

Design and Analysis of Alogrithm

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Contents

| | | |
|----------|-------------------------------------|----------|
| 1 | Q: 1 | 2 |
| 1.1 | Time complexity | 2 |
| 1.2 | pseudocode | 2 |
| 2 | Q: 2 | 2 |
| 2.1 | time complexity | 2 |
| 2.2 | Recurrence Relation | 2 |
| 2.3 | Pseudocode | 2 |
| 3 | Q: 4 | 3 |
| 3.1 | part (a) | 3 |
| 4 | Q: 5 | 3 |
| 4.1 | using Dynamic programming | 3 |
| 5 | Q: 6 | 4 |
| 5.1 | part(a) is correct | 4 |
| 5.1.1 | proof | 4 |
| 5.2 | part(b) incorrect | 5 |
| 5.2.1 | proof | 5 |
| 6 | Q: 7 | 5 |
| 6.1 | Graph | 5 |
| 6.2 | Algorithm | 5 |

1 Q: 1

1.1 Time complexity

$O(n \lg(n))$

1.2 pseudocode

```
int maximizePoints(int points[], int time[], int maxTime){
    pointsPerUnit[points.length] = 0;
    for(int i=0; i< p.length; i++){
        pointsPerUnit[i] = p[i] / t[i]
    }

    //perform sort on points and respective changes will reflect in t
    int p = 0;
    t = 0;
    i = 0;
    while(i < no_t && t <= total_time){
        if(t+time[maxTime] <= maxTime){
            t = t+time[i];
            p = p + points[i];
        }
        i++;
    }
    return p;
}
```

2 Q: 2

2.1 time complexity

$O(n^2)$

2.2 Recurrence Relation

$\text{distance}[i][j] = 1 + \min(\text{distance}[i][j-1], \text{distance}[i-1][j], \text{distance}[i-1][j-1])$

2.3 Pseudocode

$\text{distance}[i][j] = 1 + \min(\text{distance}[i][j-1], \text{distance}[i-1][j], \text{distance}[i-1][j-1])$

```

int makeString(string s1, string s2){
    for(int i=0; i< s1.length; i++){
        for(int j=0; j< s2.length; j++){
            if(i == 0 || j == 0) d[i][j] = j;
            else if (s1[i-1] == s2[j-1]){
                d[i-1][j-1]);
            }
            else{
                d[i][j] = 1+ min(d[i][j-1],d[i-1][j],d[i-1][j-1]);
            }
        }
    }
    return d[m][n];
}

```

3 Q: 4

3.1 part (a)

$s[i][j] = \text{minimum}(c[i-1][j], 1+c[i][j-1]);$

```

int substring(string x, string y){
    for(int i=0; i< x.length; i++){
        for(int j=0; j< y.length; j++){
            if(i==0) c[i][j] = j;
            else if(j == 0) c[i][j] = 1;
            else if(x[i-1] == y[j-1]) c[i][j] = 1+ c[i-1][j-1];
            else{
                c[i][j] = minimum(c[i-1][j], 1+c[i][j-1]);
            }
        }
    }
}

```

4 Q: 5

4.1 using Dynamic programming

```

int maxDiscount(int F[], int D[], int n){
    int discount[n+1];
}

```

```

discount[0] = 0;
discount[1] = 0;
int stores[n+1];
store[0] = 0;
if(d[0] < 0)d[0] = 0;
else d[0] = 1;

for(int i=2; i< n; i++){
    discount[i] = max(discount[i]-F[i-1]-1) + d[i-1],discount[i-1]);
    if(D[i] > D[i-1])
        store[i] = 1;
    else
        store[i] = 0;
    return (discount)
}
}

```

5 Q: 6

5.1 part(a) is correct

5.1.1 proof

1. The problem is to find the smallest average
2. let there be 'n' number in set 'h' and 's'
3. there will be 'n' terms of differences let smallest height be s_{height} and smallest size be s_s smallest term be s_t smallest average s_{avg}
4. $s_{\text{avg}} = \frac{s_{t1}+s_{t2}...s_{tn}}{n}$
5. s_t is only when two numbers are very close to each other
6. s_{avg} is only when each term is the least one

Hence, this greedy algorithm will give the correct solution

5.2 part(b) incorrect

5.2.1 proof

let height = {87, 82, 80, 75} and size = {10,15,20,5}

1. smallest - smallest may not be the least term
2. e.g $75 - 10 = 65$ and $75 - 20 = 55$ which means that smallest-smallest \neq smallest difference
3. Hence, this is incorrect solution

6 Q: 7

6.1 Graph

Shortest Fair problem can be mapped on Graph. where **Vertices: airports** and **weighted Edges: fair** and therefore shortest distance between Vertex 'U' to Vertex 'V' will be the shortest fair. Dijkstra Algorithm can compute the shortest distance between from source to all Vertices.

6.2 Algorithm

```
function Dijkstra(Graph, source, destination):
    create vertex set Q
    for each vertex v in Graph:
        set last[v] to null
    set dist[v] to INFINITY

    add v to Q
    set dist[source] to 0

    while Q has any vertex:
        set u to vertex in Q with min dist[u]
        remove u from Q
        for each adjacent v of u:
            set cumulative to dist[u] + weight(u, v)
            if cumulative < dist[v]:
                set dist[v] to cumulative
                set last[v] to u
    return dist[destination]
```