Statistical inference and linear models

February 20, 2018

If you get bored

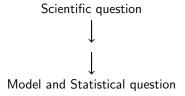
- Go to the last slide for bonus exercises
- Work on code for your research and ask question during exercise time
- But try and keep an eye out for interesting crumbs!

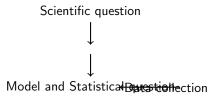


- Statistical inference
- 2 t-test, ANOVA, linear model

Scientific question

Scientific question





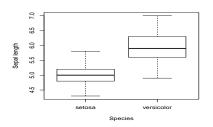
Reminder t.test

```
data("iris")
```

One t-test for sepal length between setosa and versicolor:

```
t.test(x = iris$Sepal.Length[iris$Species == "setosa"],
        y = iris$Sepal.Length[iris$Species == "versicolor"])
Welch Two Sample t-test
data: iris$Sepal.Length[iris$Species == "setosa"] and iris$Sepal.Le
t = -10.521, df = 86.538, p-value < 2.2e-16
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 -1.1057074 - 0.7542926
sample estimates:
mean of x mean of y
    5.006 5.936
```

Reminder t.test



- Means: 5.006 vs. 5.936
- Standard deviation: 0.35 and 0.52
- Standard error (SD/ \sqrt{n}): 0.05 and 0.07

When do we know it is different?

t-statistic unlikely to be large by chance

$$t = \frac{\mathsf{Mean}_1 - \mathsf{Mean}_2}{\mathsf{Variation}} \frac{\sqrt{\mathsf{Sample Size}}}{\sqrt{2}}$$

- Larger absolute difference
- Smaller variability
- Larger sample size

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Same for every statistical model

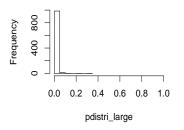
When do we know it is different? Try it!

1. Larger absolute difference

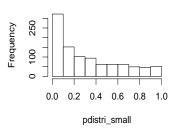
```
nbsim <- 1000
pdistri_large <- vector(length = nbsim)</pre>
pdistri_small <- vector(length = nbsim)</pre>
for (i in 1:nbsim)
  x1 \leftarrow rnorm(n = 10, mean = 2, sd = 1)
  x2 \leftarrow rnorm(n = 10, mean = 4, sd = 1) \#large diff
  x3 \leftarrow rnorm(n = 10, mean = 2.5, sd = 1) #small diff
  out_large <- t.test(x1, x2)</pre>
  out_small <- t.test(x1, x3)</pre>
  pdistri_large[i] <-out_large$p.value
  pdistri_small[i] <-out_small$p.value
```

When do we know it is different? Try it!

Prop signif= 0.985



Prop signi= 0.199



When do we know it is different? Try it!

Exercise

Follow the same approach to observe the effect of smaller variability and/or larger sample size.

By the way, what are these p-values?

Blabla Reference to a null-model Under null hypothesis, uniform distribution. Implies proportion(significance) = 0.05

T-test exercise

```
t.test(x = ..., y=..., var.equal = TRUE)
t.test(x = ..., y=..., var.equal = FALSE)
```

What if variance are different by chance only?

```
set.seed(1234)
var(rnorm(20, mean = 0, sd = 1))
[1] 1.027806
var(rnorm(20, mean = 0, sd = 1))
[1] 0.6265501
```

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A small example

Animal behavior in response to weather. Measure activity

t-test

```
fitstudent <- t.test(x = dat.behav$activity[dat.behav$weather=="rain
                     y = dat.behav$activity[dat.behav$weather=="sunn
                     var.equal = TRUE)
print(fitstudent)
Two Sample t-test
data: dat.behav$activity[dat.behav$weather == "rainy"] and dat.behav
t = 3.2752, df = 33, p-value = 0.002485
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 0.6138373 2.6270325
sample estimates:
mean of x mean of y
 6.781476 5.161041
```

ANOVA

```
fitanova <- aov(data = dat.behav, formula = activity ~ weather)

summary(fitanova)

Df Sum Sq Mean Sq F value Pr(>F)

weather 1 11.25 11.253 10.73 0.00248 **

Residuals 33 34.62 1.049

---

Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Linear regression

```
fitlm <- lm(data = dat.behav, formula = activity ~ weather)
summary(fitlm)
Call:
lm(formula = activity ~ weather, data = dat.behav)
Residuals:
   Min 1Q Median 3Q Max
-2.3547 -0.6028 0.2346 0.6419 1.6534
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 6.7815 0.4581 14.805 3.94e-16 ***
weathersunny -1.6204 0.4948 -3.275 0.00248 **
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Residual standard error: 1.024 on 33 degrees of freedom

Linear models

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