

Statistical inference - Course Project: Part 2

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Synopsis

This project aims to analyze the Tooth Growth database using confidence intervals and/or tests. This dataset has 60 observations and 3 variables, and a summary was provided with a brief of exploratory analysis. As a results of this project, supplement type has no effect on tooth growth and increasing the dose level leads to increased tooth growth.

Requeriments, Settings, and Load Data

- Requirements to reproduce this exercise: `ggplot2`, `dplyr`, and `datasets`.
- Make a copy of the original dataset and converting into a `dplyr` table.

```
dataset_tg <- ToothGrowth
dataset_tg <- tbl_df(dataset_tg)
```

```
## Warning: 'tbl_df()' was deprecated in dplyr 1.0.0.
## Please use 'tibble::as_tibble()' instead.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see where this warning was generated.
```

A brief exploratory analysis of the dataset

A data frame with 60 observations on 3 variables.

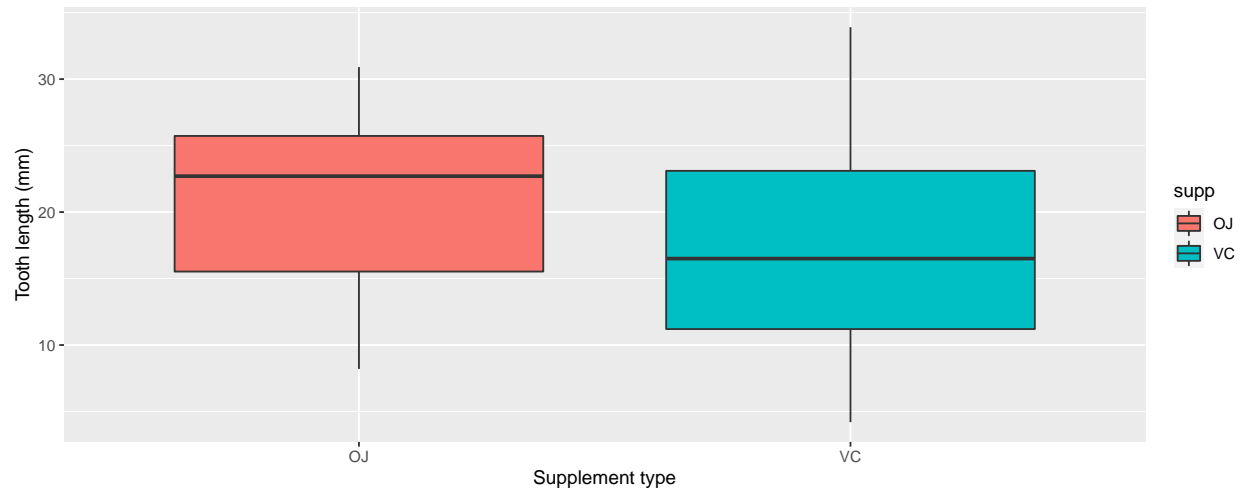
How is the data structure:

```
## tibble [60 x 3] (S3: tbl_df/tbl/data.frame)
##  $ len : num [1:60] 4.2 11.5 7.3 5.8 6.4 10 11.2 11.2 5.2 7 ...
##  $ supp: Factor w/ 2 levels "OJ","VC": 2 2 2 2 2 2 2 2 2 2 ...
##  $ dose: num [1:60] 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 0.5 ...
```

Note: The experiment counts with two kinds of supplements (VC or OJ) and there are 3 dose variation (0.5, 1.0, and 2.0 mg/day).

To synthesize all information we will use one graph.

```
ggplot(aes(x=supp, y=len), data=dataset_tg) + geom_boxplot(aes(fill=supp)) + xlab("Supplement type") + ylab("Tooth length (mm)")
```



Provide a basic summary of the data

Summary of this dataset:

```
##      len      supp      dose
##  Min.   : 4.20    OJ:30    Min.   :0.500
##  1st Qu.:13.07    VC:30    1st Qu.:0.500
##  Median :19.25                Median :1.000
##  Mean   :18.81                Mean   :1.167
##  3rd Qu.:25.27                3rd Qu.:2.000
##  Max.   :33.90                Max.   :2.000
```

For further more information about each variable, please read this document.

Compare tooth growth by supplement and dose

There are more than one comparison of tooth growth by supplement (OJ and VC) and dose. Thus, to turn this study much clearly we divided this section into 3 parts: Comparison between supplements, 1mg and 0.5 mg dose, and 2 and 1 mg dose.

Test 1: Growth Tooth Differences between supplements OJ and VC We are testing if exist some differences between those supplements. It means, we are looking for a p value greater then 0.05. Thus, we need to assume two hypothesis: H_0 equals means and H_1 means are different.

First of all, we need to check the `len` variance between OJ and VC supplement.

Those variance are far different so the `var.equal` should be set to `FALSE` (Len Variance using OJ = 43.6334368 and Len Variance using VC = 68.3272299). Now, we can use `t.test` to compare the supplements performances are the same.

```
t.test(dataset_tg_OJ$len, dataset_tg_VC$len, paired = FALSE, var.equal = FALSE)
```

```
##
##  Welch Two Sample t-test
##
```

```
## data: dataset_tg_OJ$len and dataset_tg_VC$len
## t = 1.9153, df = 55.309, p-value = 0.06063
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.1710156 7.5710156
## sample estimates:
## mean of x mean of y
## 20.66333 16.96333
```

The p-value of the test is 0.06. It means we do not have evidence to reject the null hypothesis. Supplement types seems to have no impact on Tooth growth.

Test 2: Growth Tooth Differences by dosages 2 and 1 mg/day For this test we define the H_0 as the null hypotheses of equal means between the two groups, versus the alternative hypothesis (H_1) that the two means are different.

```
t.test(filter(dataset_tg,dose==2)$len, filter(dataset_tg,dose==1)$len, paired = FALSE, var.equal = TRUE)

##
## Two Sample t-test
##
## data: filter(dataset_tg, dose == 2)$len and filter(dataset_tg, dose == 1)$len
## t = 4.9005, df = 38, p-value = 1.811e-05
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.735613 8.994387
## sample estimates:
## mean of x mean of y
## 26.100 19.735
```

As results of the `t.test` we have enough evidence to reject the null hypothesis (H_0). It means if I increase the dosage from 1mg to 2mg creates an positive effect on tooth length.

Test 3: Growth Tooth Differences between supplements OJ and VC For this test we define the H_0 as the null hypotheses of equal means between the two groups, versus the alternative hypothesis (H_1) that the two means are different.

```
t.test(filter(dataset_tg,dose==1)$len, filter(dataset_tg,dose==0.5)$len, paired = FALSE, var.equal = TRUE)

##
## Two Sample t-test
##
## data: filter(dataset_tg, dose == 1)$len and filter(dataset_tg, dose == 0.5)$len
## t = 6.4766, df = 38, p-value = 1.266e-07
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 6.276252 11.983748
## sample estimates:
## mean of x mean of y
## 19.735 10.605
```

As results of the `t.test` we have enough evidence to reject the null hypothesis (H_0). It means if I increase the dosage from 0.5mg to 1mg creates an positive effect on tooth length.

Conclusions

- By the Test 1 we can conclude that supplement has no effect on tooth growth.
- By the Test 2 and Test 3 we can conclude that increasing the dose level leads to increased tooth growth.

Assumptions

- For t-tests regarding tooth length per dosage level, the variances are assumed to be equal for the three combinations of the two groups being compared.