

# Time Complexity

 **algorithms365**  
Performance with purpose

## Time Complexity.

- \* Time Complexity is a way to describe how long an algorithm... (a step-by-step method to solve a problem) takes to run, depending on the size of the input it's given.  $T_n$ .

### 1. Identify the Basic operation's

Determine the most significant operations in the algorithm. These are operations that most affect the algorithm's runtime, such as comparisons, assignments, and Arithmetic operations.

### 2. Count the Basic operation.

Count how many times these basic operations are executed as a function of the input size  $n$ .

This involves analysis loops, recursive calls, and any other constructs that affect the runtime.

### 3 Express the Count as a function

Express the total no. of operations as a mathematical function of  $n$ , where  $n$  is the size of input.

### 4. Simplify the function

Simplify the function by keeping only the dominant term, which is the term that grows the fastest as  $n$  increases. Discard constants and less significant terms because they have a negligible effect on the growth rate for large  $n$ .

### 5 Use Big O Notation

Express the simplified function using Big O notation to describe the time complexity. Big O notation



Provides an upper bound on the growth rate, focusing on the dominant term

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Constant  $O(1)$

Index	value
0	1
1	2
2	3
3	4
4	5
5	6

numbers[5]

here time is Constant

Logarithmic  $O(\log n)$  → data half/compare

1	2	3	4	5	6	7	8	9	10
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Binary search key = 9 → Sorted

Element end → worst case scenario

1	2	3	4	5	6	7	8	9	10
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X > 9

$n/2$  |  $n/4$  |  $100 \rightarrow 10$

Linear  $O(n)$

23	48	523	65	150	72	93
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Search = 150

Quadratic  $O(n^2)$

#	ID	#	ID
1	123	1	459
2	765	2	227
3	999	3	234
4	500	4	587

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find the common element in these two arrays

$$n \times n = n^2$$

Cubic  $O(n^3)$

#	ID	#	ID	#	ID
1	123	1	643	1	56
2	765	2	344	2	765
3	999	3	123	3	45
4	500	4	456	4	67

$$n \times n \times n = n^3$$

Exponential  $O(2^n)$  → takes more time

1	2	3	4	5	6	7	8	9	10
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All possible  
subset

Factorial  $O(n!)$  → takes more time than Exponential  
Generates all possible seating arrangements for a list of friends' IDs

1	2	3	4	5	6	7	8	9	10
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1 2 3  
2 3 1  
1 3 2

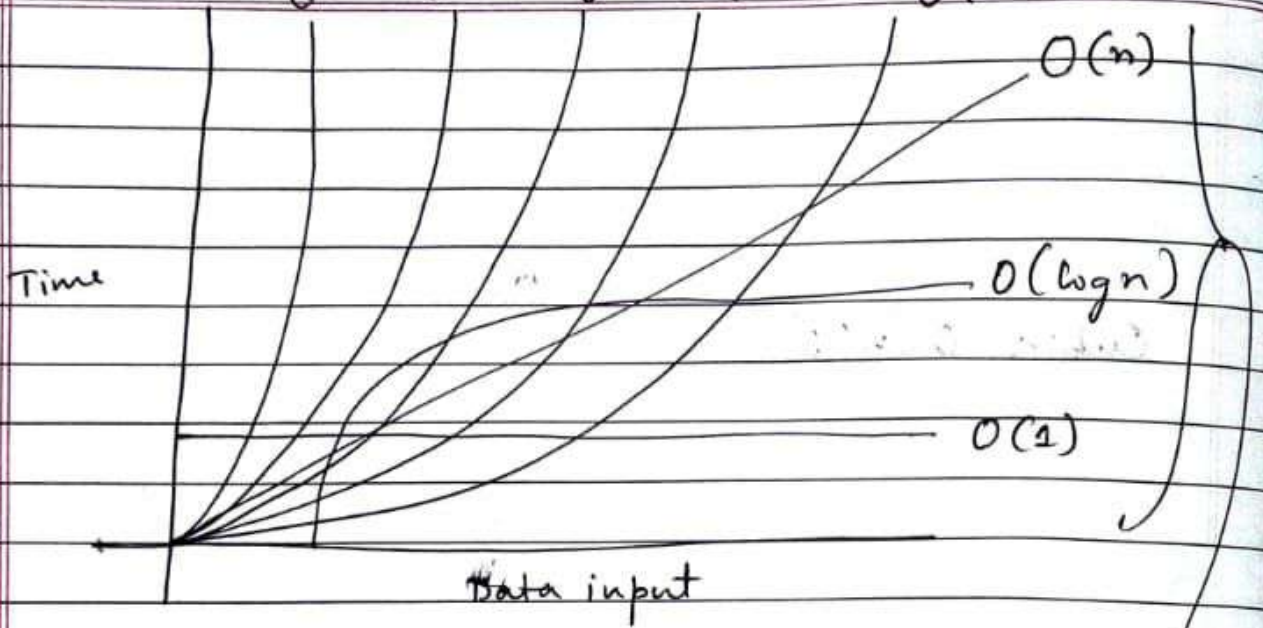


# Comparison of time complexity

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$O(n!)$   $O(n^n)$   $O(2^n)$   $O(n^3)$   $O(n^2)$



These 3 are the most used complexity in every programming