

EL2450 HOMEWORK 1

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Q 1: A gain named Tap exists in the Tank 1 model, what is its function?

A: The gain Tap models the bypass tap from the upper tank to the main tank. The value 0 means that it is currently closed. A value of 1 means fully opened.

Q 2: Edit *pid_design.m* and fill in the transfer functions for the upper and lower tank.

A: The figure below shows the result.

Q 3: What does the reference signal look like?

A: The signal starts at 40 and receives a step by 10 at 100 s which sets it to 50.

Q 4: Use the parameter generator to get values and fill in the transfer function F .

A: Done.

Q 5: Use the parameters to get different responses. Which is best?

A: The input parameters and their respective system parameters are:

Table 1: Parameter values and performance.

χ	ζ	ω_0	T_r [s]	M [%]	T_s [s]
0.5	0.7	0.1	6.38	6.67	38.1
0.5	0.7	0.2	3.31	22.6	18.8
0.5	0.8	0.2	3.19	20.9	18.4

The last parameter configuration works best. It is the fastest and even though it has quite significant overshoot, it is still within the given tolerance and is thus acceptable.

Q 6: What is the cutoff frequency for the open loop system? How was this derived?

A: The open loop system is $G_o = FG$ and the cutoff frequency is the frequency when the amplitude gain is 0 dB. Using the bode plots this frequency is found to be around $\omega_c = 0.35\text{rad/s}$. This is confirmed by the MatLab command *allmargin(Go)* which gives $\omega_c = 0.343\text{rad/s}$.

Q 7: A ZOH block is placed after the controller. What is the effect?

A: The effect of the system for different ZOH times is shown below.

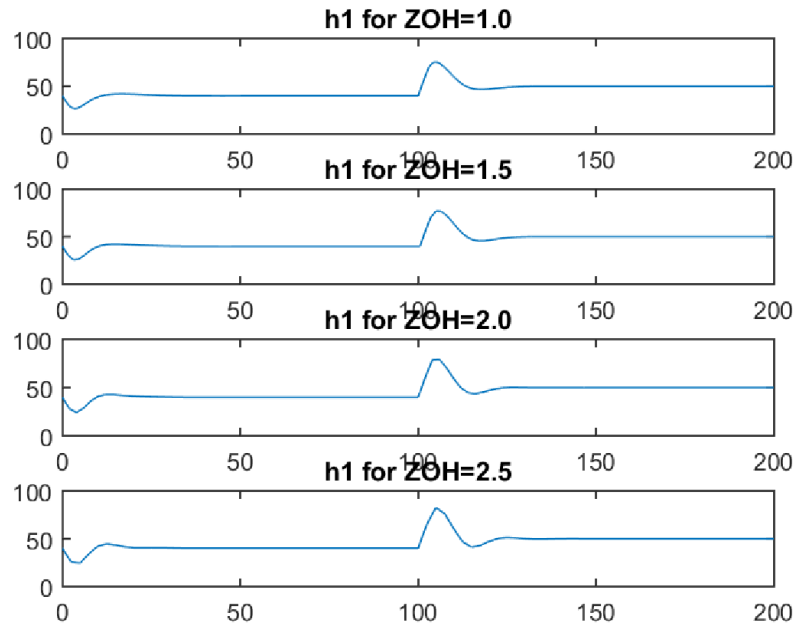


Figure 1: Upper tank level for different sampling times.

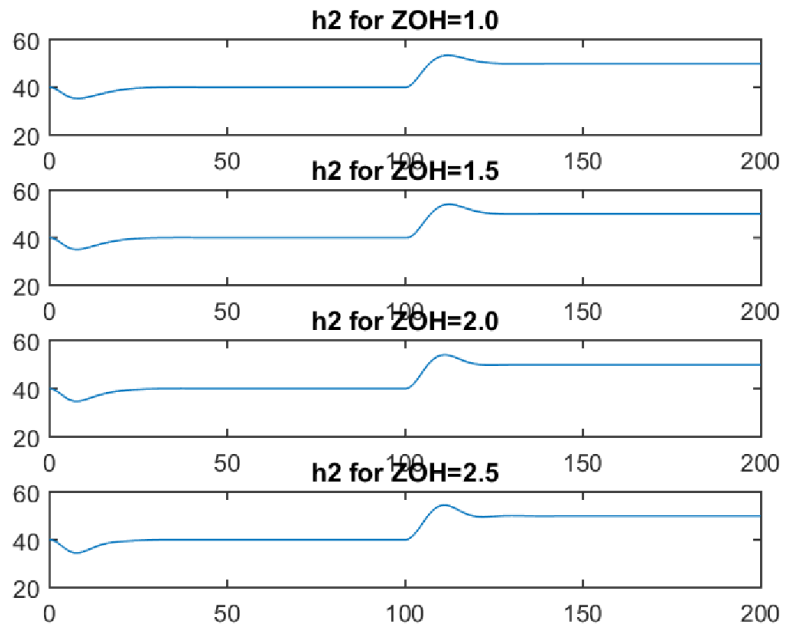


Figure 2: Lower tank level for different sampling times.

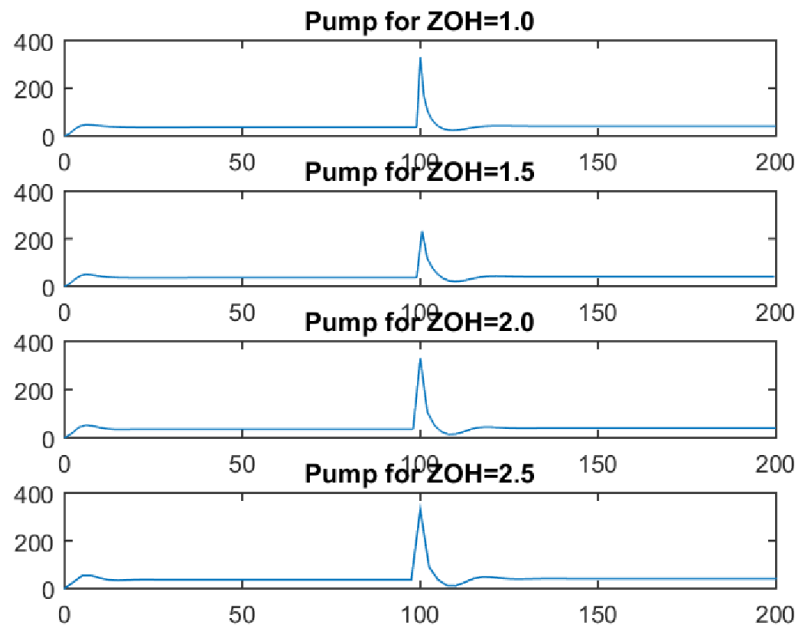


Figure 3: Pump input for different sampling times.

From the figures it can be seen that the stability and performance of the system decreases with higher sampling time. For a sampling time of about 1 second, the system is stable and the performance is smooth. At 3 second sampling time, it is oscillating and is on the verge of becoming unstable.

Q 8: Discretize the continuous controller into state space form. Replace the simulink controller block with this new discrete controller. What differences can be seen?

A: The performance of the sampled system is displayed below.

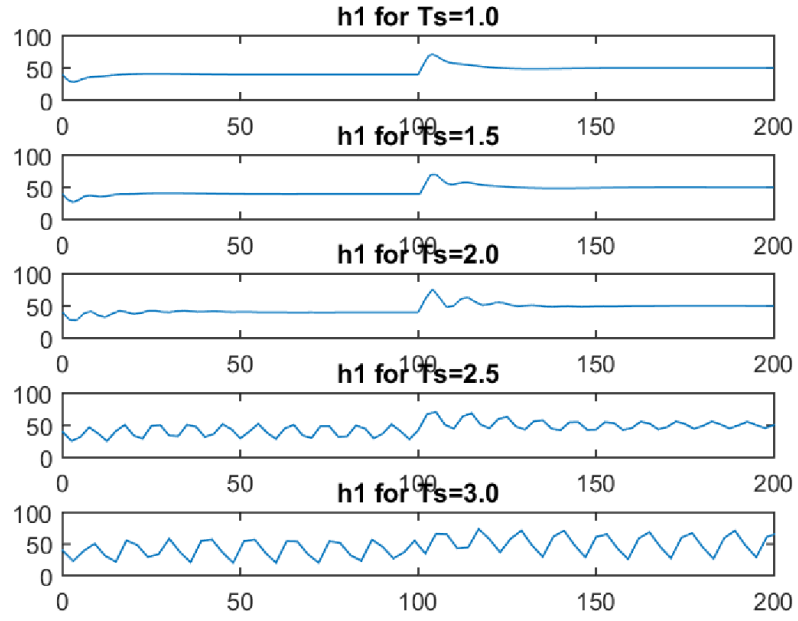


Figure 4: Upper tank level for different sampling times.

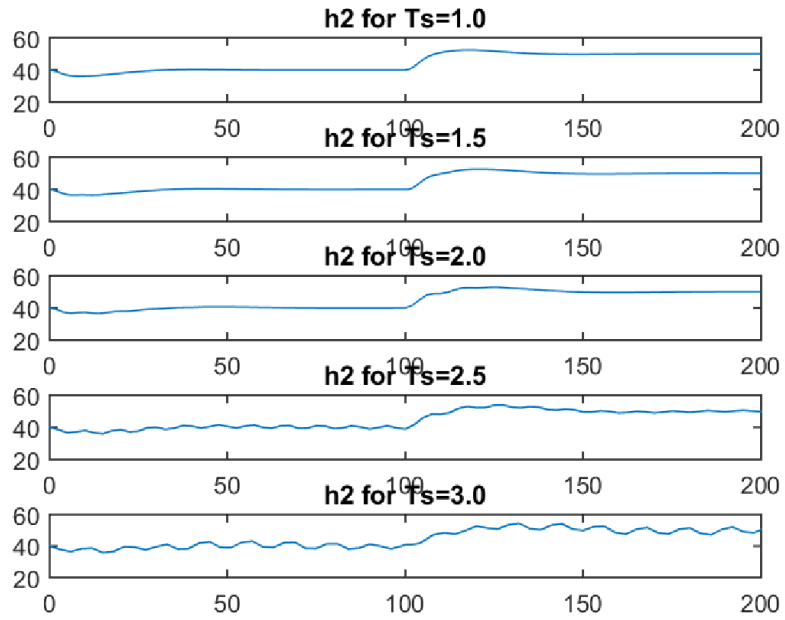


Figure 5: Lower tank level for different sampling times.

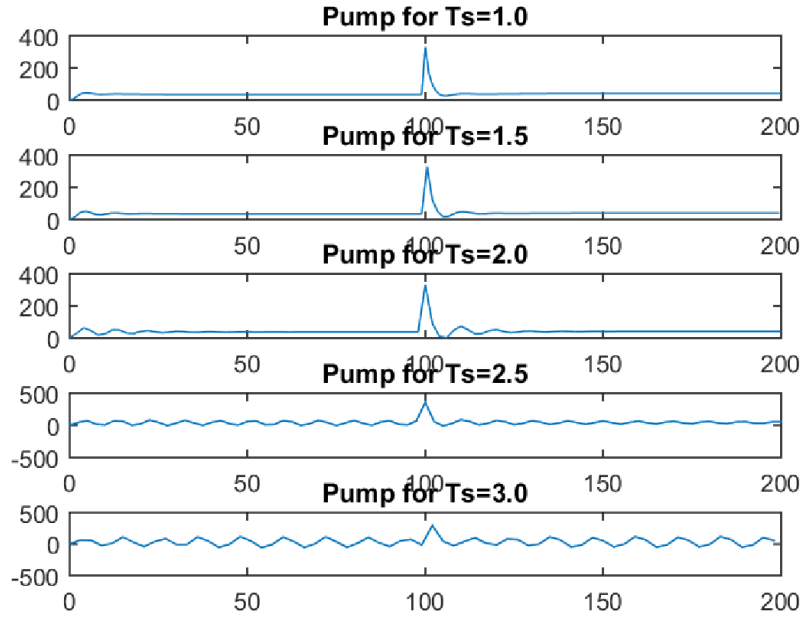


Figure 6: Pump input for different sampling times.

Comparison shows that ZOH method yields overall better results. This may be due to that the continuous system on which the ZOH method is based is more precise.

Q 9: What sampling time should be chosen?

A: The crossover frequency of the open-loop system is $\omega_c = 0.36\text{rad/s}$. The thumbrule states that the sampling frequency should be approximately $20\omega_c = 7.2\text{rad/s}$. This gives a samplingtime of $\frac{2\pi}{20\omega_c} = 0.87$ seconds

Q 10: How long can the samplingtime be without affecting the performance?

A: From question 8 it can be seen that the system is performing well up until a sampling time of about 2 seconds which is a little more than twice as fast as the rule of thumb in question 9.

Q 11: Simulate system with samplingtime at 4 seconds and estimate the control performance.

A: As can be seen below, the system is asymptotically stable but oscillating heavily. Controller performance is not good.

Q 12: Sample G, make Gd

A:

a_1	= 0.092
a_2	= 0.074