



Natural Language Processing CSE 517 / CSE 447

Lecture 5: Attention & Transformers

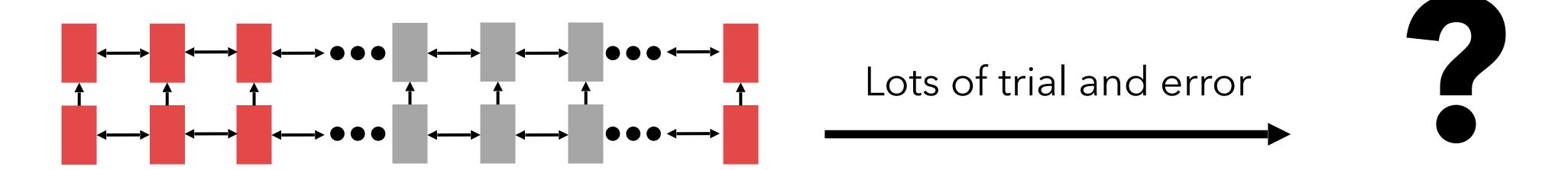
Lecturer: Yejin Choi

Slides by: Liwei Jiang

Slides adapted from John Hewitt, Hung-yi Lee

Recall RNNs...

- Circa 2016, the de facto strategy in NLP is to **encode** sentences with a bidirectional LSTM.
 - E.g., the source sentence in a translation
- Today, we try to find the better **building blocks** than recurrence that can solve the same problems, but are more **efficient**, more **versatile**, and more **flexible**.

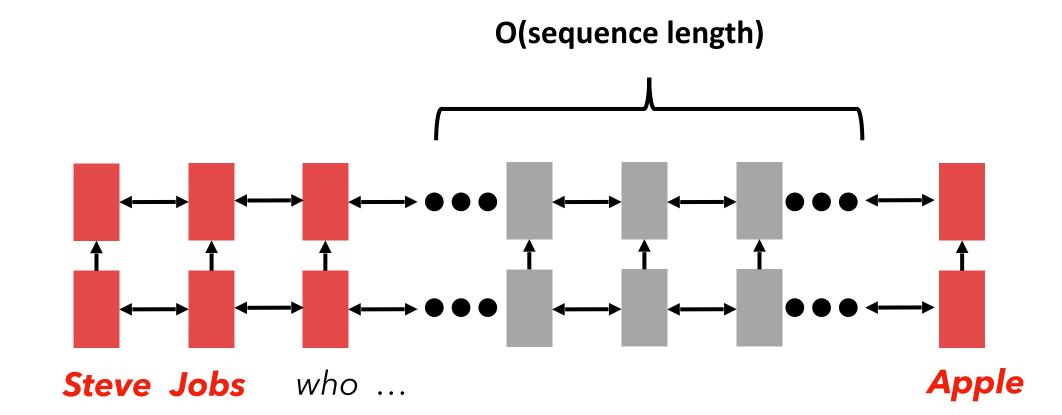


2014 to 2017-ish: Recurrence

2021 onwards

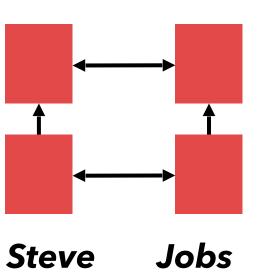
Drawbacks of RNNs: Linear Interaction Distance

- RNNs are unrolled left-to-right.
 - **Linear locality** is a useful heuristic: nearby words often affect each other's meaning!
- However, there's the vanishing gradient problem for long sequences.
 - The gradients that are used to update the network become extremely small or "vanish" as they are backpropagated from the output layers to the earlier layers.



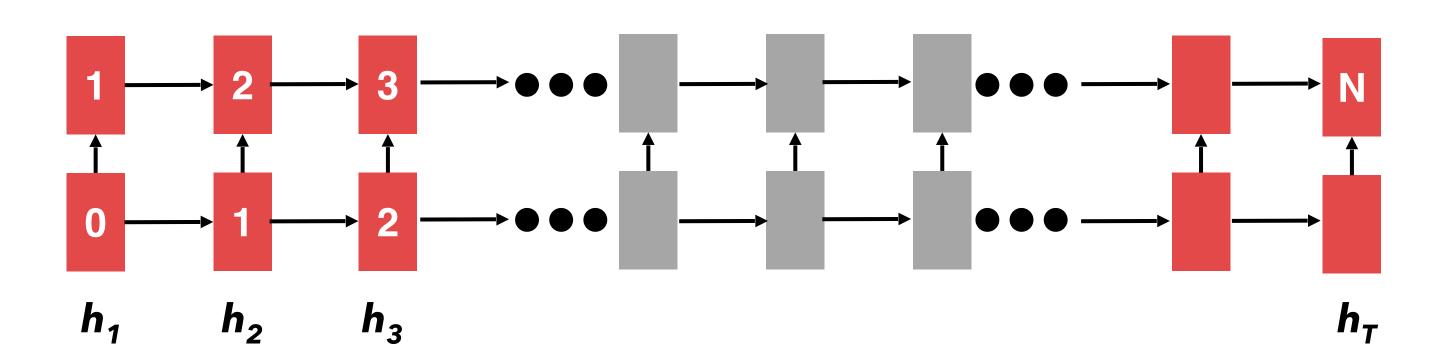


Failing to capture long-term dependences.



Drawbacks of RNNs: Lack of Parallelizability

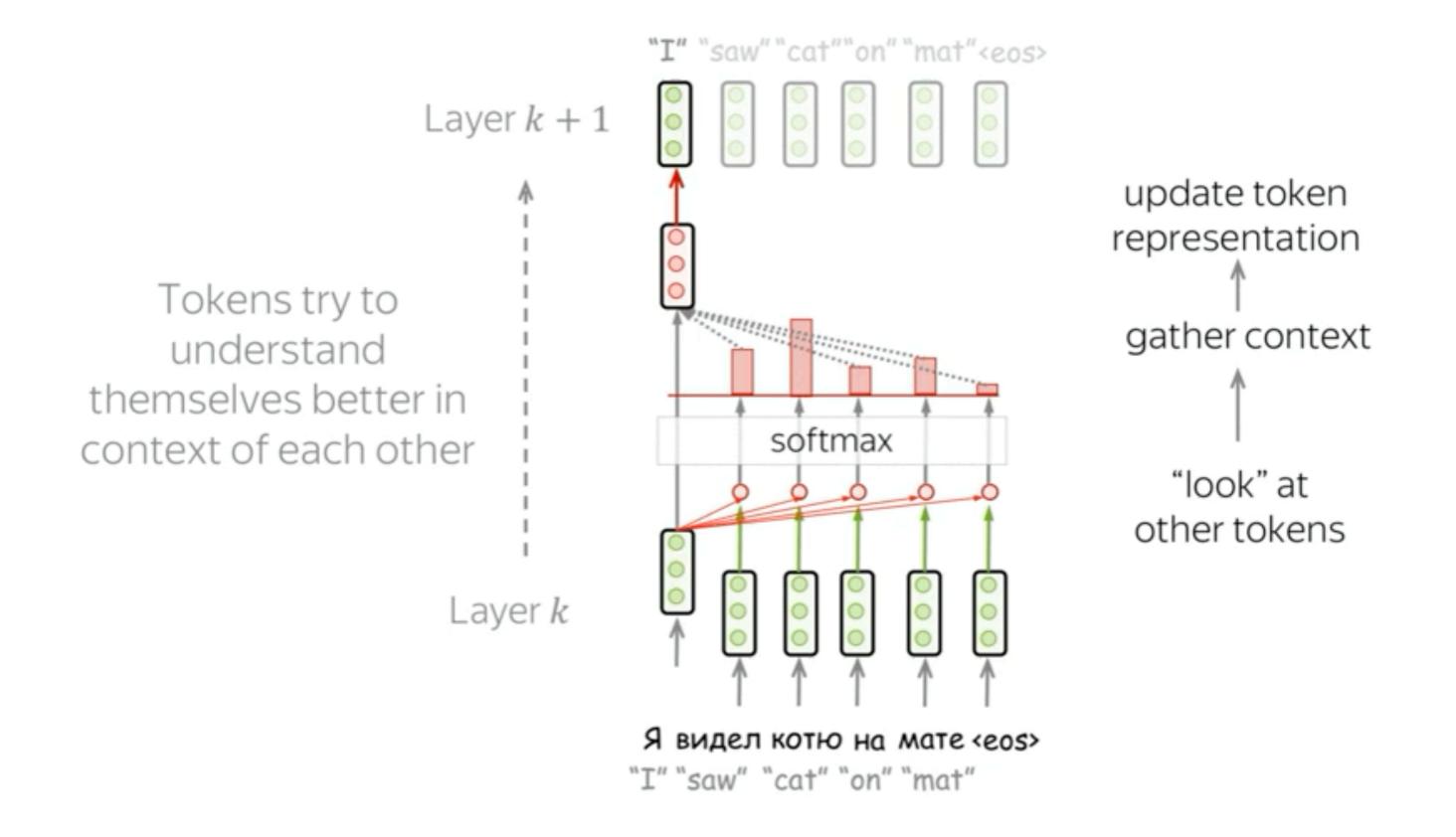
- Forward and backward passes have O(sequence length) unparallelizable operations
 - GPUs can perform many independent computations (like addition) at once!
 - But future RNN hidden states can't be computed in full before past RNN hidden states have been computed.
 - Training and inference are slow; inhibits on very large datasets!



Numbers indicate min # of steps before a state can be computed

The New De Facto Method: Attention

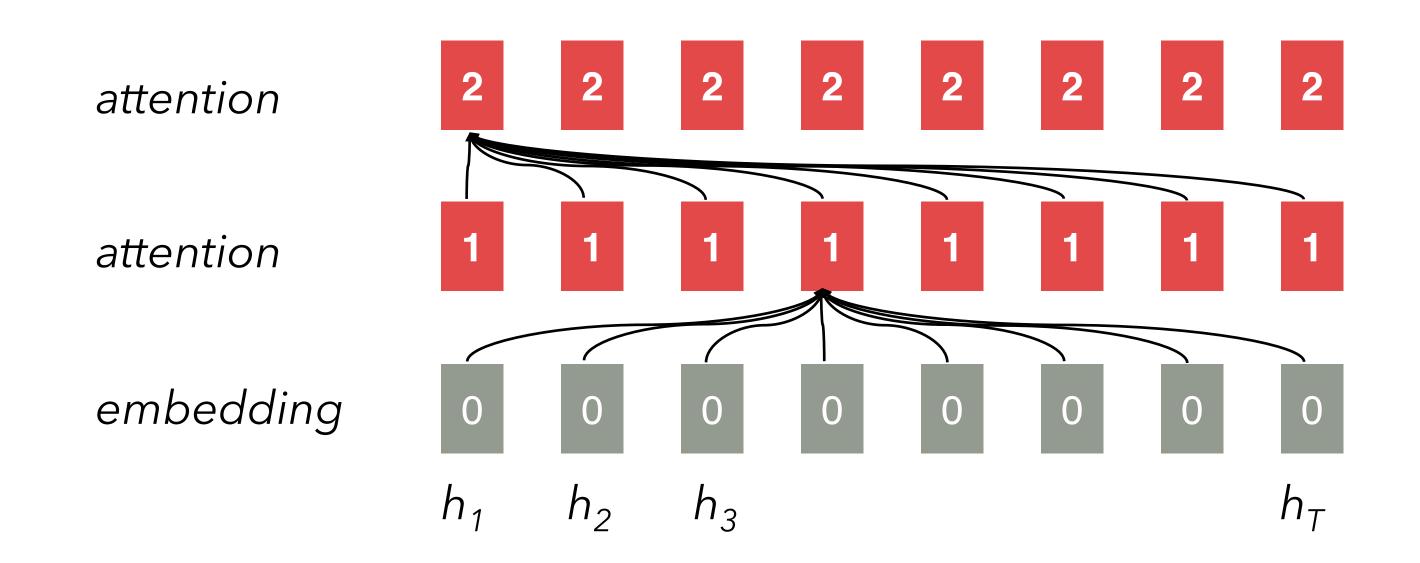
Instead of deciding the next token solely based on the previously seen tokens, each token will "look at" all input tokens at the same to decide which ones are most important to decide the next token.



In practice, the actions of all tokens are done in parallel!

Building the Intuition of Attention

- **Attention** treats each token's representation as a **query** to access and incorporate information from **a set of values**.
 - Today we look at attention within a single sequence.
- Number of unparallelizable operations does NOT increase with sequence length.
- Maximum interaction distance: O(1), since all tokens interact at every layer!

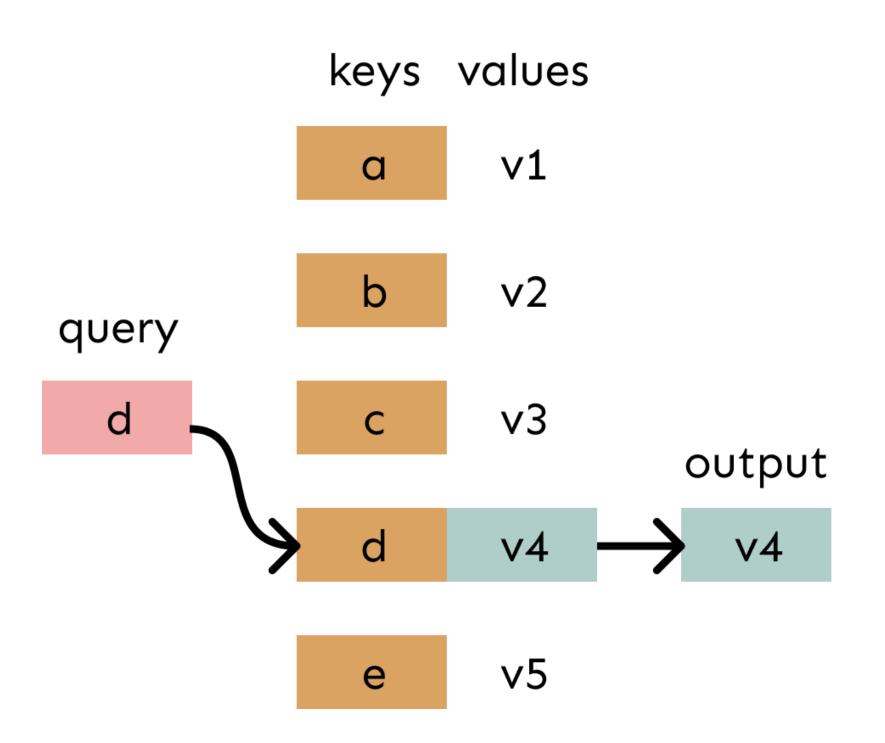


All tokens attend to all tokens in previous layer; most arrows here are omitted

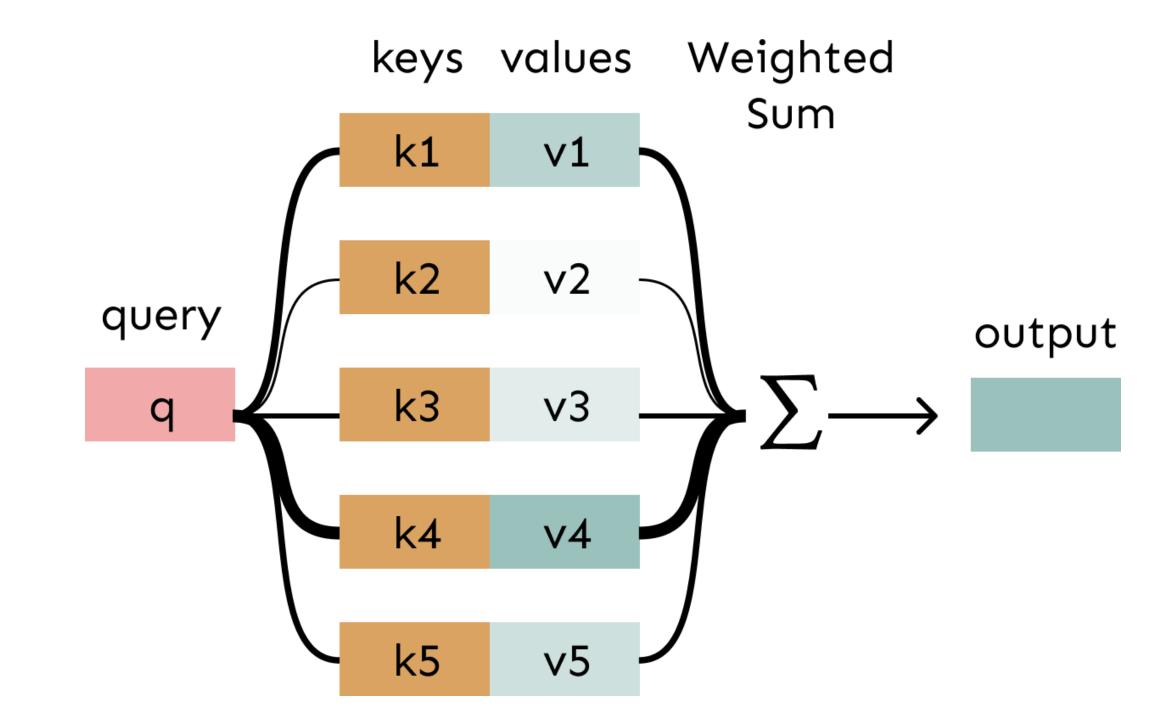
Attention as a soft, averaging lookup table

We can think of attention as performing fuzzy lookup in a key-value store.

In a **lookup table**, we have a table of **keys** that map to **values**. The **query** matches one of the keys, returning its value.



In **attention**, the **query** matches all **keys** *softly*, to a weight between 0 and 1. The keys' **values** are multiplied by the weights and summed.



Self-Attention: Basic Concepts

[Lena Viota Blog]

Each vector receives information

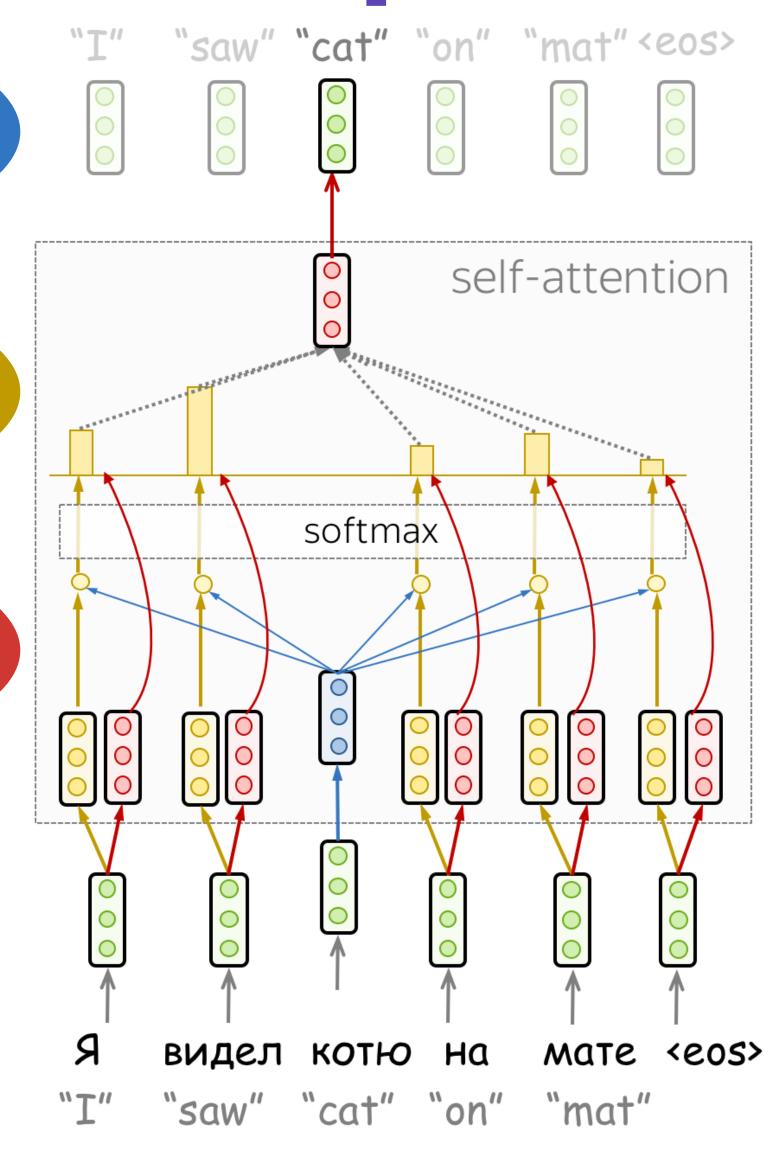


"Hey there, do you have key: saying that it has some information

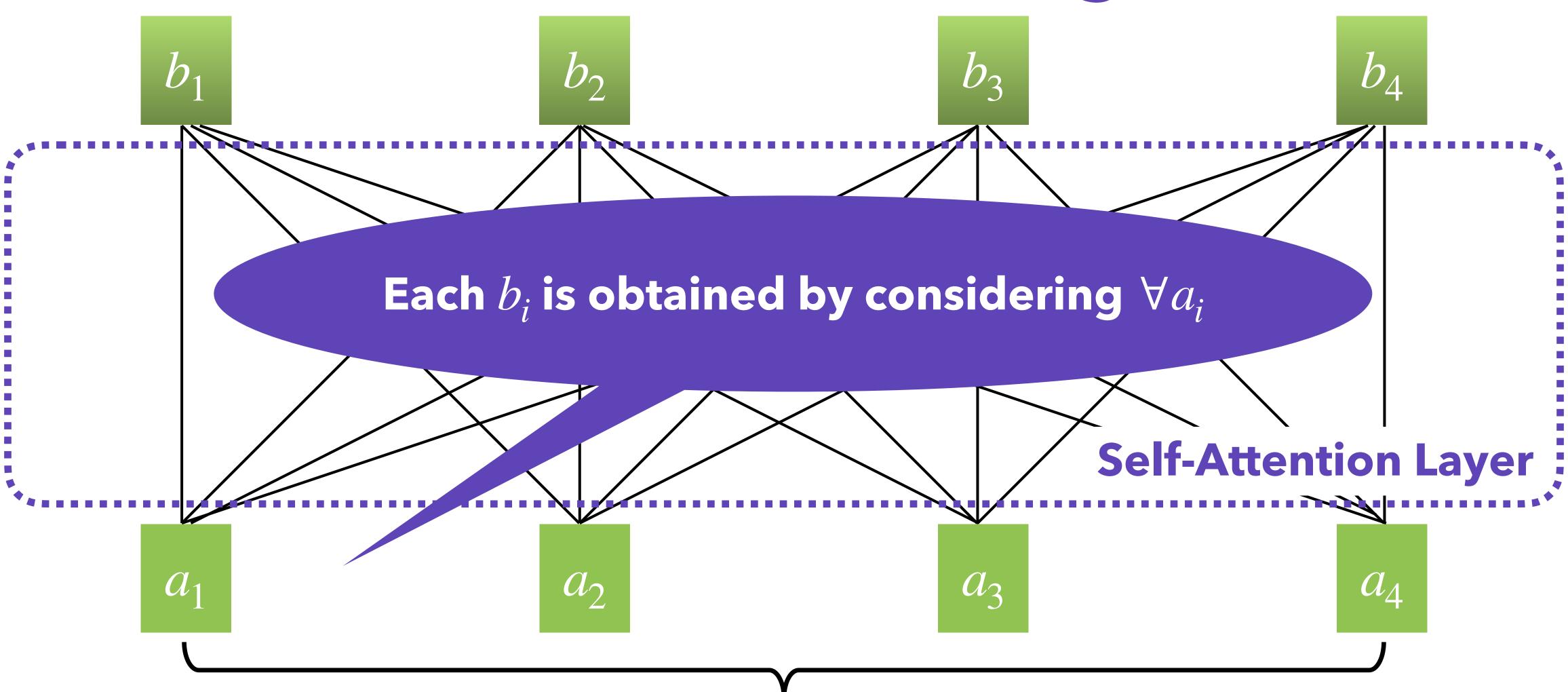
"Hi, I have this information Value: giving the information

$$\begin{bmatrix} W_V \end{bmatrix} \times \begin{bmatrix} \circ & \circ & \text{Value} \\ \circ & \circ & \text{attention output} \end{bmatrix}$$

"Here's the information I have!"



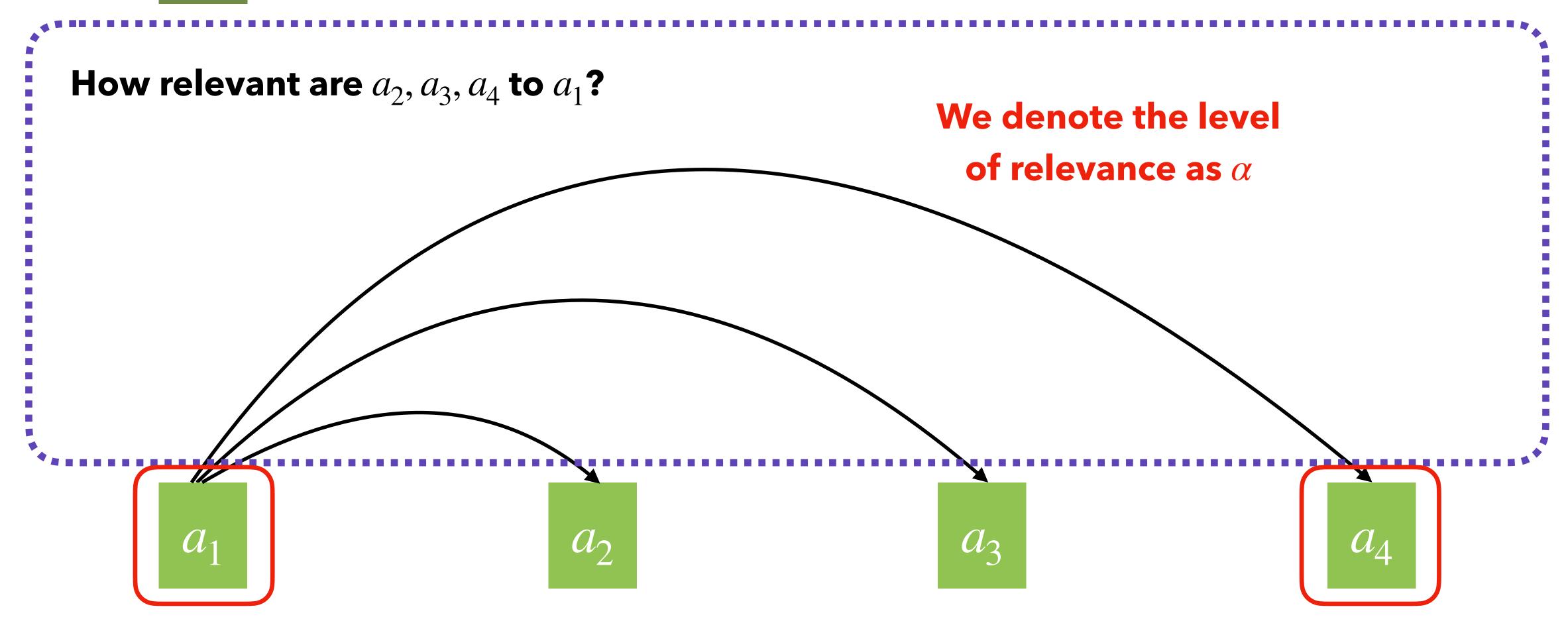
Self-Attention: Walk-through



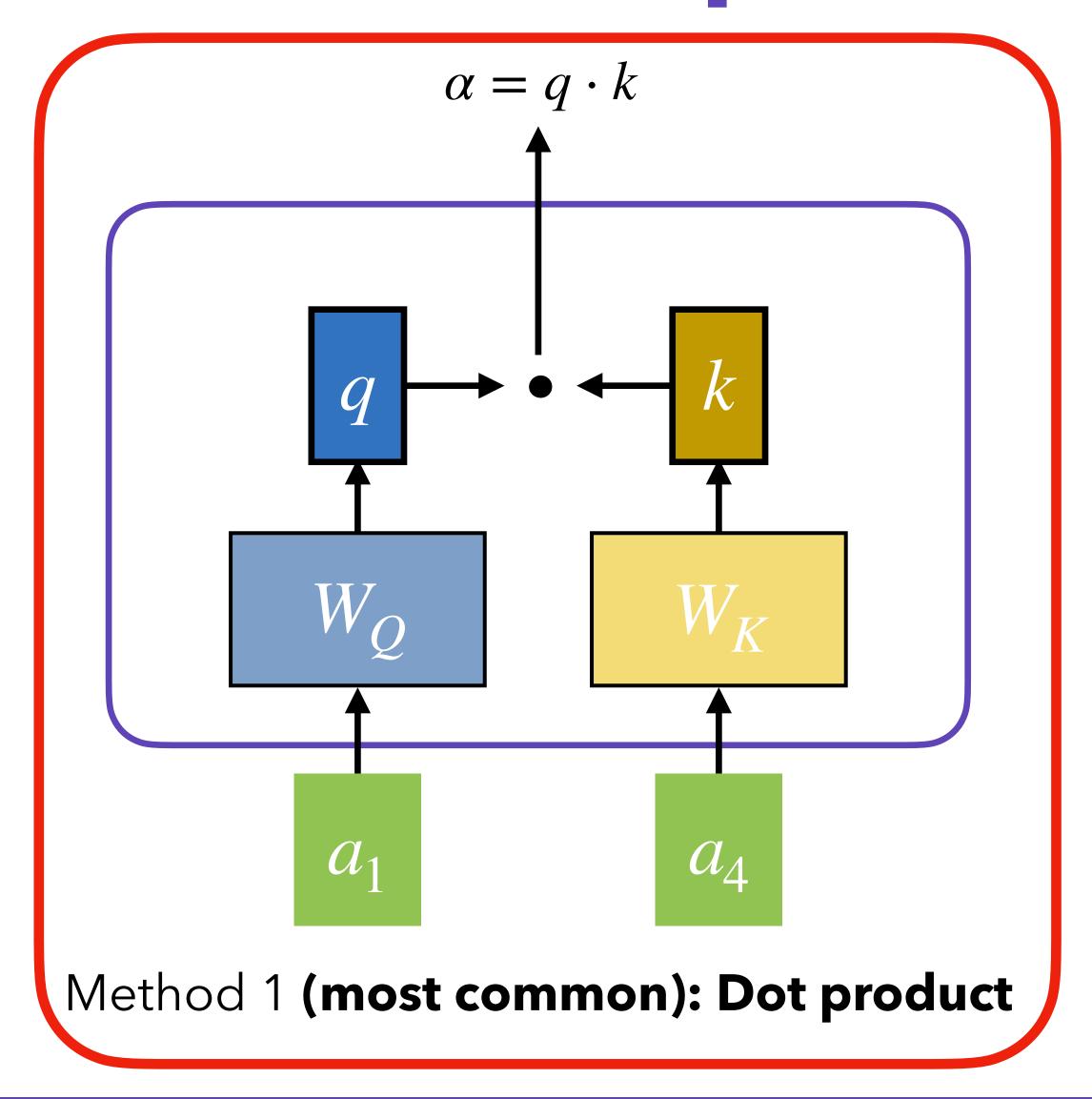
Can be either input or a hidden layer

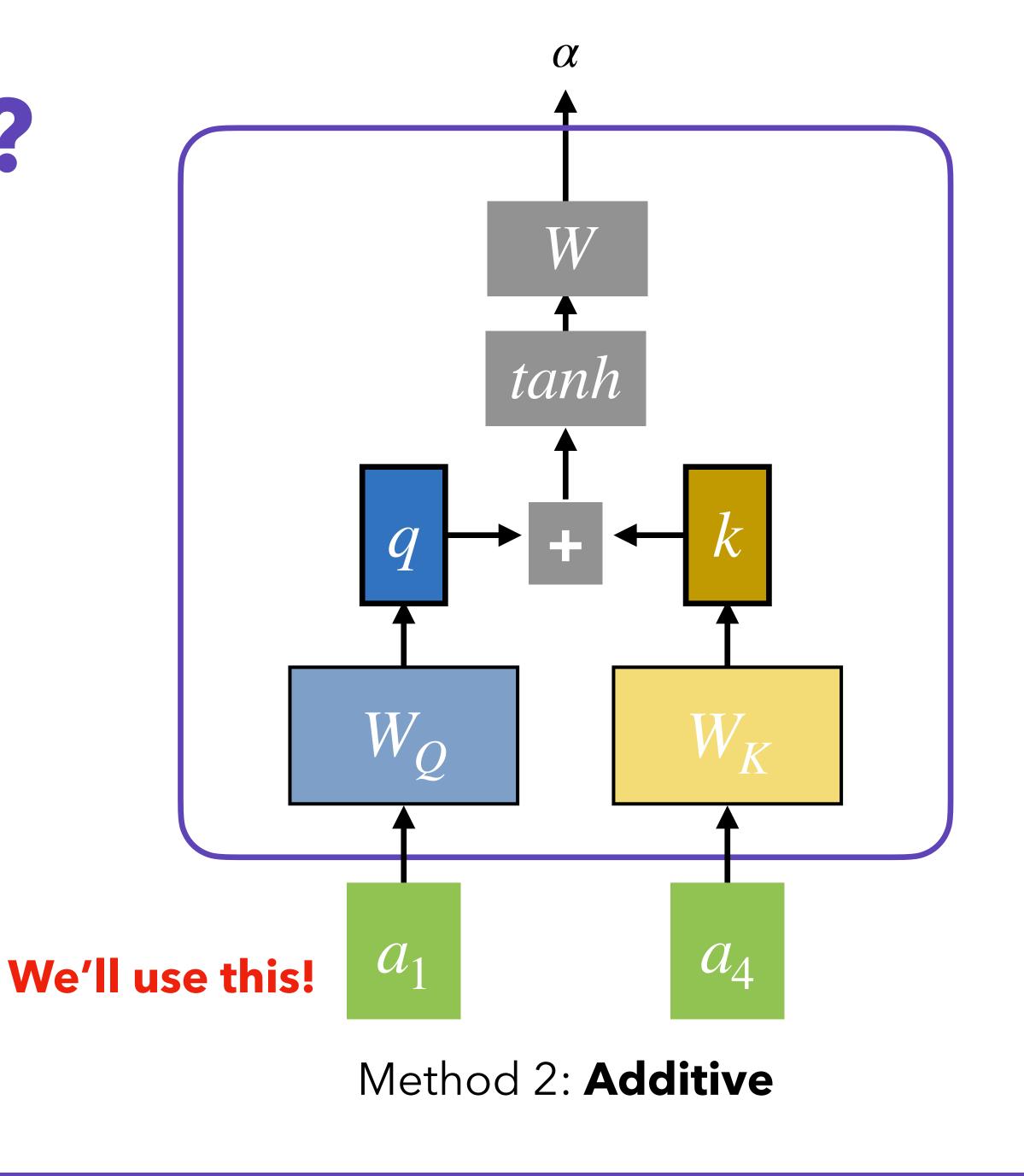
Self-Attention: Walk-through

 b_1



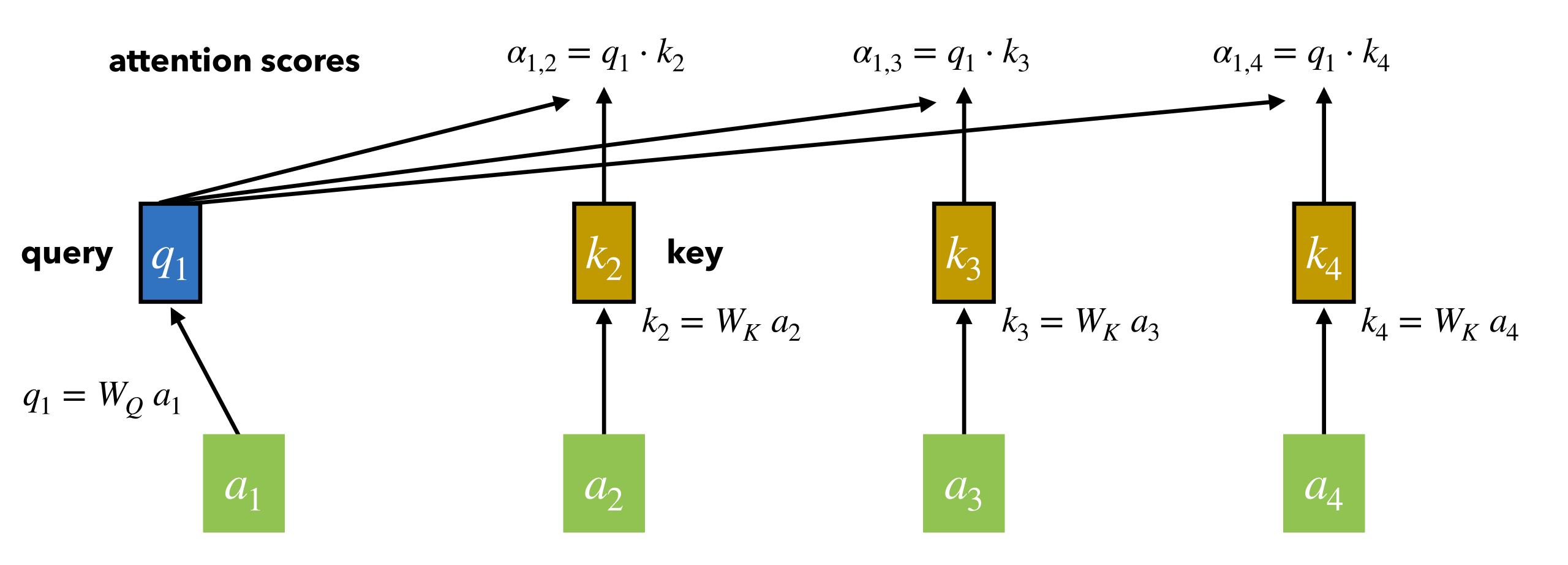
How to compute α ?

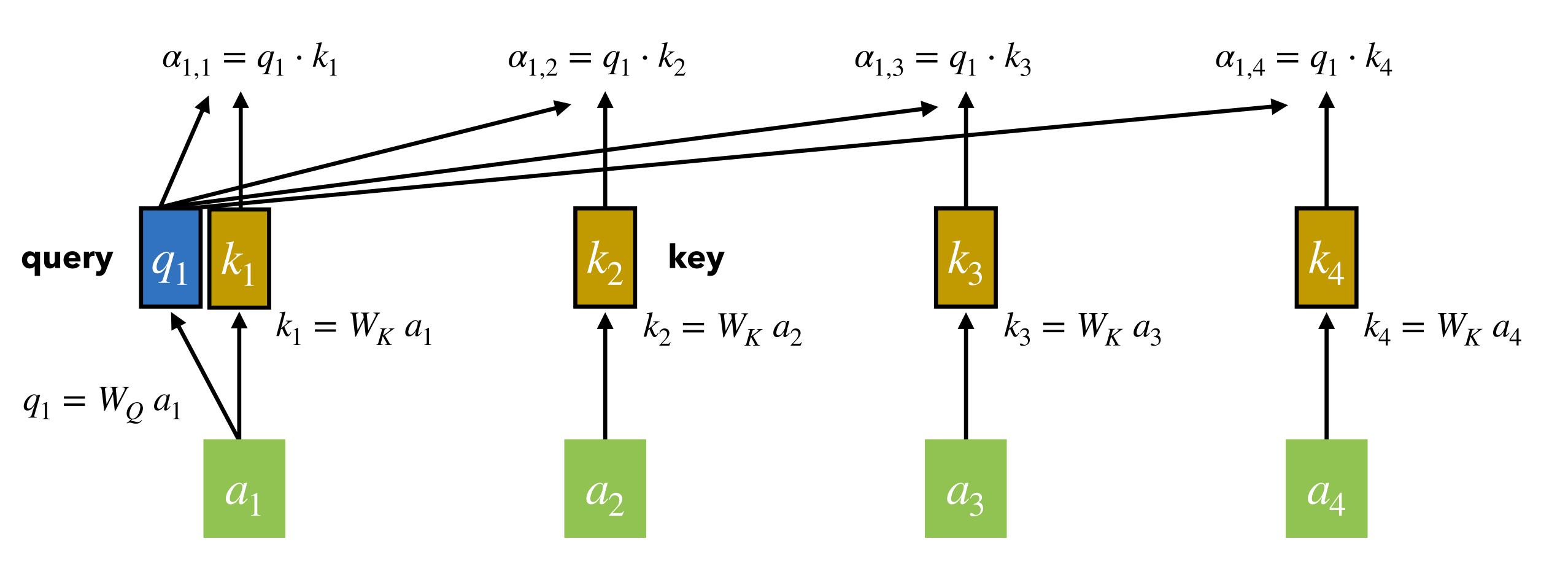


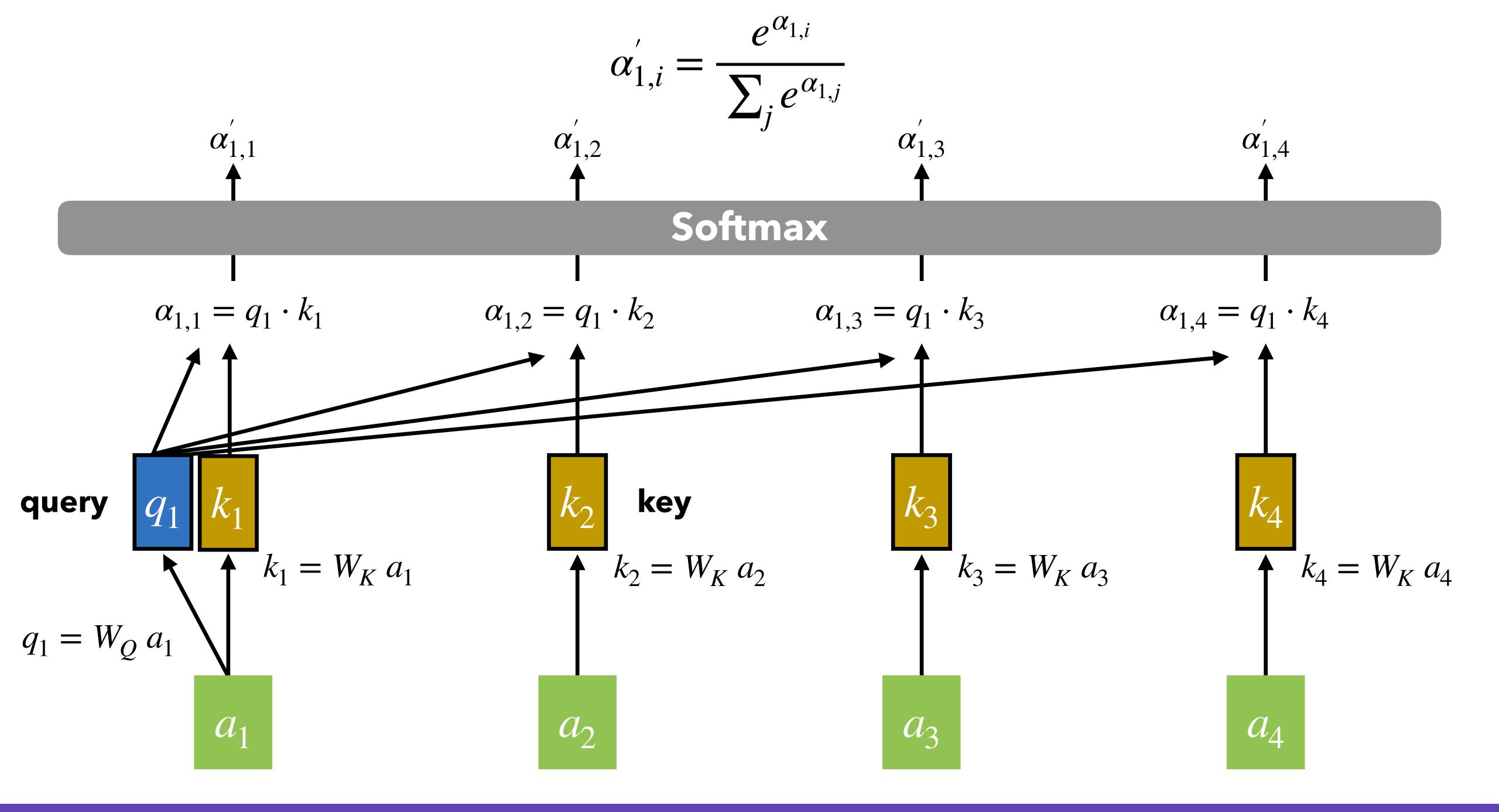


11

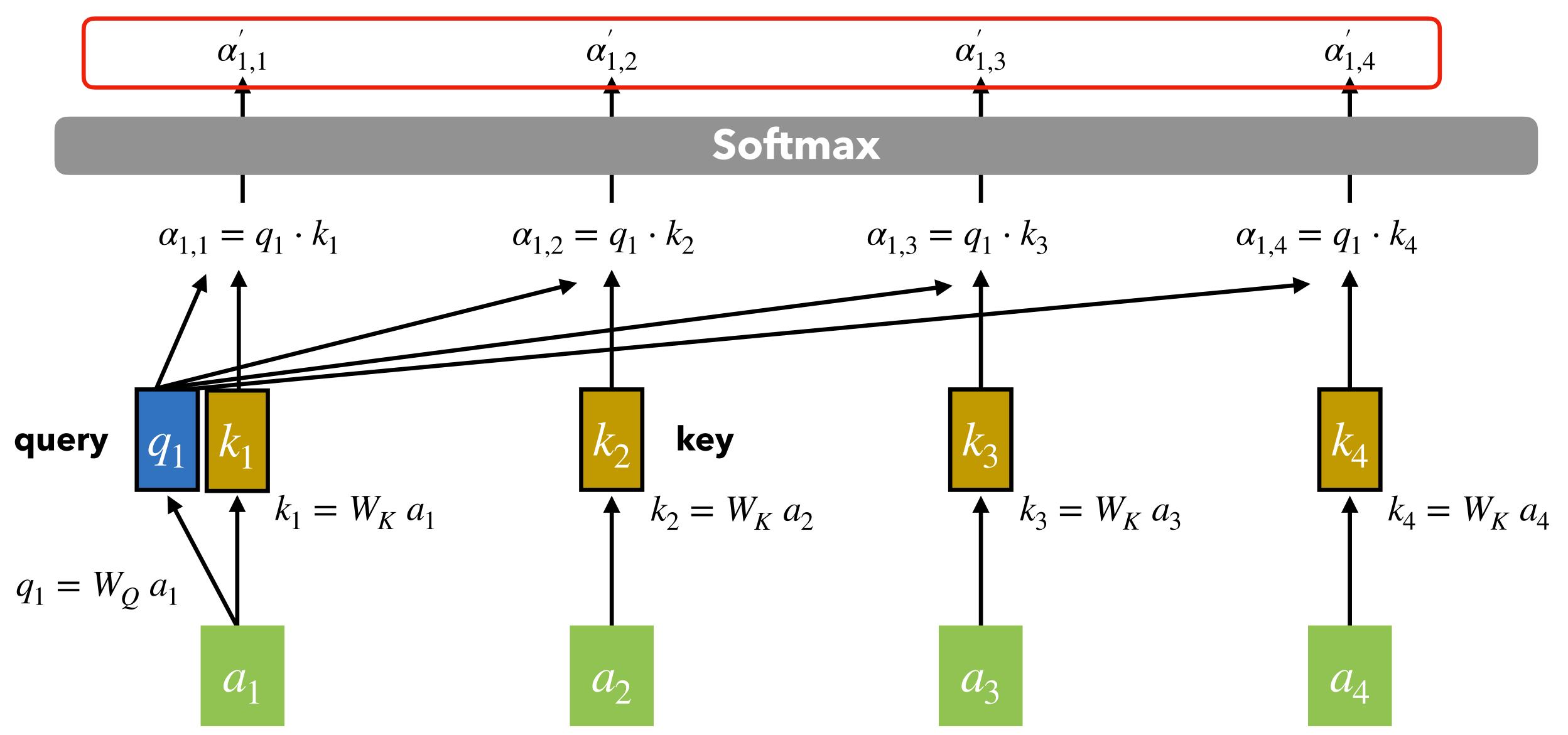
Self-Attention: Walk-through



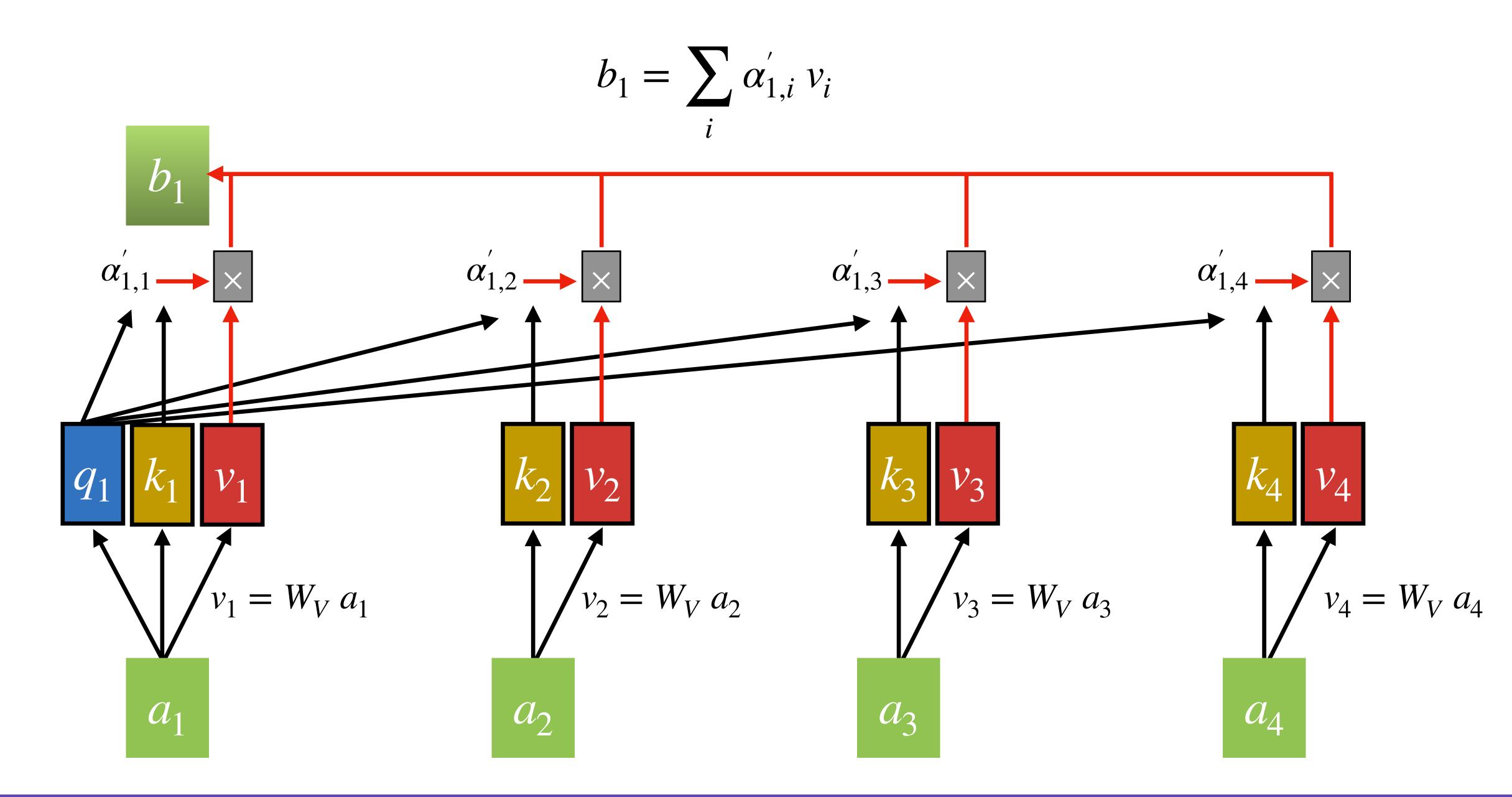




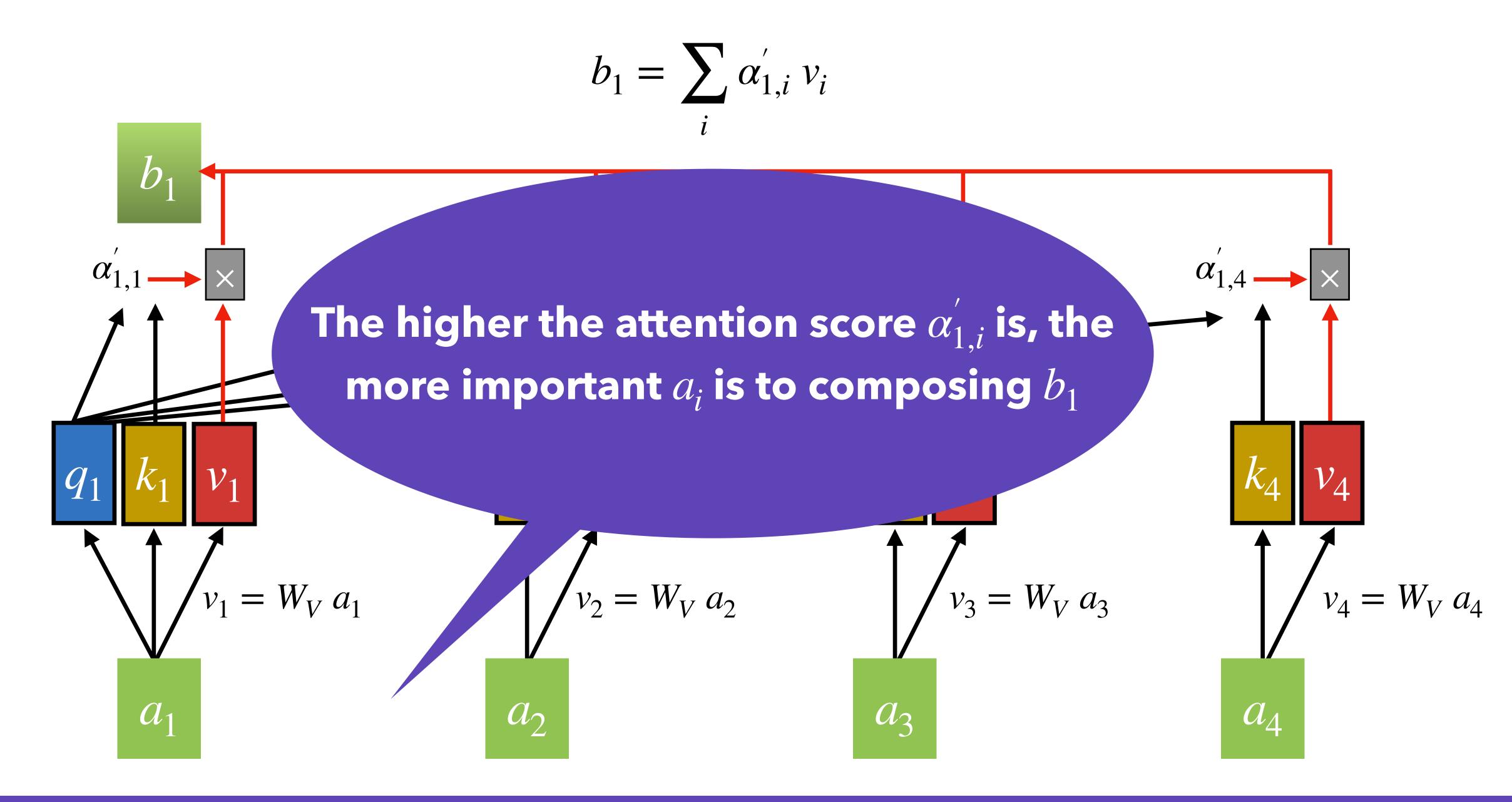
Denote how relevant each token are to $a_1!$ Use attention scores to extract information



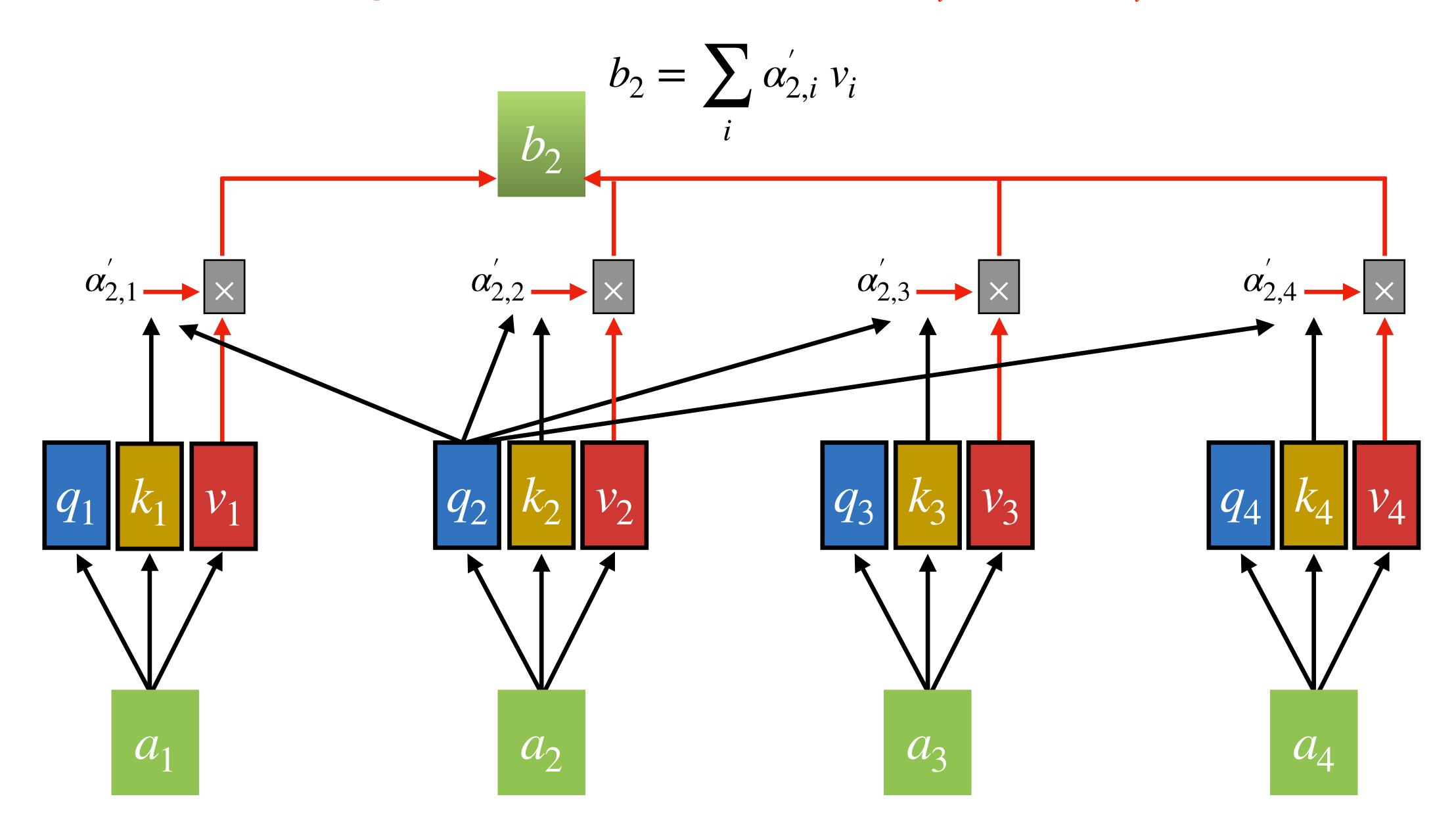
Use attention scores to extract information



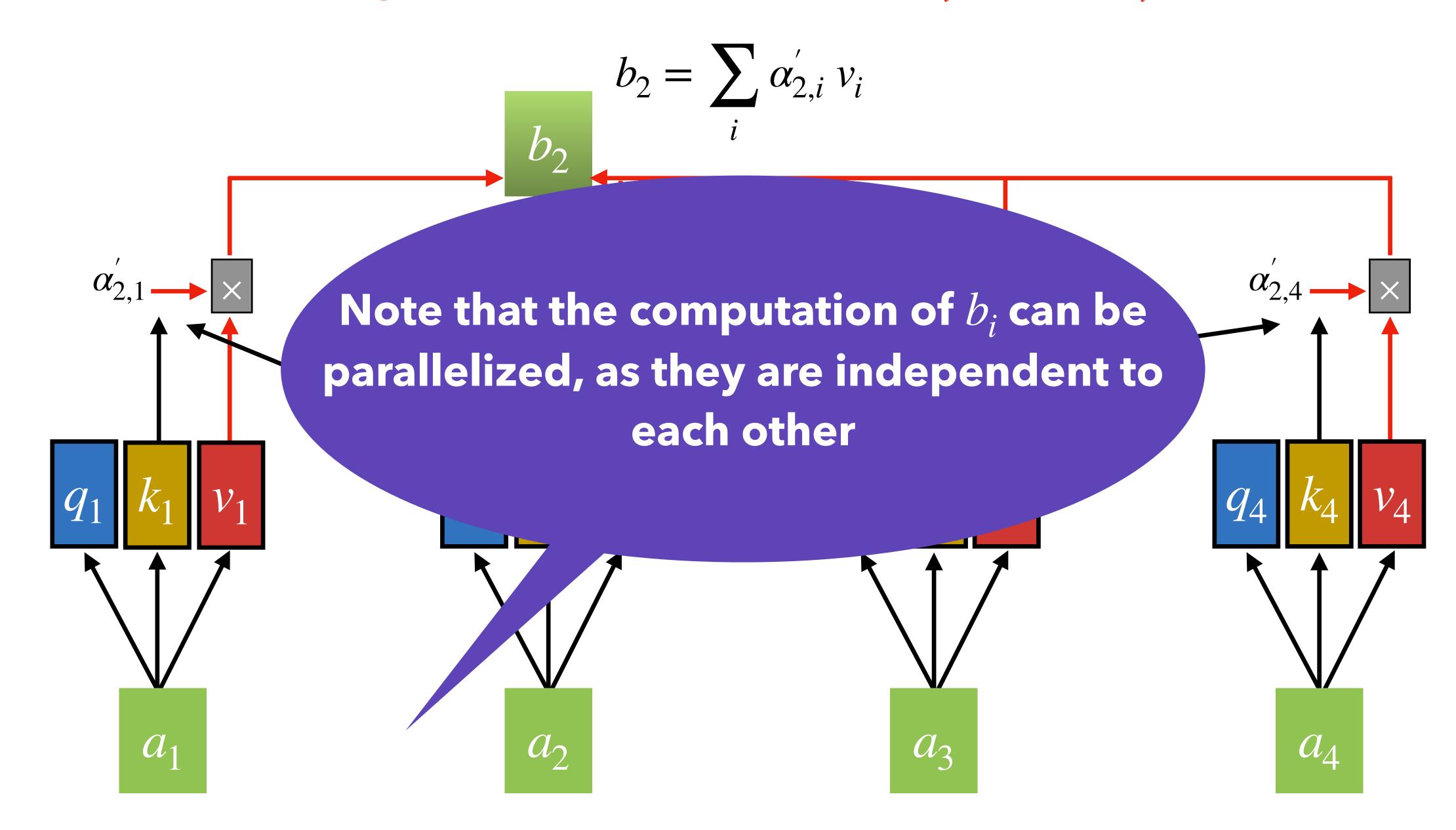
Use attention scores to extract information



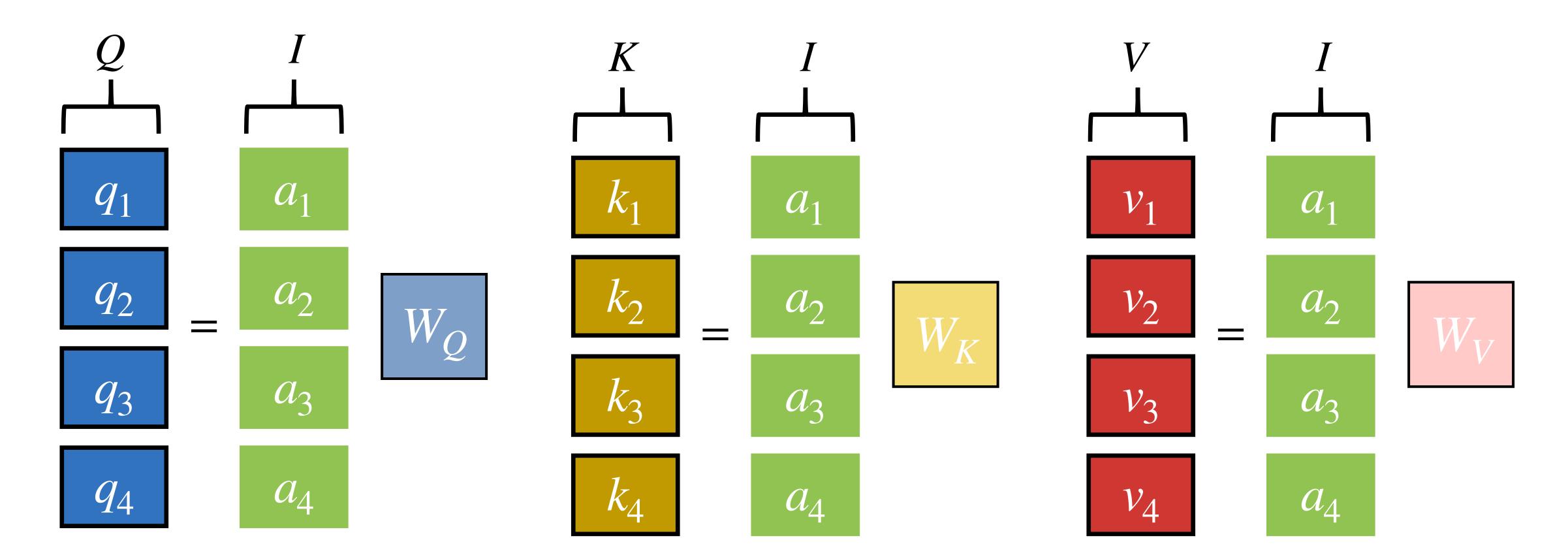
Repeat the same calculation for all a_i to obtain b_i



Repeat the same calculation for all a_i to obtain b_i



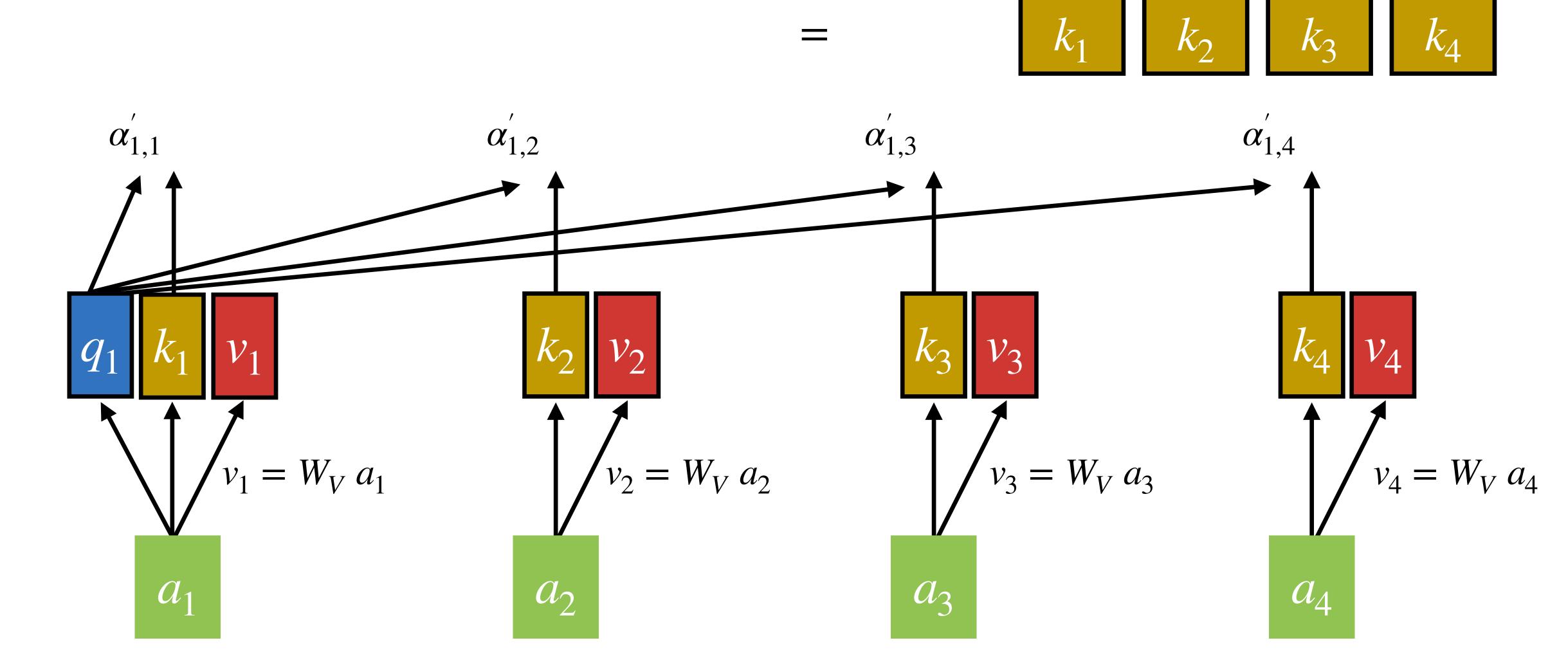
Parallelize the computation! QKV



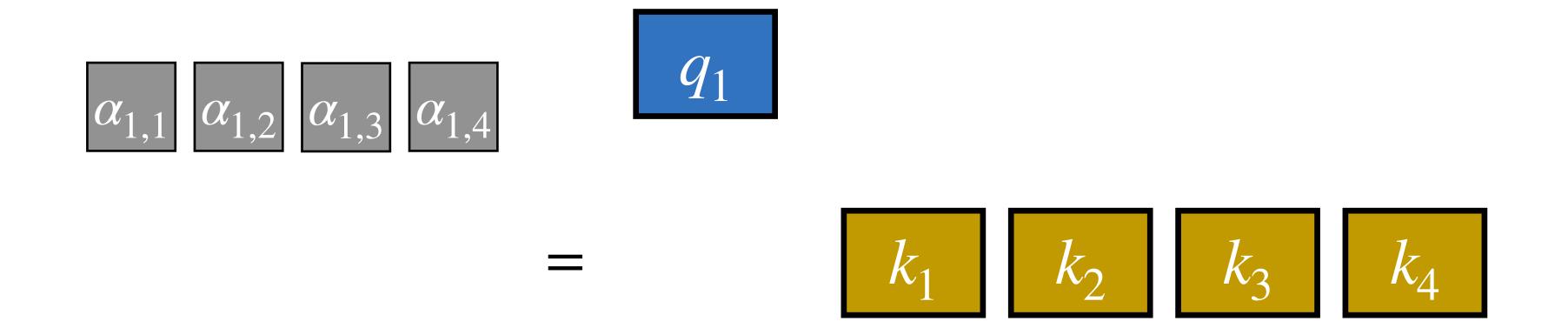
Parallelize the computation! Attention Scores

$$\left| lpha_{1,1} \right| \left| lpha_{1,2} \right| \left| lpha_{1,3} \right| \left| lpha_{1,4} \right|$$

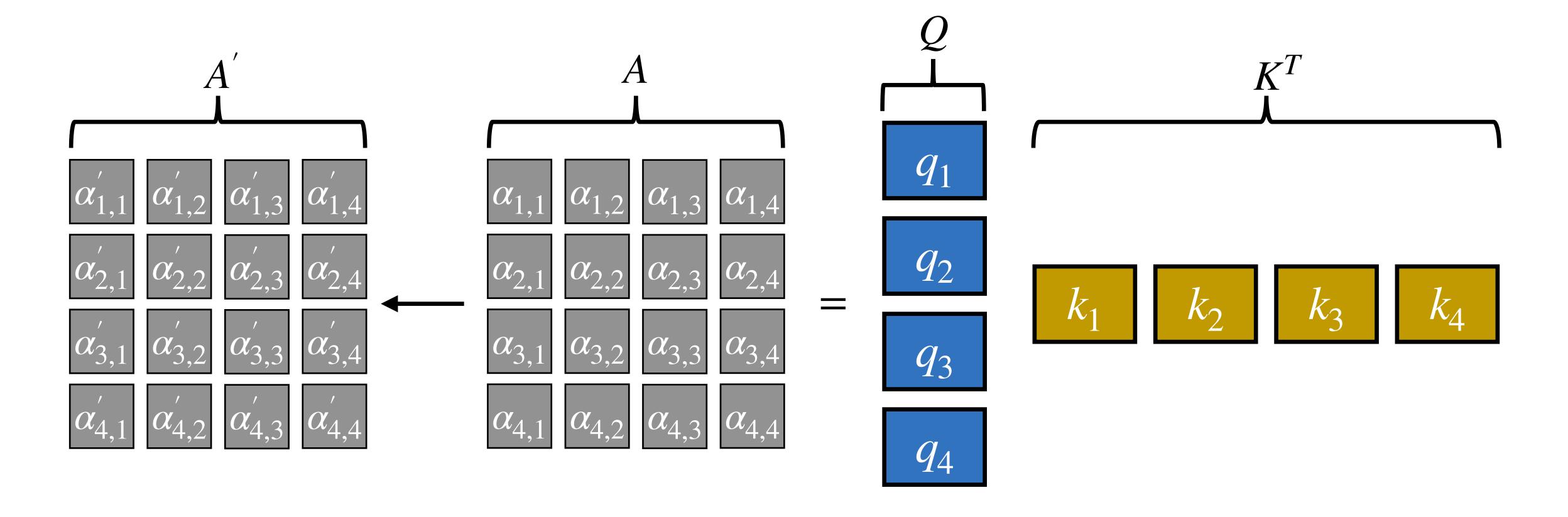


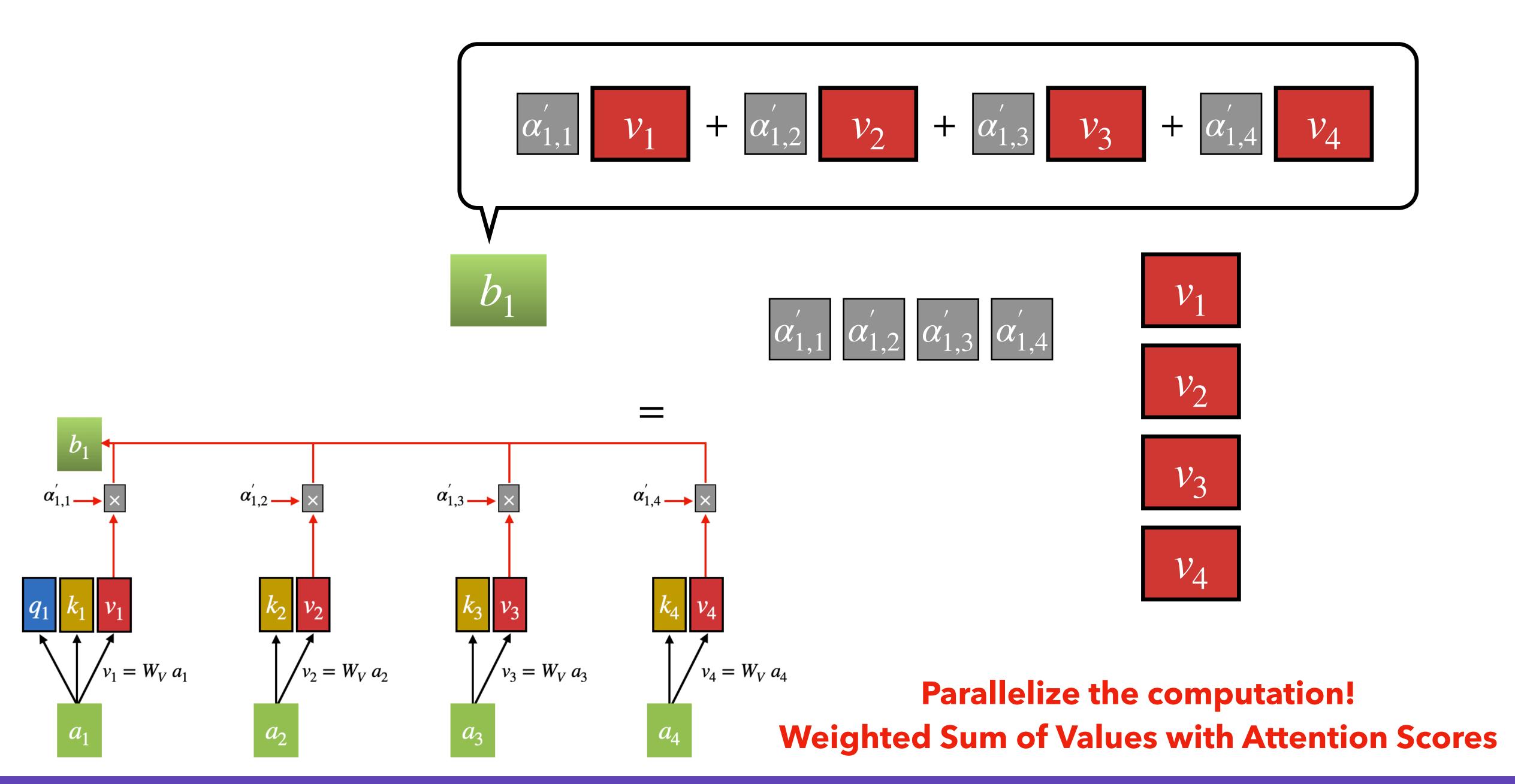


Parallelize the computation! Attention Scores

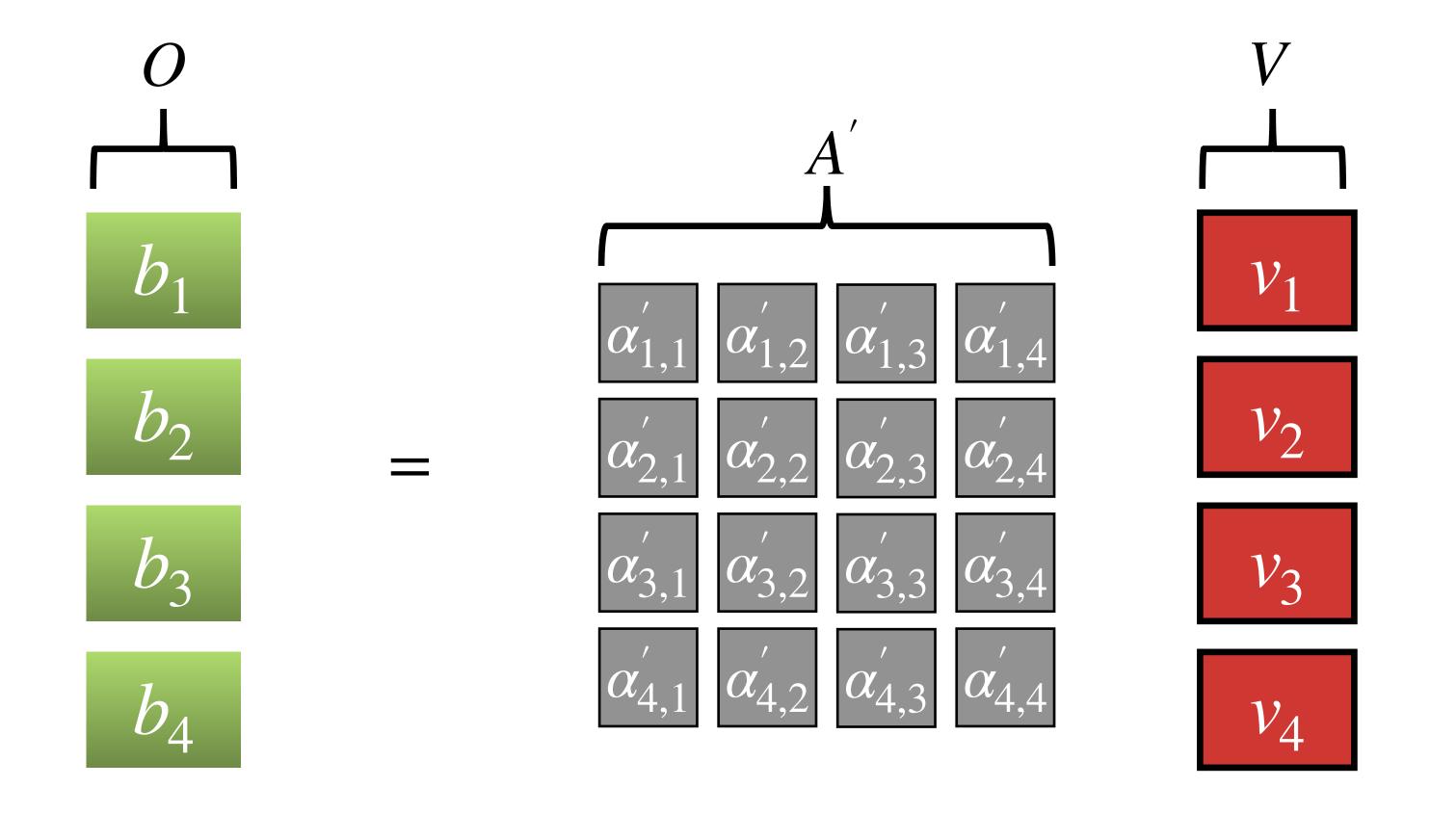


Parallelize the computation! Attention Scores

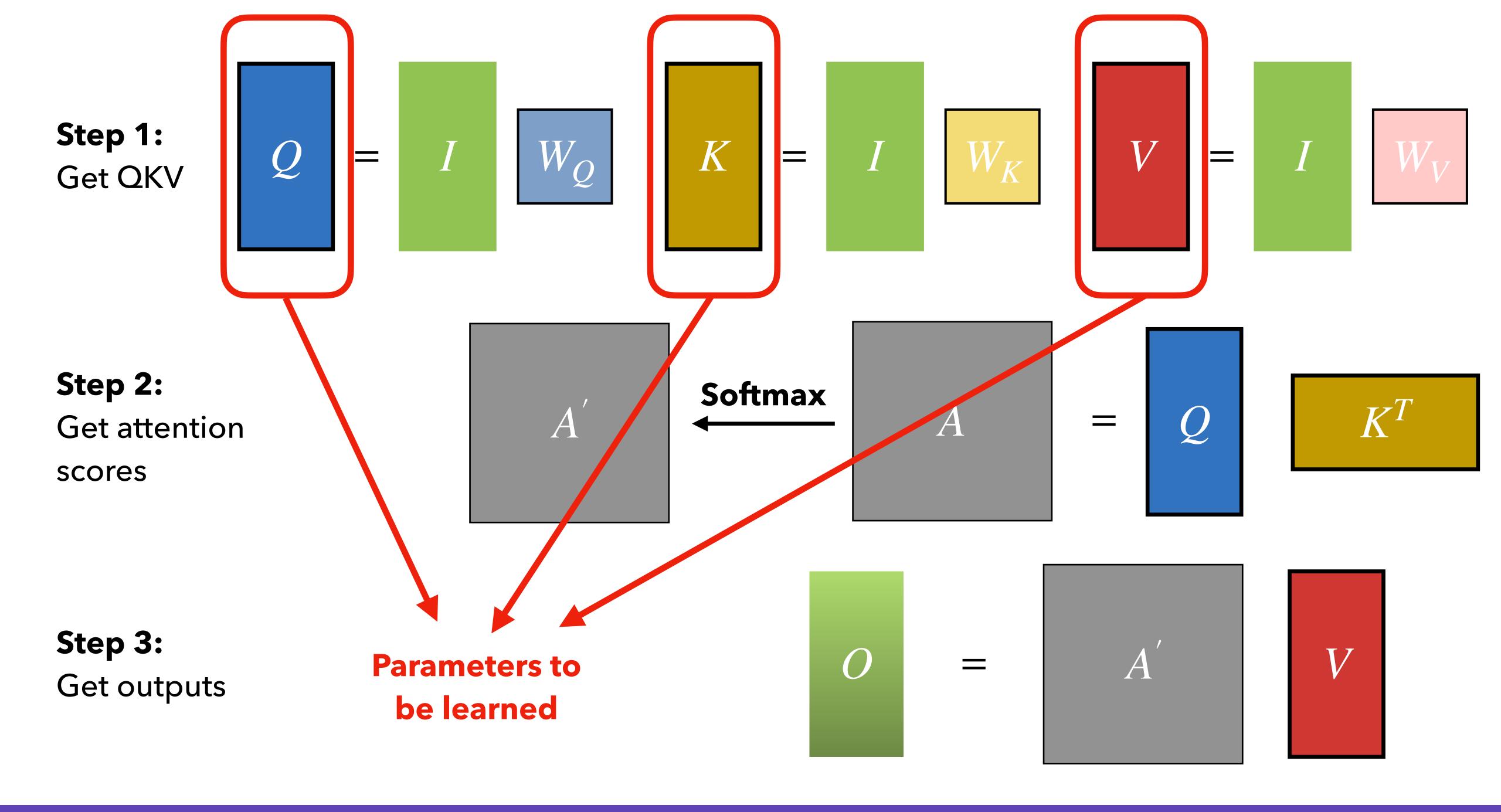




Parallelize the computation!



Parallelize the computation!
Weighted Sum of Values with Attention Scores



$$Q = I W_Q$$
 $K = I W_K$
 $V = I W_V$
 $V = I W_V$

$$A = Q K^{T}$$

$$A = I W_{Q} (I W_{K})^{T} = I W_{Q} W_{K}^{T} I^{T}$$

$$A' = \text{softmax}(A)$$

$$A = Q K^{T}$$

$$A = I W_{Q} (I W_{K})^{T} = I W_{Q} W_{K}^{T} I^{T}$$

$$O = A'V$$

The Matrices Form of Self-Attention

$$Q = I W_Q$$

$$K = I W_K$$

$$V = I W_V$$

$$I = \{a_1, \dots, a_n\} \in \mathbb{R}^{n \times d}, \text{ where } a_i \in \mathbb{R}^d$$

$$W_Q, W_K, W_V \in \mathbb{R}^{d \times d}$$

$$Q, K, V \in \mathbb{R}$$

$$A = Q K^{T}$$

$$A = I W_{Q} (I W_{K})^{T} = I W_{Q} W_{K}^{T} I^{T}$$

$$A' = \text{softmax}(A)$$

$$A = Q K^{T}$$

$$A', A \in ?$$

$$O = A^{'} V$$

$$- \bigcirc \in \mathbf{?}$$

The Matrices Form of Self-Attention

$$Q = I W_Q$$

$$K = I W_K$$

$$V = I W_V$$

$$I = \{a_1, \dots, a_n\} \in \mathbb{R}^{n \times d}, \text{ where } a_i \in \mathbb{R}^d$$

$$W_Q, W_K, W_V \in \mathbb{R}^{d \times d}$$

$$Q, K, V \in \mathbb{R}^{n \times d}$$

$$A = Q K^{T}$$

$$A = I W_{Q} (I W_{K})^{T} = I W_{Q} W_{K}^{T} I^{T}$$

$$A' = \text{softmax}(A)$$

$$A = Q K^{T}$$

$$A', A \in \mathbb{R}^{n \times n}$$

$$O = A^{'} V$$

Self-Attention: Summary

Let $w_{1:n}$ be a sequence of words in vocabulary V, like Steve Jobs founded Apple.

For each w_i , let $a_i = Ew_i$, where $E \in \mathbb{R}^{d \times |V|}$ is an embedding matrix.

1. Transform each word embedding with weight matrices W_Q, W_K, W_V , each in $\mathbb{R}^{d imes d}$

$$q_i = W_Q a_i$$
 (queries) $k_i = W_K a_i$ (keys) $v_i = W_V a_i$ (values)

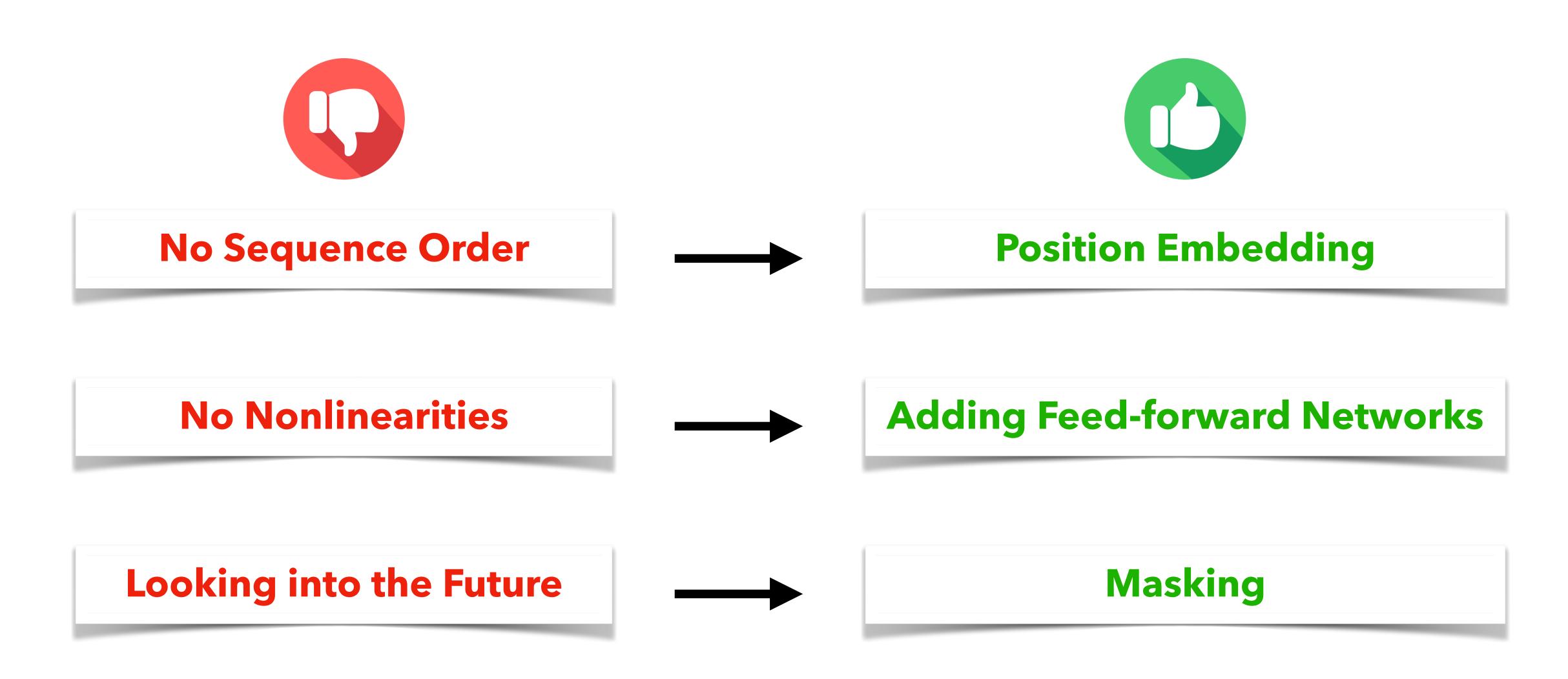
2. Compute pairwise similarities between keys and queries; normalize with softmax

$$\alpha_{i,j} = k_j q_i \qquad \qquad \alpha'_{i,j} = \frac{e^{\alpha_{i,j}}}{\sum_{i} e^{\alpha_{i,j}}}$$

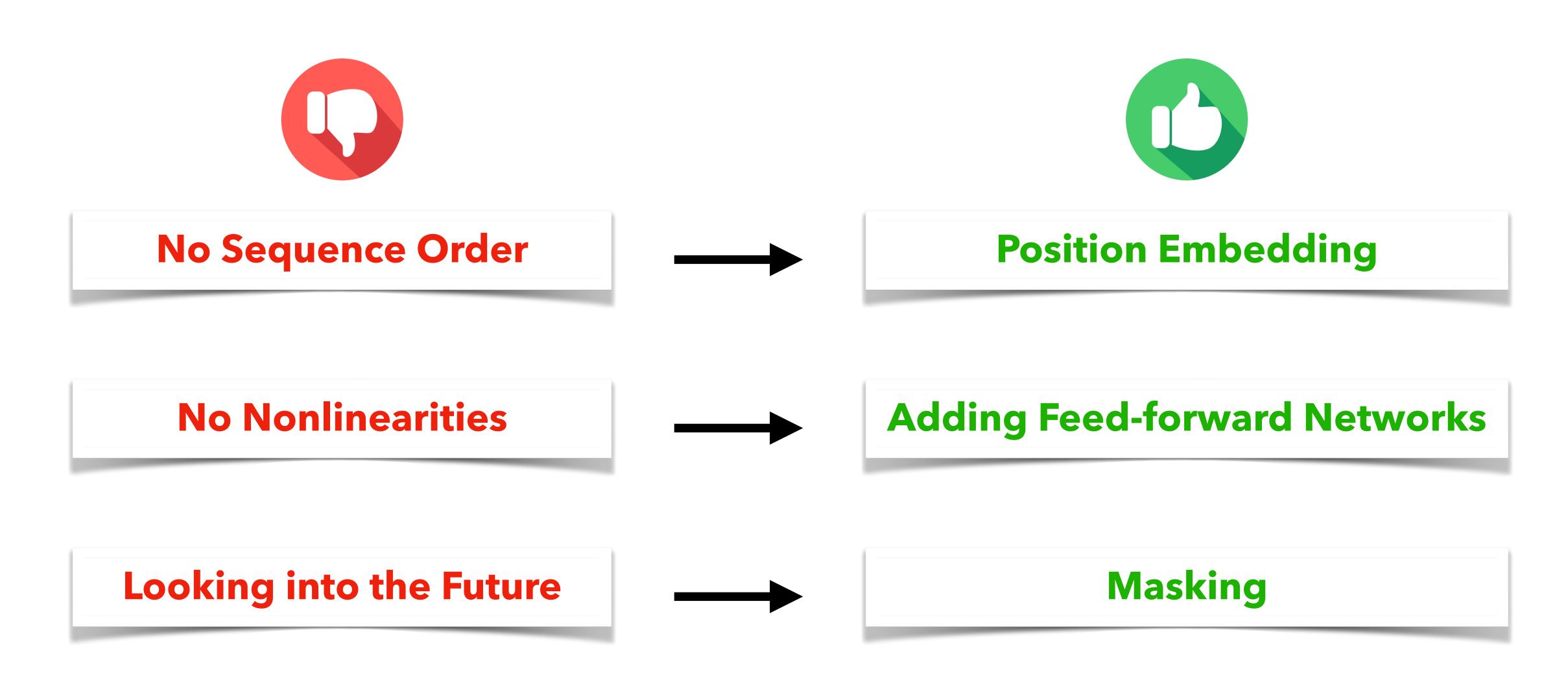
3. Compute output for each word as weighted sum of values

$$b_{i} = \sum_{j} \alpha'_{i,j} v_{j}$$

Limitations and Solutions of Self-Attention

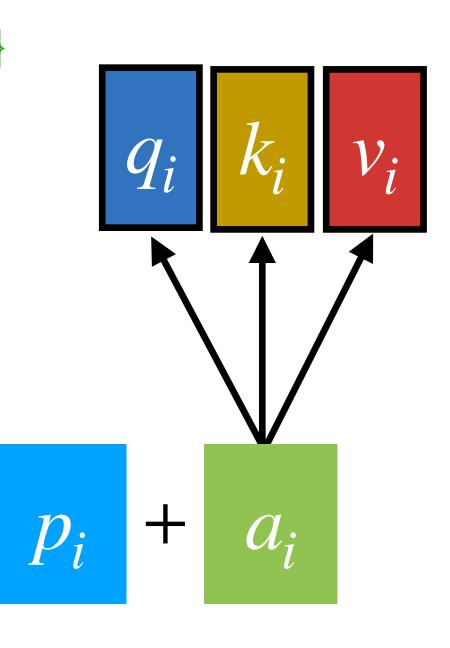


Limitations and Solutions of Self-Attention



No Sequence Order → **Position Embedding**

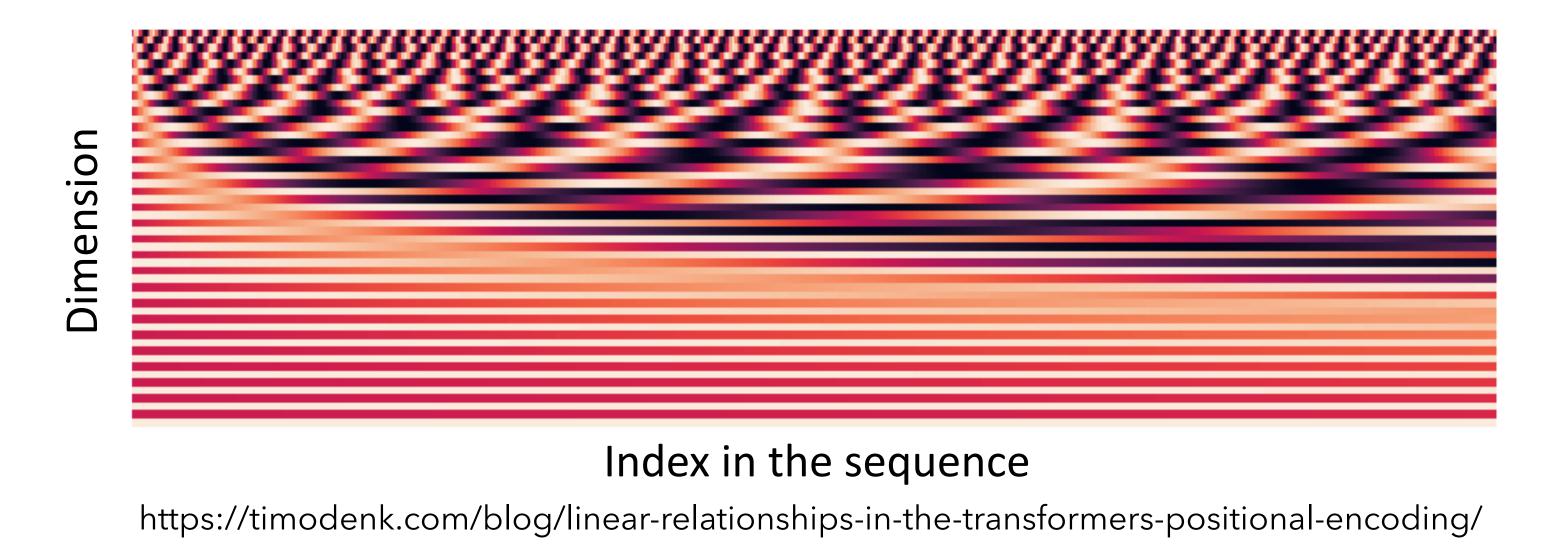
- All tokens in an input sequence are **simultaneously** fed into self-attention blocks. Thus, there's no difference between tokens at different positions.
 - We lose the position info!
- How do we bring the position info back, just like in RNNs?
 - Representing each sequence index as a vector: $p_i \in \mathbb{R}^d$, for $i \in \{1,...,n\}$
- How to incorporate the position info into the self-attention blocks?
 - Just add the p_i to the input: $\hat{a}_i = a_i + p_i$
 - where a_i is the embedding of the word at index i.
 - In deep self-attention networks, we do this at the first layer.
 - ullet We can also concatenate a_i and $p_{i'}$ but more commonly we add them.



Position Representation Vectors via Sinusoids

Sinusoidal Position Representations (from the original Transformer paper): concatenate sinusoidal functions of varying periods.

$$p_{i} = \begin{cases} \sin(i/10000^{2*1/d}) \\ \cos(i/10000^{2*1/d}) \\ \vdots \\ \sin(i/10000^{2*\frac{d}{2}/d}) \\ \cos(i/10000^{2*\frac{d}{2}/d}) \end{cases}$$





- Periodicity indicates that maybe "absolute position" isn't as important
- Maybe can extrapolate to longer sequences as periods restart!



Not learnable; also the extrapolation doesn't really work!

Learnable Position Representation Vectors

Learned absolute position representations: p_i contains learnable parameters.

- Learn a matrix $p \in \mathbb{R}^{d \times n}$, and let each p_i be a column of that matrix
- Most systems use this method.



• Flexibility: each position gets to be learned to fit the data

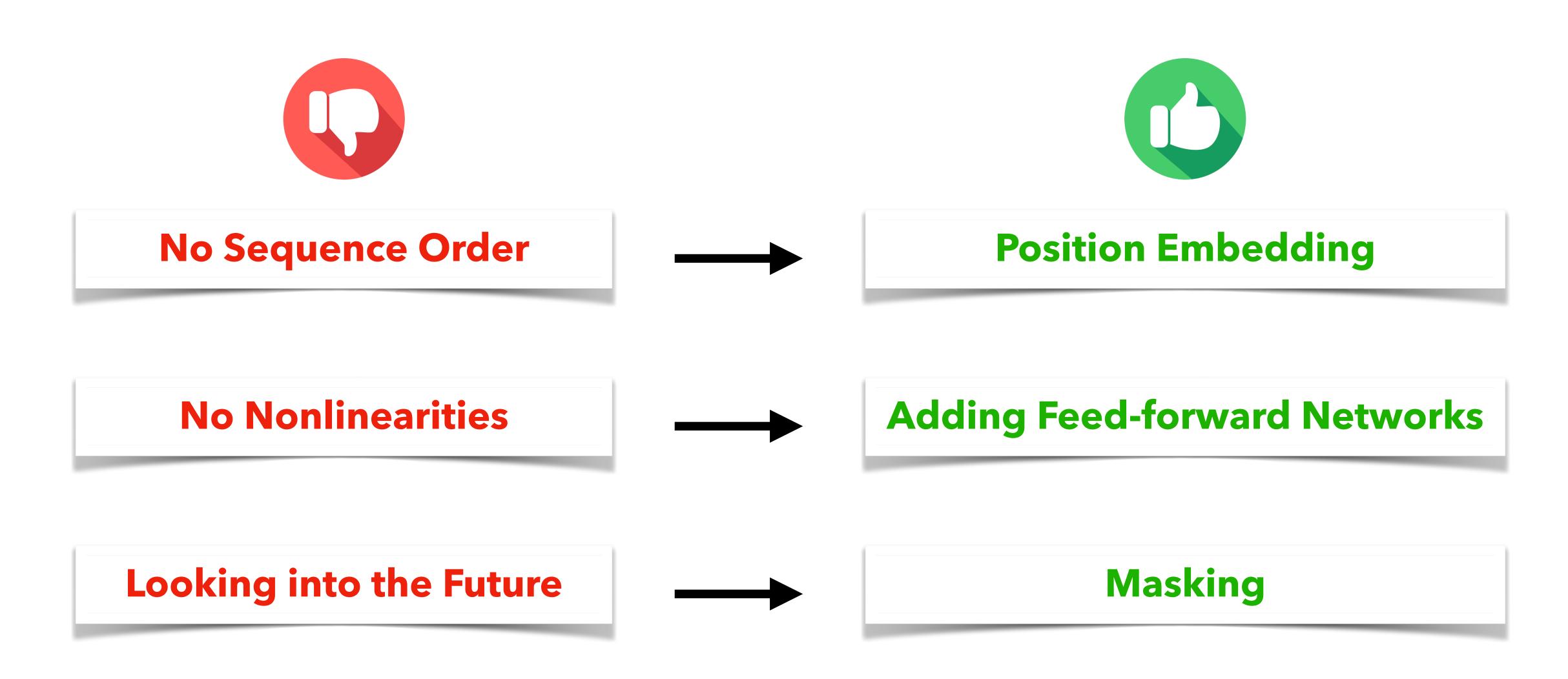


• Cannot extrapolate to indices outside 1,...,n.

Sometimes people try more flexible representations of position:

- Relative linear position attention [Shaw et al., 2018]
- Dependency syntax-based position [Wang et al., 2019]

Limitations and Solutions of Self-Attention

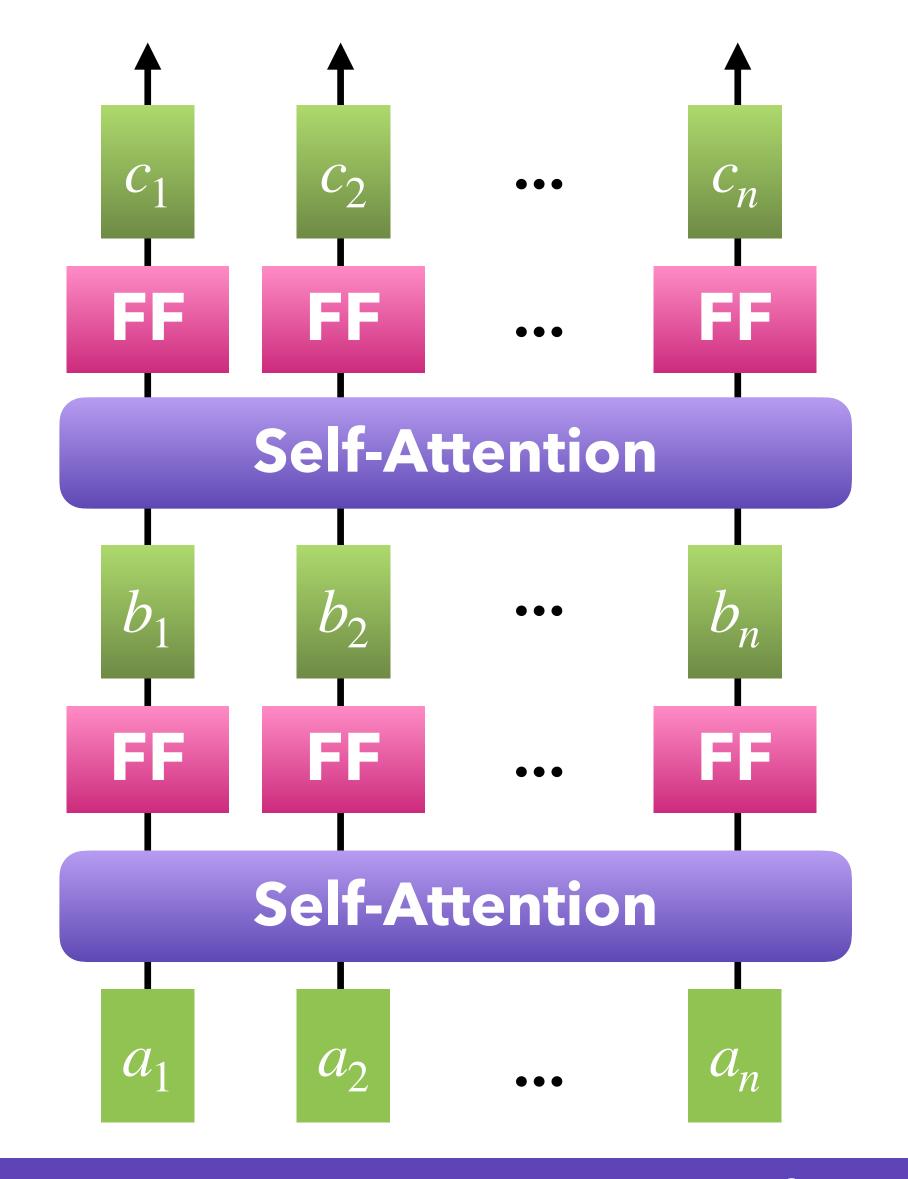


No Nonlinearities → Add Feed-forward Networks

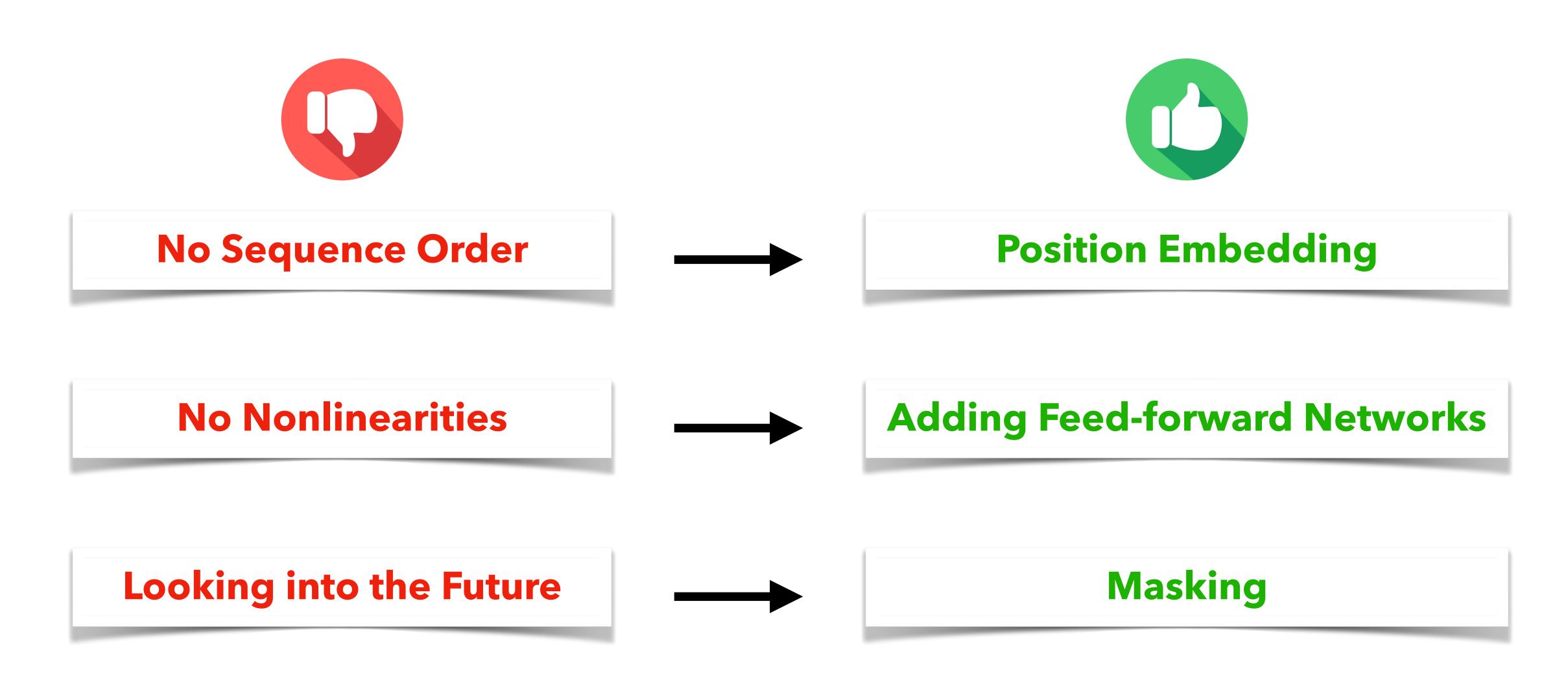
There are **no element-wise nonlinearities** in self-attention; stacking more self-attention layers just re-averages value vectors.



Easy Fix: add a feed-forward network to post-process each output vector.

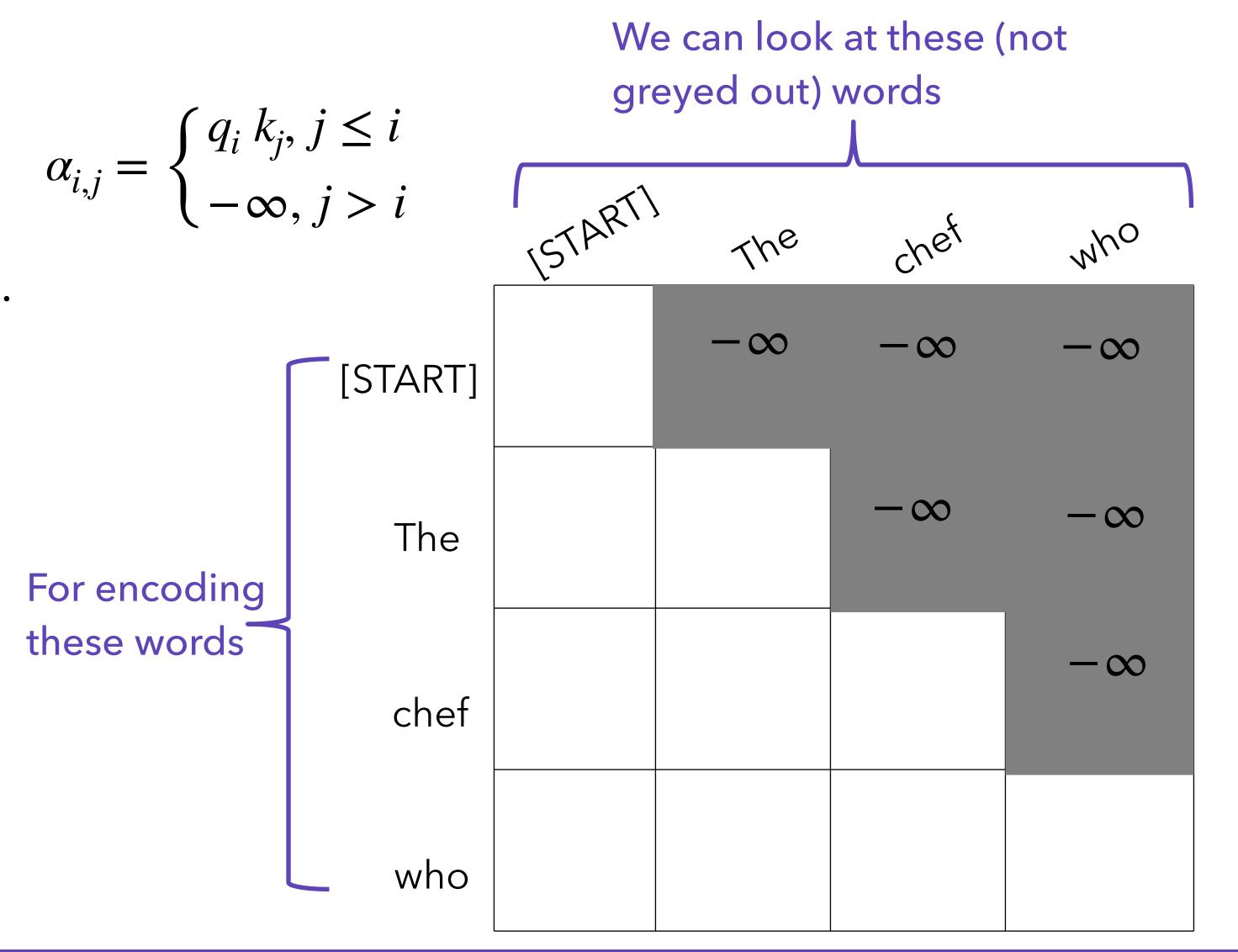


Limitations and Solutions of Self-Attention



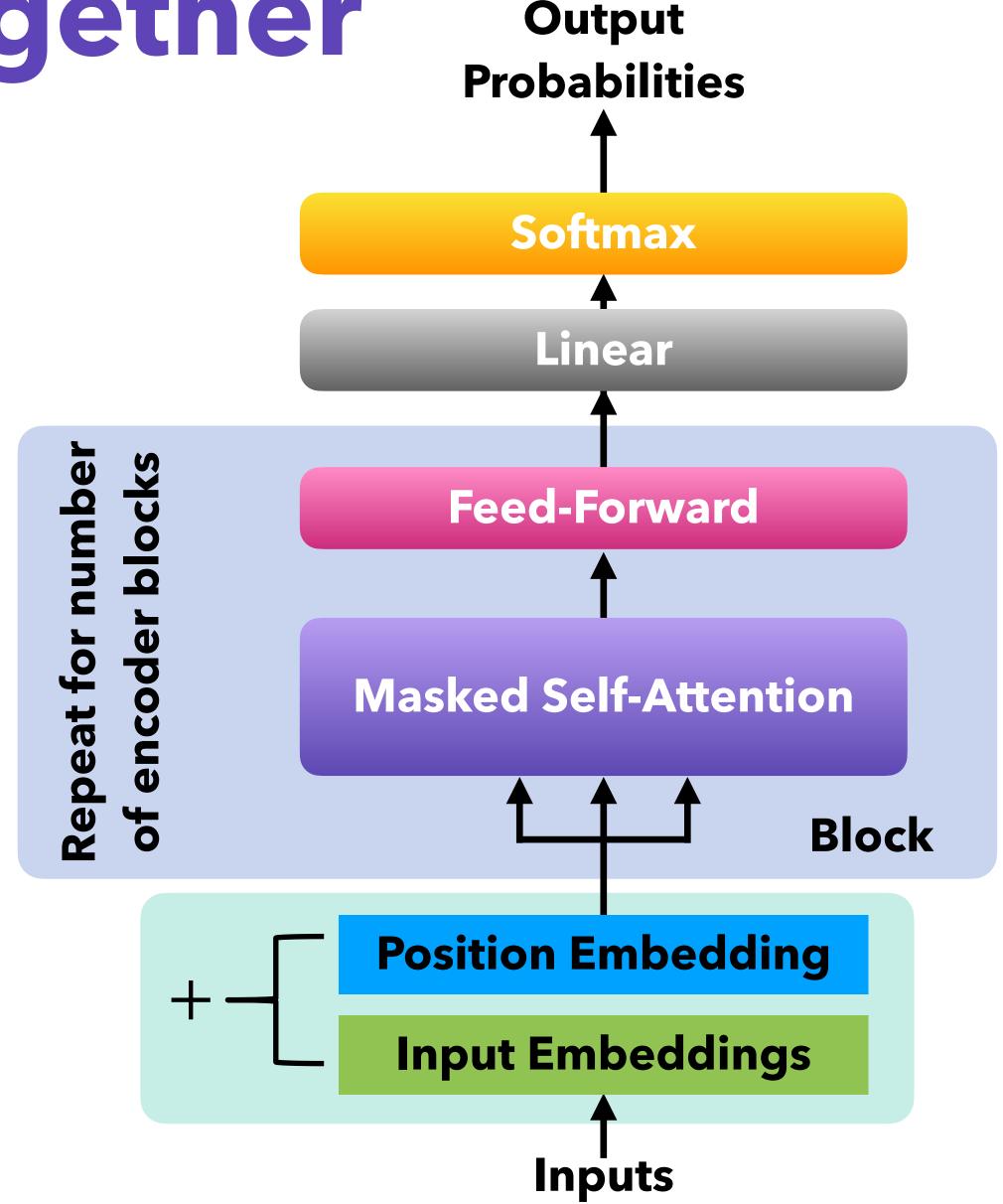
Looking into the Future \rightarrow Masking

- In decoders (language modeling, producing the next word given previous context), we need to ensure we don't peek at the future.
- At every time-step, we could change the set of keys and queries to include only past words. (Inefficient!)
- To enable parallelization, we mask out attention to future words by setting attention scores to $-\infty$.



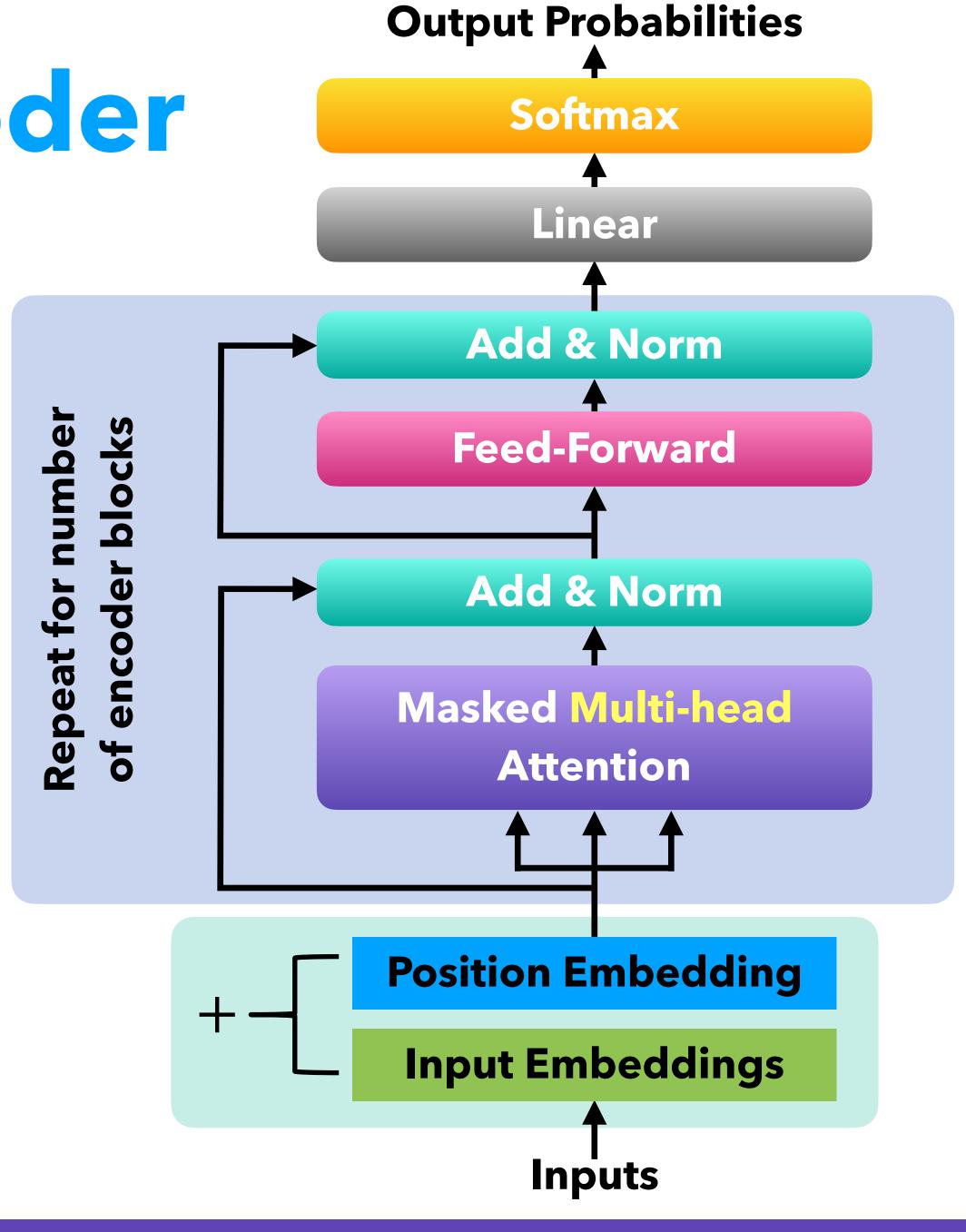
Now We Put Things Together

- Self-attention
 - The basic computation
- Positional Encoding
 - Specify the sequence order
- Nonlinearities
 - Adding a feed-forward network at the output of the self-attention block
- Masking
 - Parallelize operations (looking at all tokens)
 while not leaking info from the future



The Transformer Decoder

- A **Transformer decoder** is what we use to build systems like language models.
- It's a lot like our minimal self-attention architecture, but with a few more components.
 - Residual connection ("Add")
 - Layer normalization ("Norm")
- Replace self-attention with multi-head self-attention.

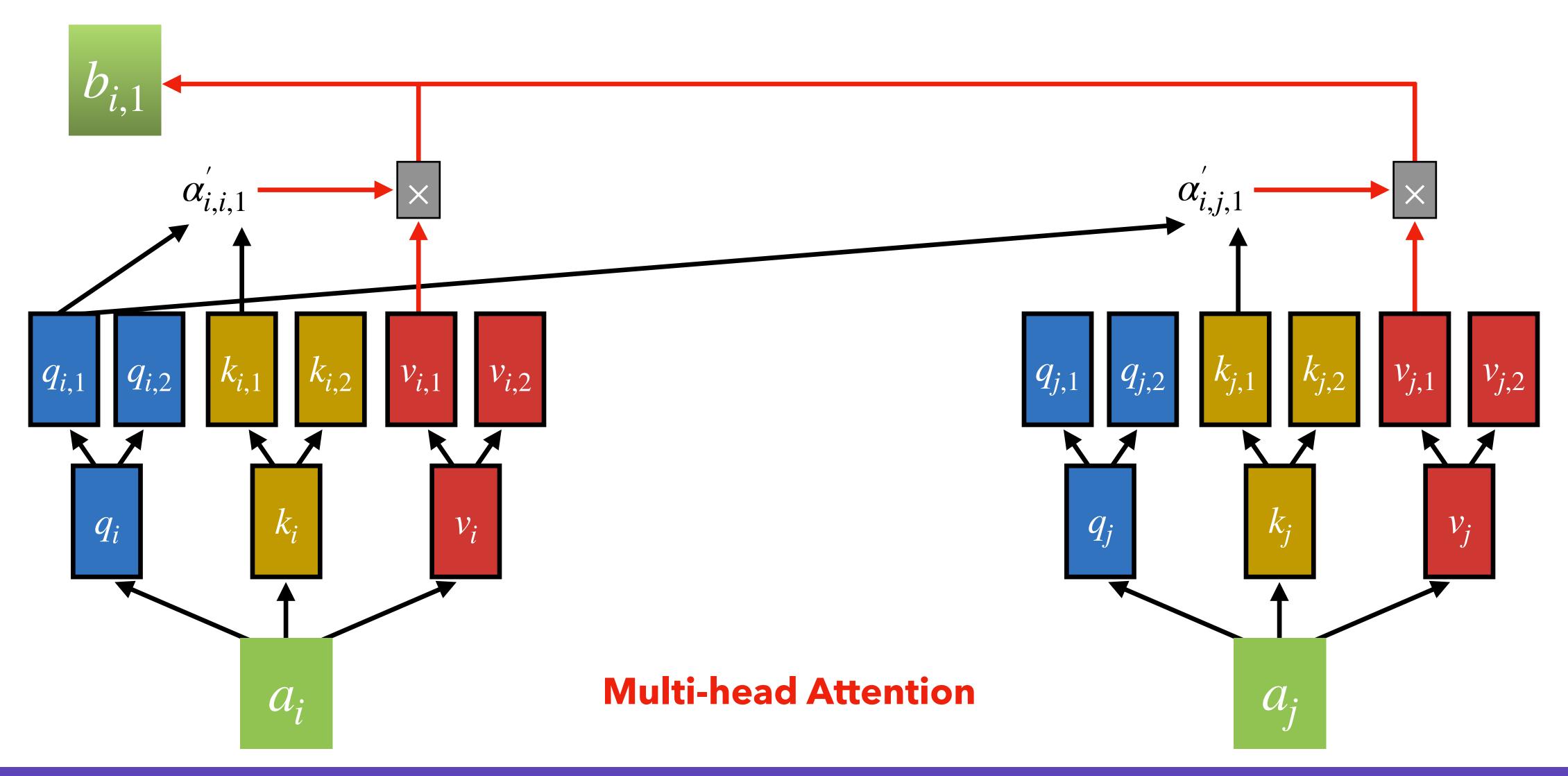


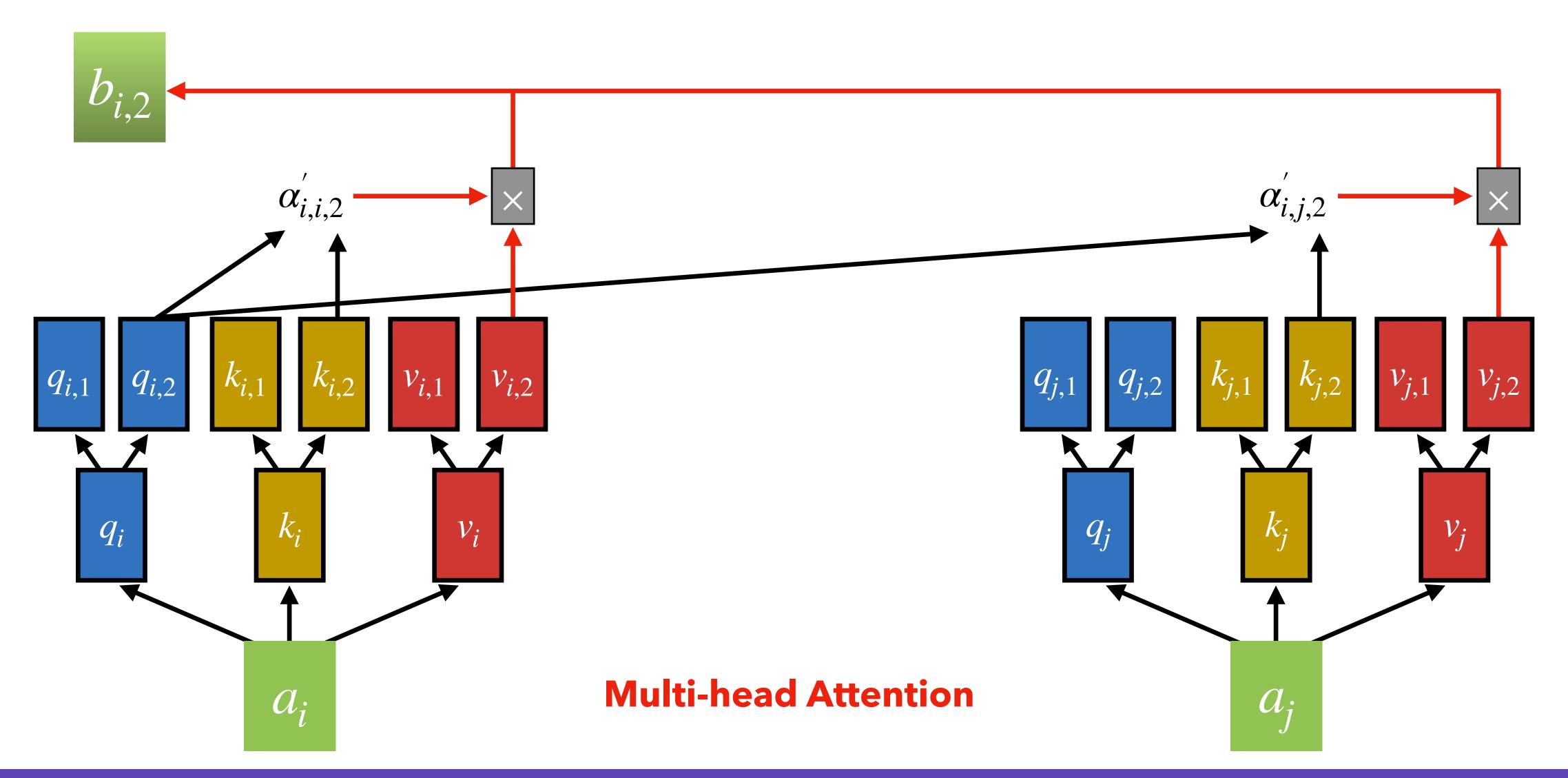
Why Multi-head Attention?

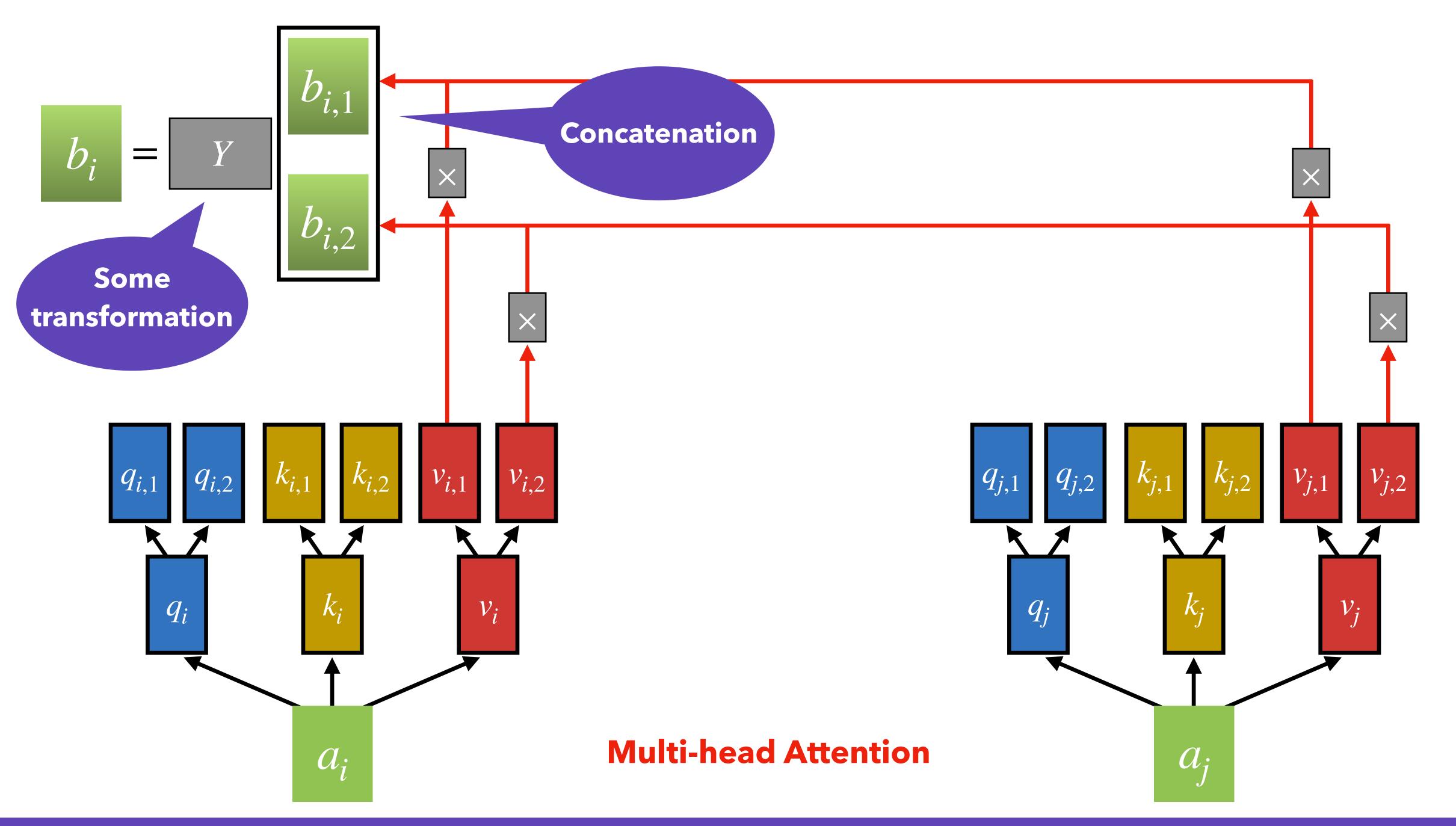
What if we want to look in multiple places in the sentence at once?

Instead of having only one attention head, we can create multiple sets of (queries, keys, values) independent from each other!

Multi-Head Attention: Walk-through







Recall the Matrices Form of Self-Attention

$$Q = I W_Q$$

$$K = I W_K$$

$$V = I W_V$$

$$\begin{cases} I = \{a_1, \dots, a_n\} \in \mathbb{R}^{n \times d}, \text{ where } a_i \in \mathbb{R}^d \\ W_Q, W_K, W_V \in \mathbb{R}^{d \times d} \\ Q, K, V \in \mathbb{R}^{n \times d} \end{cases}$$

$$O, K, V \in \mathbb{R}^{n \times d}$$

$$O = A^{'} V$$

Multi-head Attention in Matrices

- ullet Multiple attention "heads" can be defined via multiple $W_Q,\,W_K,\,W_V$ matrices
- Let $W_Q^l, W_K^l, W_V^l \in \mathbb{R}^{d \times \frac{d}{h}}$, where h is the number of attention heads, and l ranges from 1 to h.
- Each attention head performs attention independently:
 - $O^l = \operatorname{softmax}(I \ W_O^l \ W_K^{l^T} \ I^T) \ I \ W_V^l$
- ullet Concatenating different O^l from different attention heads.
 - $O = [O^1; ...; O^n] Y$, where $Y \in \mathbb{R}^{d \times d}$

The Matrices Form of Multi-head Attention

$$Q^{l} = I W_{Q}^{l}$$

$$K^{l} = I W_{K}^{l}$$

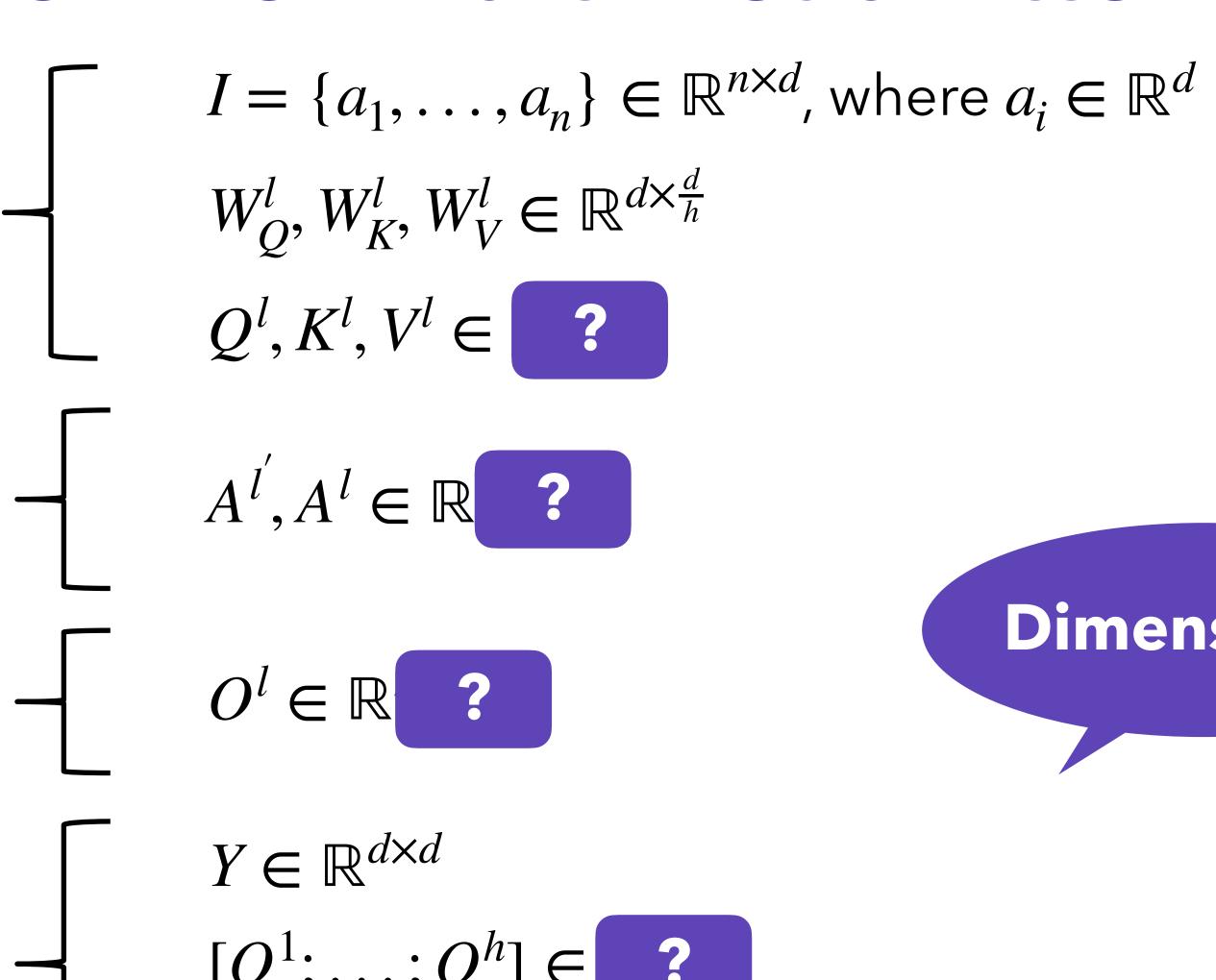
$$V^{l} = I W_{V}^{l}$$

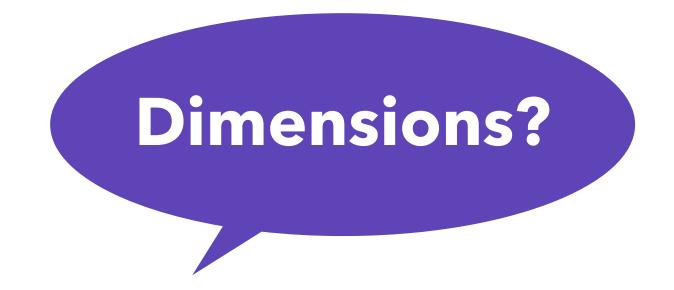
$$A^{l} = Q^{l} K^{l}^{T}$$

$$A^{l'} = \operatorname{softmax}(A^{l})$$

$$O^{l} = A^{l'} V^{l}$$

$$O = [O^1; \dots; O^h] Y$$





The Matrices Form of Multi-head Attention

$$Q^{l} = I W_{Q}^{l}$$

$$K^{l} = I W_{K}^{l}$$

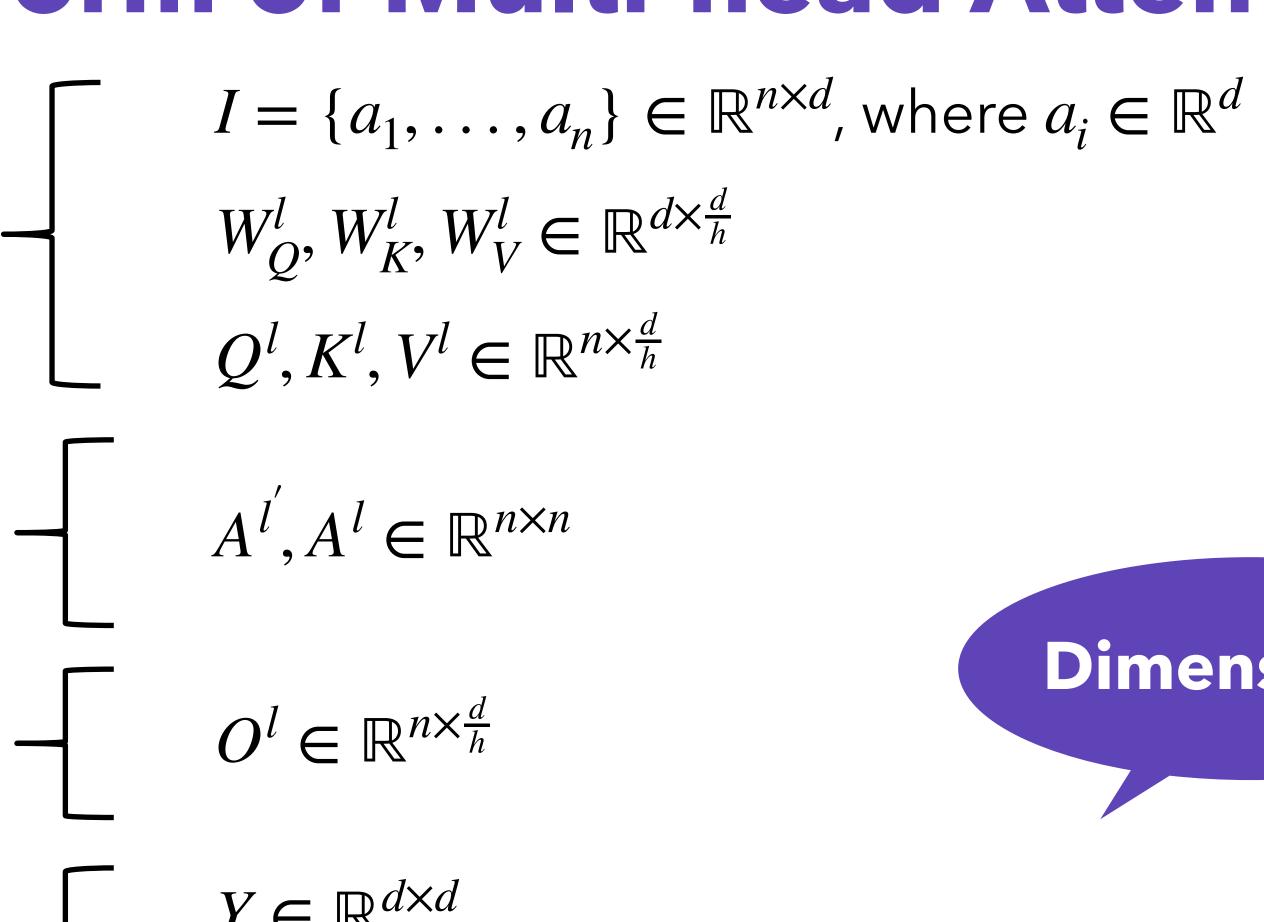
$$V^{l} = I W_{V}^{l}$$

$$A^{l} = Q^{l} K^{l}^{T}$$

$$A^{l'} = \text{softmax}(A^{l})$$

$$O = [O^1; \dots; O^h] Y$$

 $O^l = A^{l'} V^l$



$$Y \in \mathbb{R}^{d \times d}$$

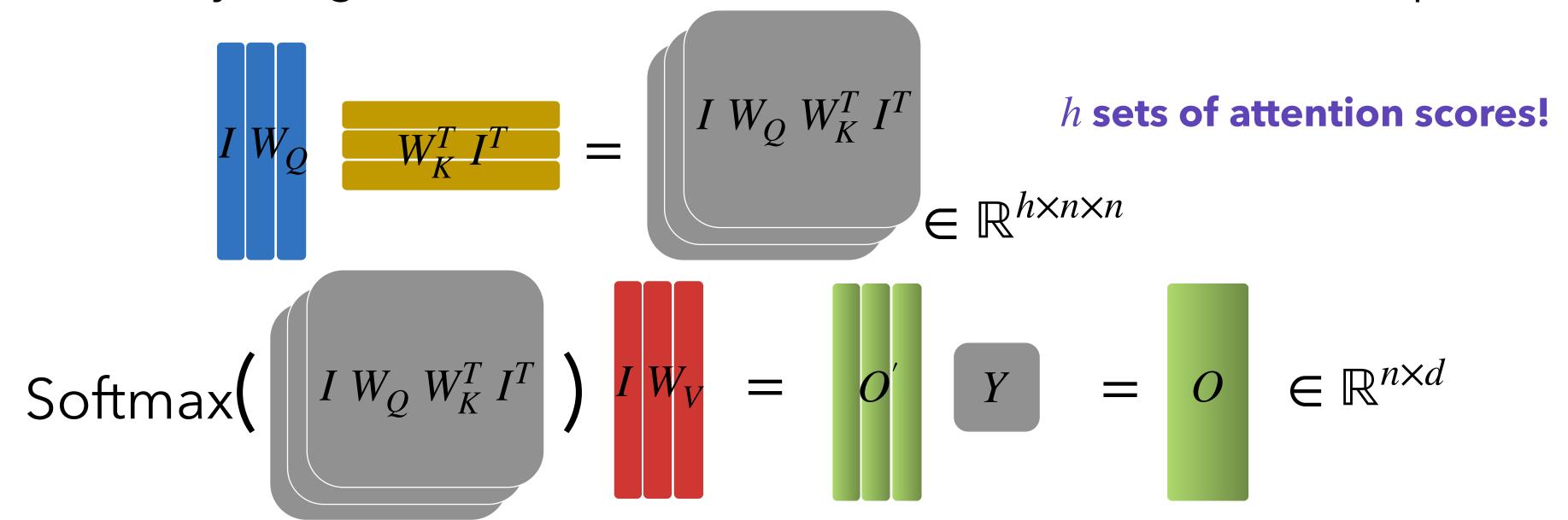
$$[O^1; \dots; O^h] \in \mathbb{R}^{n \times d}$$

$$O \in \mathbb{R}^{n \times d}$$



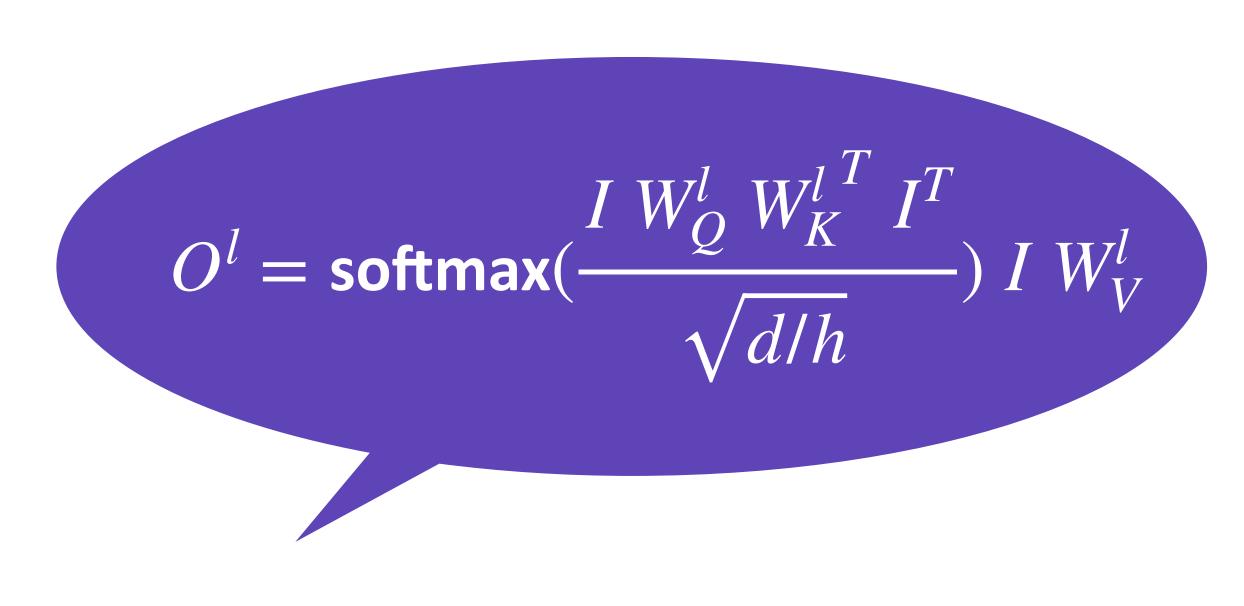
Multi-head Attention is Computationally Efficient

- ullet Even though we compute h many attention heads, it's not more costly.
 - We compute $I W_O \in \mathbb{R}^{n \times d}$, and then reshape to $\mathbb{R}^{n \times h \times \frac{d}{h}}$.
 - Likewise for IW_K and IW_V .
 - Then we transpose to $\mathbb{R}^{h \times n \times \frac{d}{h}}$; now the head axis is like a batch axis.
 - Almost everything else is identical. All we need to do is to reshape the tensors!



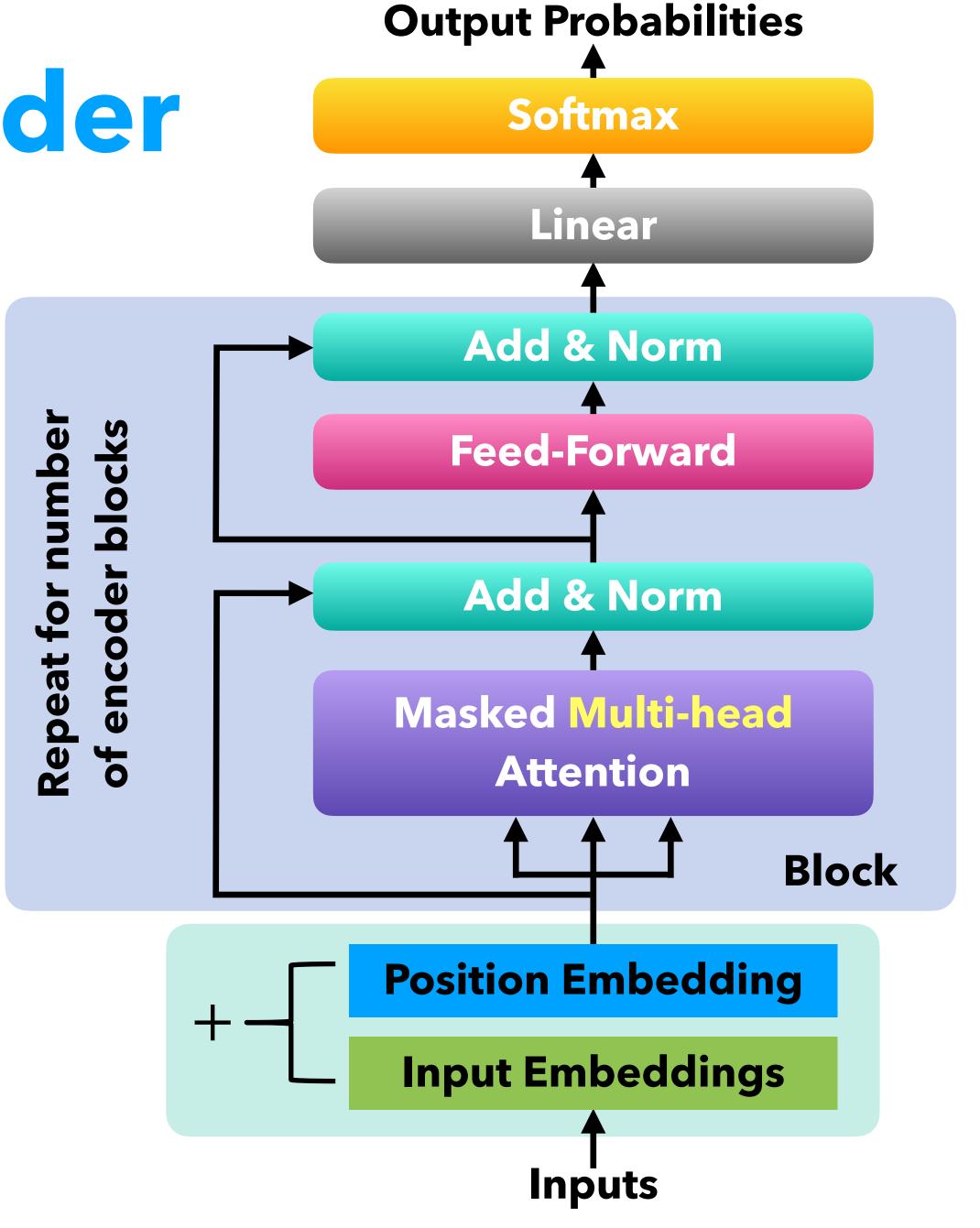
Scaled Dot Product [Vaswani et al., 2017]

- "Scaled Dot Product" attention aids in training.
- ullet When dimensionality d becomes large, dot products between vectors tend to become large.
 - Because of this, inputs to the softmax function can be large, making the gradients small.
- Instead of the self-attention function we've seen:
 - $\bullet \ O^l = \operatorname{softmax}(I \ W_Q^l \ W_K^{l^T} \ I^T) \ I \ W_V^l$
- We divide the attention scores by $\sqrt{d/h}$, to stop the scores from becoming large just as a function of d/h (the dimensionality divided by the number of heads).



The Transformer Decoder

- Now that we've replaced self-attention with multi-head self-attention, we'll go through two optimization tricks:
 - Residual connection ("Add")
 - Layer normalization ("Norm")



Residual Connections

[He et al., 2016]

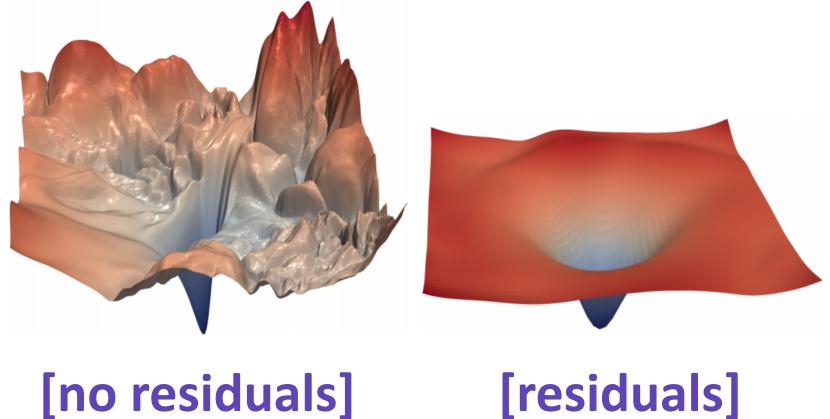
- Residual connections are a trick to help models train better.
 - Instead of $X^{(i)} = \text{Layer}(X^{(i-1)})$ (where i represents the layer)

$$X^{(i-1)}$$
 — Layer $X^{(i)}$

• We let $X^{(i)} = X^{(i-1)} + \text{Layer}(X^{(i-1)})$ (so we only have to learn "the residual" from the previous layer)



- Gradient is great through the residual connection; it's 1!
- Bias towards the identity function!



[Loss landscape visualization, Li et al., 2018, on a ResNet]

Layer Normalization

[Ba et al., 2016]

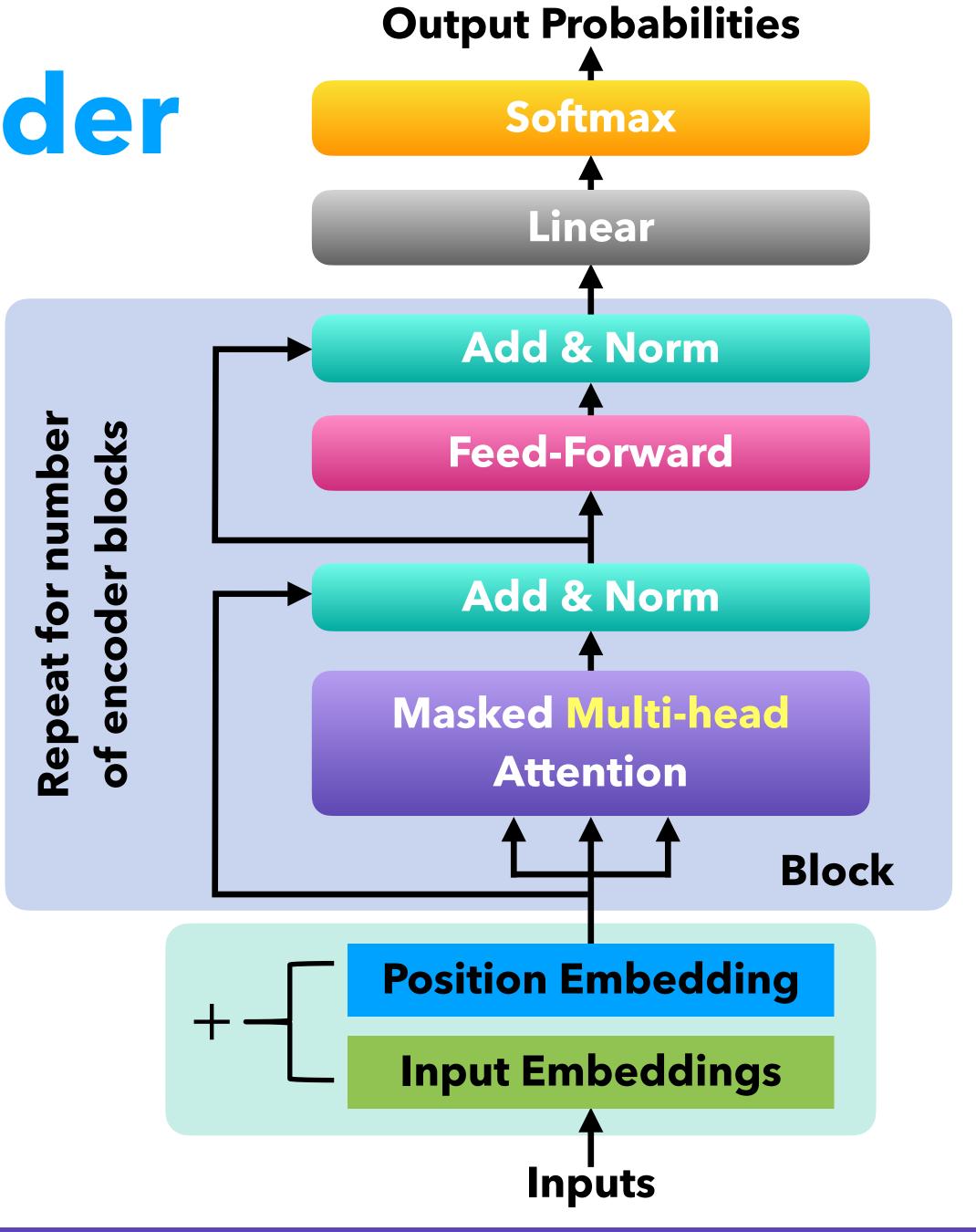
- Layer normalization is a trick to help models train faster.
- Idea: cut down on uninformative variation in hidden vector values by normalizing to unit mean and standard deviation within each layer.
 - LayerNorm's success may be due to its normalizing gradients [Xu et al., 2019]
- Let $x \in \mathbb{R}^d$ be an individual (word) vector in the model.
- Let $\mu = \sum_{j}^{n} x_{j}$; this is the mean; $\mu \in \mathbb{R}$.
- Let $\sigma = \sqrt{\frac{1}{d} \sum_{j=1}^{d} \left(x_j \mu \right)^2}$; this is the standard deviation; $\sigma \in \mathbb{R}$.
- Let $\gamma \in \mathbb{R}^d$ and $\beta \in \mathbb{R}^d$ be learned "gain" and "bias" parameters. (Can omit!)
- Then layer normalization computes:

Normalize by scalar mean and scalar mean and solution
$$\frac{x-\mu}{\sqrt{\sigma+\epsilon}}*\gamma+\beta$$
 Modulate by learned element-wise gain an bias

element-wise gain and bias

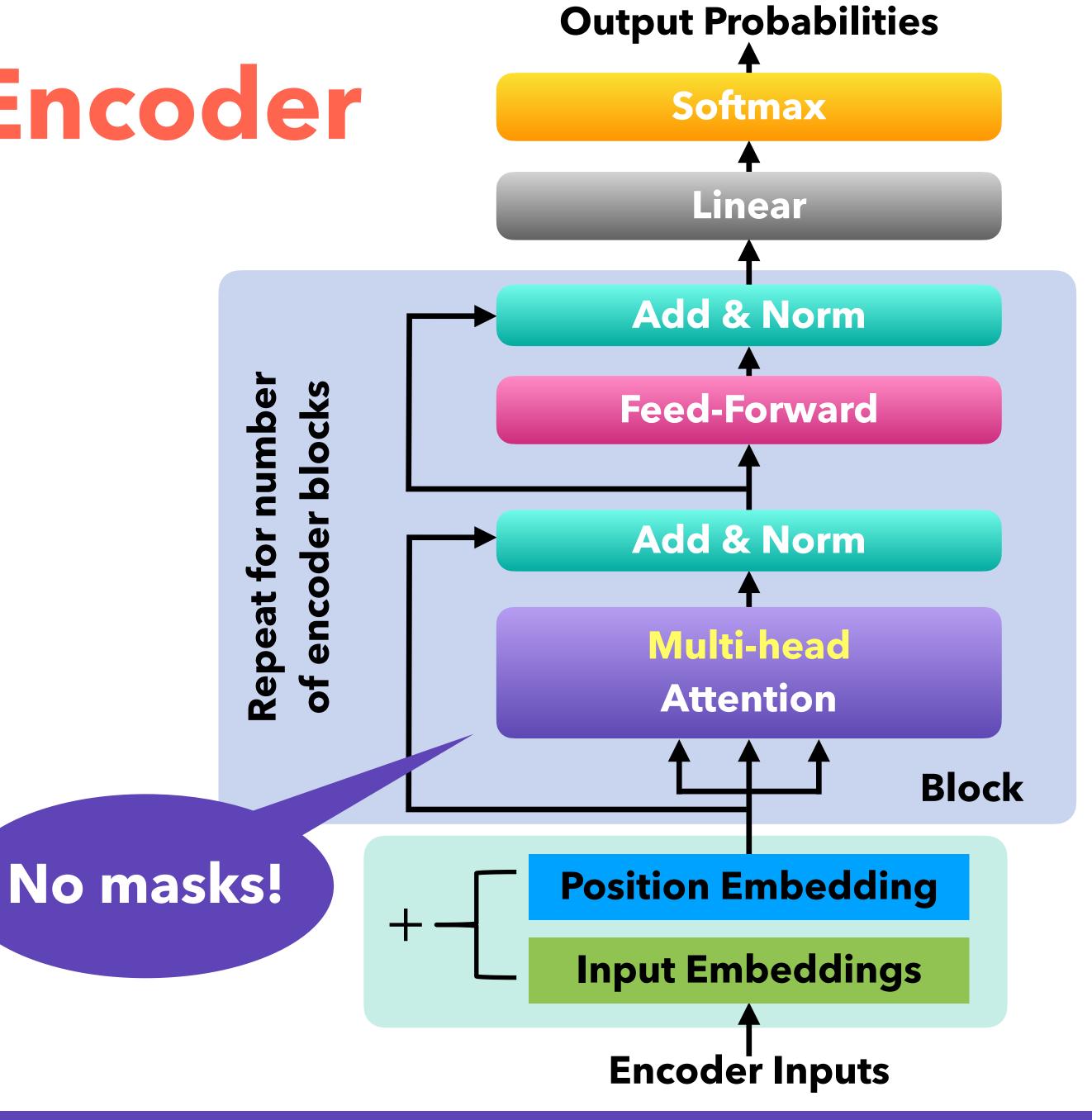
The Transformer Decoder

- The Transformer Decoder is a stack of Transformer Decoder **Blocks**.
- Each Block consists of:
 - Masked Multi-head Self-attention
 - Add & Norm
 - Feed-Forward
 - Add & Norm



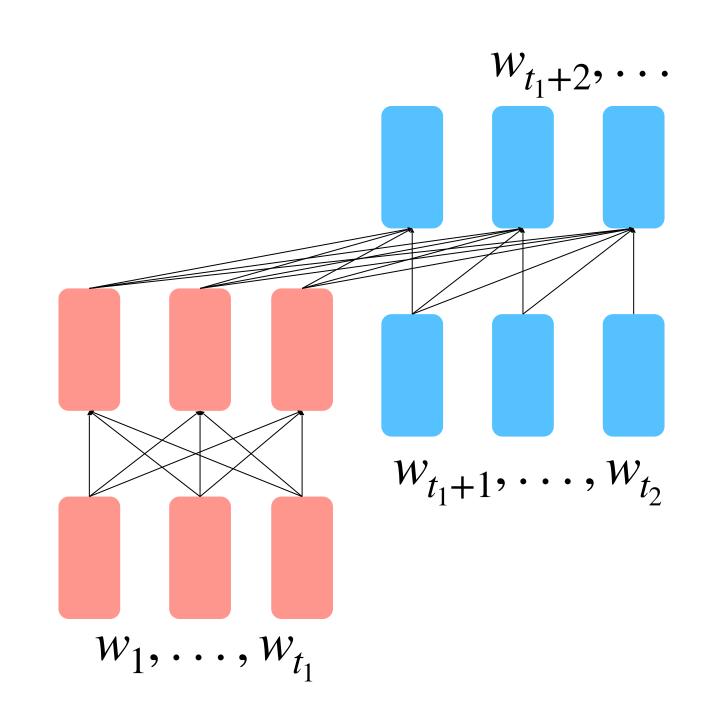
The Transformer Encoder

- The Transformer Decoder constrains to unidirectional context, as for language models.
- What if we want bidirectional context, like in a bidirectional RNN?
- We use Transformer Encoder –
 the ONLY difference is that we
 remove the masking in selfattention.

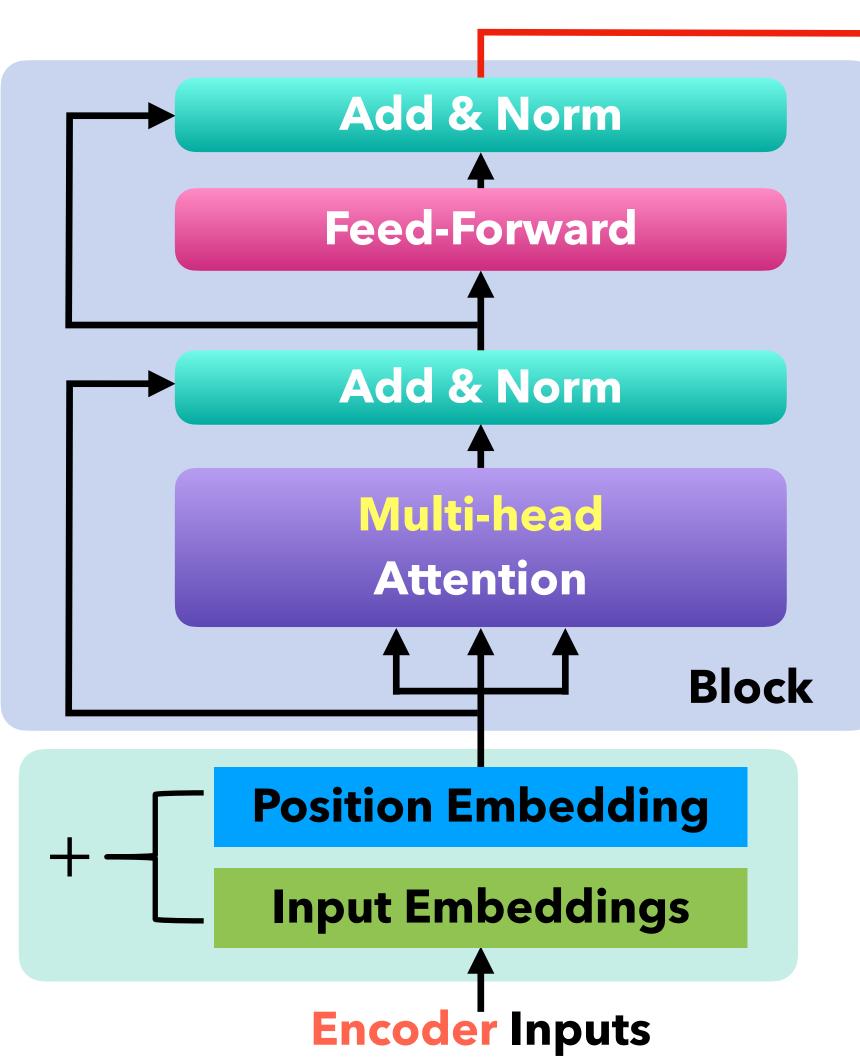


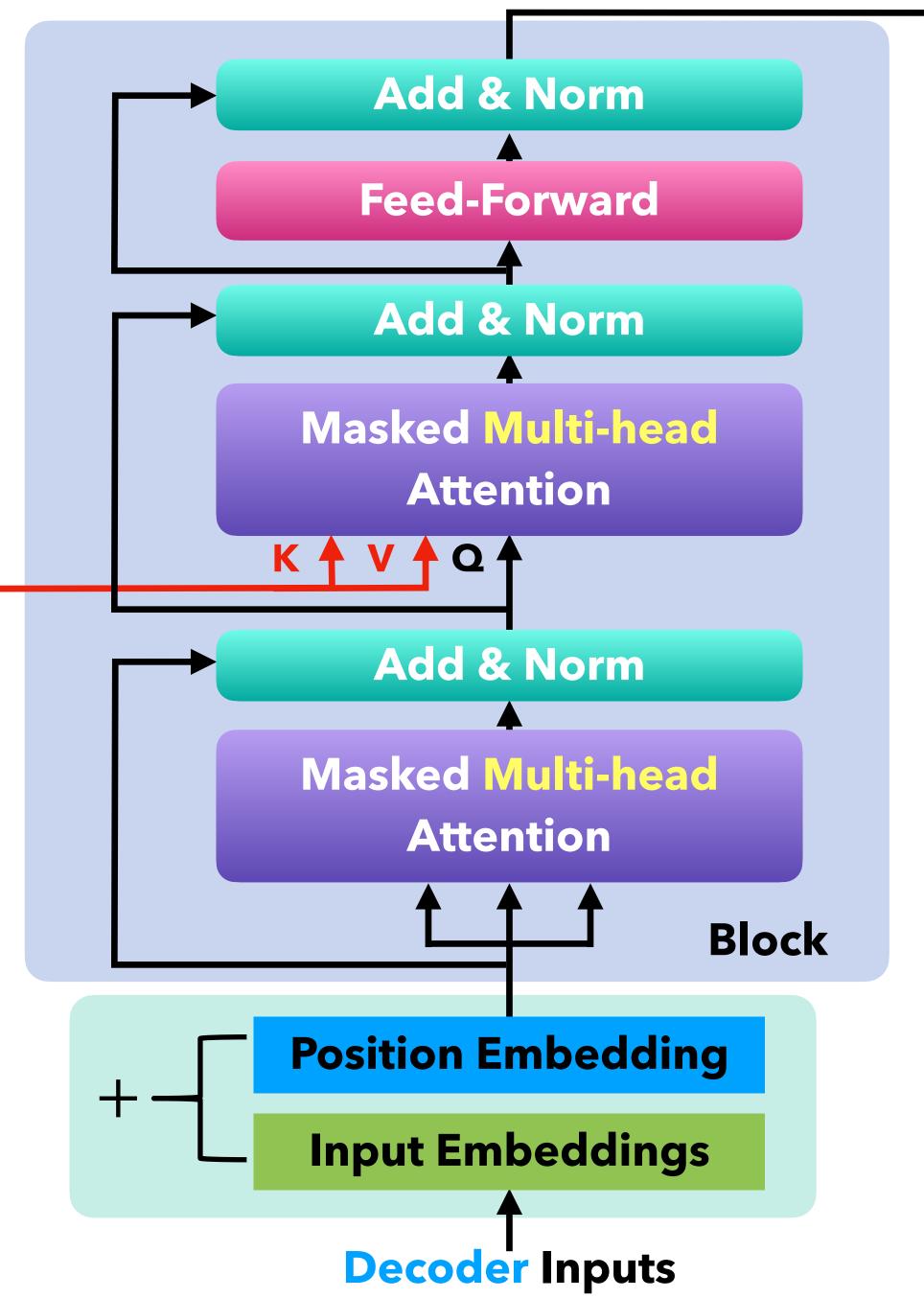
The Transformer Encoder-Decoder

- More on Encoder-Decoder models will be introduced in the next lecture!
- Right now we only need to know that it processes the source sentence with a bidirectional model
 (Encoder) and generates the target with a unidirectional model (Decoder).
- The Transformer Decoder is modified to perform cross-attention to the output of the Encoder.



Cross-Attention





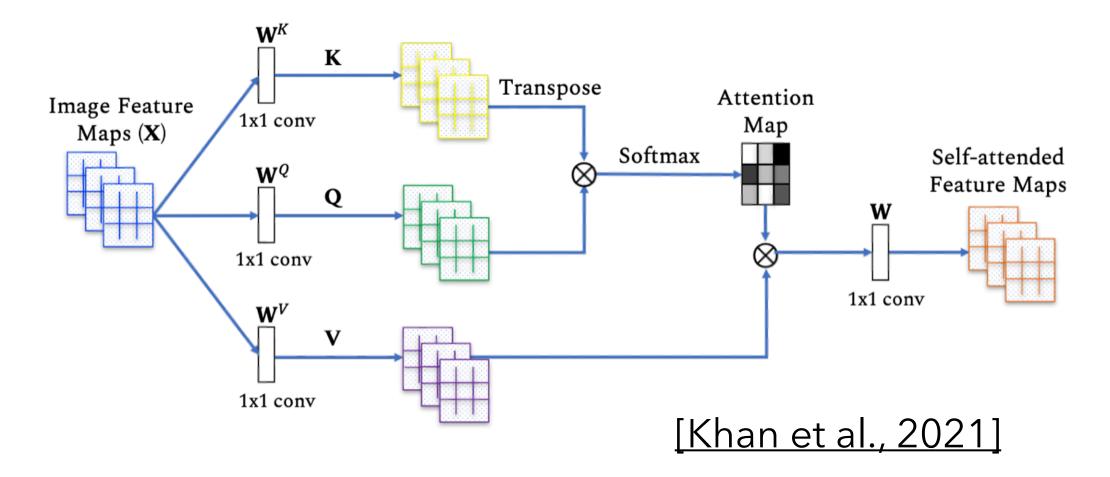
Cross-Attention Details

- Self-attention: queries, keys, and values come from the same source.
- Cross-Attention: keys and values are from Encoder (like a memory); queries are from Decoder.
- Let $h_1, ..., h_n$ be output vectors from the Transformer encoder, $h_i \in \mathbb{R}^d$.
- Let $z_1, ..., z_n$ be input vectors from the Transformer decoder, $z_i \in \mathbb{R}^d$.
- Keys and values from the encoder:
 - $\bullet \quad k_i = W_K h_i$
 - $\bullet \quad v_i = W_V h_i$
- Queries are drawn from the decoder:
 - $\bullet \ q_i = W_Q z_i$

The Revolutionary Impact of Transformers

- Almost all current-day leading language models use Transformer building blocks.
 - E.g., GPT1/2/3/4, T5, Llama 1/2, BERT, ... almost anything we can name
 - Transformer-based models dominate nearly all NLP leaderboards.
- Since Transformer has been popularized in language applications, computer vision also adapted Transformers, e.g., Vision
 Transformers.

What's next after
Transformers?



Thank you!

- Many thanks to John Hewitt for sharing his amazing slide deck on Transformers for us to adapt from!
- Also thanks to the online course from Hung-yi Lee, based on which we developed the walk-through
 of self-attention and multi-head attention!