Abstract

Algorithmic Advances for the

Design and Analysis of Being a Good Boy

Handsome Dan

20XX

Since the beginning of recorded history, being a good boy is one of the most

fundamental societal problems facing all canines. In this dissertation, we develop a

mathematical framework for being a good boy and provide algorithms for optimal

good boy behavior.

In the first chapter, we present a decision theoretic framework for modeling standard

good boy tricks, including "sit", "stay", "paw", and "down". We show our framework is

flexible enough to incorporate Bayesian priors based on standard exponential families.

As an application of our framework, we demonstrate that the problem of learning to

optimally walk your human is polynomial time solvable.

In the second chapter, we present a suite of algorithms for computing optimal

good boy behavior. We show that, perhaps surprisingly, greedy algorithms fail to

provide even a constant factor approximation. On the other hand, we develop a class

of semidefinite programming based algorithms which allow for approximately optimal

good boy behavior in polynomial time.

# Algorithmic Advances for the Design and Analysis of Being a Good Boy

A Dissertation
Presented to the Faculty of the Graduate School
Of
Yale University
In Candidacy for the Degree of
Doctor of Philosophy

By Handsome Dan

Dissertation Directors: Peter Salovey

 ${\rm May}\ 20{\rm XX}$ 

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Perhaps the greatest paper of all is the walks we took along the way. This disser is dedicated to everyone who gave me a head pat during my time here at Yale.	tation

### Acknowledgment

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Thank you to my many collaborators from whom I have learned so much. In particular, Clifford the Big Red Dog and Airbud who have been by side at the whiteboard for all these years. The work appearing in this dissertation would not be possible without the bones we've shared together. I thank those dogs who came before me, Lassie and Wishbone, for paving the way in this field.

Finally, thank you to my dearest family for their undying love: my mother, my father, and my 9 siblings in the litter. Your continued support and playtime has been the greatest gift of all.

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## Contents

### Chapter 1

### Introduction

#### 1.1 Motivation

The problem of good boy behavior has been well established in the literature. We follow the convention of? for the potential outcomes model. Moreover, we build on the work of? and? for design and analysis of experiments. We really cited these just so we'd have a non-empty bibliography.

In order to ensure that we have made proper use of the figure directory, we should create a figure. Figure ?? shows the optimal good boy, the original Handsome Dan. Finally, we end this motivation with nonsense text to fill it out.

Hello, here is some text without a meaning. This text should show what a printed text will look like at this place. If you read this text, you will get no information. Really? Is there no information? Is there a difference between this text and some nonsense like "Huardest gefburn"? Kjift – not at all! A blind text like this gives you information about the selected font, how the letters are written and an impression of the look. This text should contain all letters of the alphabet and it should be written in of the original language. There is no need for special content, but the length of words should match the language.

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Figure 1.1: Optimal Good Boy

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## Chapter 2

## Good Boy Decision Theoretic Framework

#### 2.1 Good boy behavior

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#### 2.2 Formal theory

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### Chapter 3

## Efficient Good Boy Algorithms

#### 3.1 Greedy algorithms fail

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#### 3.2 Semdefinite programming approaches

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## Contents

# Appendix A

## **Proof of Mathematical Theorems**

This appendix contains the proofs of all claims made in main body of the dissertation.

#### A.1 Proof of Theorem 1

The proof is left as an exercise to the reader.