per head is = **112\*7 = 784**

Part time employees are paid 12 /h and for 4 hrs from the table = **12 \* 4 = 48**

For 14 parttime employees = **48 \* 14 = 672**

Therefore, minimum daily cost is = **784 + 672 = 1456**

### **B ) If 1 hr break is provided**

If one hour break is provided, then full time employees will work for only 7 hrs

And the cost will be = **14\*8 = 98**, and for 7 employees = **98 \* 7 = 686**

Since part time employees does not have a break, their cost will remain at = **672**

Total minimum daily cost after providing 1 hrs break is = **686 + 672 = 1358**

Minimum cost = **98 \$**.

### **Question 2 )**

C = number of collegiate bags

M = number of minis

**Maximize**

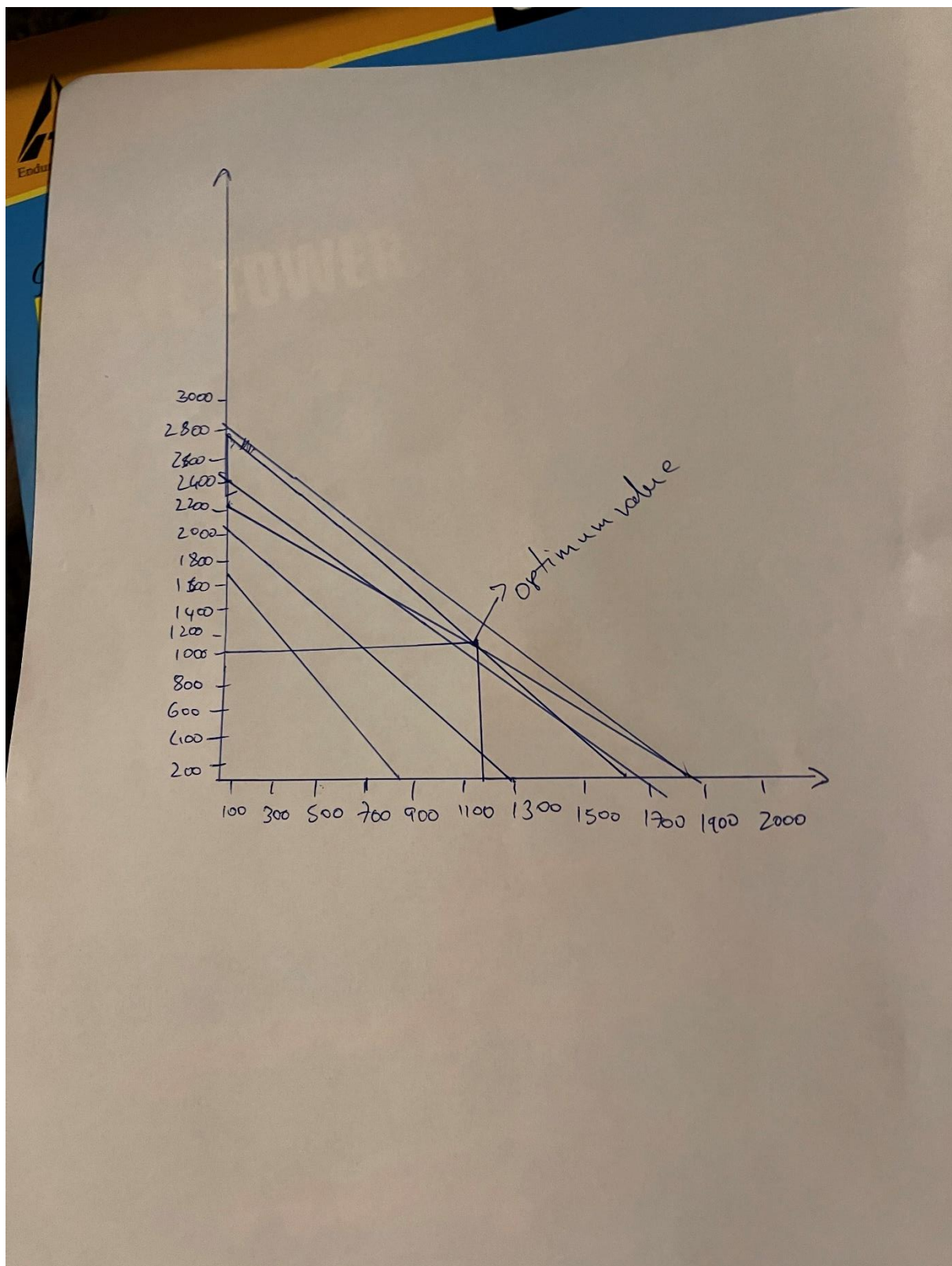
$$\mathbf{Z = 32C + 24M}$$

St

$$3C + 2M \leq 5000, C \leq 1000, M \leq 1200$$

$$45C + 40M \leq 35 \cdot 60 \cdot 40, 45C + 40M \leq 84000$$

$$C, M \geq 0$$



Graphical representation

### Question 3)

X = large, Y = Medium, Z = small

#### A) Decision Variables

Storage space for each size for X1, Y1, Z1.

Production per day X2, Y2, Z2

Forecast of sales X3, Y3, Z3

Total 9 decision variables

#### B) LP formulation.

$$\text{Max } P = 420(X1+X2+X3) + 360(Y1+Y2+Y3) + 300(Z1+Z2+Z3)$$

St

$$X1+Y1+Z1 \leq 750$$

$$X2+Y2+Z2 \leq 900$$

$$X3+Y3+Z3 \leq 450$$

Productions :

$$20X1+15Y1+12Z1 \leq 13000$$

$$20X2+15Y2+12Z2 \leq 12000$$

$$20X3+15Y3+12Z3 \leq 5000$$

Storage:

$$X1+X2+X3 \leq 900$$

$$Y1+Y2+Y3 \leq 1200$$

$$Z1+Z2+Z3 \leq 7500$$

$$1/750(X1 + Y1 + Z1) - 1/900(X2 + Y2 + Z2) = 0$$

$$1/750(X1 + Y1 + Z1) - 1/450(X3 + Y3 + Z3) = 0$$

Therefore:  $X1, X2, X3, Y1, Y2, Y3, Z1, Z2, Z3 \geq 0$

#### C) R pdf file in git hub