

Automata - Revision (I) - 2020 - Set Operations

1. Example(1) Let: $U = \{a, b, c, d, e, f, g, h, i, j\}$, $A = \{a, b, c\}$, $B = \{a, f, g\}$, $C = \{h, i, f\}$, Find:

- $A \cup B = \{a, b, c, f, g\}$
- $A \cap C = \{f\}$
- $A - B = \{b, c\}$
- $A' \cup B' = \{d, e, f, g, h, i, j\} \cup \{b, c, d, e, h, i, j\} = \{b, c, d, e, f, g, h, i, j\}$
- $(A \cup B)' = \{d, e, h, i, j\}$
- $|B| = 3$, $|U| = 10$
- $P(A) = \{ \Phi, \{a\}, \{b\}, \{c\}, \{a, b\}, \{a, c\}, \{b, c\}, \{a, b, c\} \}$,

$$|P(A)| = 8 = 2^3 = 2^{|A|}$$

2. Example(2) Find the Cardinality for:

- 1. $\Phi = \text{null} = 0$
- 2. $\{a, b\} = 2$
- 3. $\{1, 2, 3, 4, 5, 6\} = 6$
- 4. $\{\Phi\} = 1$
- 5. $\{\{\}\} = 1$

3. Let the set A is $\{1, 2, 3\}$ and B is $\{2, 3, 4\}$. Then the number of elements in $A \cup B$ is?
a) 4 b) 5
c) 6 d) 7

A

4. Let the set A is $\{1, 2, 3\}$ and B is $\{2, 3, 4\}$. Then number of elements in $A \cap B$ is?
a) 1 b) 2 c) 3 d) 4

B

5. The intersection of the sets $\{1, 2, 5\}$ and $\{1, 2, 6\}$ is the set _____
a) $\{1, 2\}$
b) $\{5, 6\}$
c) $\{2, 5\}$
d) $\{1, 6\}$

A

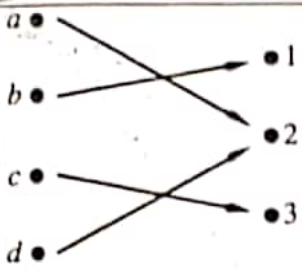
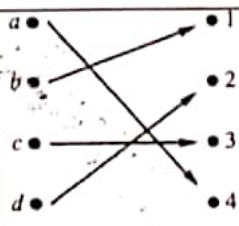
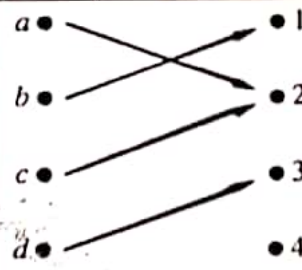
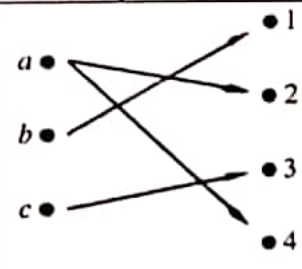
6. Two sets are called disjoint if there _____ is the empty set.
a) Union
b) Difference
c) Intersection
d) Complement

C

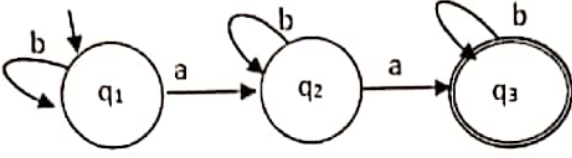
7. Which of the following two sets are disjoint?
a) $\{1, 3, 5\}$ and $\{1, 3, 6\}$
b) $\{1, 2, 3\}$ and $\{1, 2, 3\}$
c) $\{1, 3, 5\}$ and $\{2, 3, 4\}$
d) $\{1, 3, 5\}$ and $\{2, 4, 6\}$

D

8.	The difference of $\{1, 2, 3\}$ and $\{1, 2, 5\}$ is the set _____ a) $\{1\}$ b) $\{5\}$ c) $\{3\}$ d) $\{2\}$	C
9.	The complement of the set A is _____ a) $A - B$ b) $U - A$ c) $A - U$ d) $B - A$	B
10.	What is the Cardinality of the Power set of the set $\{0, 1, 2\}$? a) 8 b) 6 c) 7	A
11.	7. If A is $\{\{\Phi\}, \{\Phi, \{\Phi\}\}\}$, then the power set of A has how many element? a) 2 b) 4 c) 6 d) 8	B
12.	<p>Example (3):</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> <p>(a) One-to-one, not onto</p> </div> <div style="text-align: center;"> <p>(b) Onto, not one-to-one</p> </div> <div style="text-align: center;"> <p>(c) One-to-one, and onto</p> </div> <div style="text-align: center;"> <p>(d) Neither one-to-one nor onto</p> </div> <div style="text-align: center;"> <p>(e) Not a function</p> </div> </div>	
13.	<p>a. onto b. into c. one to one d. one one onto</p>	C

14.	 <p>a. onto b. into c. one to one d. one one onto</p>	A
15.	 <p>A. bijective B. injective C. surjective D. composite function</p>	A
16.	 <p>A. bijective B. injective C. surjective D. Not bijective</p>	D
17.	 <p>A. bijective B. injective C. surjective D. Not a function</p>	D

18.	<p>Surjective function is also called _____.</p> <p>A. onto B. into C. one to one D. one one onto</p>	A
19.	<p>One to one onto function is also called _____.</p> <p>A. bijective B. injective C. surjective D. composite function</p>	A
20.	<p>Suppose there are 50 people in a room. Then, at least how many people must have their birthday in the same month?</p> <p>a. 50/12 b. 12/50 c. 5 d. 4</p>	C
21.	<p>Let $A = \{0; 1; 2; 3\}$ and R a relation over A: $R = \{(0; 0); (0; 1); (0; 3); (1; 1); (1; 0); (2; 3); (3; 3)\}$</p> <p>a. R is reflexive, not symmetric, and not transitive b. R is not reflexive, not symmetric, and transitive c. R is not reflexive, symmetric, and not transitive d. R is not reflexive, not symmetric, and not transitive</p>	B
22.	<p>Let $f(x) = 2x + 3$ and $g(x) = 3x + 2$ be functions on N. What is $(g \circ f)(x)$?</p> <p>a. $(g \circ f)(x) = 6x + 11$. b. $(g \circ f)(x) = 6x + 7$. c. $(g \circ f)(x) = 5x + 5$. d. $(g \circ f)(x) = 6x + 5$.</p>	A
23.	<p>Let $L = \{a, b, c\}$, $w = abb$ and $u = bcaa$, Find wu</p> <p>a. abbbcaa b. bcaaabb c. abb+bcaa d. bcaa+abb</p>	A
24.	<p>Let $L = \{a, b, c\}$, $w = abb$ and $u = bcaa$, Find wu</p> <p>a. 7 b. 3 c. 4</p>	A
25.	<p>Let $L = \{a, b, c\}$, $w = abb$ and $u = bcaa$, Find $(wu)^2$</p> <p>a. abbbcaa b. bcaaabb c. aacbbba d. bcaa+abb</p>	C
26.	<p>If $A = \{a, ba\}$, which of the following strings is NOT in A^*:</p> <p>a. bb</p>	A

	b. λ c. aa d. baa	
27.	If $\Sigma = \{ab, c\}$, $u = abcc$ and $v = cab$, then, $ u^2 v $ equals a. 11 b. 8 c. 7 d. 5	A
28.	What is the language defined by the following DFA:  a. {babab} b. $\{bn a bn a bn, n \geq 0\}$ c. $\{bn a bm a, m, n \geq 0\}$ d. $\{bn a bm a bk, m, n, k \geq 0\}$	
Automata - Revision (I) - 2020 - Regular Expression		
29.	Which of the following does not represent the given language? Language: $\{0, 01\}$ a) $0+01$ b) $\{0\} \cup \{01\}$ c) $\{0\} \cup \{0\}1$ d) $\{0\} \cdot \{01\}$	D
30.	According to the given language, which among the following expressions does it correspond to? Language $L = \{x \in \{0, 1\}^* x \text{ is of length 4 or less}\}$ a) $(0+1+0+1+0+1+0+1)^4$ b) $(0+1)^4$ c) $(01)^4$ d) $(0+1+\epsilon)^4$	D
31.	Which among the following looks similar to the given expression? $((0+1) \cdot (0+1))^*$ a) $\{x \in \{0, 1\}^* x \text{ is all binary number with even length}\}$ b) $\{x \in \{0, 1\}^* x \text{ is all binary number with odd length}\}$ c) $\{x \in \{0, 1\}^* x \text{ is all binary number with odd length}\}$ d) $\{x \in \{0, 1\}^* x \text{ is all binary number with even length}\}$	A
32.	Concatenation Operation refers to which of the following set operations: a) Union b) Dot c) Kleene d) Two of the options are correct	B
33.	Concatenation of R with Φ outputs: a) R b) Φ	B

	c) $R \cdot \Phi$ d) None of the mentioned	
२६.	RR^* can be expressed in which of the forms: a) R^+ b) R^- c) $R^+ \cup R^-$ d) R	A
२७.	Which among the following are incorrect regular identities? a) $\epsilon R = R$ b) $\epsilon^* = \epsilon$ c) $\Phi^* = \epsilon$ d) $R\Phi = R$	D
२८.	$(0+\epsilon)(1+\epsilon)$ represents a) $\{0, 1, 01, \epsilon\}$ b) $\{0, 1, \epsilon\}$ c) $\{0, 1, 01, 11, 00, 10, \epsilon\}$ d) $\{0, 1\}$	A
२९.	Regular Expression R and the language it describes can be represented as: a) $R, R(L)$ b) $L(R), R(L)$ c) $R, L(R)$ d) All of the mentioned	C
३०.	Let for $\Sigma = \{0,1\}$ $R = ([1])^*$, the language of R would be a) $\{w \mid w \text{ is a string of odd length}\}$ b) $\{w \mid w \text{ is a string of length multiple of 3}\}$ c) $\{w \mid w \text{ is a string of length 3}\}$ d) All of the mentioned	B
३१.	If $\Sigma = \{0,1\}$, then Φ^* will result to: a) ϵ b) Φ c) $[$ d) None of the mentioned	A
३२.	The finite automata accept the following languages: a) Context Free Languages b) Context Sensitive Languages c) Regular Languages d) All the mentioned	C
३३.	Which of the following regular expressions represents the set of strings which do not contain a substring 'rt' if $\Sigma = \{r, t\}$ a) $(rt)^*$ b) $(tr)^*$	D

	c) (r^*t^*) d) (t^*r^*)	
12.	Regular expression for all strings starts with ab and ends with bba is. a) aba^*b^*bba b) $ab(ab)^*bba$ c) $ab(a+b)^*bba$ d) All of the mentioned	C
13.	There are _____ tuples in finite state machine. a) 4 b) 5 c) 6 d) unlimited	B

rest (2). Cont.

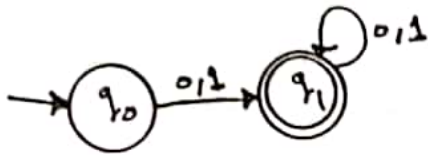
DFA

1

Construct the following DFA:

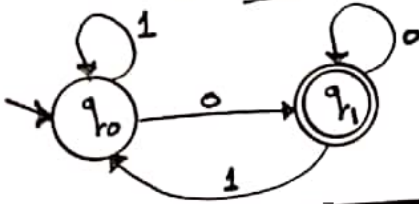
(1) The DFA that accepts the language $L = \{w \in \{0,1\}^+\}$.

Ans.



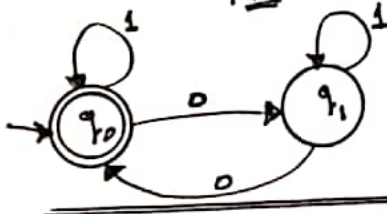
(2) The DFA that accepts the language $L = \{w \in \{0,1\}^* : w \text{ ends with } 0\}$.

Ans.



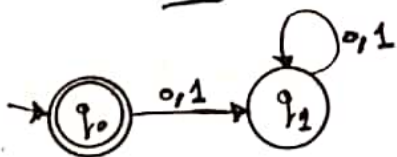
(3) The DFA that accepts the language $L = \{w \in \{0,1\}^* : w \text{ with even number of 0's}\}$.

Ans.



(4) The DFA that accepts the language $L = \{ \epsilon \}$.

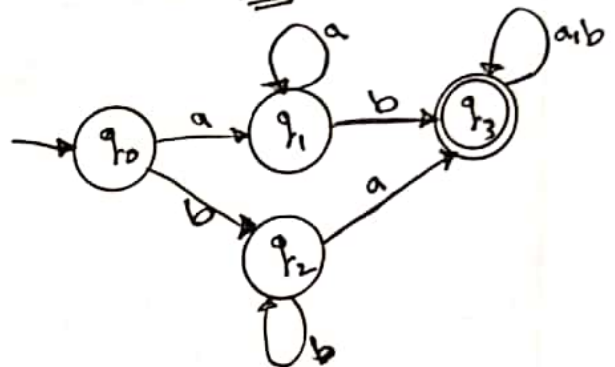
Ans.



(VI) Design a DFA and state its Formal description that accept the following languages :-

(1) The language that contain all strings in the alphabet $\{a,b\}^*$ which contain the substring "ab" or "ba".

Ans.

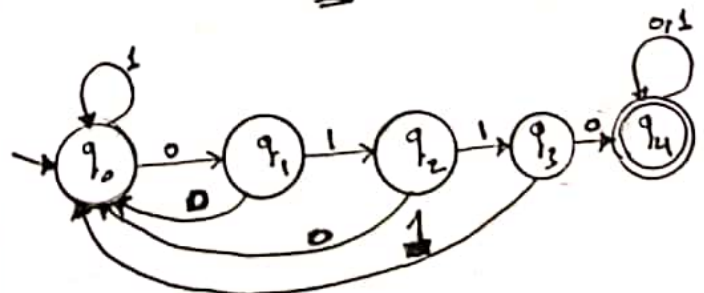


* Formal description :-

q	a	b
q_0	q_1	q_2
q_1	q_1	q_3
q_2	q_3	q_2
q_3	q_3	q_3

(2) The language that contain all the strings in the alphabet $\{0,1\}^*$ which contains "0110" as substring.

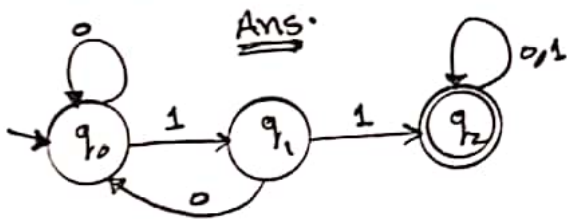
Ans.



formal description:-

S	0	1
q ₀	q ₁	q ₀
q ₁	q ₀	q ₂
q ₂	q ₀	q ₃
q ₃	q ₄	q ₀
q ₄	q ₄	q ₄

(3) The Language that contain all the strings in the alphabet {0,1}* which contain at least two consecutive 1's.

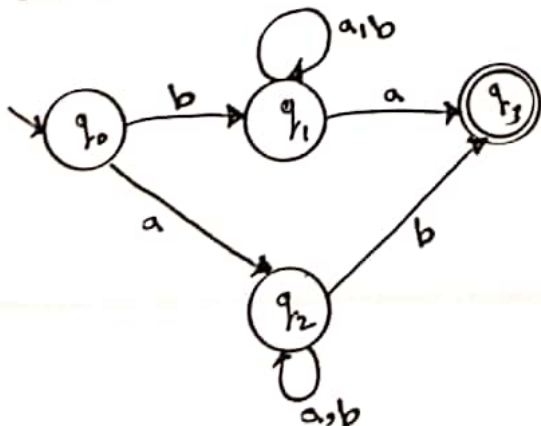


* The formal description:-

S	0	1
q ₀	q ₀	q ₁
q ₁	q ₀	q ₂
q ₂	q ₂	q ₂

NFA & Convert NFA to DFA

* Ex: Convert From NFA to DFA:-



Ans:-

~: الحالة الأولى *

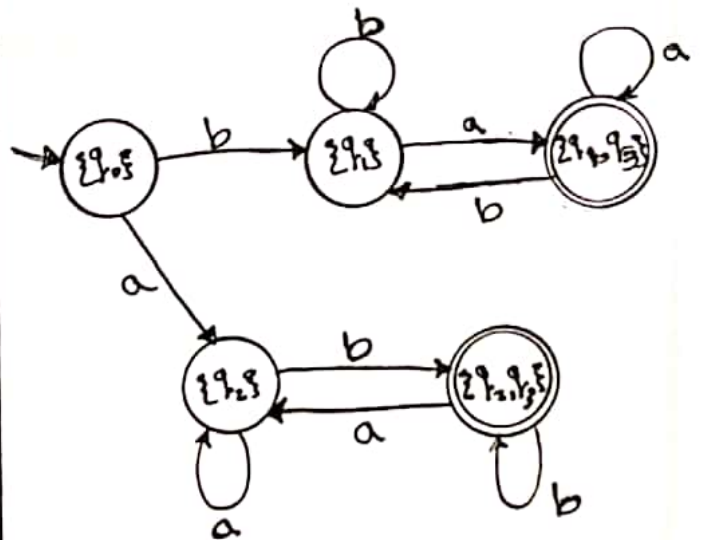
S	a	b
q ₀	{q ₂ }	{q ₁ }
q ₁	{q ₁ , q ₃ }	{q ₁ }
q ₂	{q ₂ }	{q ₂ , q ₃ }
q ₃	Φ	Φ

~: الحالة الثانية *

start →

S	a	b
{q ₀ }	{q ₂ }	{q ₁ }
{q ₂ }	{q ₂ }	{q ₂ , q ₃ }
{q ₁ }	{q ₁ , q ₃ }	{q ₁ }
{q ₂ , q ₃ }	{q ₂ }	{q ₂ , q ₃ }
{q ₁ , q ₃ }	{q ₁ , q ₃ }	{q ₁ }

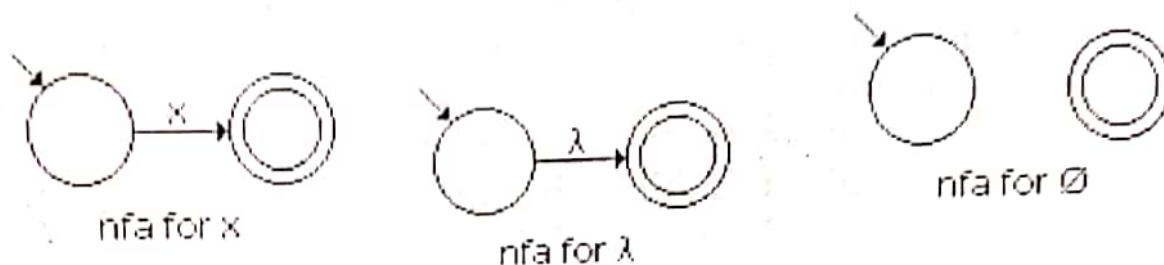
~: الحالة الثالثة *



~: Final state q₂ *

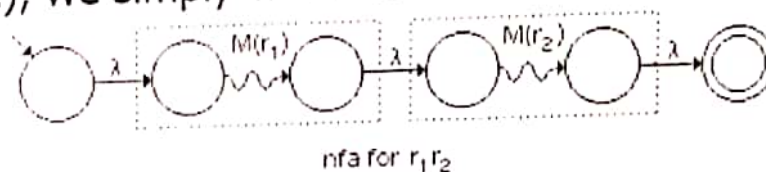
Final state q₃ state or

- From Primitive Regular Expressions to NFAs

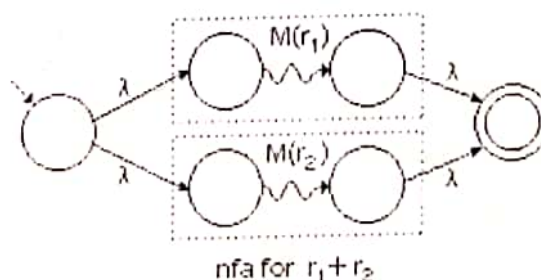


- From Regular Expressions to NFAs

- For **concatenation** (strings in $L(r_1)$ followed by strings in $L(r_2)$), we simply chain the NFAs together, as shown.

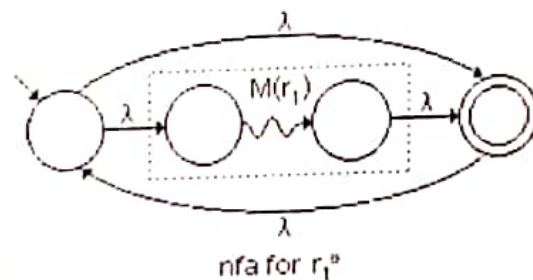


- The $+$ denotes "or" in a regular expression, so it makes sense that we would use an NFA with a choice of paths. (This is one of the reasons that it's easier to build an NFA than a DFA.)



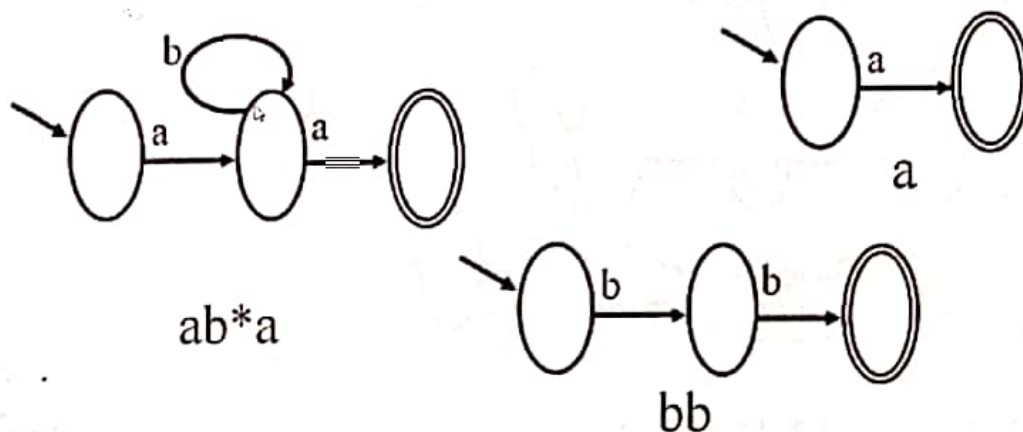
- The **star** denotes zero or more applications of the regular expression, so we need to set up a loop in the NFA.

We can do this with a backward-pointing and a forward-pointing λ arc to bypass the NFA entirely.



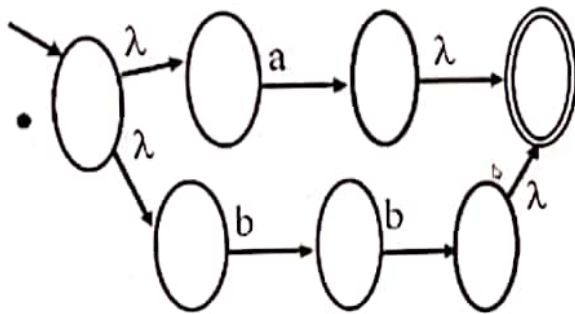
• Example

- Construct an NFA equivalent to the regular expression (show all steps clearly): " $ab^*a + (a + bb)^*$ "

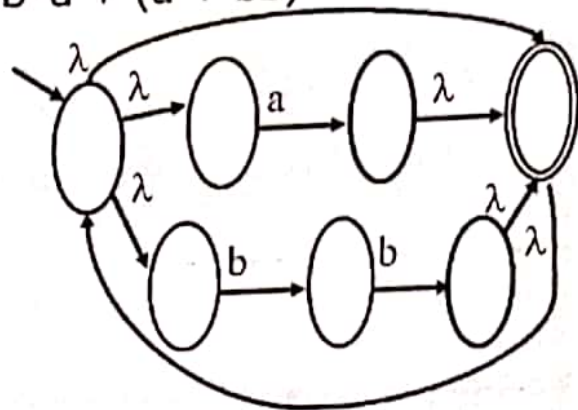


• **Example**

- Construct an NFA equivalent to the regular expression (show all steps clearly): " $ab^*a + (a + bb)^*$ "



$a + bb$



$(a + bb)^*$

• **Example**

- Construct an NFA equivalent to the regular expression (show all steps clearly): " $ab^*a + (a + bb)^*$ "

