

$$\phi = \alpha_1 + \alpha_2 x, \dim L = 1, n = 2$$

- симплекс элементы.

Комплекс элементы - количество узлов $(n) > 2$.

$$\varphi = \alpha_1 + \alpha_2 x + \alpha_3 x^2 = N\Phi$$

$$\varphi = \alpha_1 + \alpha_2 x + \dots + \alpha_n x^{n-1}$$

$$\begin{cases} \Phi_i = \alpha_1 + \alpha_2 x_i + \alpha_3 x_i^2 \\ \Phi_j = \alpha_1 + \alpha_2 x_j + \alpha_3 x_j^2 \\ \Phi_k = \alpha_1 + \alpha_2 x_k + \alpha_3 x_k^2 \end{cases} \rightarrow \alpha_1, \alpha_2, \alpha_3$$

$$\alpha_1 = \Phi_i, \alpha_2 = \frac{-3\Phi_i + 4\Phi_j - \Phi_k}{L}, \alpha_3 = \frac{2(\Phi_i - 2\Phi_j + \Phi_k)}{L^2}$$

$$\begin{aligned} \varphi &= \alpha_1 + \alpha_2 x + \alpha_3 x^2 = \\ &= \underbrace{\Phi_i \left(1 - \frac{3x}{L} + \frac{2x^2}{L^2}\right)}_{N_i} + \underbrace{\Phi_j \left(\frac{4x}{L} - \frac{4x^2}{L^2}\right)}_{N_j} + \underbrace{\Phi_k \left(-\frac{x}{L} + \frac{2x^2}{L^2}\right)}_{N_k} = \\ &= N_i \Phi_i + N_j \Phi_j + N_k \Phi_k = [N]\{\Phi\} \end{aligned}$$

$$N_i = 1 - \frac{3x}{L} + \frac{2x^2}{L^2}, \quad N_j = \frac{4x}{L} - \frac{4x^2}{L^2}, \quad N_k = -\frac{x}{L} + \frac{2x^2}{L^2}$$

Формулы для нахождения функций форм без использования системы уравнений:

$$N_i = \frac{f_j f_k}{f_j f_k|_{x=x_i}}, \quad N_j = \frac{f_i f_k}{f_i f_k|_{x=x_j}}, \quad N_k = \frac{f_i f_j}{f_i f_j|_{x=x_k}}$$