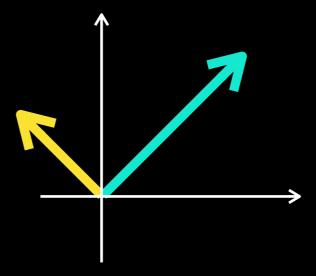
Linear regression: Predicting values of diamonds

Linear Algebra Essentials

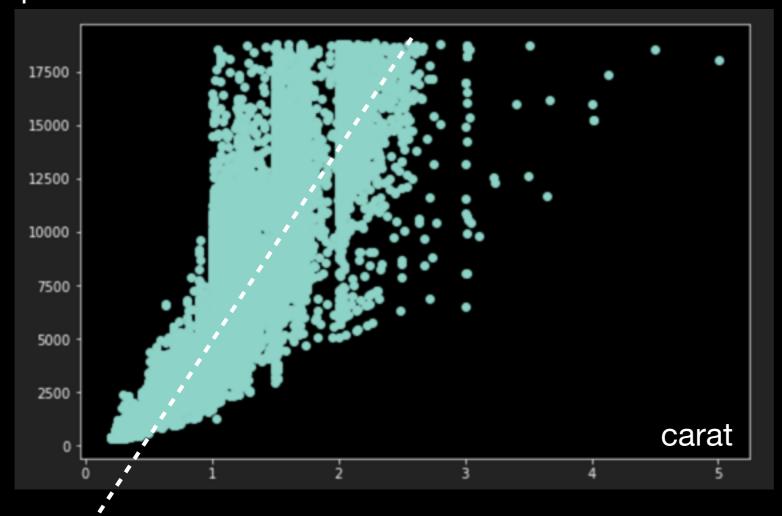


https://www.kaggle.com/shivam2503/diamonds

```
data = pd.read_csv("diamonds.csv")
 data.head()
                        cut color clarity
Unnamed: 0
                                            depth
                                                   table
             carat
             0.23
                   Ideal
                             Ε
                                            61.5
                                                   55.0
                                                          326
                                                                 3.95 3.98 2.43
                                    SI2
             0.21
                   Premium E
                                            59.8
                                                          326
                                                                 3.89
                                                                      3.84
                                    SI1
                                                   61.0
                                                                           2.31
             0.23
                             Ε
                                            56.9
                                                                 4.05
                                                                      4.07
                   Good
                                    VS1
                                                   65.0
                                                          327
                                                                           2.31
                                                                 4.20
                                                                      4.23 2.63
             0.29
                   Premium
                                            62.4
                                    VS2
                                                   58.0
                                                          334
             0.31
                                    SI2
                                            63.3
                                                                 4.34 4.35 2.75
                                                   58.0
                                                          335
                    Good
```

```
cut: { Fair, Good, Very Good, Premium, Ideal } —> { 0, 1, 2, 3, 4, } color: { D, E, ..., J } —> { 0, 1, ... }
```

price



$$per-carat = \frac{price}{carat^2}$$

	carat	cut	color	clarity	depth	table	price	X	у	Z	per-carat	_cut	_color	_clarity
0	0.23	Ideal	Е	SI2	61.5	55.0	326	3.95	3.98	2.43	6162.570888	4	1	1
1	0.21	Premium	Е	SI1	59.8	61.0	326	3.89	3.84	2.31	7392.290249	3	1	2
2	0.23	Good	Е	VS1	56.9	65.0	327	4.05	4.07	2.31	6181.47 44 80	1	1	4
3	0.29	Premium	l .	VS2	62.4	58.0	334	4.20	4.23	2.63	3971.462545	3	5	3
4	0.31	Good	J	SI2	63.3	58.0	335	4.34	4.35	2.75	3485. 9 52133	1	6	1

```
1 y = data['per-carat'].values
Z X = data[['_cut', '_color', '_clarity', 'carat', 'x', 'y', 'z']].values.T
   X = np.vstack([np.ones(len(y)), X])
4 X[:,:5]
array([[1. , 1. , 1. , 1. , 1. ],
      [4., 3., 1., 3., 1.],
      [1. , 1. , 1. , 5. , 6. ],
      [1. , 2. , 4. , 3. , 1. ],
      [0.23, 0.21, 0.23, 0.29, 0.31],
      [3.95, 3.89, 4.05, 4.2, 4.34],
      [3.98, 3.84, 4.07, 4.23, 4.35],
      [2.43, 2.31, 2.31, 2.63, 2.75]])
1 a = np.linalg.inv(X.dot(X.T)).dot(X).dot(y)
2 a
array([7284.4611339 , 170.43665284, -426.58684553, 744.52169235,
      1050.68424425, -579.38546073, -49.47883071, -159.67421698])
   data['predict'] = X.T.dot(a) * X[4, :]**2
   (np.abs(data['predict'] - data['price']) / (data['predict'] + data['price'])).mean()
0.059826076519396296
```

```
data[['carat', 'price', 'predict']].head()
                                                    predict
                                      carat price
                                   0 0.23
                                           326
                                                 299.006316
                                   1 0.21
                                           326
                                                 276.340114
                                   2 0.23
                                           327
                                                  387.826706
                                   3 0.29
                                           334
                                                 432.143039
                                     0.31
                                           335
                                                 268.766773
                                       data[['carat', 'price', 'predict']].tail()
                                         carat price
                                                         predict
                                   53935 0.72
                                               2757 3129.279901
                                   53936 0.72
                                               2757
                                                     2873.389260
                                   53937 0.70
                                               2757 2803.317007
                                   53938 0.86
                                               2757 2421,687999
                                   53939 0.75
                                               2757 2952.714656
10000
                           20000
                                                       30000
```

price