Homework 4

- 1. For the given matrices: A(2 x 3), B(2 x 2), C(3 x 3), D(3 x 4) of (n rows x m columns) find which expression are legit:
 - (a) AB
- (b) BA
- (c) AC

- (d) ACD (e) $D^{T}A^{T}$ (f) C D^{T} (g) $(A^{T}B)^{T}$ D
- 2. Find the matrix that transforms any vector **x** from 3-dimensional vector space into vector $\mathbf{y} = 2\mathbf{x}$.
- 3. Find the matrix that transforms any vector $\mathbf{x} = [x_1, x_2, x_3]$ to vector $y = [x_1, -2x_2, -x_3]$
- 4. Find the matrix that transforms any vector $\mathbf{x} = [x_1, x_2, x_3]$ to vector $y = [x_2, -x_1, x_3]$
- 5. Find the rank of the given matrices. Are these matrices invertible? Why?

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 5 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 3 & -2 \\ 3 & 0 & 6 \end{bmatrix} \quad C = \begin{bmatrix} 2 & 1 & 3 \\ 6 & 3 & 9 \\ 4 & 2 & 6 \end{bmatrix}$$

6. Optional.

The triangle corners are represented by the following vectors:

$$[(1, 1, 1), (2, 3, -1), (-1, 0, 4)]$$

How the area of the triangle changes if we linearly transform its vectors by

the matrix
$$A = \begin{bmatrix} 1 & 4 & 0 \\ 2 & 3 & 0 \\ 0 & 1 & 2 \end{bmatrix}$$
?