

# Last Time

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- What is a **policy**?

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- How is a **Markov decision process** defined?
- What is a **policy**?
- How do we **evaluate** policies?

# Guiding Questions

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- How do we reason about the **future consequences** of actions in an MDP?
- What are the basic **algorithms for solving MDPs**?

# MDP Example: Up-Down Problem

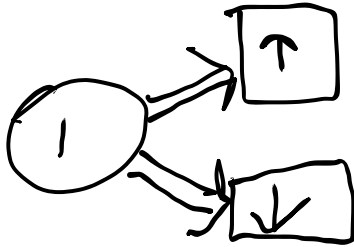
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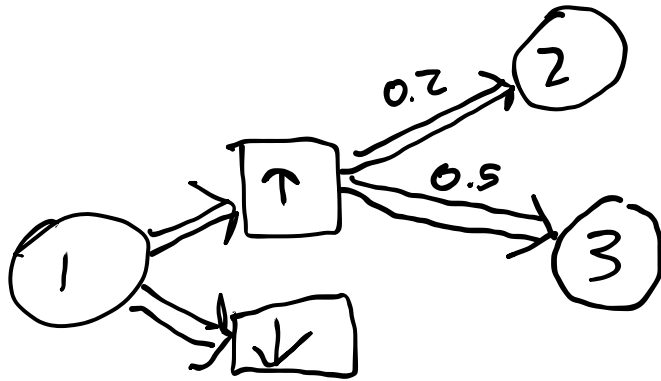




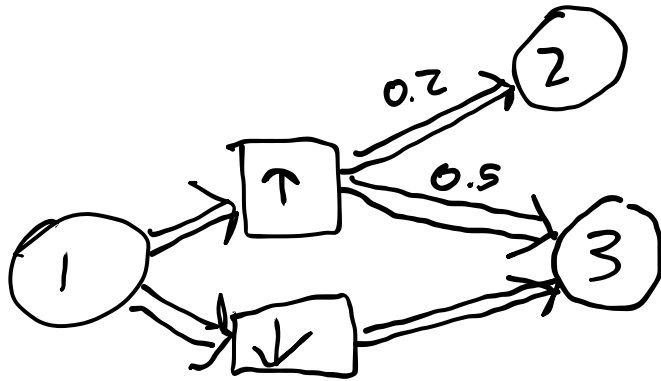
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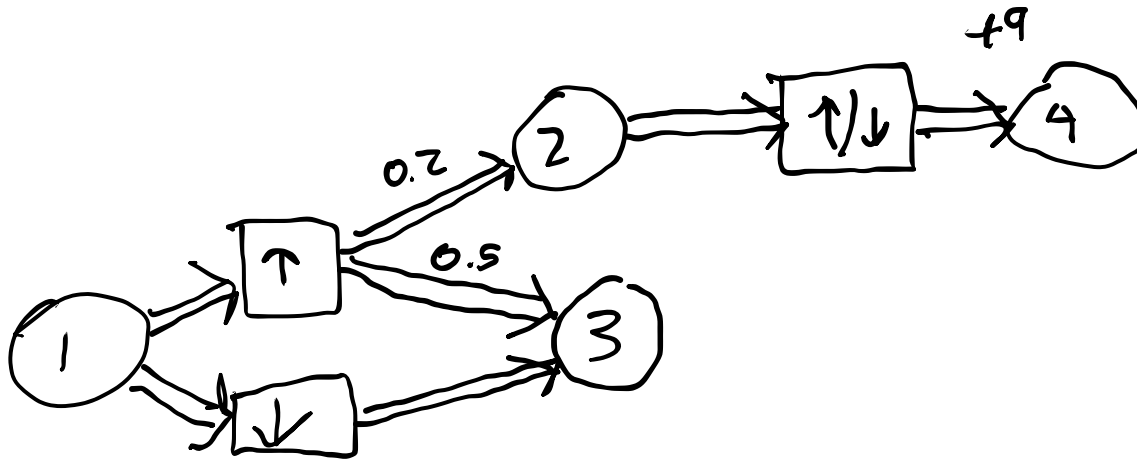
# MDP Example: Up-Down Problem



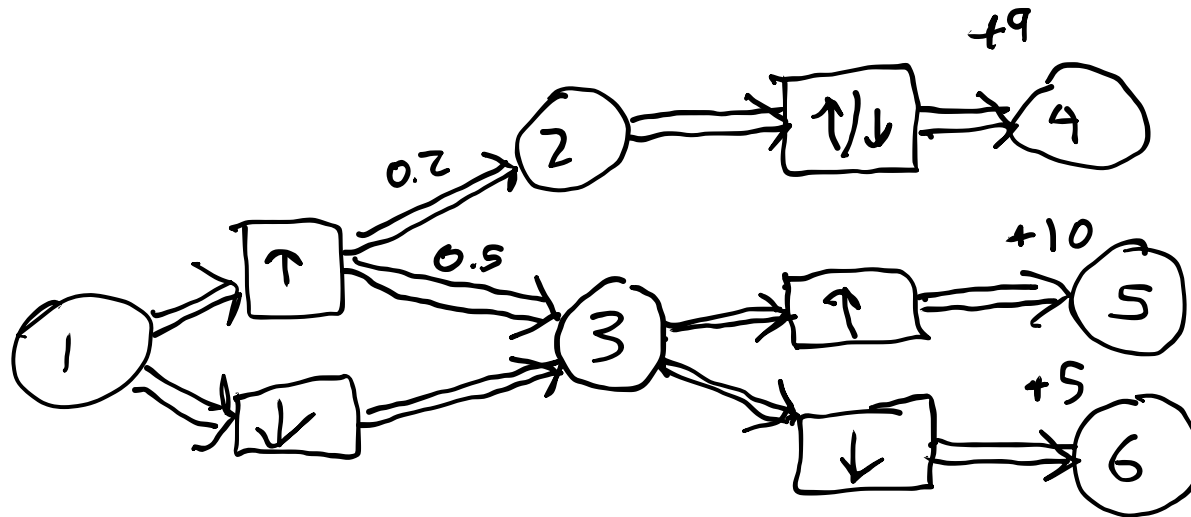
# MDP Example: Up-Down Problem



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# Value Functions

# Matrix Evaluation

# Policy Iteration



# Policy Iteration

## Algorithm: Policy Iteration

Given: MDP  $(S, A, R, T, \gamma, b)$

initialize  $\pi, \pi'$  (differently)

while  $\pi \neq \pi'$

$$\pi \leftarrow \pi'$$

$$V^\pi \leftarrow (I - \gamma T^\pi)^{-1} R^\pi$$

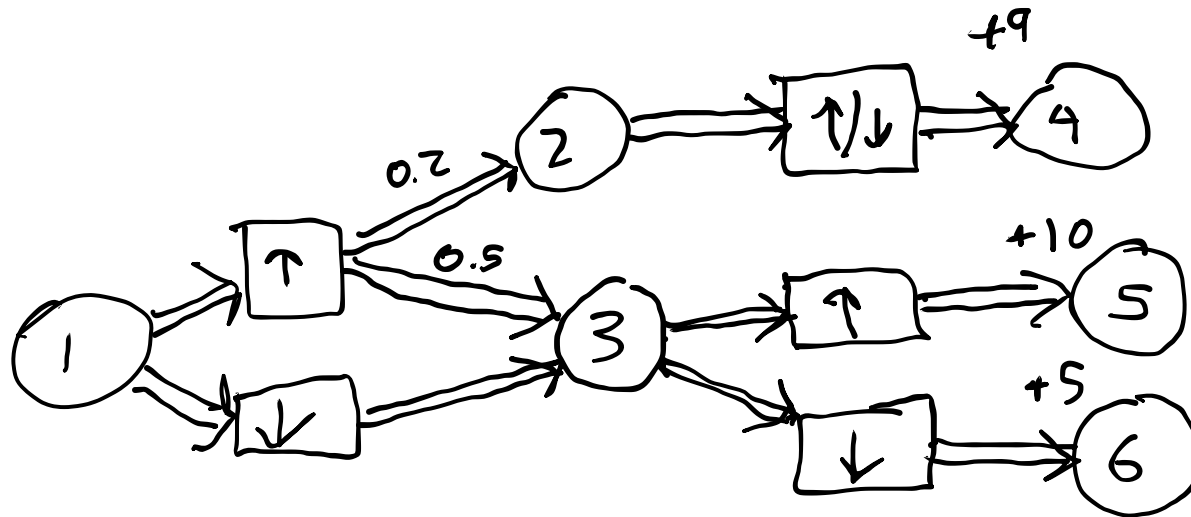
$$\pi'(s) \leftarrow \operatorname{argmax}_{a \in A} (R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^\pi(s'))$$

return  $\pi$

# Bellman's Equation

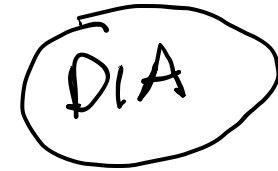
# Value Function Policies

# Backup by hand example



# Breakout Rooms: DIA Run

Boulder.

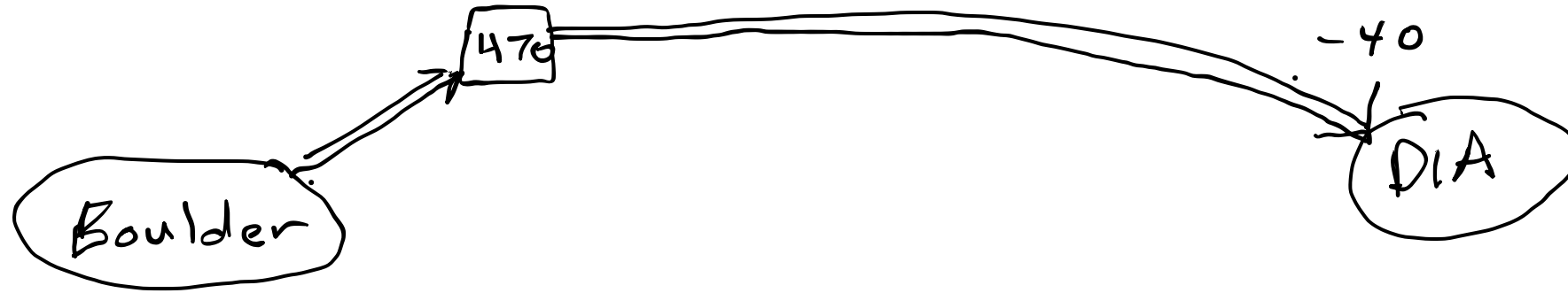


# Breakout Rooms: DIA Run

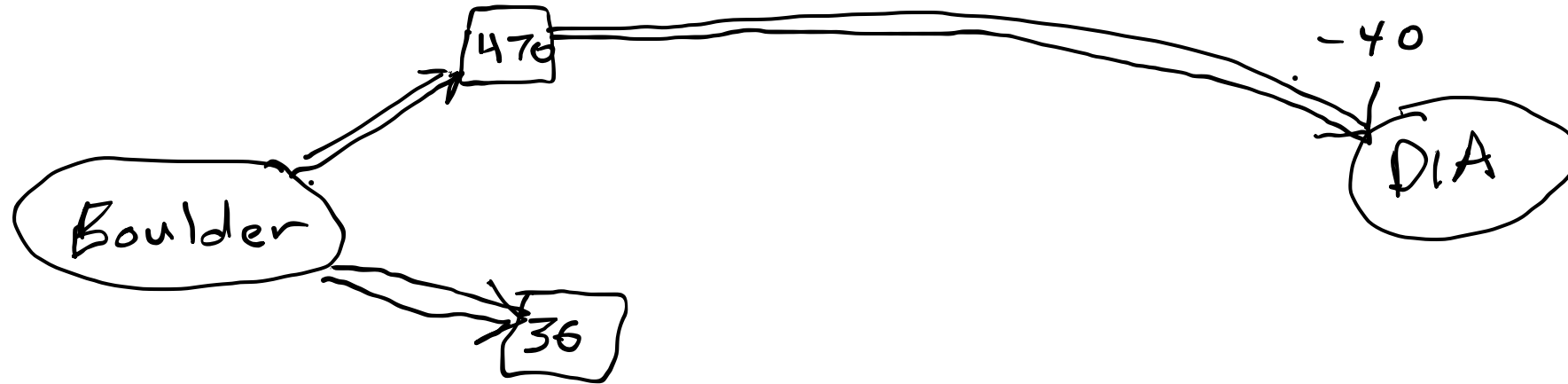
Boulder

DIA

# Breakout Rooms: DIA Run

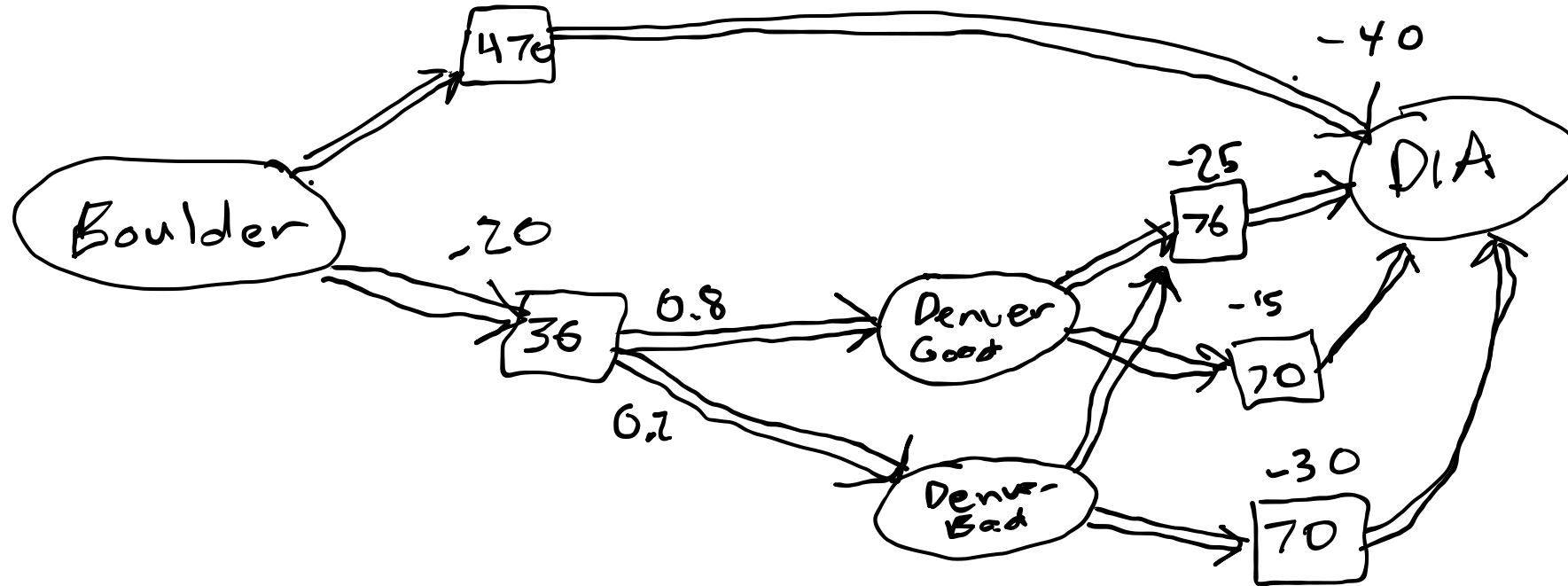


# Breakout Rooms: DIA Run





# Breakout Rooms: DIA Run



# Value Iteration

# Value Iteration

## Algorithm: Value Iteration

Given: MDP  $(S, A, R, T, \gamma, b)$ , tolerance  $\epsilon$

initialize  $V, V'$  (differently)

while  $\|V - V'\|_\infty < \epsilon$

$V \leftarrow V'$

$$V'(s) \leftarrow \max_{a \in A} \left( R(s, a) + \gamma \sum_{s' \in S} T(s'|s, a) V^\pi(s') \right) \quad \forall s \in S$$

return  $V'$

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