

ICE-7

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1) Negation: $\neg p$

| p | $\neg p$ |
|-------|----------|
| True | False |
| False | True |

2) Conjunction: $p \wedge q$

| P | Q | $P \wedge Q$ |
|-------|-------|--------------|
| True | True | True |
| True | False | False |
| False | True | False |
| False | False | False |

3) Disjunction: $p \vee q$

| P | Q | $p \vee q$ |
|-------|-------|------------|
| True | True | True |
| True | False | True |
| False | True | True |
| False | False | False |

4) Implication: $p \Rightarrow q$

| P | Q | $p \Rightarrow q$ |
|-------|-------|-------------------|
| True | True | True |
| True | False | False |
| False | True | True |
| False | False | True |

5) Bi-Implication: $p \Leftrightarrow q$

| P | Q | $p \leftrightarrow q$ |
|-------|-------|-----------------------|
| True | True | True |
| True | False | False |
| False | True | False |
| False | False | True |

6) Contradiction: $p \wedge \neg p$

| P | Q | $p \wedge \neg p$ |
|-------|-------|-------------------|
| True | False | False |
| False | True | False |

7) Compound Propositions: (20%)

a. $(p \wedge q) \vee \neg q$

| P | Q | $(p \wedge q) \vee \neg q$ |
|-------|-------|----------------------------|
| True | True | True |
| True | False | True |
| False | True | False |
| False | False | True |

b. $(p \vee \neg q) \wedge \neg p$

| P | Q | $(p \vee \neg q) \wedge \neg p$ |
|-------|-------|---------------------------------|
| True | True | False |
| True | False | False |
| False | True | False |
| False | False | True |

c. $\neg(p \rightarrow q) \text{ and } p \wedge \neg q$

| p | q | r | $(p \wedge q) \rightarrow (p \wedge r)$ |
|---|---|---|---|
| 0 | 0 | 0 | True |
| 0 | 0 | 1 | True |
| 0 | 1 | 0 | True |
| 0 | 1 | 1 | True |
| 1 | 0 | 0 | True |
| 1 | 0 | 1 | True |
| 1 | 1 | 0 | False |
| 1 | 1 | 1 | True |

8) Among these given compound propositions equivalent? Show the truth table output side by side for each statement

a. $(p \wedge q) \rightarrow r$ and $P \rightarrow (q \wedge r)$

| p | q | r | $(p \wedge q) \rightarrow r$ | $P \rightarrow (q \wedge r)$ |
|---|---|---|------------------------------|------------------------------|
| 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 |

expressions not are equivalent

b. $(p \rightarrow q) \wedge (q \rightarrow p)$ and $p \leftrightarrow q$

| p | q | $(p \rightarrow q) \wedge (q \rightarrow p)$ | $p \leftrightarrow q$ |
|---|---|--|-----------------------|
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 |

expressions are equivalent

c. $\neg(p \rightarrow q)$ and $p \wedge \neg q$

| p | q | $\neg (p \rightarrow q)$ | $p \wedge \neg q$ |
|---|---|--------------------------|-------------------|
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 |
| 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 |

expressions are equivalent

d. $(p \rightarrow q) \wedge (p \rightarrow r)$ and $p \rightarrow (q \wedge r)$

| p | q | r | $(p \rightarrow q) \wedge (p \rightarrow r)$ | $p \rightarrow (q \wedge r)$ |
|---|---|---|--|------------------------------|
| 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 1 | 1 | 1 |
| 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 0 |
| 1 | 0 | 1 | 0 | 0 |
| 1 | 1 | 0 | 0 | 0 |
| 1 | 1 | 1 | 1 | 1 |

expressions are equivalent

9) Tautology:

Tautology means all have the same 1 or true as input

a. $p \vee \neg p$

| p | $p \vee \neg p$ |
|-------|-----------------|
| False | True |
| True | True |

b. $\sim (a \wedge b) \leftrightarrow (\sim a \vee \sim b)$

| a | b | $\sim(a \wedge b) \leftrightarrow (\sim a \vee \sim b)$ |
|-------|-------|---|
| False | False | 1 |
| False | True | 1 |
| True | False | 1 |
| True | True | 1 |

c. $((a \vee b) \wedge (a \rightarrow c)) \wedge (b \rightarrow c) \rightarrow c$

| a | b | c | $((a \vee b) \wedge (a \rightarrow c)) \wedge (b \rightarrow c) \rightarrow c$ |
|-------|-------|-------|--|
| False | False | False | True |
| False | False | True | True |
| False | True | False | True |
| False | True | True | True |
| True | False | False | True |
| True | False | True | True |
| True | True | False | True |
| True | True | True | True |

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