

# Gate 2022- Instrumentation Engineering

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**Question 11:** The input  $x(t)$  to a system is related to its output  $y(t)$  as

$$\frac{dy(t)}{dt} + y(t) = 3x(t-3)u(t-3)$$

Here  $u(t)$  represents a unit-step function.

The transfer function of this system is

(A)  $\frac{e^{-3s}}{s+3}$

(B)  $\frac{3e^{-3s}}{s+1}$

(C)  $\frac{3e^{-(s/3)}}{s+1}$

(D)  $\frac{e^{-(s/3)}}{s+3}$

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**Solution:**

$$\frac{dy(t)}{dt} + y(t) = 3x(t-3)u(t-3) \quad (1)$$

By applying Laplace Transform on both sides

$$sY(s) + Y(s) = 3X(s)e^{-3s} \quad (2)$$

Laplace transform of  $x(t-t_o)$  is  $X(s)e^{-st_o}$  where  $X(s)$  is laplace transform of  $x(t)$

$$Y(s)(s+1) = 3X(s)e^{-3s} \quad (3)$$

$$H(s) = \frac{Y(s)}{X(s)} = \frac{3e^{-3s}}{s+1} \quad (4)$$