

Physics (2)

Section (4)

Electric Flux

$$\Phi_E = EA_{\perp} = EA \cos \theta$$

$$\Phi_{E,i} = E_i \, \Delta A_i \, \cos \theta_i = \, \overrightarrow{\mathbf{E}}_i \cdot \Delta \overrightarrow{\mathbf{A}}_i$$

$$\Phi_E \approx \sum \vec{\mathbf{E}}_i \cdot \Delta \vec{\mathbf{A}}_i$$

$$\Phi_E \equiv \int \vec{\mathbf{E}} \cdot d\vec{\mathbf{A}}$$
surface

The electric field makes an angle θ_i with the vector $\Delta \vec{A}_i$, defined as being normal to the surface element.

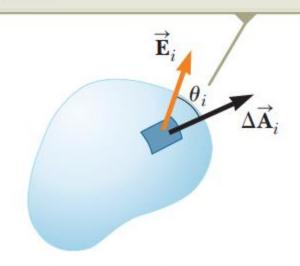


Figure 24.3 A small element of surface area ΔA_i in an electric field.

Electric Flux

MCQ:

1- A 40.0-cm-diameter circular loop is rotated in a uniform electric field until the position of maximum electric flux is found. The flux in this position is measured to be $5.20 \times 10^5 \text{ N} \cdot \text{m}^2/\text{C}$. What is the magnitude of the electric field?

- a) $4.14 \times 10^6 \text{ N/C}$
- b) $4.14 \times 10^3 \text{ N/C}$
- c) $9.45 \times 10^9 \text{ N/C}$
- d) 0 N/C

Answer: a

In this section, we describe a general relationship between the net electric flux through a closed surface (often called a *gaussian surface*) and the charge enclosed by the surface. This relationship, known as *Gauss's law*, is of fundamental importance in the study of electric fields.

the net flux through *any* closed surface surrounding a point charge q is given by q/ϵ_0 and is independent of the shape of that surface.

$$\Phi_E = \oint \vec{\mathbf{E}} \cdot d\vec{\mathbf{A}} = \frac{q_{\text{in}}}{\epsilon_0}$$
 (24.6)

Exercise 2:

Find the net electric flux through the spherical closed surface shown in Figure P24.8. The two charges on the right are inside the spherical surface.

Solution:

The gaussian surface encloses the +1.00-nC and -3.00-nC charges, but not the +2.00-nC charge. The electric flux is therefore

$$\Phi_E = \frac{q_{\text{in}}}{\epsilon_0} = \frac{\left(1.00 \times 10^{-9} \text{ C} - 3.00 \times 10^{-9} \text{ C}\right)}{8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2} = \boxed{-226 \text{ N} \cdot \text{m}^2/\text{C}}$$

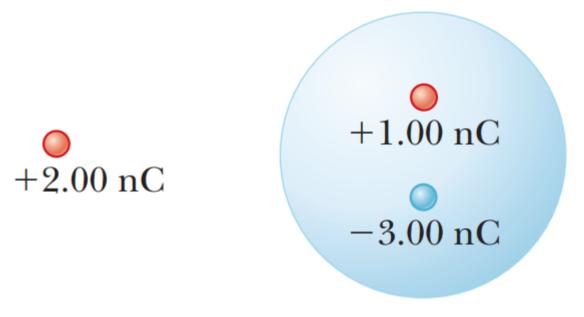


Figure P24.8

MCQ:

2- The following charges are located inside a submarine: $5.00 \,\mu\text{C}$, $-9.00 \,\mu\text{C}$, $27.0 \,\mu\text{C}$, and $-84.0 \,\mu\text{C}$.

Calculate the net electric flux through the hull of the submarine.

a)
$$-6.89 \times 10^6 \text{ N} \cdot \text{m}^2/\text{C}$$

b)
$$6.89 \times 10^6 \,\mathrm{N} \cdot \mathrm{m}^2/\mathrm{C}$$

c)
$$-6.89 \times 10^3 \text{ N} \cdot \text{m}^2/\text{C}$$

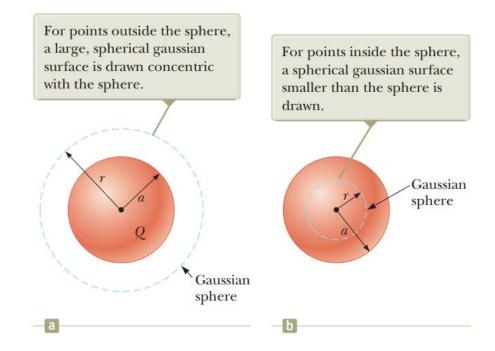
d)
$$6.89 \times 10^3 \text{ N} \cdot \text{m}^2/\text{C}$$

Answer: a

Exercise 2:

An insulating solid sphere of radius 0.5 m has a uniform volume charge density and carries a total positive charge of 5 nC.

- a) Calculate the magnitude of the electric field at a point 0.8 m from the centre of the sphere.
- b) Calculate the magnitude of the electric field at a point 0.3 m from the centre of the sphere.
- c) Calculate the magnitude of the electric field at a point on the surface of the sphere.



a) Calculate the magnitude of the electric field at a point 0.8 m from the centre of the sphere.

Solution:

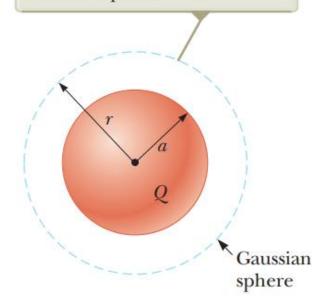
We use the formula for calculating the electric field for a point outside the sphere.

(1)
$$E = \frac{Q}{4\pi\epsilon_0 r^2} = k_e \frac{Q}{r^2}$$
 (for $r > a$)

For $Q = 5 \text{ nC} = 5 \times 10^{-9} \text{ C}$, and r = 0.8 m we get:

$$E = 8.99 \times 10^9 \times \frac{5 \times 10^{-9}}{0.8^2} = 70.23 \text{ N/C}$$

For points outside the sphere, a large, spherical gaussian surface is drawn concentric with the sphere.



b) Calculate the magnitude of the electric field at a point 0.3 m from the centre of the sphere.

Solution:

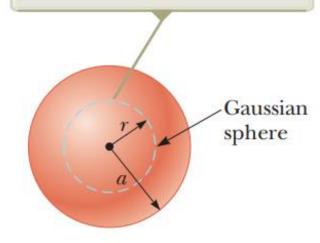
We use the formula for calculating the electric field for a point inside the sphere.

(2)
$$E = \frac{Q/\frac{4}{3}\pi a^3}{3(1/4\pi k_e)} r = k_e \frac{Q}{a^3} r \text{ (for } r < a)$$

For $Q = 5 \text{ nC} = 5 \times 10^{-9} \text{ C}$, r = 0.3 m, and a = 0.5 m we get:

$$E = 8.99 \times 10^9 \times \frac{5 \times 10^{-9}}{0.5^3} \times 0.3 = 107.88 \text{ N/C}$$

For points inside the sphere, a spherical gaussian surface smaller than the sphere is drawn.



c) Calculate the magnitude of the electric field at a point on the surface of the sphere.

Solution:

Equation (1) shows that the electric field approaches a value from the outside given by

$$E = \lim_{r \to a} \left(k_e \frac{Q}{r^2} \right) = k_e \frac{Q}{a^2}$$

From the inside, Equation (2) gives

$$E = \lim_{r \to a} \left(k_e \frac{Q}{a^3} r \right) = k_e \frac{Q}{a^3} a = k_e \frac{Q}{a^2}$$

Using either formula and substituting for $Q = 5 \text{ nC} = 5 \times 10^{-9} \text{ C}$, and a = 0.5 m we get:

$$E = 8.99 \times 10^9 \times \frac{5 \times 10^{-9}}{0.5^2} = 179.8 \text{ N/C}$$

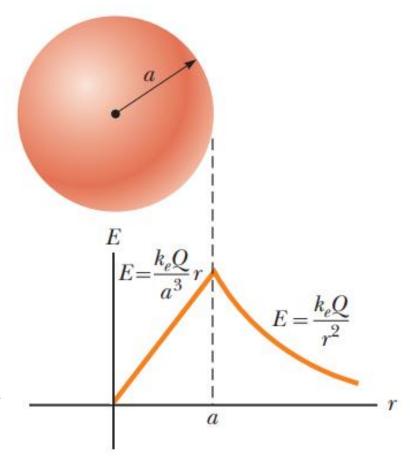


Figure 24.11

MCQ:

- 3- An insulating solid sphere of radius 0.7 m has a uniform volume charge density and carries a total positive charge of 9 μ C.
- (a) Calculate the magnitude of the electric field at a point 1.2 m from the centre of the sphere.
 - a) $51.88 \times 10^9 \text{ N/C}$
 - b) $56.19 \times 10^3 \text{ N/C}$
 - c) $12.74 \times 10^2 \text{ N/C}$
 - d) $97.17 \times 10^6 \text{ N/C}$

Answer: b

- (b) Calculate the magnitude of the electric field at a point 0.4 m from the centre of the sphere.
 - a) $91.61 \times 10^6 \text{ N/C}$
 - b) $54.79 \times 10^9 \text{ N/C}$
 - c) $94.36 \times 10^3 \text{ N/C}$
 - d) $92.86 \times 10^2 \text{ N/C}$

Answer: c