

Q-1

```
for (i=0; i<n; i++)
    for (j=0; j<i; j++)
        stmt;
```

Soln	i	j	No. of times executed.
initial	0	0 (x)	0
	1	0 ✓ 1 (x)	1
	2	0 ✓ 1 ✓ 2 x	2
	3	0 } 1 } ✓ 2 } 3 x	3

This process continues upto n

$$1 + 2 + 3 + \dots + n$$

$$= \frac{n(n+1)}{2}$$

$$f(n) = \frac{n^2 + 1}{2} = O(n^2)$$

Q-2

$$3n^2 + 2$$

= complexity  $O(n^2)$

Q → 3

$$T[n] = T[n-1] + 1$$

$$T(n) = \begin{cases} 1 & \text{if } n \geq 0 \\ T(n-1) + 1 & n > 0 \end{cases}$$

$$T(n) = T(n-1) + 1$$

Substitute  $T(n-1)$ 

$$T(n) = [T(n-2) + 1] + 1$$

$$T(n) = T(n-2) + 2$$

if Substitute again

$$T(n) = [T(n-3) + 1] + 2$$

$$T(n) = T(n-3) + 3$$

⋮

Continues for  $k$  times:

$$T(n) = T(n-k) + k \quad (\text{Assume } n-k=0)$$

$$\therefore \text{ } \cancel{n-k}$$

$$T(n) = T(n-n) + n$$

$$= T(0) + n$$

$$T(n) = 1 + n \quad \text{is the time}$$

Since  $1+n$  belongs to the linear class  $O(n)$  that is why it is called  $O(n)$ .

④

$$f(n) = 10000$$

complexity  $O(1)$



constant time.

⑤

$$f(n) = n!$$

$$n! \Rightarrow n(n-1)(n-2) \dots$$

factorial (int n)

{ if (n == 0 || n == 1) }  $\Rightarrow O(1)$

return 1;

return n \* factorial (n-1); } Individual et  
will take  $O(1)$

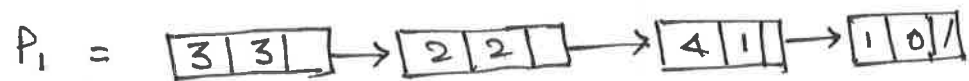
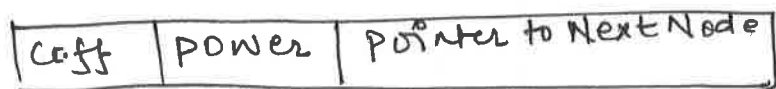
complexity  $O(\underline{n})$

Q→2  $P_1 = 3n^3 + 2n^2 + 4n + 1$

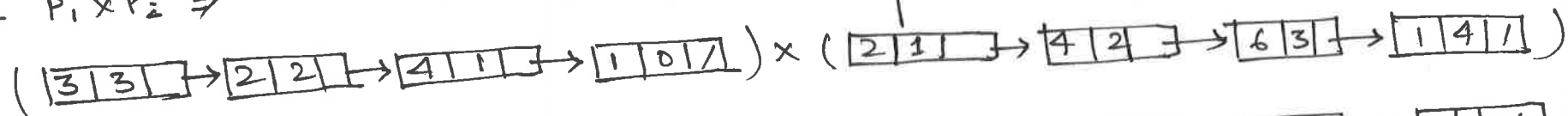
$P_2 = 2n + 4n^2 + 6n^3 + n^4$

Polynomial Multiplication using linked list

LinkedList Node Structure



Step 1  $P_1 \times P_2 \Rightarrow$



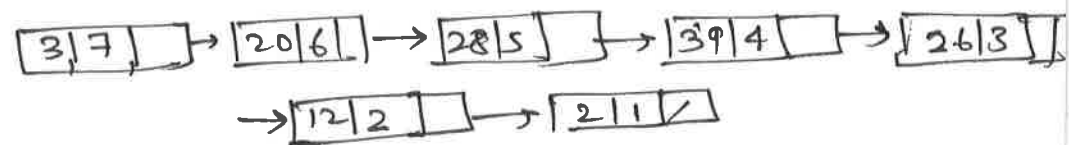
Step 2  $(\text{6|4} \rightarrow \text{4|3} \rightarrow \text{8|2} \rightarrow \text{2|1|}) + ((\text{3|3} \rightarrow \text{2|2} \rightarrow \text{4|1} \rightarrow \text{1|0|}) \times \text{4|2} \rightarrow \text{6|3} \rightarrow \text{1|4|})$

Step=3  $((\text{6|4} \rightarrow \text{4|3} \rightarrow \text{8|2} \rightarrow \text{2|1|} + \text{12|5} \rightarrow \text{8|4} \rightarrow \text{16|3} \rightarrow \text{4|2|})) + ((\text{3|3} \rightarrow \text{2|2} \rightarrow \text{4|1} \rightarrow \text{1|0|}) \times (\text{6|3} \rightarrow \text{1|4|}))$

Step=4  $((\text{12|5} \rightarrow \text{14|4} \rightarrow \text{20|3} \rightarrow \text{12|2} \rightarrow \text{2|1|} + (\text{18|6} \rightarrow \text{12|5} \rightarrow \text{24|4} \rightarrow \text{6|3|})) + (\text{3|3} \rightarrow \text{12|2} \rightarrow \text{4|1} \rightarrow \text{1|0|}) \times (\text{1|4|}))$

Step=5  $(\text{18|6} \rightarrow \text{24|5} \rightarrow \text{38|4} \rightarrow \text{26|3} \rightarrow \text{12|2} \rightarrow \text{2|1|} + (\text{3|7} \rightarrow \text{26|4} \rightarrow \text{4|5} \rightarrow \text{1|4|}))$

Final Result



$= 3n^7 + 20n^6 + 28n^5 + 39n^4 + 26n^3 + 12n^2 + 2n \text{ Ans}$

Question 3:

Initial Linked List

3->	19->	10->	1->	12->	20->	15->	9->	11->	18
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Step 1

3->	19->	10->	1->	12->	20->	15->	9->	11->	18
-----	------	------	-----	------	------	------	-----	------	----

Step 2

3->	10->	1->	12->	19->	15->	9->	11->	18->	20
-----	------	-----	------	------	------	-----	------	------	----

Step 3

3->	1->	10->	12->	15->	9->	11->	18->	19->	20
-----	-----	------	------	------	-----	------	------	------	----

Step 4

1->	3->	10->	12->	9->	11->	15->	18->	19->	20
-----	-----	------	------	-----	------	------	------	------	----

Step 5

1->	3->	9->	10->	11->	12->	15->	18->	19->	20
-----	-----	-----	------	------	------	------	------	------	----

Step 6

1->	3->	9->	10->	11->	12->	15->	18->	19->	20
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No swap made

Final Sorted Linked  
List

1->	3->	9->	10->	11->	12->	15->	18->	19->	20
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