

Parameter Table

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1 Purpose

This script picks up after model.Rnw to process bootstrap results and make a parameter table. It assumes the current working directory is the script directory containing this file.

1.1 Package

Listing 1:

```
> library(metrumrg)
```

2 inputs

'wikitab' gives us a quick synthesis of 'rlog' and the 'lookup' of wiki notation in 1005.ctl. We do some science on the result first, and then some aesthetics for printing in a \LaTeX table. Table 1.

Listing 2:

```
> tab <- wikitab(1005, '../nonmem')
> tab$estimate <- signif(as.numeric(tab$estimate), 3)
> tab$tool <- NULL
> tab$run <- NULL
> tab$se <- NULL
> tab
```

	parameter	description		
1	THETA1	apparent oral clearance		
2	THETA2	central volume of distribution		
3	THETA3	absorption rate constant		
4	THETA4	intercompartmental clearance		
5	THETA5	peripheral volume of distribution		
6	THETA6	male effect on clearance		
7	THETA7	weight effect on clearance		
8	OMEGA1.1	interindividual variability of clearance		
9	OMEGA2.1	interindividual clearance-volume covariance		
10	OMEGA2.2	interindividual variability of central volume		
11	OMEGA3.1	interindividual clearance-Ka covariance		
12	OMEGA3.2	interindividual volume-Ka covariance		
13	OMEGA3.3	interindividual variability of Ka		
14	SIGMA1.1	proportional error		
15	SIGMA2.2	additive error		
			model estimate	
1	CL/F (L/h) ~ theta_1 * theta_6 ^MALE * (WT/70)^theta_7	* e^eta_1	16	
2	V_c /F (L) ~ theta_2 * (WT/70)^1	* e^eta_2	14	
3	K_a (h^-1) ~ theta_3	* e^eta_3	6	
4		Q/F (L/h) ~ theta_4	15	
5		V_p /F (L) ~ theta_5	12	
6		MALE_CL/F ~ theta_6	11	

```

7          WT_CL/F ~ theta_7      13
8          IIV_CL/F ~ Omega_1.1  10
9          cov_CL,V ~ Omega_2.1   8
10         IIV_V_c /F ~ Omega_2.2  7
11         cov_CL,Ka ~ Omega_3.1   2
12         cov_V,Ka ~ Omega_3.2   3
13         IIV_K_a ~ Omega_3.3    4
14         err_prop ~ Sigma_1.1   5
15         err_add ~ Sigma_2.2    9

prse
1      15
2      14
3      13
4       3
5       5
6       2
7       8
8       6
9       7
10      9
11      4
12     12
13     11
14      1
15     10

```

Now we can extract some information from the model statements.

Listing 3:

```

> tab$units <- justUnits(tab$model)
> tab$model <- noUnits(tab$model)
> tab$name <- with(tab, wiki2label(model))
> tab[c('model','units','name')]

```

```

                                model units
1  CL/F ~ theta_1 * theta_6 ^MALE * (WT/70)^theta_7 * e^eta_1  L/h
2                                V_c /F ~ theta_2 * (WT/70)^1 * e^eta_2    L
3                                K_a ~ theta_3 * e^eta_3 h^-1
4                                Q/F ~ theta_4    L/h
5                                V_p /F ~ theta_5    L
6                                MALE_CL/F ~ theta_6
7                                WT_CL/F ~ theta_7
8                                IIV_CL/F ~ Omega_1.1
9                                cov_CL,V ~ Omega_2.1
10                               IIV_V_c /F ~ Omega_2.2
11                               cov_CL,Ka ~ Omega_3.1
12                               cov_V,Ka ~ Omega_3.2
13                               IIV_K_a ~ Omega_3.3
14                               err_prop ~ Sigma_1.1
15                               err_add ~ Sigma_2.2

```

```

      name
1      CL/F
2      V_c/F
3      K_a
4      Q/F
5      V_p/F
6 MALE_CL/F
7      WT_CL/F
8      IIV_CL/F
9      cov_CL,V
10 IIV_V_c/F
11 cov_CL,Ka
12 cov_V,Ka
13      IIV_K_a
14 err_prop
15      err_add

```

3 variance

The estimates for the matrix diagonals are variances, and their square roots have special meaning. In model 1005, interindividual variability was modelled exponentially, in which case square root of variance gives an approximate CV; alternatively, and exact CV can be calculated. For proportional error terms like ERR1, square root gives an exact CV. For additive error terms like ERR2, square root gives standard deviation.

We can use functions of 'parameter' to sort out the various error components, as they are used in this model.

3.1 exponential

Listing 4:

```

> expo <- is.iiv(tab$parameter) & is.diagonal(tab$parameter)
> tab$parameter[expo]

```

```

[1] "OMEGA1.1" "OMEGA2.2" "OMEGA3.3"

```

Listing 5:

```

> tab$cv[expo] <- cvLognormal(tab$estimate[expo])
> tab[,c('parameter','name','estimate','cv')]

```

	parameter	name	estimate	cv
1	THETA1	CL/F	16	NA
2	THETA2	V_c/F	14	NA
3	THETA3	K_a	6	NA

```

4      THETA4      Q/F      15      NA
5      THETA5      V_p/F    12      NA
6      THETA6 MALE_CL/F    11      NA
7      THETA7      WT_CL/F    13      NA
8      OMEGA1.1    IIV_CL/F    10 148.409790
9      OMEGA2.1    cov_CL,V    8      NA
10     OMEGA2.2    IIV_V_c/F    7  33.100350
11     OMEGA3.1    cov_CL,Ka    2      NA
12     OMEGA3.2    cov_V,Ka    3      NA
13     OMEGA3.3    IIV_K_a    4  7.321076
14     SIGMA1.1    err_prop    5      NA
15     SIGMA2.2    err_add     9      NA

```

3.2 proportional

Listing 6:

```

> writeLines(read.nmctl('../nonmem/ctl/1005.ctl')$err)

Y=F*(1+ERR(1)) + ERR(2)
IPRE=F
; <doc>

```

Listing 7:

```

> prop <- is.random(tab$parameter) & tab$name %contains% 'prop'
> tab$parameter[prop]

[1] "SIGMA1.1"

```

Listing 8:

```

> tab$cv[prop] <- sqrt(tab$estimate[prop])
> tab[,c('parameter','name','estimate','cv')]

  parameter      name estimate      cv
1   THETA1      CL/F      16      NA
2   THETA2      V_c/F      14      NA
3   THETA3      K_a       6      NA
4   THETA4      Q/F      15      NA
5   THETA5      V_p/F      12      NA
6   THETA6 MALE_CL/F      11      NA
7   THETA7      WT_CL/F      13      NA
8  OMEGA1.1    IIV_CL/F     10 148.409790
9  OMEGA2.1    cov_CL,V      8      NA
10 OMEGA2.2    IIV_V_c/F      7  33.100350
11 OMEGA3.1    cov_CL,Ka      2      NA
12 OMEGA3.2    cov_V,Ka      3      NA
13 OMEGA3.3    IIV_K_a      4  7.321076
14 SIGMA1.1    err_prop      5  2.236068
15 SIGMA2.2    err_add       9      NA

```

3.3 additive

Listing 9:

```
> add <- is.residual(tab$parameter) & tab$name %contains% 'add'
> tab$parameter[add]
```

```
[1] "SIGMA2.2"
```

Listing 10:

```
> tab$sd[add] <- sqrt(tab$estimate[add])
> tab[,c('parameter', 'name', 'estimate', 'cv', 'sd')]
```

	parameter	name	estimate	cv	sd
1	THETA1	CL/F	16	NA	NA
2	THETA2	V_c/F	14	NA	NA
3	THETA3	K_a	6	NA	NA
4	THETA4	Q/F	15	NA	NA
5	THETA5	V_p/F	12	NA	NA
6	THETA6	MALE_CL/F	11	NA	NA
7	THETA7	WT_CL/F	13	NA	NA
8	OMEGA1.1	IIV_CL/F	10	148.409790	NA
9	OMEGA2.1	cov_CL,V	8	NA	NA
10	OMEGA2.2	IIV_V_c/F	7	33.100350	NA
11	OMEGA3.1	cov_CL,Ka	2	NA	NA
12	OMEGA3.2	cov_V,Ka	3	NA	NA
13	OMEGA3.3	IIV_K_a	4	7.321076	NA
14	SIGMA1.1	err_prop	5	2.236068	NA
15	SIGMA2.2	err_add	9	NA	3

4 covariance

The estimates of matrix off-diagonals are covariances, and are more useful if transformed to correlations. We could extract the matrices manually, or use package shortcuts.

Listing 11:

```
> cor <- omegacor(run=1005,project='../nonmem')
> cor
```

	[,1]	[,2]	[,3]
[1,]	1.0000000	0.8492811	-0.1163229
[2,]	0.8492811	1.0000000	-0.5607054
[3,]	-0.1163229	-0.5607054	1.0000000

Listing 12:

```
> half(cor)
```

```

      1.1      2.1      2.2      3.1      3.2      3.3
1.0000000  0.8492811  1.0000000 -0.1163229 -0.5607054  1.0000000

```

Listing 13:

```
> offdiag(half(cor))
```

```

      2.1      3.1      3.2
0.8492811 -0.1163229 -0.5607054

```

Listing 14:

```
> off <- is.iiv(tab$parameter) & is.offdiagonal(tab$parameter)
> tab$parameter[off]
```

```
[1] "OMEGA2.1" "OMEGA3.1" "OMEGA3.2"
```

Listing 15:

```
> tab$cor[off] <- offdiag(half(cor))
> tab[,c('parameter','name','estimate','cv','sd','cor')]
```

	parameter	name	estimate	cv	sd	cor
1	THETA1	CL/F	16	NA	NA	NA
2	THETA2	V _c /F	14	NA	NA	NA
3	THETA3	K _a	6	NA	NA	NA
4	THETA4	Q/F	15	NA	NA	NA
5	THETA5	V _p /F	12	NA	NA	NA
6	THETA6	MALE_CL/F	11	NA	NA	NA
7	THETA7	WT_CL/F	13	NA	NA	NA
8	OMEGA1.1	IIV_CL/F	10	148.409790	NA	NA
9	OMEGA2.1	cov _{CL,V}	8	NA	NA	0.8492811
10	OMEGA2.2	IIV_V _c /F	7	33.100350	NA	NA
11	OMEGA3.1	cov _{CL,Ka}	2	NA	NA	-0.1163229
12	OMEGA3.2	cov _{V,Ka}	3	NA	NA	-0.5607054
13	OMEGA3.3	IIV_K _a	4	7.321076	NA	NA
14	SIGMA1.1	err _{prop}	5	2.236068	NA	NA
15	SIGMA2.2	err _{add}	9	NA	3	NA

5 confidence interval

We wish to include 95 percentiles in our table as confidence intervals.

Listing 16:

```
> boot <- read.csv('../nonmem/1005bootlog.csv',as.is=TRUE)
> head(boot)
```

```

X tool run parameter      moment      value
1 1  nm7    1      ofv minimum 2459.17577365853
2 2  nm7    1      THETA1 estimate      9.90635
3 3  nm7    1      THETA1      prse      <NA>
4 4  nm7    1      THETA1      se      <NA>
5 5  nm7    1      THETA2 estimate     21.8851
6 6  nm7    1      THETA2      prse      <NA>

```

Listing 17:

```

> boot <- boot[boot$moment=='estimate',]
> boot <- data.frame(cast(boot,... ~ moment))
> head(boot)

```

```

X tool run parameter estimate
1 2  nm7    1      THETA1  9.90635
2 5  nm7    1      THETA2  21.8851
3 8  nm7    1      THETA3  0.0708169
4 11 nm7    1      THETA4  3.36905
5 14 nm7    1      THETA5  94.6453
6 17 nm7    1      THETA6  0.972457

```

Listing 18:

```

> boot <- boot[,c('run','parameter','estimate')]
> sapply(boot,class)

```

```

      run      parameter      estimate
"integer" "character"    "factor"

```

Listing 19:

```

> boot$estimate <- as.numeric(as.character(boot$estimate))
> unique(boot$parameter)

```

```

[1] "THETA1" "THETA2" "THETA3" "THETA4" "THETA5" "THETA6"
[7] "THETA7" "OMEGA1.1" "OMEGA2.1" "OMEGA2.2" "OMEGA3.1" "OMEGA3.2"
[13] "OMEGA3.3" "SIGMA1.1" "SIGMA2.1" "SIGMA2.2"

```

Listing 20:

```

> quan <- function(x,probs)as.character(signif(quantile(x,probs=probs,na.rm=TRUE)
,3))
> boot$lo <- with(boot, reapply(estimate,parameter,quan,probs=.05))
> boot$hi <- with(boot, reapply(estimate,parameter,quan,probs=.95))
> head(boot)

```

```

run parameter estimate      lo      hi
1 1      THETA1  9.9063500  7.31  11.1
2 1      THETA2 21.8851000  19.2  27.9
3 1      THETA3  0.0708169  0.0625 0.0838
4 1      THETA4  3.3690500  2.78  4.91
5 1      THETA5 94.6453000  85.6  559
6 1      THETA6  0.9724570  0.847  1.25

```


Listing 21:

```
> boot <- unique(boot[,c('parameter','lo','hi')])
> boot
```

	parameter	lo	hi
1	THETA1	7.31	11.1
2	THETA2	19.2	27.9
3	THETA3	0.0625	0.0838
4	THETA4	2.78	4.91
5	THETA5	85.6	559
6	THETA6	0.847	1.25
7	THETA7	0.61	1.91
8	OMEGA1.1	0.128	0.321
9	OMEGA2.1	0.0606	0.183
10	OMEGA2.2	0.047	0.158
11	OMEGA3.1	-0.0448	0.0261
12	OMEGA3.2	-0.0577	-0.0049
13	OMEGA3.3	0.0236	0.0811
14	SIGMA1.1	0.0399	0.0587
15	SIGMA2.1	0	0
16	SIGMA2.2	0.0836	0.329

Listing 22:

```
> boot$ci <- with(boot, parens(glue(lo,',',hi)))
> boot
```

	parameter	lo	hi	ci
1	THETA1	7.31	11.1	(7.31,11.1)
2	THETA2	19.2	27.9	(19.2,27.9)
3	THETA3	0.0625	0.0838	(0.0625,0.0838)
4	THETA4	2.78	4.91	(2.78,4.91)
5	THETA5	85.6	559	(85.6,559)
6	THETA6	0.847	1.25	(0.847,1.25)
7	THETA7	0.61	1.91	(0.61,1.91)
8	OMEGA1.1	0.128	0.321	(0.128,0.321)
9	OMEGA2.1	0.0606	0.183	(0.0606,0.183)
10	OMEGA2.2	0.047	0.158	(0.047,0.158)
11	OMEGA3.1	-0.0448	0.0261	(-0.0448,0.0261)
12	OMEGA3.2	-0.0577	-0.0049	(-0.0577,-0.0049)
13	OMEGA3.3	0.0236	0.0811	(0.0236,0.0811)
14	SIGMA1.1	0.0399	0.0587	(0.0399,0.0587)
15	SIGMA2.1	0	0	(0,0)
16	SIGMA2.2	0.0836	0.329	(0.0836,0.329)

Listing 23:

```
> tab <- stableMerge(tab,boot[,c('parameter','ci')])
> tab
```

parameter	description	
1 THETA1	apparent oral clearance	
2 THETA2	central volume of distribution	
3 THETA3	absorption rate constant	
4 THETA4	intercompartmental clearance	
5 THETA5	peripheral volume of distribution	
6 THETA6	male effect on clearance	
7 THETA7	weight effect on clearance	
8 OMEGA1.1	interindividual variability of clearance	
9 OMEGA2.1	interindividual clearance-volume covariance	
10 OMEGA2.2	interindividual variability of central volume	
11 OMEGA3.1	interindividual clearance-Ka covariance	
12 OMEGA3.2	interindividual volume-Ka covariance	
13 OMEGA3.3	interindividual variability of Ka	
14 SIGMA1.1	proportional error	
15 SIGMA2.2	additive error	

	model	estimate	prse
1 CL/F ~ theta_1 * theta_6 ^MALE * (WT/70)^theta_7 * e^eta_1		16	15
2 V_c /F ~ theta_2 * (WT/70)^1 * e^eta_2		14	14
3 K_a ~ theta_3 * e^eta_3		6	13
4 Q/F ~ theta_4		15	3
5 V_p /F ~ theta_5		12	5
6 MALE_CL/F ~ theta_6		11	2
7 WT_CL/F ~ theta_7		13	8
8 IIV_CL/F ~ Omega_1.1		10	6
9 cov_CL,V ~ Omega_2.1		8	7
10 IIV_V_c /F ~ Omega_2.2		7	9
11 cov_CL,Ka ~ Omega_3.1		2	4
12 cov_V,Ka ~ Omega_3.2		3	12
13 IIV_K_a ~ Omega_3.3		4	11
14 err_prop ~ Sigma_1.1		5	1
15 err_add ~ Sigma_2.2		9	10

units	name	cv	sd	cor	ci
1 L/h	CL/F	NA	NA	NA	(7.31,11.1)
2 L	V_c/F	NA	NA	NA	(19.2,27.9)
3 h^-1	K_a	NA	NA	NA	(0.0625,0.0838)
4 L/h	Q/F	NA	NA	NA	(2.78,4.91)
5 L	V_p/F	NA	NA	NA	(85.6,559)
6	MALE_CL/F	NA	NA	NA	(0.847,1.25)
7	WT_CL/F	NA	NA	NA	(0.61,1.91)
8	IIV_CL/F	148.409790	NA	NA	(0.128,0.321)
9	cov_CL,V	NA	NA	0.8492811	(0.0606,0.183)
10	IIV_V_c/F	33.100350	NA	NA	(0.047,0.158)
11	cov_CL,Ka	NA	NA	-0.1163229	(-0.0448,0.0261)
12	cov_V,Ka	NA	NA	-0.5607054	(-0.0577,-0.0049)
13	IIV_K_a	7.321076	NA	NA	(0.0236,0.0811)
14	err_prop	2.236068	NA	NA	(0.0399,0.0587)
15	err_add	NA	3	NA	(0.0836,0.329)

6 aesthetics

Here we format the table for printing.

Listing 24:

```
> tab$name <- NULL
> tab$parameter <- NULL
> tab$model <- wiki2latex(tab$model)
> tab$estimate <- as.character(tab$estimate)
> tab$estimate <- paste(tab$estimate, '$', tab$units, '$')
> tab$units <- NULL
```

Note that no parameter defines more than one of CV, SD, and COR. We could collapse these into a single column, and add a descriptive flag.

Listing 25:

```
> m <- as.matrix(tab[,c('cv', 'sd', 'cor')])
> tab$variability <- suppressWarnings(apply(m, 1, max, na.rm=TRUE))
> tab$variability[is.infinite(tab$variability)] <- NA
> i <- is.defined(m)
> i[!i] <- NA
> tab$statistic <- apply(i, 1, function(x) {
+   p <- colnames(i)[x]
+   ifelse(all(is.na(p)), NA, p[!is.na(p)])
+ })
> toPercent <- with(tab, !is.na(statistic) & statistic=='cv')
> tab$variability[toPercent] <- percent(tab$variability[toPercent])
> tab$variability <- as.character(signif(tab$variability, 3))
> tab$statistic <- map(tab$statistic, from=c(NA, 'cv', 'cor', 'sd'), to=c(NA, '\\\\%CV', 'CORR', 'SD'))
> tab$variability <- paste(tab$statistic, tab$variability, sep=' = ')
> tab$variability[is.na(tab$statistic)] <- NA
> tab$statistic <- NULL
> tab$cv <- NULL
> tab$sd <- NULL
> tab$cor <- NULL
```

7 simple parameter table

We can make a quick parameter table that does not use wikitab markup. Table 2.

Listing 26:

```
> tab <- rlog(1005, '../nonmem', tool='nm7', file=NULL)
> head(tab)
```

Table 1: Parameter Estimates from Population Pharmacokinetic Model Run 1005

description	model	estimate	prse	ci
apparent oral clearance	$CL/F \sim \theta_1 \cdot \theta_6^{MALE} \cdot (WT/70)^{\theta_7} \cdot e^{\eta_1}$	16 L/h	15	(7.31,11.1)
central volume of distribution	$V_c/F \sim \theta_2 \cdot (WT/70)^{\theta_1} \cdot e^{\eta_2}$	14 L	14	(19.2,27.9)
absorption rate constant	$K_a \sim \theta_3 \cdot e^{\eta_3}$	6 h ⁻¹	13	(0.0625,0.0838)
intercompartmental clearance	$Q/F \sim \theta_4$	15 L/h	3	(2.78,4.91)
peripheral volume of distribution	$V_p/F \sim \theta_5$	12 L	5	(85.6,559)
male effect on clearance	$MALE_{CL/F} \sim \theta_6$	11	2	(0.847,1.25)
weight effect on clearance	$WT_{CL/F} \sim \theta_7$	13	8	(0.61,1.91)
interindividual variability of clearance	$IIV_{CL/F} \sim \Omega_{1.1}$	10	6	(0.128,0.321)
interindividual clearance-volume covariance	$cov_{CL,V} \sim \Omega_{2.1}$	8	7	(0.0606,0.183)
interindividual variability of central volume	$IIV_{V_c/F} \sim \Omega_{2.2}$	7	9	(0.047,0.158)
interindividual clearance-Ka covariance	$cov_{CL,Ka} \sim \Omega_{3.1}$	2	4	(-0.0448,0.0261)
interindividual volume-Ka covariance	$cov_{V,Ka} \sim \Omega_{3.2}$	3	12	(-0.0577,-0.0049)
interindividual variability of Ka	$IIV_{Ka} \sim \Omega_{3.3}$	4	11	(0.0236,0.0811)
proportional error	$err_{prop} \sim \Sigma_{1.1}$	5	1	(0.0399,0.0587)
additive error	$err_{add} \sim \Sigma_{2.2}$	9	10	(0.0836,0.329)

```

tool  run parameter  moment      value
1  nm7 1005      ofv  minimum 2405.91625845151
2  nm7 1005      THETA1 estimate    9.50754
3  nm7 1005      THETA1 prse         9.84
4  nm7 1005      THETA1 se          0.935942
5  nm7 1005      THETA2 estimate    22.7907
6  nm7 1005      THETA2 prse         9.56

```

Listing 27:

```

> tab$tool <- NULL
> tab$run <- NULL
> tab <- tab[tab$moment %in% c('estimate','prse'),]
> unique(tab$parameter)

[1] "THETA1" "THETA2" "THETA3" "THETA4" "THETA5" "THETA6"
[7] "THETA7" "OMEGA1.1" "OMEGA2.1" "OMEGA2.2" "OMEGA3.1" "OMEGA3.2"
[13] "OMEGA3.3" "SIGMA1.1" "SIGMA2.1" "SIGMA2.2"

```

Listing 28:

```

> tab$value <- signif(as.numeric(tab$value),3)
> tab$parameter <- factor(tab$parameter,levels=unique(tab$parameter))#to preserve
  row order during cast
> tab <- cast(tab,parameter ~ moment)
> tab

```

	parameter	estimate	prse
1	THETA1	9.5100	9.84
2	THETA2	22.8000	9.56
3	THETA3	0.0714	7.35
4	THETA4	3.4700	15.40
5	THETA5	113.0000	21.00
6	THETA6	1.0200	11.20
7	THETA7	1.1900	28.40
8	OMEGA1.1	0.2140	22.80
9	OMEGA2.1	0.1210	26.40
10	OMEGA2.2	0.0945	33.20
11	OMEGA3.1	-0.0116	173.00
12	OMEGA3.2	-0.0372	36.10
13	OMEGA3.3	0.0466	34.70
14	SIGMA1.1	0.0492	10.90
15	SIGMA2.1	0.0000	Inf
16	SIGMA2.2	0.2020	33.50

Listing 29:

```
> tab$parameter <- parameter2wiki(tab$parameter)
> tab
```

	parameter	estimate	prse
1	theta_1	9.5100	9.84
2	theta_2	22.8000	9.56
3	theta_3	0.0714	7.35
4	theta_4	3.4700	15.40
5	theta_5	113.0000	21.00
6	theta_6	1.0200	11.20
7	theta_7	1.1900	28.40
8	Omega_1.1	0.2140	22.80
9	Omega_2.1	0.1210	26.40
10	Omega_2.2	0.0945	33.20
11	Omega_3.1	-0.0116	173.00
12	Omega_3.2	-0.0372	36.10
13	Omega_3.3	0.0466	34.70
14	Sigma_1.1	0.0492	10.90
15	Sigma_2.1	0.0000	Inf
16	Sigma_2.2	0.2020	33.50

Listing 30:

```
> tab$parameter <- wiki2latex(tab$parameter)
> tab
```

	parameter	estimate	prse
1	θ_1	9.5100	9.84
2	θ_2	22.8000	9.56
3	θ_3	0.0714	7.35
4	θ_4	3.4700	15.40

```

5    $\mathrm{\theta_5}$ 113.0000 21.00
6    $\mathrm{\theta_6}$ 1.0200 11.20
7    $\mathrm{\theta_7}$ 1.1900 28.40
8    $\mathrm{\Omega_{1.1}}$ 0.2140 22.80
9    $\mathrm{\Omega_{2.1}}$ 0.1210 26.40
10   $\mathrm{\Omega_{2.2}}$ 0.0945 33.20
11   $\mathrm{\Omega_{3.1}}$ -0.0116 173.00
12   $\mathrm{\Omega_{3.2}}$ -0.0372 36.10
13   $\mathrm{\Omega_{3.3}}$ 0.0466 34.70
14   $\mathrm{\Sigma_{1.1}}$ 0.0492 10.90
15   $\mathrm{\Sigma_{2.1}}$ 0.0000 Inf
16   $\mathrm{\Sigma_{2.2}}$ 0.2020 33.50

```

Table 2: Simple Parameter Table

parameter	estimate	prse
θ_1	9.5100	9.84
θ_2	22.8000	9.56
θ_3	0.0714	7.35
θ_4	3.4700	15.40
θ_5	113.0000	21.00
θ_6	1.0200	11.20
θ_7	1.1900	28.40
$\Omega_{1.1}$	0.2140	22.80
$\Omega_{2.1}$	0.1210	26.40
$\Omega_{2.2}$	0.0945	33.20
$\Omega_{3.1}$	-0.0116	173.00
$\Omega_{3.2}$	-0.0372	36.10
$\Omega_{3.3}$	0.0466	34.70
$\Sigma_{1.1}$	0.0492	10.90
$\Sigma_{2.1}$	0.0000	Inf
$\Sigma_{2.2}$	0.2020	33.50