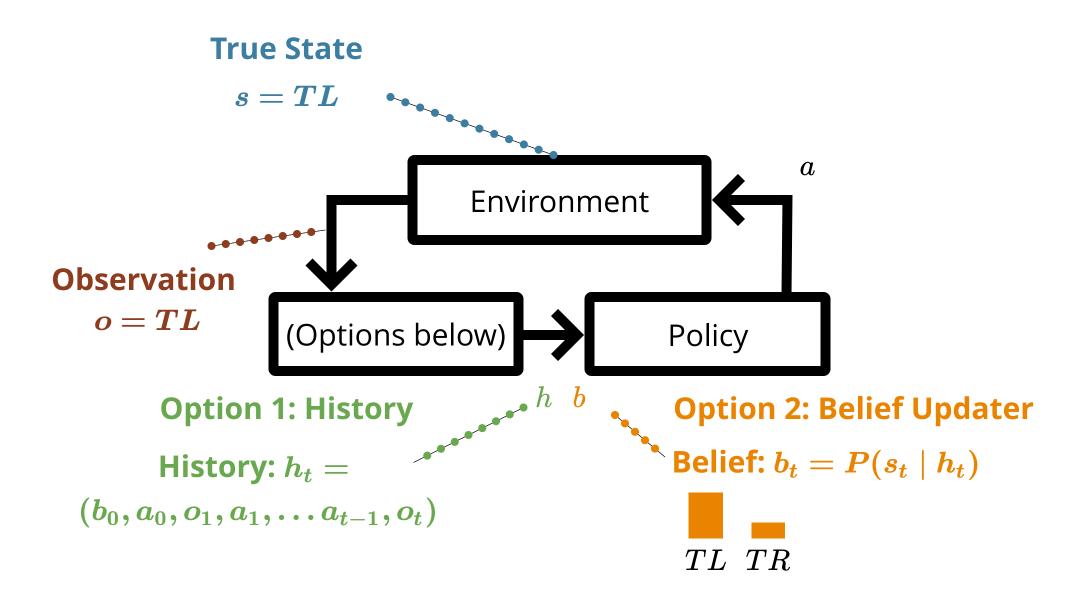
Particle Filters

POMDP Sense-Plan-Act Loop



```
function update(b::Vector{Float64}, ₱, a, o)
    S, T, O = ₱.S, ₱.T, ₱.O
    b' = similar(b)
    for (i', s') in enumerate(S)
        po = O(a, s', o)
        b'[i'] = po * sum(T(s, a, s') * b[i] for (i, s) in enumerate(S))
    end
    if sum(b') ≈ O.O
        fill!(b', 1)
    end
    return normalize!(b', 1)
end
```

$$b_t(s) = P(s_t = s \mid h_t)$$

```
function update(b::Vector{Float64}, ₱, a, o)
    S, T, O = ₱.S, ₱.T, ₱.O
    b' = similar(b)
    for (i', s') in enumerate(S)
        po = O(a, s', o)
        b'[i'] = po * sum(T(s, a, s') * b[i] for (i, s) in enumerate(S))
end
if sum(b') ≈ 0.0
    fill!(b', 1)
end
return normalize!(b', 1)
end
```

$$b_t(s) = P(s_t = s \mid h_t)$$
 $b' = au(b, a, o)$

```
function update(b::Vector{Float64}, ₱, a, o)
    S, T, O = ₱.S, ₱.T, ₱.O
    b' = similar(b)
    for (i', s') in enumerate(S)
        po = O(a, s', o)
        b'[i'] = po * sum(T(s, a, s') * b[i] for (i, s) in enumerate(S))
    end
    if sum(b') ≈ O.O
        fill!(b', 1)
    end
    return normalize!(b', 1)
end
```

b' = au(b, a, o)

$$b'(s') \propto Z(o \mid a,s') \sum_s T(s' \mid s,a) \, b(s)$$
 function update(b::Vector{Float64}, \mathcal{T} , a, o)
$$S, \, \mathsf{T}, \, 0 = \mathcal{T}.S, \, \mathcal{T}.\mathsf{T}, \, \mathcal{T}.0$$

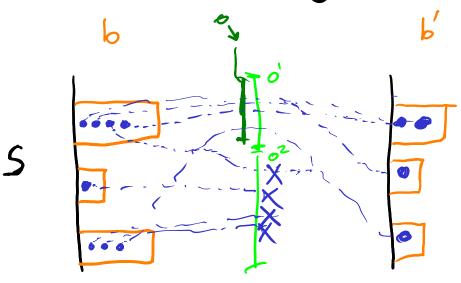
$$b' = similar(b)$$
 for (i', s') in enumerate(S)
$$po = 20(a, s', o)$$

$$b'[i'] = po * sum(\mathsf{T}(s, a, s') * b[i] \text{ for } (i, s) \text{ in enumerate}(S))$$
 end
$$if \, sum(b') \approx 0.0$$

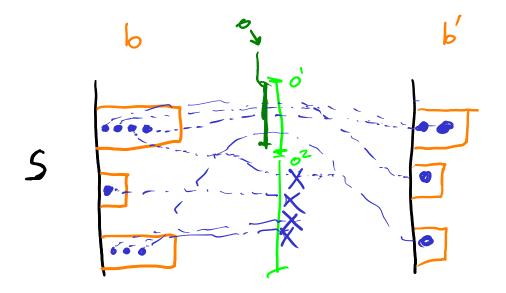
$$fill!(b', 1)$$
 end
$$return \, normalize!(b', 1)$$
 end

 $b_t(s) = P(s_t = s \mid h_t)$

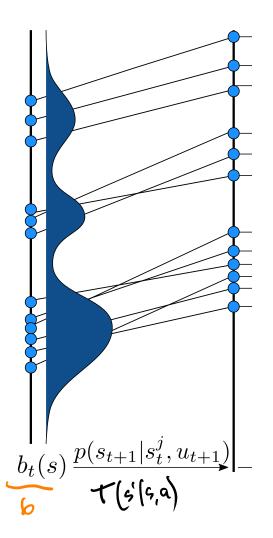
Rejection Particle Filter

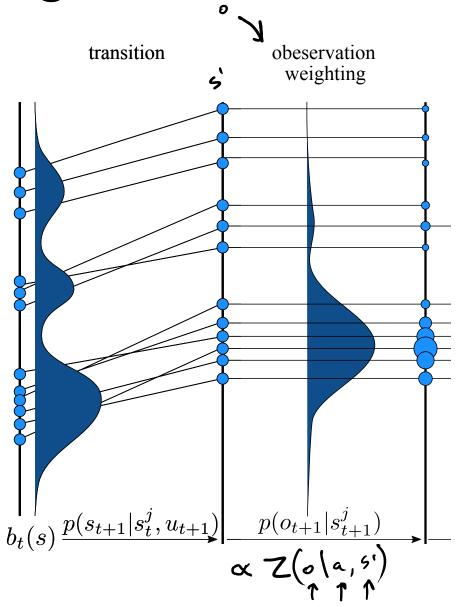


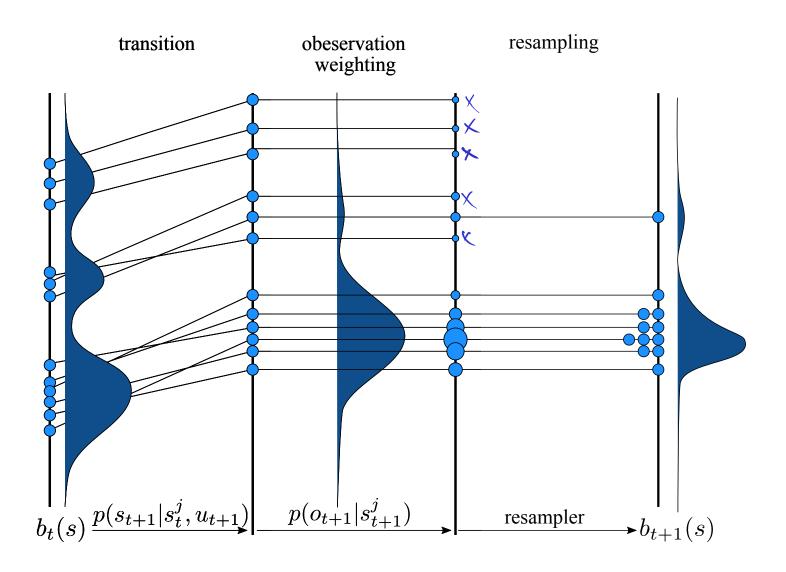
Rejection Particle Filter



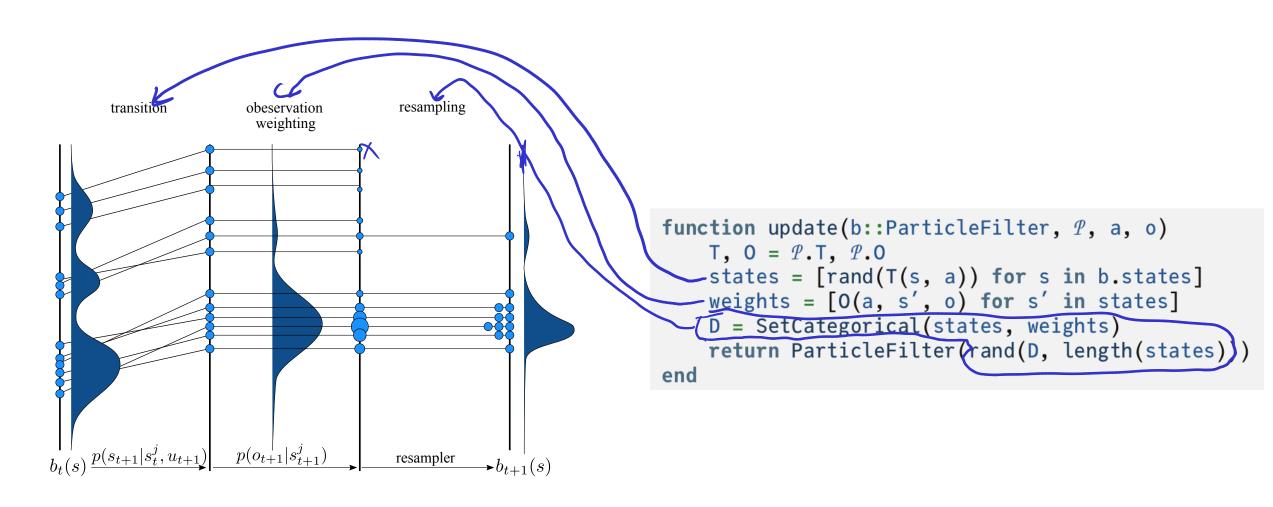
transition

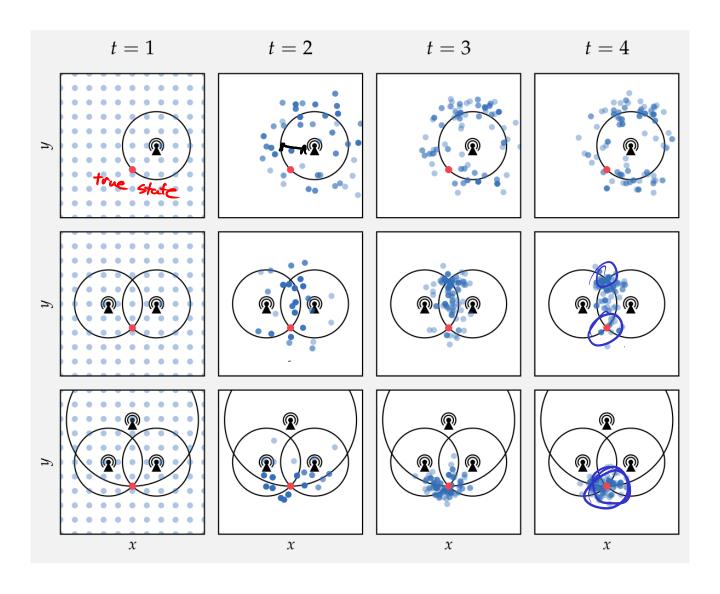


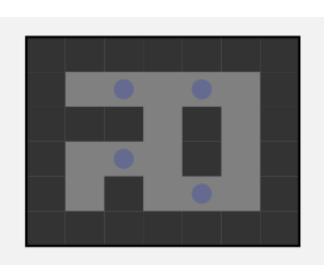


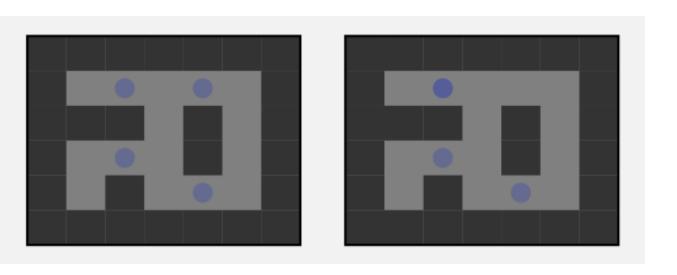


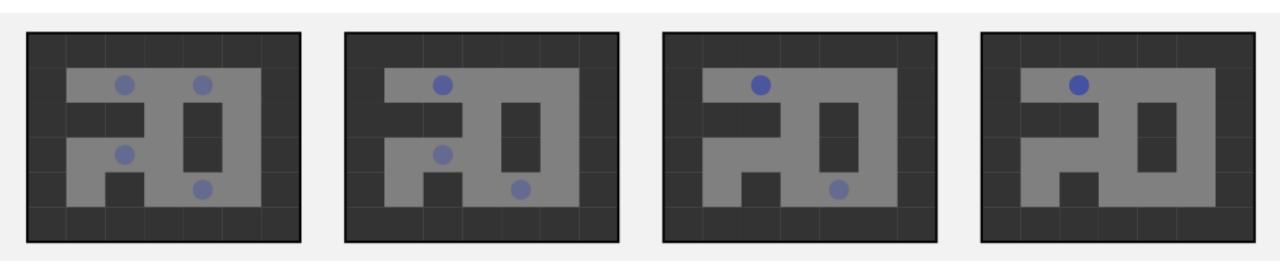
```
function update(b::ParticleFilter, P, a, o)
    T, 0 = P.T, P.O
    states = [rand(T(s, a)) for s in b.states]
    weights = [0(a, s', o) for s' in states]
    D = SetCategorical(states, weights)
    return ParticleFilter(rand(D, length(states)))
end
```

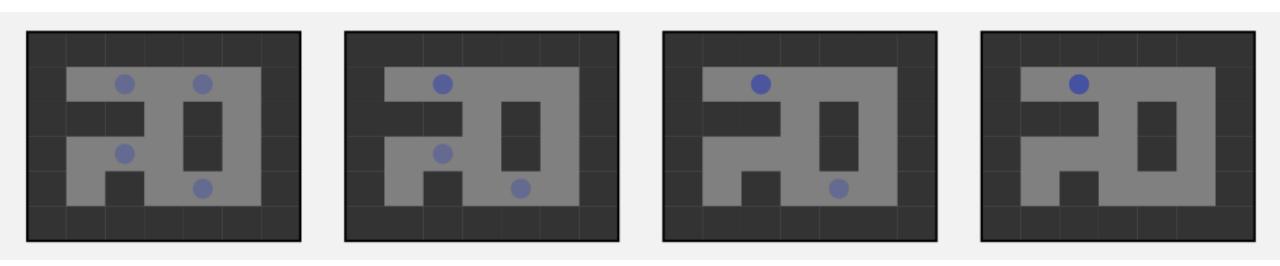




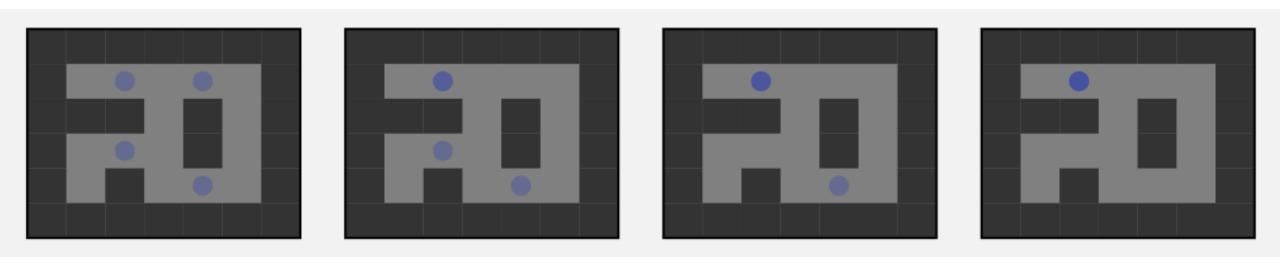






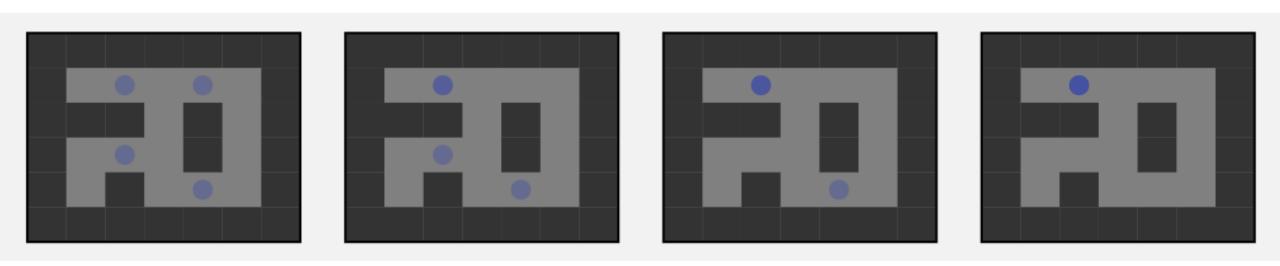


Solution: Domain specific particle injection based on:



Solution: Domain specific particle injection based on:

Weights



Solution: Domain specific particle injection based on:

- Weights
- Particle Diversity

Important Particle Filter Properties

Important Particle Filter Properties

• Often the number of particles does **NOT** need to scale exponentially with the dimension (i.e. $n \neq k^d$)

Important Particle Filter Properties

- Often the number of particles does **NOT** need to scale exponentially with the dimension (i.e. $n \neq k^d$)
- Implementation should have O(n) complexity.

