

SPECIALE TITEL HER!

Anders Holst Rasmussen

June 6, 2021

Contents

1	Introduction	3
2	Experimental Methods	5
2.1	Detector setup	5
2.2	Experimental setup	5
2.3	The detectors	6
2.4	AUSAlib and ROOT	8
2.4.1	Unpacker	9
2.4.2	Calibrator	9
2.4.3	Sorter	10
3	Data Reduction	12
3.1	Calibration	12
3.2	Identifying the particles	13
3.2.1	Identifying a hit	14
3.3	Angular cut	15
3.4	Momentum cut	16
3.5	Multiplicity cut	17
4	Analysis	19
4.1	The effects of the cuts	19
4.1.1	The effect of the angular cut	21
4.1.2	The effect of the momentum cut	21
4.1.3	The effect of the multiplicity cut	22
4.1.4	The combined effect of all the cuts	22
4.2	The excitation energy of ^8Be	23
4.3	Angular efficiency of the setup	24
4.4	Angular correlations of α -particles and β -particles	29

1 Introduction

In this thesis i will make a thorough analysis of the the delayed β -decay of ^8Li . The first part of the thesis will will be governing getting data from a detector sorted into an appropriate data structure that can be analyzed. The second part is a more physics analysis of the α -particle pair that is produced, and their correlation to the β -particle. Lastly a discussion of the result and setup will be conducted.

1. We are interested in the decay, and want to describe what is happening.
2. Different levels which gives a continuum of $2+$ state.
3. ^8Li har spin $+2$
4. We expect $2+$ structure in ^8Be
5. There exists earlier measurements of ^8B made in the AU group.
6. ^8B is the mirror core?? And has been measured very precisely.
7. Measure Li with same precision.
8. A beautiful spectrum from the alphas.
9. Look at a single alpha.
10. Look at coincidence.
11. Better to look at both and add, recoil will give widening.
12. read bataratjaa
13. We are interested in beta alfa angles for ^{12}B

14. People have measured this angle precisely, because they were looking for deviations in the standard model.

We want to examine the β -delayed decay of ^8Li , which is an unstable isotope of Lithium. Lithium normally occurs stable as ^6Li and ^7Li , with the latter being the more abundant with 92.5% of all atoms. The longest living radioactive lithium isotope is ^8Li , with a half-life of 839 ms [ref.](#)

^8Li is an interesting atom, as it will decay into ^8Be , which is a constituent in the triple-alpha process in stellar astrophysics. ^8Be creates a bottleneck for the creation of heavier elements, as it is very short lived, and has a half-life of 1×10^{-16} s.

^8Li will also decay into ^8Be at different energy levels, which will give a continuum of the $2+$ state from ^8Li .

The Sub-atomic group at Aarhus University has previously measured decay of the mirror nuclei, ^8B . Since there exists very precise measurement, we want to obtain similar precise measurements of ^8Li .

2 Experimental Methods

The data used in this thesis stems from an experiment carried out at the IGISOL facility, at the University of Jyväskylä. Originally the experiment was scheduled for May 2020, but was postponed due to the ongoing Corona pandemic.

2.1 Detector setup

The detection setup consists of 6 double sided silicon detectors (DSSD), and 6 single sided silicon detectors (SSD). The detectors are $5\text{ cm} \times 5\text{ cm}$ and placed in a cube around the a target in the center, as shown on figure [fig. 2.1](#). The setup is designed with measuring the opening angle of the β in mind, and therefore the detectors covers 51% of the solid angle.

2.2 Experimental setup

The setup is designed to measure $\beta\alpha$ angular correlations in the β -delayed particle decay of ^8Li . When measuring multiple particles, the setup is highly dependent on the coverage of the solid angle. Therefore the setup is designed to have a large solid angle coverage, with high α -particle resolution, while still being able to measure β -particles.

This is has been achieved by creating a cube of six double sided silicon detectors (DSSD), all backed by a 1 mm single sided detector (SSD). To gain the largest solid angle, the detectors where placed as close to one another as possible. A 3D printed case was designed to hold the detectors in place, and achieved a solid angle coverage of 51% for the DSSD's. An illustration of the setup, together with the different detectors' thickness can be seen on

Detector	Thickness [μm]	PAD	Thickness [μm]
Det1	67	n/a	n/a
Det2	1002	P2	1036
Det3	65	P3	1497
Det4	60	P4	1490
DetU	60	PU	1498
DetD	1043	PD	1038

fig. 2.1. Even though the setup was designed to hold 12 detectors in total, there were only 11 detectors in the actual experiment. This was due to one of the SSD's being defect, so it was removed from the setup.

2.3 The detectors

As mentioned above, there were two types of detectors present in the setup. The first type is the Double sided silicon detector. As the name suggests, it consists of two sides, a front layer and a back layer. Each layer consists of 16 strips, that are placed in rows next to each other. The two layers are then arranged so each side are mutually orthogonal, which defectively makes pixels where each strip intersects a strip on the other side.

The strips on the front side are p-doped, while the back side are n-doped. When a charged particle hits the detector, it will ionize the atoms in the semi-conductor, and produce an electron-hole pair. The number of electron-hole pairs is proportional to the energy of the charged particle. The bias voltage on the detector collects the electrons and holes on opposite sides of the strip, where the charge is collected on aluminum contacts and a signal is measured. Energy is not deposited in these contacts, and therefore they constitute to a so called dead layer.

The detectors are square 5×5 cm and with their 16×16 strips, they have an effective grid of 256 pixels of 9 mm. 4 of the 6 detectors have a thickness of $60 \mu\text{m}$ and a dead layer of 100 nm dead layer. These detectors are the ones called Det1, Det3, Det4 and DetU in the setup seen on fig. 2.1. The other 2 detectors (Det2 and DetD) were both 1 mm.

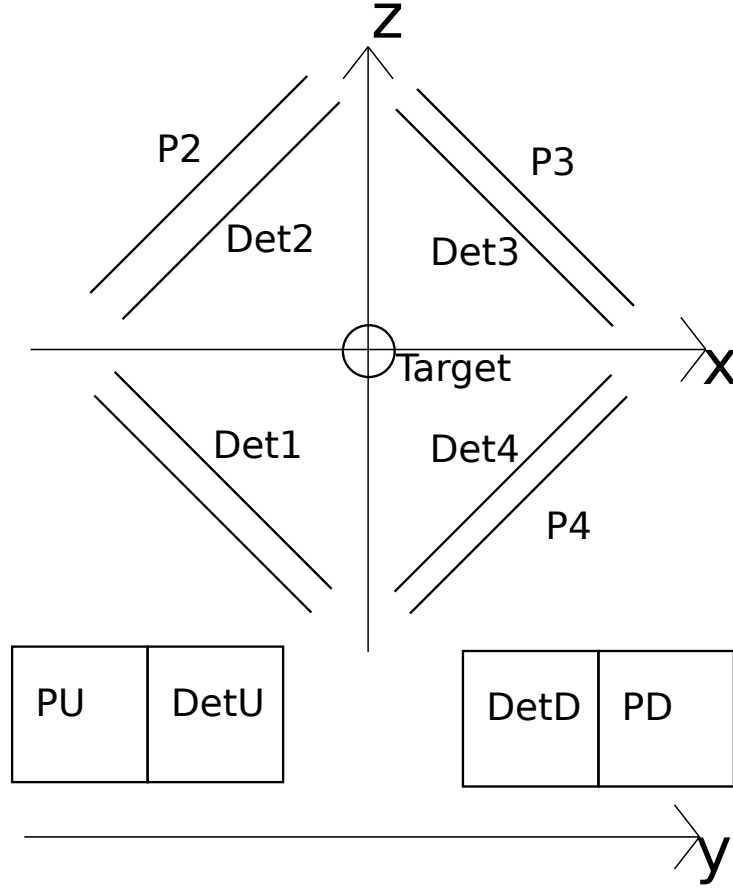


Figure 2.1: illustration of the setup. Note that the SSD P1 was absent from the actual experiment, due to failure in the detector

The other type of detector was the SSD's also known as pads. They are different from the DSSD's, in that they only have one side, and no strips. Therefore they do not contain a grid, the same way the DSSD's do, and will therefore not provide any information as to where on the detector a particle has hit. But the reason they are in this setup, is because they are thicker. They are used to measure the energy deposited by a β -particle, and to determine if a given particle is a β -particle. An α -particle will deposit all of its energy into the first DSSD it encounter, and be effectively stopped completely by it. But a β -particle will deposit almost no energy in a thin DSSD, and travel through it, ending up depositing some energy in the SSD. Therefore one can roughly distinguish the α -particles from the β -particles,

by observing whether a particle has a hit in the DSSD and the SSD.

Since there are also two thick DSSD's in the setup, one can also get some information from a β -particle from these thicker detectors, as it will deposit more energy in these detectors.

2.4 AUSAlib and ROOT

ROOT is an object oriented C++ framework that is designed primarily for data analysis in high-energy and nuclear physics. It was created at CERN in 1995, and has since grown and become the dominant analysis software at both CERN and many other nuclear and particle physics laboratories. ROOT was designed to handle large amounts of data with high computing efficiency.

ROOT makes an intelligent data structure by creating a "Tree" with the class `TTree`. This tree will then have "branches" which corresponds to some variable of the given detection event, such as the energy of the front strip or identity of the detector. This `TTree` then allows for reading of an individual branch, while ROOT takes care of the memory management. One can also store a `TTree` to the disk in the form a `.root` file.

AUSAlib is a tool that build on top of ROOT. It was created by the subatomic group at Aarhus University. Before this tool was created, everyone in the group had to more or less create their own tools to get data from the detectors into a useful data structure. This meant that a lot of time was wasted just trying to access data from experiments. AUSAlib was therefore created, so the basic tasks of data extraction was automated.

AUSAlib has a lot of functionalities, but there are **XX** tools that was used in this thesis, namely the *Sorter*, *Calibrator* and the *AbstractSortedAnalyzer*.

2.4.1 Unpacker

The **Unpacker** converts raw data from the detectors into a ROOT TTree. This is done by using the unpacking program **ucesb** [ref](#). This will setup the branch structure of the data. Some of these branches are **FT** and **BT**, which is a vector of the TDC (time) values for each event, for the front and backside of the detector. They are vectors because they contain information for each particle hits in a given time slot, for which there can be multiple. There are also the branches **FE** and **BE**, which is the ADC (energy) associated with the events.

2.4.2 Calibrator

Since the detectors work, by measuring an electrical charge that comes from the charged particle, the detectors needs to translate a specific charge to energy deposited.

To do that, we use the **Calibrator**-tool, which is designed to convert a channel number into an actual energy. Assuming that the channel numbers are linearly related to the energies, a known radioactive source can be measured, and the expected spectrum can be compared to the measured. This is done for each strip in each detector.

The **Calibrator** starts by running a peak-finding algorithm over some calibration data, to roughly identify the locations of the peaks, followed by a multi-Gaussian fit to find the most precise peak location. The positions of the peaks can then be compared to the expected energies, giving an associated energy to a given channel.

As mentioned earlier, all of the detectors have a small aluminum dead layer. All particles that pass through this layer will loses some amount of energy depending on the stopping power of the material and the effective thickness of the dead layer Δx_{eff} , which furthermore depends on the angle of incidence, θ . The relationship between the effective thickness and the actual thickness

is described as $\Delta x_{eff} = \Delta x / \cos(\theta)$. This gives the measured energy as

$$E' = E - \frac{dE}{dx} \frac{\Delta x}{\cos(\theta)},$$

where E is the original energy of the particle, dE/dx is the stopping power of the material and Δx is the thickness of the dead layer.

These calculations are all handled by the **Calibrator**. As input it takes an unpacked measurement of a source, a file specifying the locations of the expected peaks and a file specifying the spacial locations of the detectors. From this it calculates the energy loss, and creates a linear relationship between channel numbers and energies. This is then written to the disk as a separate calibration file, which can be parsed to other modules.

It is important to note that the Calibrator does not modify any data. Therefore the energy loss is unaccounted for. Instead it corrects the expected energy spectrum, which means that the resulting calibration is still valid. The energy loss correction is therefore still needed in the analysis, as the effect is unaccounted for in measurements.

2.4.3 Sorter

The sorter is used after a successful calibration. It generates a ROOT file based on the unpacked data, and applies the calibration. It is also responsible for matching and combining events from the front-side to the back-side of the detector. If there were one hit in the front side and one in the back, the matching is fairly trivial. If there however were multiple hits in both front and back, the **Sorter** will run a matching algorithm, which pairs the hits with the lowest energy differences.

When the events have been matched, the hits on the individual sides of each detector are merged into a single event. Therefore each event can now be considered a multiple of particle hits. This makes it possible to associate physical properties with each particle, such as direction and energy.

There has still not been done any filtering of the data, which is what we will discuss in chapter [3](#).

3 Data Reduction

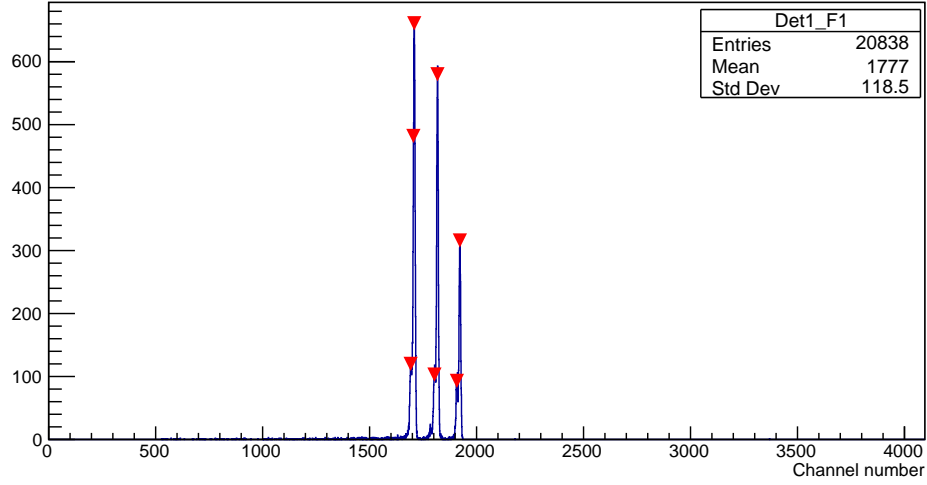
3.1 Calibration

To actually calibrate the detectors, we use an α -source with a known spectrum. The source is placed in the target position, and each detector is in turn placed in front of the source. The radioactive source used to calibrate this setup contained ^{148}Gd , ^{239}Pu and ^{244}Cm . Each isotope has a prominent main peak, and several sub peaks. The proprieties of which is listed in table 3.1.

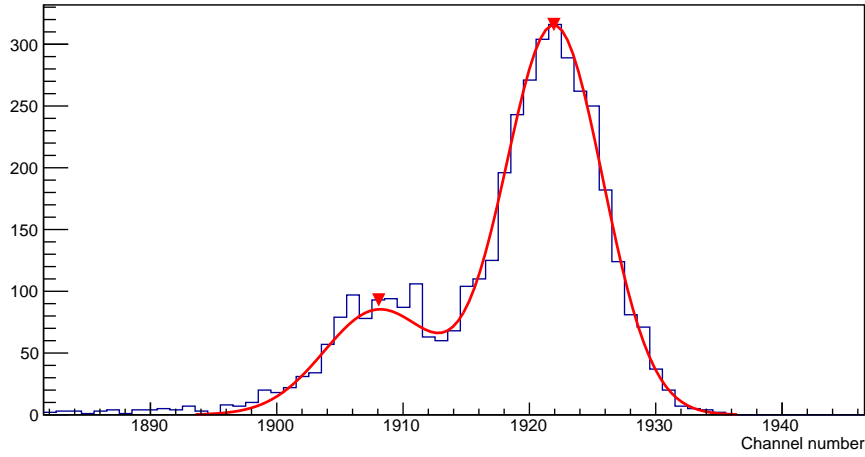
Isotope	E_α [keV]
^{148}Gd	3182.690
^{239}Pu	5105.5
	5144.3
	5156.59
^{244}Cm	5762.64
	5804.96

Table 3.1: Decay energies for each isotope used in the calibration.

A typical single strip spectrum is shown on fig. 3.1a, where the calibrator has given an estimate of where the peaks are, illustrated by the red triangles. fig. 3.1b shows a closer look at the ^{244}Cm peak, where the red line shows the Calibrator-fit over both the main peak and the sub peak.



(a) A spectrum of the calibration source, with channel number along the x-axis. The red triangles indicate the positions the **Calibrator** has guessed as the peaks.



(b) A closer look at the ^{244}Cm peak on the above figure. The red line is a fit performed by the **Calibrator**, and the red triangles indicate the guessed peaks.

Figure 3.1: Calibrations of detector 1

3.2 Identifying the particles

After utilizing the AUSAlib tools, the data is ready to be analyzed. Even though the theory dictates that a decay will consist of two α -particles and one β -particles, it is not realistic to just assume that each detected event will consist only of this configuration of particles.

Therefore we need some cut on what events we will allow through to the analysis. Specifically we are going to impose 3 cuts on the data, a angular cut, a momentum cut and a multiplicity cut.

3.2.1 Identifying a hit

After a hit has been detected, and all the relevant information has been extracted from the hit, we can start to analyze what type of particle has hit the detector.

A important distinction between an α -particle and a β -particle is the different interactions with a detector. An α -particle will be completely stopped by a standard $60\ \mu\text{m}$ detector, while a β -particle will pass through it, depositing only a small amount of energy.

This is the reason for the PAD's behind each DSSD. The idea is that only a β -particle will be detected in the PAD's, so if a hit has some energy in a DSSD *and* the corresponding PAD, it will be classified as a β -particle.

This approach however does not work as well as intended. Often what happens is that the thin DSSD will not pick up any energy deposited, and the hit will therefore not be counted. But not all of the detectors are $60\ \mu\text{m}$. We have two detectors that are around $1000\ \mu\text{m}$ thick. These detectors are much better at picking up a signal from a β -particle, so one of the criteria for being a β -particle in this setup is to have hit either Det2 or DetD.

These two criteria are however not enough to uniquely determine that a hit was a β -particle. We still have to consider the events where a detector has multiple hits. Since a PAD gives no usable information regarding where a particle has hit, we cannot say which particle was a β -particle and which where an α -particle.

Therefore if the β -particle criteria are true, we mark the particle as a *possible* β . But since it might as well have been a α -particle, we also mark it as such. Every hit that does not uphold to the β -particle criteria are of course marked only as a possible α -particle.

When all the particles have been identified, we impose the first cut to the data. A multiplicity cut that says we need at least two α -particles. If there are less, we discard the event.

When we at least have two distinct particles that can be α -particles, we look at their mutual difference in momentum. The particle pair with the least difference in momentum will be chosen as the only α -particles that can be present in an event. Then we have assured that every other particle we see in the event, is possible β -particle candidates.

When each particle has been identified or discarded, all remaining particle-specific information is stored to the given particle for easy analysis henceforth.

3.3 Angular cut

When ^8Be decays, and produces the two α -particles, it will do so under conservation of momentum. The decay in any direction, but the angle θ between them will be close to 180° . Therefore the first cut that we give to the data, is that two of the particles that are α candidates, must have a mutual angle of close to 180° .

On fig. 3.2 a plot of all the the mutual angles are shown. A quick glance will give that most particles will have mutual angle of close to 180° .

By looking at this, we see that most of the angles will lie close to 180° , and now we must decide exactly where to do the cutoff. By taking a sharp cutoff at $\cos(\theta) \geq -0.99$, we will exclude a great deal of good measurements, on the other hand, a too soft cut will not accomplish anything, as too many "wrong" particles will let through the check. By trying different cuts, we have found that $\cos(\theta) \geq -0.95$ is a good cutoff, and this corresponds to 161° .

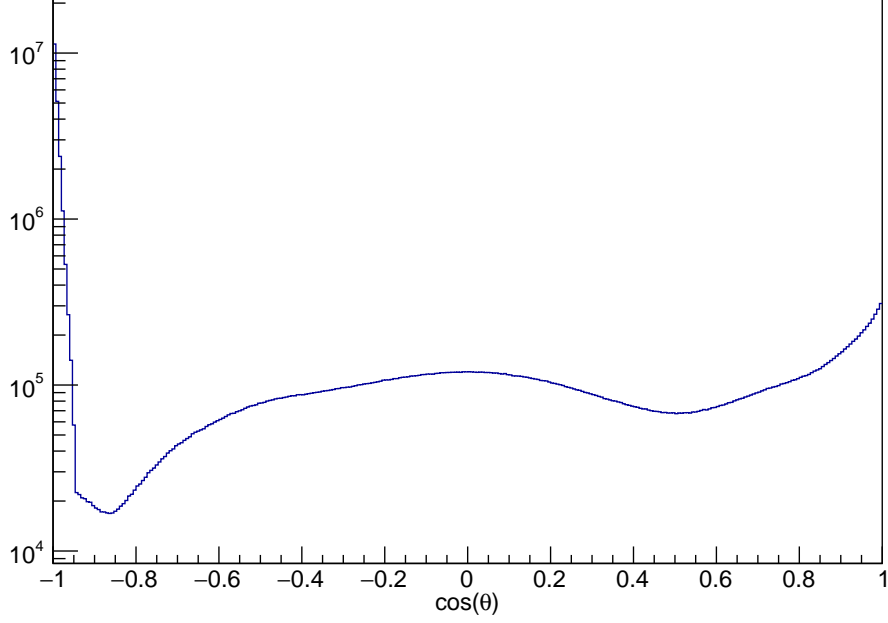


Figure 3.2: A histogram of all the mutual angles between all particles.

3.4 Momentum cut

The second cut we perform on the data is a *total* momentum cut. On fig. 3.3 the total momentum for the two identified α -particles are shown. A prominent peak lies around 13.000 keV/c, and ends around 40.000 keV/c. We impose a cut of maximum 40 MeV/c, as this will include the large amount of pairs lying in the peak, which must be α - α pairs. A α -particle with energy 1500 keV will have a momentum of 105 MeV/c, and a free electron of 3000 keV will have a momentum of 1.7 MeV/c. The majority of particles lies around these energies, and no matter where the β -particle will hit, the total momentum is still much larger than the 40 MeV/c cutoff.

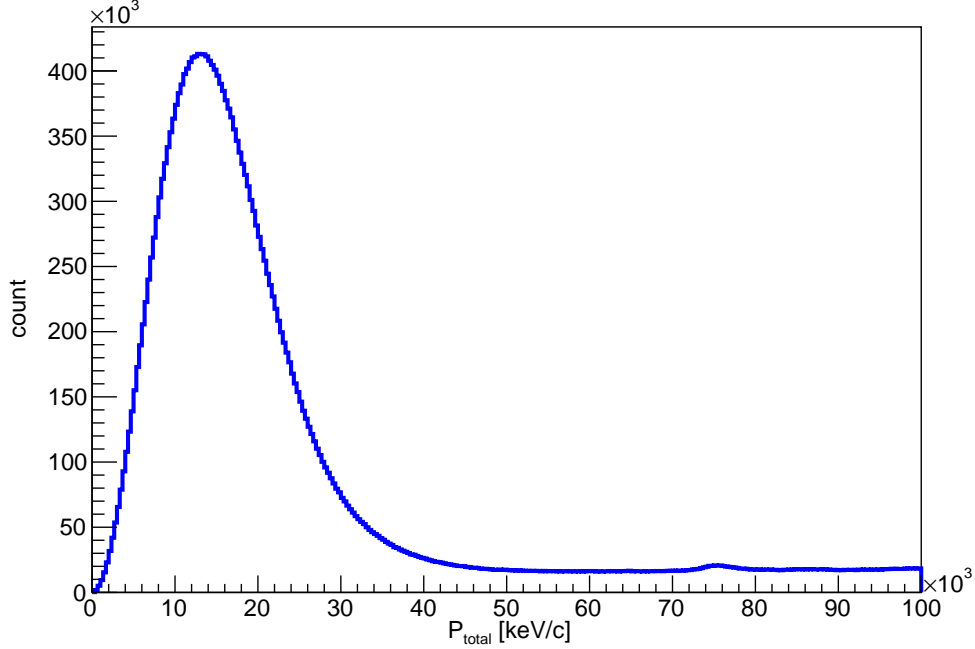


Figure 3.3: The total momentum of the two α -particles.

3.5 Multiplicity cut

The last cut that we want to impose on the data, is a multiplicity cut. This cut is just to ensure that we have the amount of particles that we expect. Therefore a hard criteria is that there must be at least two distinctly identified α -particles.

With regards to the β -particles, we are more loose. Here we say that there must at least be one, but more can occur. This is quite rare, but the we still take that event into account, as the β -particles should have an isotropic distribution, and therefore should not in any case be affected by the other α -particles. On fig. 3.4 we see the multiplicity of β -particles, and in most of the events, we have not detected any β -particles, and when we do, there is a even fewer events with more than one beta. So most of the time, we are in the expected case with two α -particle and one β -particle. add that beta

spreads around in the setup

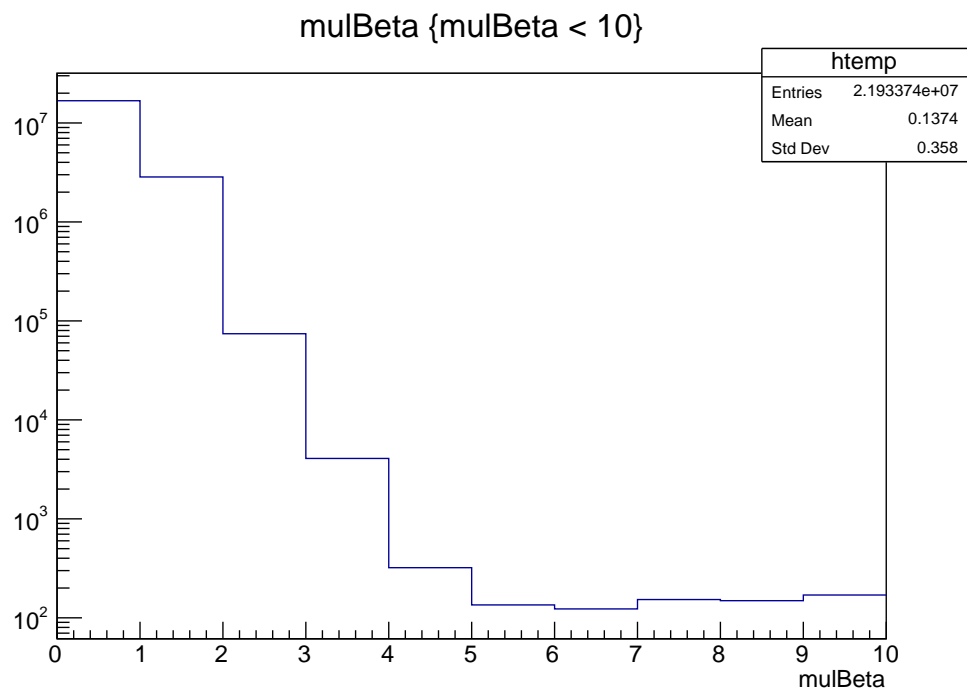


Figure 3.4: The multiplicity of the β -particles.

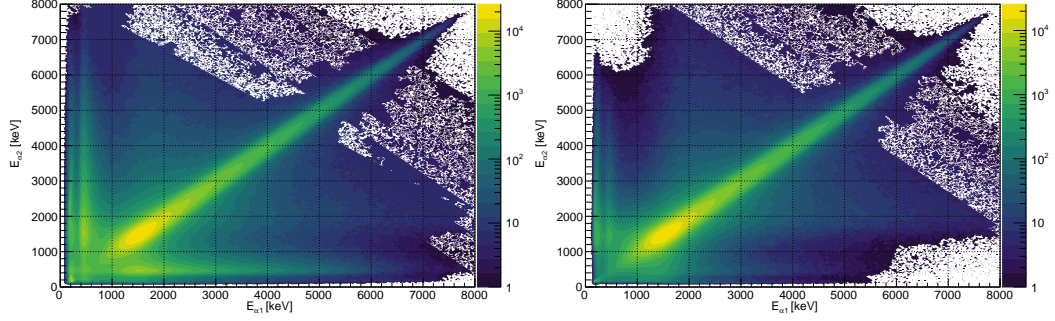
4 Analysis

4.1 The effects of the cuts

How does the cuts imposed in the previous chapter affect the data then? First we need to look at how the data looks, without any cuts. On fig. 4.1a the energy of the first α -particle ($E_{\alpha 1}$) is plotted against the energy of the second α -particle ($E_{\alpha 2}$). This gives us a nice view of what is considered α -particle pairs. There is a prominent line going diagonally through the graph, where both particles have around the same energy. This line is expected, as the α -particles will have close to equal energy, when decaying from ${}^8\text{Be}$.

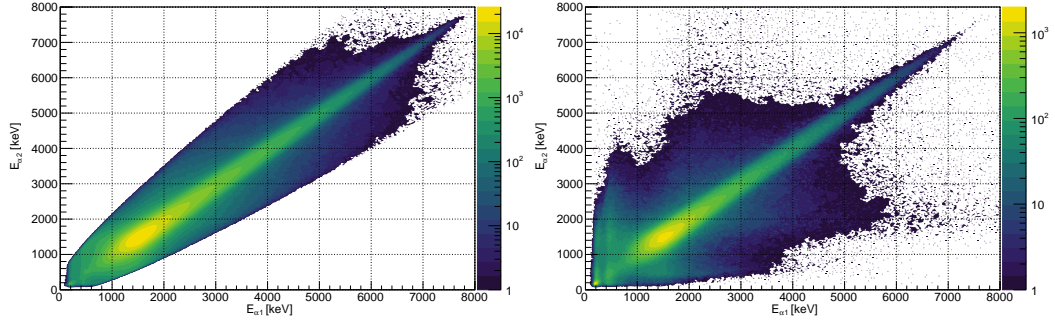
This means that there is a lot of particle pairs that have been identified as α - α , but properly was α -noise, noise-noise, α - β or β - β pairs.

The lines occurring from $E_{\alpha 2} \approx 400 \text{ keV}$ are a clear example of a α - β pair. In this line, $\alpha 1$ has been identified correctly as a α -particle, which will have energies ranging from 500-6000 keV, whereas the the other particle has a more constant energy, corresponding to the energy a β -particle can deposit in a detector. So by doing no cuts at all, we are left with a lot of cases where we have no real control over what particle type we are dealing with.



(a) No cuts on the data

(b) An angular cut. The angle between the two particles must be greater than 160° .



(c) A momentum cut. The total momentum of the particles must be less than $40 \text{ MeV}/c$

(d) A β -multiplicity cut. There must exist at least one β -particle and two α -particles in the event.

Figure 4.1: A collection of the different effects the cuts impose on the energy of the α -particles. On all the above figures, the energy of the first α -particle ($E_{\alpha 1}$) is plotted against the energy of the second α -particle ($E_{\alpha 2}$). The intensity scale is in logarithmic, to get a better view of all the different particle configurations.

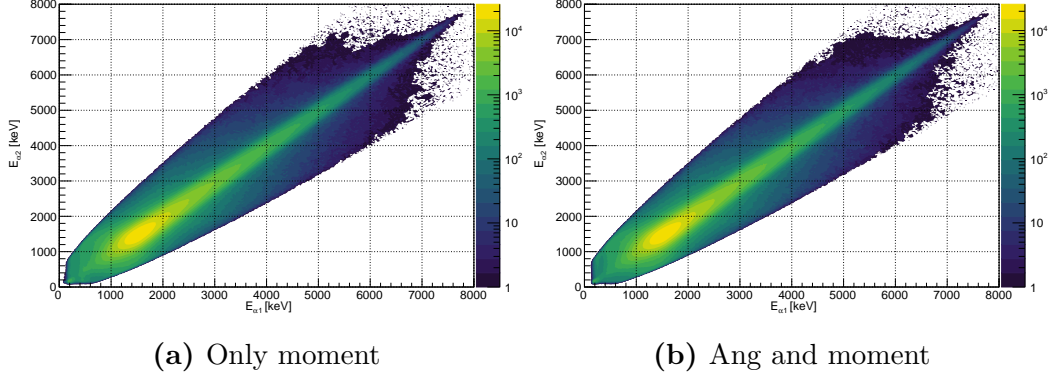


Figure 4.2: A comparison of the momentum cut with and without the angular cut.

4.1.1 The effect of the angular cut

By imposing the angular cut, we get the first real reduction in data. If the angle between the two α -particles are less than $\cos(\theta) = -0.95 \approx 160^\circ$, we sort away a good part of the β - α pairs, as seen on fig. 4.1b. But there are still a good portion of wrong pairs left, and we move on to impose a cut on the momentum of the particles.

4.1.2 The effect of the momentum cut

Again the aim is to sort the data, so that we can identify the particles. On fig. 4.1c the total momentum of the two particles has been limited to a maximum of 40 MeV/c. This cut sorts away all of the vertical and horizontal lines from a β - α pair. With this drastic cut, it looks like there is no use for the angular cut, which might be true. On figure 4.2 we can see the comparison of the effect of the momentum cut, with and without an angular cut. There does not seem to be a very large difference. Since momentum already takes the direction of the particles into account, as well as their energies, the angular cut will seem a bit redundant. However, we keep the angular cut on the data, as it will not take away any "good" measurements, but only some noise that slips through the multiplicity cut. Looking at fig. 4.4, we see the blue line as the momentum cut and the magenta line as the momentum and angular cut.

The two histograms lie very close to each other, except in the low energy ranger. Here we see a slight reduction in the magenta line, indicating that the pure angular cut will sort some β -particles from the data. It is therefore a justified cut to still impose on the data.

4.1.3 The effect of the multiplicity cut

The multiplicity of the β -particles should not interfere so much with the α -particles, but looking at fig. 4.1d, we see a drastic change in the pairs with energies far from each other. This is due to a general reduction in data. With the requirement that there must be one β -particle present in the event *and* that it must have hit either Det2 or DetD, we are left with a lot fewer measurements, which in turn gives a lower probability of noisy pairs.

4.1.4 The combined effect of all the cuts

By combining all of the cuts we are satisfied with the sorting of particles. On fig. 4.3 we see the effect of all the cuts. There is a very prominent line of particles with roughly the same energy. The line is thinner at higher energies, and widens as it goes towards lower energies. The reason for the widening, is the recoil energy from the β -decay. If the α -particles have low energy, they are more susceptible to other forces around it, and will lose a larger portion of their energy to the β -particle recoil.

On fig. 4.4 all the cuts are shown as individually, highlighting the effect that each cut provides. Here it is worth noting that not all β -particles have been successfully removed from the data. A slight peak at low energies still remain for the black line in the figure. This is also clear on fig. 4.3, where there is a high intensity at the ≈ 200 keV energy range.

So far we have only considered that the α -particles are sorted correctly. But there is still a question for whether the β -particles will be clouded by wrong identifications. On fig. 4.5 we see the energy deposited in the two detectors that are capable of measuring β -particles, and the pad behind Det2. The energy from the pad and DetD, shows one peak around 400 keV and 300 keV,

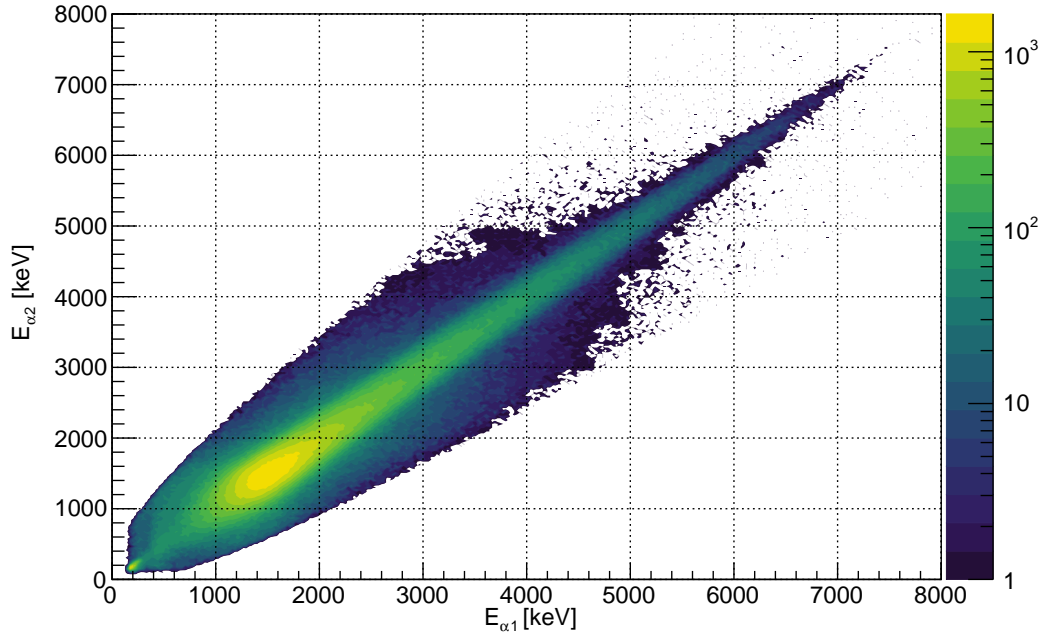


Figure 4.3: The energy of the first α -particle plotted against the energy of the second α -particle. All of the data reduction cuts are used here.

respectively. Det2 shows two peaks, one close to 400 keV, and one close to 800 keV. This is rather interesting, as we do not expect β -particles to deposit two different energies. Both detectors and the pad where 1000 μm thick, so we expect that the energy deposited would be roughly the same.

4.2 The excitation energy of ^8Be

With the α -particles sorted correctly, we can start to look at the excitation energy of ^8Be . All products of this decay will hit our detectors, and the entire energy of the decay can be measured. On fig. 4.6 the sum of both α -particles energies are shown.

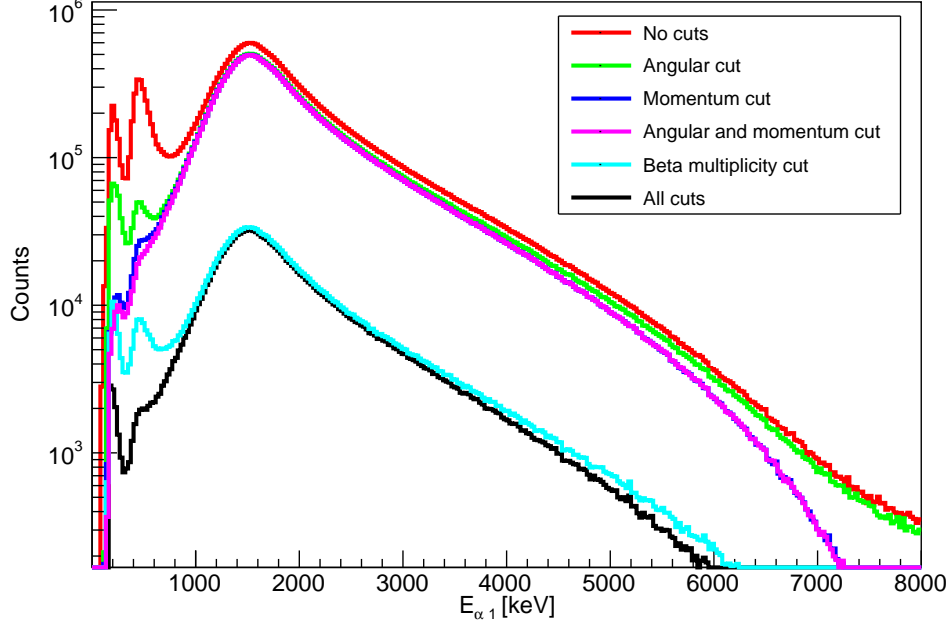


Figure 4.4: A comparison of all the cut, where the energy of the first α -particle is plotted.

4.3 Angular efficiency of the setup

Since the detectors are unable to cover the entire solid angle, there will always be some mutual angles that are more likely to be measured. If we only look at one detector, a very large number of angles are not covered, but small mutual angles such as $\theta \approx 0$, are very easy to measure, as it is just a measurement of two particles in the same pixel. This effect becomes apparent on fig. 4.7, where the angular efficiency is shown for Det2. For a single detector, there cannot be angles of $\theta = 90$ and higher, as the detector is flat. In this detector, the lowest angle found was $\cos(\theta) = 0.21 = 77^\circ$.

In this setup however, we have a cube of square detectors, whose normal vectors are all pointing in towards target at the center. This gives a much larger coverage of all mutual angles. The placement of the detectors gives that angles around $\theta \approx 90^\circ$ are also very favored. This makes sense, almost no

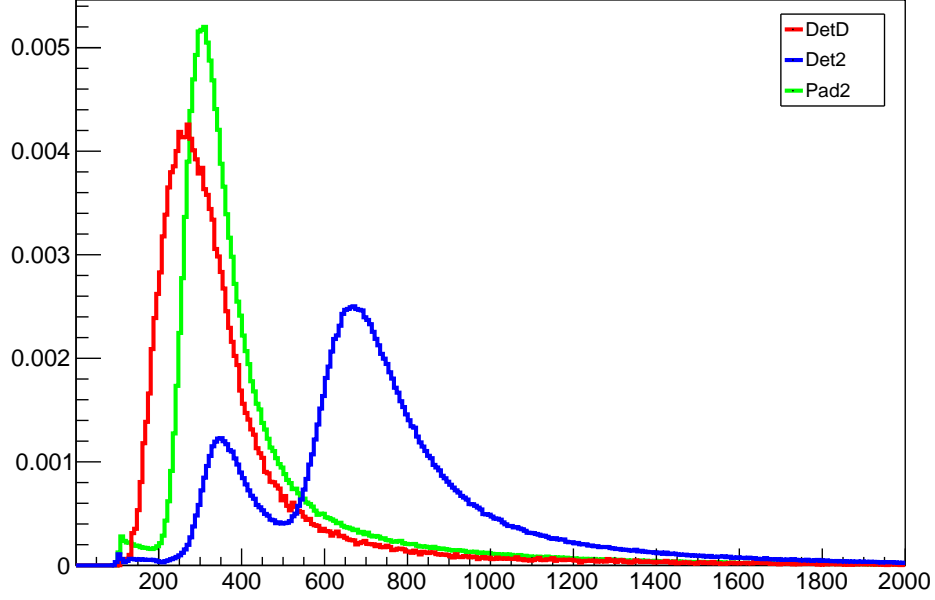


Figure 4.5: Energy deposited by β -particles in Det2 (blue), DetD (red) and Pad2 (green). PadD has been omitted, due to an error in the pad.

matter what pixel was hit, there is a corresponding pixel 90° to both sides. In the same way, will there always be a corresponding pixel $\approx 180^\circ$ from each pixels. This effect can be seen on fig. 4.8.

This histogram was created by using the spacial coordinates of the entire setup. First the positions of each pixel in each detector was found. Then two loops running over each pixel pair i, j , finds the angle between these pixels and saves it.

There is still a geometric effect that is not accounted for in the above analysis. We still need to consider that not all pixels in the detector has the same effective area. A pixel furthest out in a detector will have a effective area smaller than the area of a pixel in the center. This effect can be seen on fig. 4.9a. Here we see that there is a much higher count of particles hitting the center of the detector, and fewer hitting the edges. A white line crossing through the middle is a defect strip, which did not measure anything. Sadly,

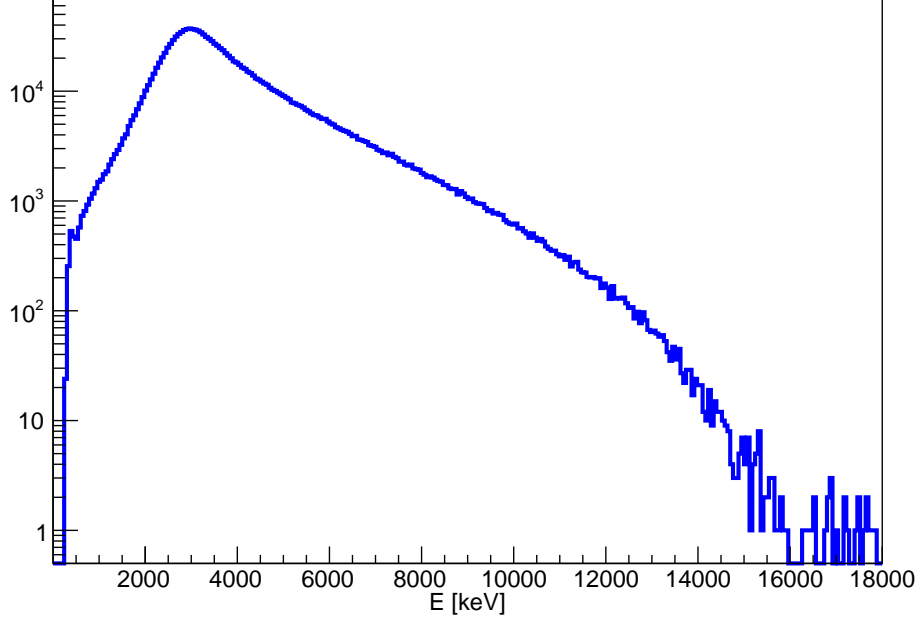


Figure 4.6: The energy spectra of both α -particles, that is the excitation energy of ^8Be .

some of the detectors had defect strips, but on a large scale it was not very noticeable.

To account for this effect, each pixel will be associated with a corresponding area-efficiency (Eff_A). This is calculated as

$$\text{Eff}_A = \frac{A \cos(\theta)}{4\pi r^2}, \quad (4.1)$$

where r is the distance to the pixel, A is the area of the pixel and θ is the angle between the hit direction and the normal vector of the detector as shown on fig. 4.10. The area of all pixel is the same for all detectors, so the constants A and 4π can be ignored when comparing the efficiency.

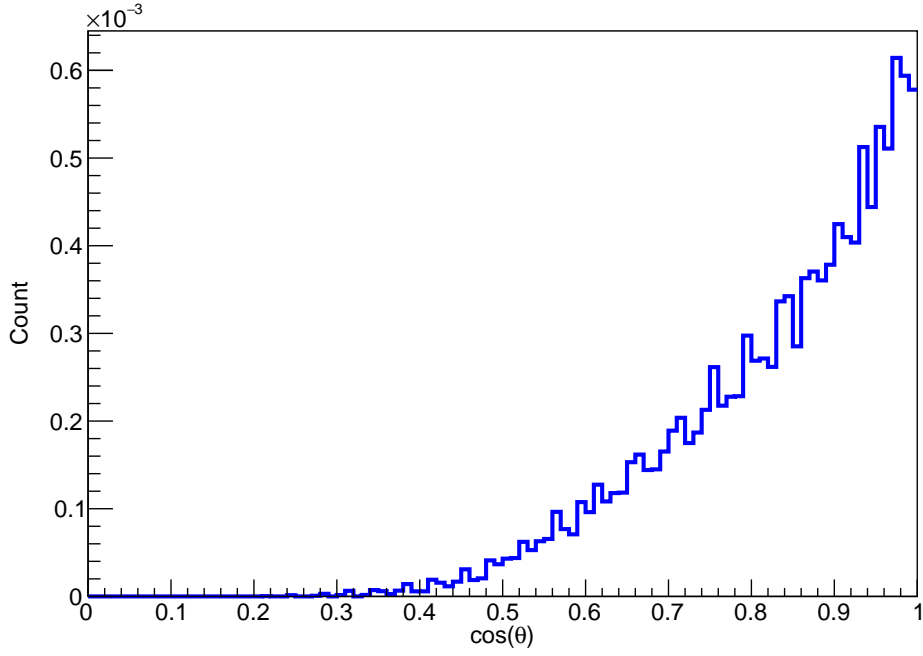


Figure 4.7: The angular efficiency of a single detector (Det2). For one flat detector, there can never be angles of 90° and higher.

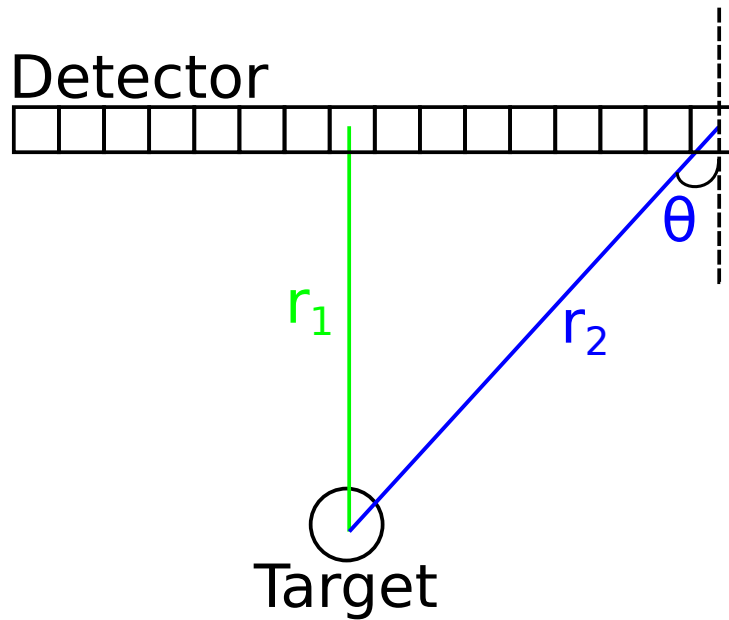


Figure 4.10: A illustration of two hits in different pixels. The blue hit will see a smaller effective area of the pixel by a factor determined by eq. (4.1).

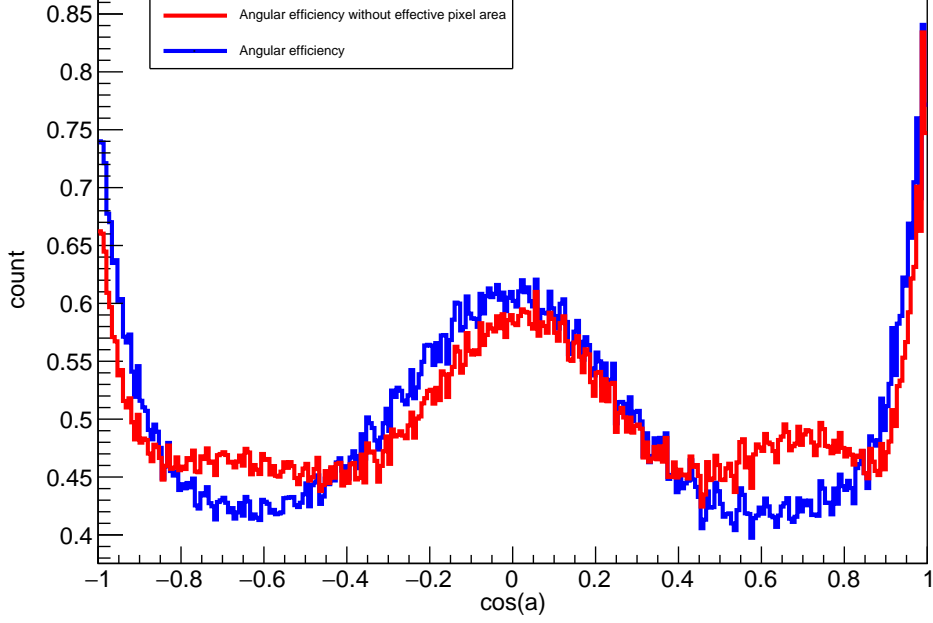
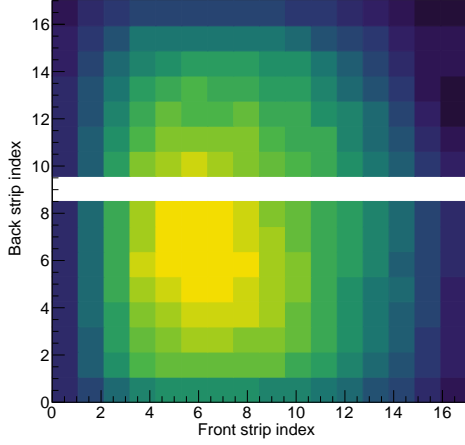


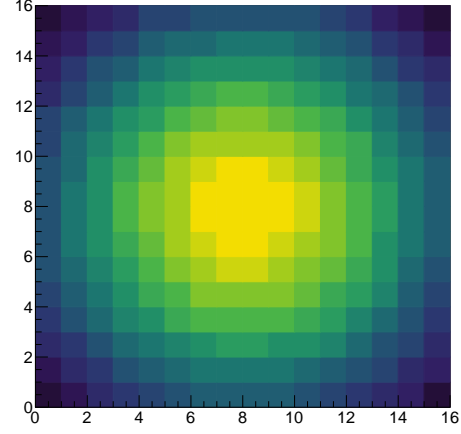
Figure 4.8: Two normalized histograms of the angular efficiency of the entire setup. The red histogram does not account for the effective area of a pixel. The blue is the true angular efficiency.

On fig. 4.11 two histograms can be seen. The red line represents the angular efficiency of the setup, without accounting for the relative area of the pixels, while the blue line is a weighted histogram for the same angles, with each pixels relative area accounted for.

The form of the two histograms are quite similar around 1, 0 and -1 but in between there is a rather prominent difference. Therefore it is important that the effective area of the pixel is accounted for, when we in section 4.4 will look at the angular correlations of the β -particle in the setup.



(a) A plot over the number of hits in each strip for Det2. The white line in the middle is a defect strip, that did not measure anything.



(b) A theoretical intensity Det2.

4.4 Angular correlations of α -particles and β -particles

From what we know in [ref til beta = isotrop](#) the β -particles must have an isotropic distribution. Since we only have two detectors in the setup that are capable of measuring β -particles, we cannot measure the angle from one particle to something constant, i.e. the beam. Therefore we measure the angle between both α -particles and the β -particles. This is done by first finding the angle between the first α -particle α_1 , and create a histogram of this. Then the angle between the second α -particle α_2 is measured, and a histogram is created. The two histograms are then added, to get the full picture of the mutual angles of the particles. This can be seen on [fig. 4.11](#) as the green line.

The blue line in this figure is the angular efficiency for the specific case, where the α -particles can hit in any given detector, but the β -particles can only hit in the two specific detectors Det2 and DetD. The two histograms has both been normalized, for a better comparison. By dividing the two histograms

with each other, we get a better comparison. If they were to be close to equal, we would see a flat curve. But what we see on fig. 4.12 is not very flat. There are small fluctuations in the line, which stems from the inaccuracy of calculated angular efficiency. But the main shape of the curve is at most time not around $y = 1$.

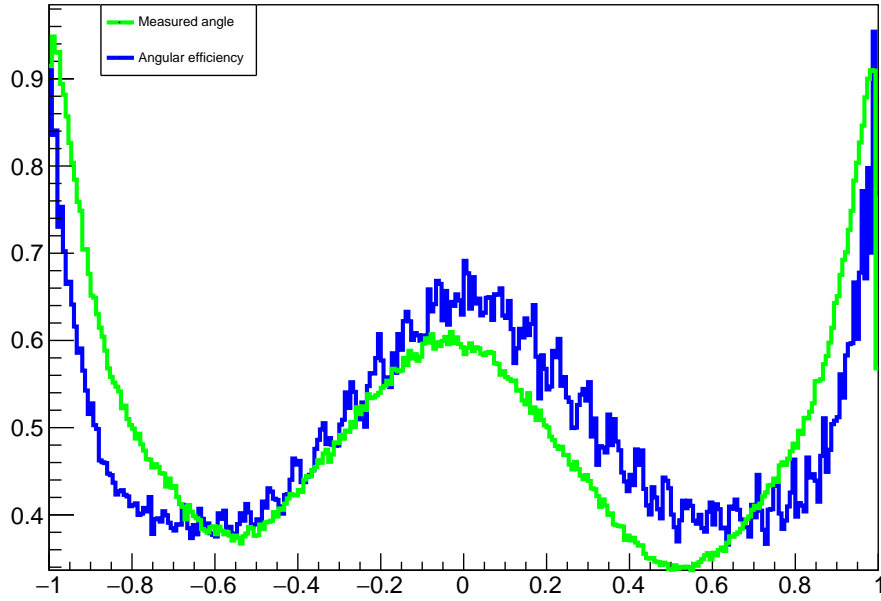


Figure 4.11: Some figure of the efficiency of the setup without efficiency of each pixel.

There are two different explanations as to why this might be. The first explanation is that the beam did not hit the target in the center. The calculated efficiency assumes that the beam hits precisely in the middle, but in any setup, there can be a few millimeters of errors.

By finding the angular efficiency of the setup, with different values for the center and comparing this to the measured angles, we have found a slight correction for the center of the beam. This can be seen on fig. 4.13a, where the beam has been moved to the coordinates $(-3, -3, 0)$, as opposed to the previous of $(0, 0, 0)$. The division for the two histograms on fig. 4.13b shows a more stable line from $\cos(-0.4)$ to $\cos(0.4)$, but the edges are still not very

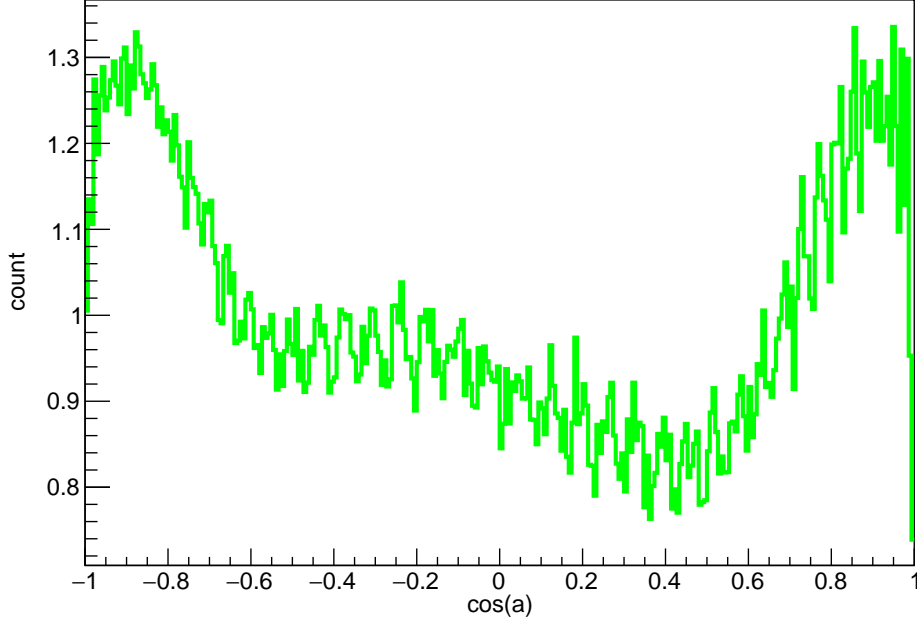
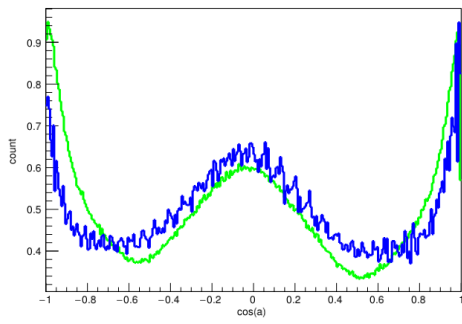


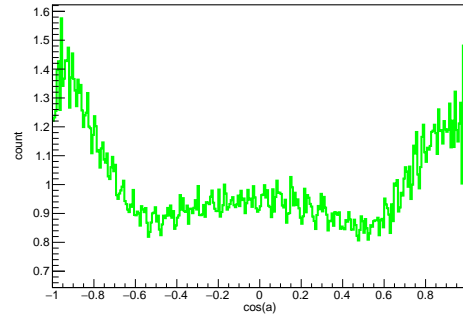
Figure 4.12: Data divided by the angular efficiency.

alike. Looking at $\cos(1)$, we see a rapid fall, which indicates that we have measured a lot fewer parallel β and α -particles than the setup is designed to handle. This can be due to the fact that some of the strips were defect. The calculated angular efficiency does not know which strips were defect, and will therefore have a lot higher efficiency for parallel particles. The defect strips will therefore also play a role in the grand scheme, and is a possible explanation as to why there is a difference in the calculated and the measured data.

Another effect that will sway the data, is the target holder. This device will provide a shadow over the top and bottom detector, and since one of the β -detectors are the bottom one, it will skew the data in an unforeseeable way.



(a) The angular efficiency and the data, with a correction for the center of the beam.



(b) Measured β - α -particle angular distribution divided by the calculated angular efficiency of the setup, with a correction for position of the beam.

5 Conclusion

Bibliography