ETM 540 Group Project

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Abstract

The paper aims to study the efficiency of the education system of Organization for Economic Development (OECD) countries and it examines efficiency by looking at the relationship between defined inputs and outputs. Data Envelopement Analysis (DEA), which is a vastly used tool for measuring efficiency, has been conducted to measure the efficiency of the education system of the countries. This project is available on GitHub: https://github.com/AndeyNunes/educationDEA

Introduction

The paper aims to study the efficiency of the education system of 25 countries from the Organization for Economic Development (OECD). Using Data Envelopement Analysis (DEA) to examine relative efficiency between defined inputs and outputs.

- ** What is DEA? ** cite Dr. Anderson's book [2] and Bogetoft and Otto (2011) [3]
- ** What is the question we want to answer using DEA? **
- ** Where does our data come from and how are we planning to use it to answer our question? **

The following OECD countries were dropped from the analysis due to missing data:

For inputs, we considered each country's education spending per student in US dollars and the number of hours teachers spend with students. Per student data will help us to eliminate the size effect of a country with large GDP and thus large budget for education.

As our goal is to evaluate the efficiency of the country's education system, we decided to use PISA score as measumement of success. PISA is widely recognized performance yardstick to assess the competency of a country's school system. PISA focus on three segment: reading, mathematic and science.

Our project looks first at a single input of Total Spending per student and single output of average PISA score. We then expand on the model by including additional input of Total Hours teachers spend and an additional output, tertiary graduation rate, along with the more granualar PISA scores for a multiple input multiple output model.

SITE ALL DATA SOURCES IN REFERENCES, including links to websites

Summary of the data are included in the Appendix.

Table 1: Countries not included due to missing data

Var1	Freq
	1
Australia	1
Belgium	1
Denmark	1
Estonia	1
France	1
Iceland	1
Ireland	1
Lithuania	1
Sweden	1
Switzerland	1
United Kingdom	1

Literature Review

Data Envelope Analysis has been used to evaluate educational efficiencies in OECD countries. [5]

Methodology

In a DEA model, the efficiency of a Decision Making Unit (DMU) is actually a relative efficiency which is determined by comparing the studied unit's performance in producing output with a target. [2] In our study, DMUs are the country's education system. The objective here is to find the efficiency of this education system in making educational achievements, measured by the PISA test scores and college graduation rates, using the resources invested in the system, measured in time and money.

Our DEA model is based on output-orientation because the focus of the model is on improving and optimizing the output based on the input as observed in studied units. We assumed that each country has a given fund for spending on education which is influened by various factors including the GDP, education budgets, and political factors.

The basic DEA model is based on an assumption of constant returns to scale. This means that efficient output with a given input can be scaled up or down in a linear or constant rate. Anderson describes this as exhibiting no limit to how big an operation can get with the ratio of input, whereas often in reality, there are structural differences that inhibit such behavior. [2] The DEA model in our study is based on variable returns to scale (VRS) on the nature of the inputs and outputs. With VRS specified, input can scale up or down, but the output may not scale up or down by the same amount. [3] In fact in the case of test scores, there is an upper limit on the output.

Consider n number of education system DMUj which consumes $x_{i,j}$ inputs and produce $y_{r,j}$ output. The education system operates in variable returns to scale. So this output oriented model can be expressed by a linear algebric model where the objective will be to maximize the efficiency scores of j education system. The efficiency scores can be defined by

 ϕ

Max
$$\phi$$

subject to
$$\sum_{j=1}^{n} x_{i,j} \lambda_{j} \leq x_{i,k} \,\,\forall \,\, i$$

$$\sum_{j=1}^{n} y_{r,j} \lambda_{j} \geq \phi_{r,k} \,\,\forall \,\, r$$

$$\lambda_{j} \geq 0 \,\,\forall \,\, j$$

$$\sum_{j=1}^{n} \lambda_{j} = 1$$

Here, a country's education system is considered efficient if the efficiency score ϕ is 1. The country with score of 1 lies in the efficient frontier which is a linear combination of all the countries with efficiency scores of 1. The countries with scores less than 1 will be considered as relatively inefficient in comparison to the target specified by λ . The vector λ is specific amount of a unit j used in setting the target for performance for studied unit k. To accommodate the variable returns to scale of our studied input and output, a constarint that λ sums up to 1 is added to the model. Also, as it is a output oriented model, the first (input) constraint will be satisfied while trying to exceed the second constraint (output) by as much possible.

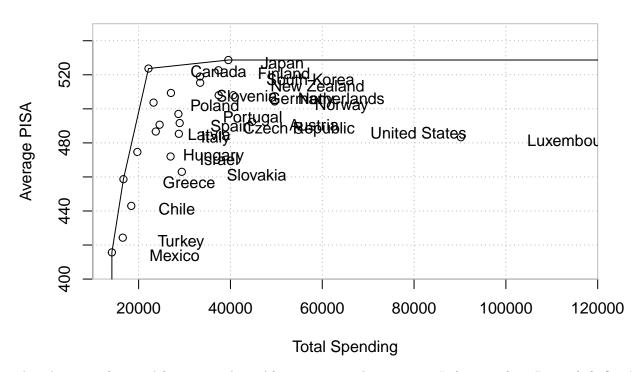
The discussed methodology has been used to perform two DEA model and analysis for the 25 OECD countries for which we have all the data points.

DEA Model

Part A: Single input, single output

For this first part, we will set up and solve a DEA model using total educational spending per student for the input and the aggregated PISA test score average for the single output.

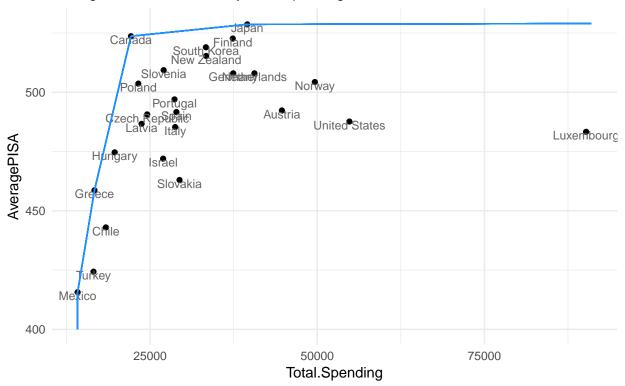
2015 OECD data DEA plot



This plot is not formated for easy reading. After examining the dea.plot() function from Bogetoft & Otto's Benchmarking package, we were able to emulate the graphic in ggplot.

DEA plot of 2015 OECD Countries

Average Education Scores by Total Spending



ggsave("single output DEA.png") # uncomment this to update the png file for the presentation

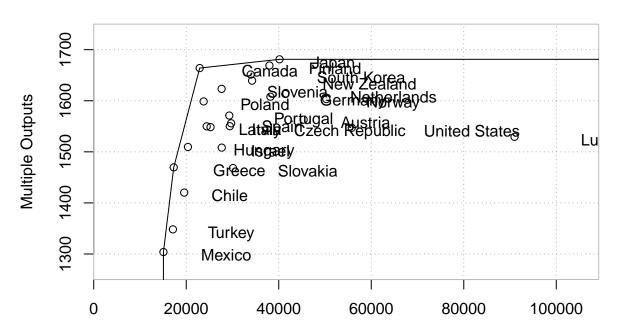
Part B: Multiple Inputs and Outputs

We're also interested in how many hours each country's teachers spend teaching per year as another input, and the tertiary graduation rate as another output. Additionally, we are also using the different science, math, and reading PISA scores that made up the averagePISA input from the single input single output model.

Here's a model with two inputs, total educational spending per student and average teacher hours per year, and two outputs, Average PISA score and tertiary graduation rate.

```
ylab = "Multiple Outputs",
ylim = c(1250,1750), main = "2015 OECD data DEA plot")
```

2015 OECD data DEA plot

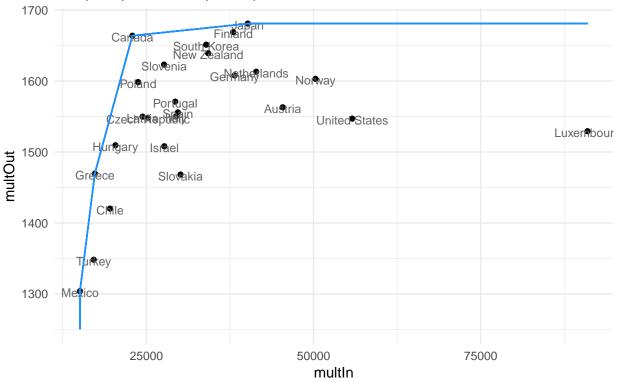


Total Spending + Teaching Hours

```
# warning, the geom_segment calls are not reproducible and must be hand specified
DEAdata$multIn <- DEAdata$Total.Spending + DEAdata$Teaching.Hours
DEAdata$multOut <- DEAdata$SciencePISA + DEAdata$ReadingPISA + DEAdata$MathematicsPISA +
  DEAdata$Tertiary.Graduation.Rate
ggplot(DEAdata, aes(x = multIn, y = multOut)) +
   geom point() +
   geom text(aes(label = Countries), size = 3,
             nudge_x = 2, nudge_y = -2, color = "gray40") +
   geom_segment(aes(x = 91000, y = 1681, xend = 40162, yend = 1681), color = "dodgerblue") +
   geom_segment(aes(x = 40162, y = 1681, xend = 22910, yend = 1664), color = "dodgerblue") +
   geom_segment(aes(x = 22910, y = 1664, xend = 17298, yend = 1470), color = "dodgerblue") +
  geom_segment(aes(x = 17298, y = 1470, xend = 15071, yend = 1304), color = "dodgerblue") +
   geom_segment(aes(x = 15071, y = 1304, xend = 15071, yend = 1250), color = "dodgerblue") +
  theme_minimal() +
   labs(xlab = "Total Spending + Teaching Hours",
        ylab = "SciencePISA + ReadingPISA + MathematicsPISA + Tertiary Graduation Rate") +
   ggtitle("DEA plot of 2015 OECD Countries",
          subtitle = "Multiple Input and Multiple Output")
```

DEA plot of 2015 OECD Countries

Multiple Input and Multiple Output



ggsave("multiple output DEA.png") # uncomment this to update the png file for the presentation

Results and discussion

Saving 6.5×4.5 in image

Single input - output results

The average efficiency for the Total Spending yielding Average PISA score is 0.952.

Table 2: Results of Single input-Single output DEA displaying efficiency scores and positive lambda values

	Eff	Canada	Greece	Japan	Mexico	
Austria	0.931	0.000	0.000	1.000	0.000	
Canada	1.000	1.000	0.000	0.000	0.000	
Chile	0.925	0.313	0.687	0.000	0.000	
Czech Republic	0.936	0.861	0.000	0.139	0.000	
Finland	0.990	0.124	0.000	0.876	0.000	
Germany	0.962	0.120	0.000	0.880	0.000	
Greece	1.000	0.000	1.000	0.000	0.000	
Hungary	0.959	0.555	0.445	0.000	0.000	
Israel	0.899	0.723	0.000	0.277	0.000	
Italy	0.923	0.620	0.000	0.380	0.000	
Japan	1.000	0.000	0.000	1.000	0.000	
South Korea	0.985	0.356	0.000	0.644	0.000	
Latvia	0.929	0.909	0.000	0.091	0.000	
Luxembourg	0.914	0.000	0.000	1.000	0.000	
Mexico	1.000	0.000	0.000	0.000	1.000	
Netherlands	0.961	0.000	0.000	1.000	0.000	
New Zealand	0.978	0.353	0.000	0.647	0.000	
Norway	0.954	0.000	0.000	1.000	0.000	
Poland	0.961	0.937	0.000	0.063	0.000	
Portugal	0.946	0.625	0.000	0.375	0.000	
Slovakia	0.881	0.582	0.000	0.418	0.000	
Slovenia	0.970	0.719	0.000	0.281	0.000	
Spain	0.935	0.609	0.000	0.391	0.000	
Turkey	0.930	0.000	0.942	0.000	0.058	
United States	0.922	0.000	0.000	1.000	0.000	

Multiple input - output results

The average efficiency for the Total Spending yielding Average PISA score is 0.972.

References

Data Sources

Data sourced from https://data.oecd.org/

[1] Anderson, T. R. (2019) Operations Research Using R

Table 3: Results of Multiple Input Multiple Output DEA displaying efficiency scores and positive lambda

	Eff	Canada	Finland	Greece	Japan	South Korea	Mexico	Poland	Slovenia	Turkey
Austria	0.938	0.119	0.000	0.000	0.881	0.000	0	0.000	0.000	0
Canada	1.000	1.000	0.000	0.000	0.000	0.000	0	0.000	0.000	0
Chile	0.969	0.041	0.072	0.887	0.000	0.000	0	0.000	0.000	0
Czech Republic	0.955	0.602	0.000	0.000	0.000	0.197	0	0.202	0.000	0
Finland	1.000	0.000	1.000	0.000	0.000	0.000	0	0.000	0.000	0
Germany	0.972	0.707	0.000	0.000	0.293	0.000	0	0.000	0.000	0
Greece	1.000	0.000	0.000	1.000	0.000	0.000	0	0.000	0.000	0
Hungary	0.984	0.374	0.000	0.475	0.000	0.000	0	0.151	0.000	0
Israel	0.953	0.229	0.436	0.335	0.000	0.000	0	0.000	0.000	0
Italy	0.971	0.354	0.477	0.142	0.000	0.000	0	0.000	0.027	0
Japan	1.000	0.000	0.000	0.000	1.000	0.000	0	0.000	0.000	0
South Korea	1.000	0.000	0.000	0.000	0.000	1.000	0	0.000	0.000	0
Latvia	0.954	0.503	0.054	0.135	0.000	0.000	0	0.000	0.308	0
Luxembourg	0.924	0.392	0.000	0.000	0.608	0.000	0	0.000	0.000	0
Mexico	1.000	0.000	0.000	0.000	0.000	0.000	1	0.000	0.000	0
Netherlands	0.970	0.249	0.000	0.000	0.751	0.000	0	0.000	0.000	0
New Zealand	0.996	0.353	0.000	0.000	0.647	0.000	0	0.000	0.000	0
Norway	0.977	0.224	0.685	0.000	0.092	0.000	0	0.000	0.000	0
Poland	1.000	0.000	0.000	0.000	0.000	0.000	0	1.000	0.000	0
Portugal	0.956	0.399	0.246	0.000	0.114	0.051	0	0.190	0.000	0
Slovakia	0.909	0.565	0.000	0.000	0.386	0.049	0	0.000	0.000	0
Slovenia	1.000	0.000	0.000	0.000	0.000	0.000	0	0.000	1.000	0
Spain	0.941	0.986	0.000	0.000	0.014	0.000	0	0.000	0.000	0
Turkey	1.000	0.000	0.000	0.000	0.000	0.000	0	0.000	0.000	1
United States	0.943	1.000	0.000	0.000	0.000	0.000	0	0.000	0.000	0

- [2] Anderson, T. R. (2019) Data Envelopment Analysis Using R
- [3] Bogetoft, P., Otto, L. (2011) Benchmarking with DEA, SFS, and R. Springer.
- [4] Gavurova, B., Kocisova, K., Belas, L., & Krajcik, V. (2017). Relative efficiency of government expenditure on secondary education. Journal of International Studies, 10(2), 329-343. doi:10.14254/2071-8330.2017/10-2/23
- [5] Zhu, H. (2019) Create Awesome LaTeX Table with knitr::kable and kableExtra. https://haozhu233.github. io/kableExtra/awesome_table_in_pdf.pdf

Appendix

Data Summary


```
## $ AveragePISA
                                    <dbl> 502, 492, 503, 524, 443, 491, 50...
## $ HDI
                                    <dbl> 0.936, 0.903, 0.913, 0.920, 0.84...
## $ Primary.education
                                    <chr> "9,546", "11,689", "10,211", "9,...
                                    <chr> "12,303", "15,477", "13,070", "1...
## $ Secondary.education
                                    <chr> "20,344", "17,555", "17,320", "0...
## $ Tertiary.education
## $ Total.Spending
                                    <dbl> 42193, 44721, 40601, 22149, 1840...
## $ Tertiary.Graduation.Rate
                                    <dbl> NA, 86.1, 31.4, 93.0, 91.2, 76.4...
                                    <dbl> 59.77, 25.01, 43.90, 37.59, 35.9...
## $ Bachelors.Graduation.rates
## $ Masters
                                    <dbl> 20.53, 20.29, 26.76, 11.78, 10.1...
## $ Doctorates
                                    <dbl> 2.618, 1.862, 0.639, 1.559, 0.26...
## $ Spending.as.percentage.of.GDP <chr> "5.32%", "5.45%", "6.55%", "", "...
                                    <dbl> 825, 658, NA, 761, 1157, 676, NA...
## $ Teaching. Hours
## $ X
                                    <lgl> NA, NA, NA, NA, NA, NA, NA, NA, ...
## $ X.1
                                    <lg> NA, NA, NA, NA, NA, NA, NA, NA, NA, ...
## $ X.2
                                    <lgl> NA, NA, NA, NA, NA, NA, NA, NA, ...
## $ X.3
                                    <lgl> NA, NA, NA, NA, NA, NA, NA, NA, ...
## $ X.4
                                    <lgl> NA, NA, NA, NA, NA, NA, NA, NA, ...
```

Let's glance at the teaching hours and the graduation rate:

head(cbind(data\$Countries, data\$Teaching.Hours, data\$Tertiary.Graduation.Rate))

```
##
        [,1]
                           [,2]
                                          [,3]
                           "825.4093373" NA
## [1,] "Australia"
## [2,] "Austria"
                          "658.2"
                                         "86.079"
## [3,] "Belgium"
                          NA
                                         "31.35"
## [4,] "Canada"
                          "760.623341"
                                         "93.005"
## [5,] "Chile"
                          "1157.36"
                                         "91.196"
## [6,] "Czech Republic" "676.3166667" "76.361"
```

Deleted sections

Part B:

Run a DEA with a single input, but multiple outputs:

Alternative Intro Materials

Education has long been identified as a catalyst for human development. The rise of every civilization has coincided with a shift in attitude towards attaining and valuing knowledge, and the peak of each civilization usually aligns with peaks in their attained knowledge. For this reason, most historical societies tried to place an emphasis in the process of individual citizens attaining the available knowledge to maximize an individual's contributions to society. This process, however, was informal and was only available to a select few.

After the renaissance period, the approach to education process was far or less standarized. Societies realized the need to produce educated individuals that can tackle new problems faced by society and governments throughout the world, started to shape their educational curriculum's based on the country's need. Today, most countries have curricula that are directly based on this but adapted to fit their national goals and cultural values. The focus and the mission of each country's educational administration directly reflects their future aspirations and social, political, and economical goals.

For example, the United States Department of Education's mission statement includes "to promote student achievement and preparation for global competitiveness." In Germany, the education department is grouped with research and controlled under the department of Education and Research. Their mission includes

"promote education and research for they are the foundations on which we will build our future in a changing world". In Mexico, the department's goal is "to create general conditions that permit the assurance of quality education to all Mexicans". These differing mission objectives, though all noble, point out the subtle differences each society attaches to the education process.

The subtle differences can also translate to funding policies. Currently, budgets for Education Departments around the world constitues a good percentage of each countries overall GDP. For countries within the "Organization for Economic Development" (OECD), current budgets stand between 4-8 percent of their entire GDP. Globally, the current spending on education alone is estimated at ~5 trillion U.S dollars with this figure estimated to reach ~10 trillion dollars in the year 2030. This is a huge investment without any short term returns. For politicians whose lifespan in the political arena is limited (*Democratic Soceities*), such spending would need justification and buy in.

Additional extra code, ok to delete if not needed for final Thursday deadline

Some quick analysis of the results:

Note that we're missing quite a few elements of data for tertiary graduation rate. We can see that with these changed inputs, Canada, Mexico and Japan remain efficient but several other countries, including Turkey, Slovenia, and Poland have become fully efficient, implying that they do a good job utilizing their teacher's hours efficiently. Greece has the highest weight applied to its graduation rate, implying that they do relatively well on this measure.