#### 1

# **GATE ASSIGNMENT 4**

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## Download all python codes from

https://github.com/Ananthoju-Pranav-Sai/EE3900/blob/main/Gate Assignment 2/codes

### and latex-tikz codes from

https://github.com/Ananthoju-Pranav-Sai/EE3900/ tree/main/Gate\_Assignment\_2/ Gate Assignment 2.tex

## 1 GATE EC 2010 Q.16

For an N-point FFT Algorithm with  $N = 2^m$  which one of the following statements is TRUE?

- A It is not possible to construct a signal flow graph with both input and output in normal order
- B The number of butterflies in the  $m^{th}$  stage in N/m
- C In-place computation requires storage of only 2N node data
- D computation of a butterfly requires only one complex multiplication.

### 2 Solution

The FFT algorithm decomposes the DFT into  $\log_2 N$ , each of which consists of N/2 butterfly computations.

Each butterfly computes 2 complex numbers  $p+\alpha q$  and  $p-\alpha q$  where  $\alpha$  is a complex number.

The number of butterflies in  $m^{th}$  stage is N/2. So, option (B) is incorrect.

There are  $\log_2 N$  stages and each stage consists of N/2 butterflies and each butterfly consists 2 nodes. So computation requires storage  $N \log_2 N$  node data. So, option (C) is incorrect

As each butterfly computes 2 complex number  $p+\alpha q$  and  $p-\alpha q$ , so it requires one complex multiplication  $(\alpha q)$  and 2 complex additions. So, option (D) is correct.

It is possible to construct a signal flow graph with input and output in normal. Example for m=3.

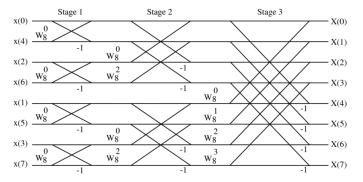


Fig. 4: Signal flow graph for m=3