# $CNF \cdot SAT$

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TODO A CNF-SAT is an equation ...

#### **Definitions**

We will call  $\mathit{CNF}$  as a structure consisting of sets of literal sets. Defining recursively:

Symbol	Type	
$\mathbf{S}$		A set of disjunctions
D	$\{L\}$	A set of literals
${f L}$	$x, \neg x$	A positive or negated variable
$\mathbf{x}$	$\mid \; \top, \bot$	A variable

## 1 Equations

Set Notation · CNF 
$$\{\{a, \overline{b}\}, \{b, \overline{c}, \overline{d}\}, \{\overline{a}, \overline{c}\}\}$$
  
Arithmetic · CNF  $(a + \overline{b}) \cdot (b + \overline{c} + \overline{d}) \cdot (\overline{a} + \overline{c})$   
Negated · DNF  $\neg (ab + \overline{b}cd + ac)$ 

#### **CNF** Environment Formulas

**Zugzwang.** If a disjunction consists of one literal, the value of this literal is fixed.

$$\{X\} \in S \Rightarrow X = \top$$
  
 $\{x_i \cdot \overline{x}_i\} \subseteq S \Rightarrow S = \bot$ 

### **DNF** Environment Formulas