**SYDE 556/750**

# Simulating Neurobiological Systems
# Lecture 2: Neurons

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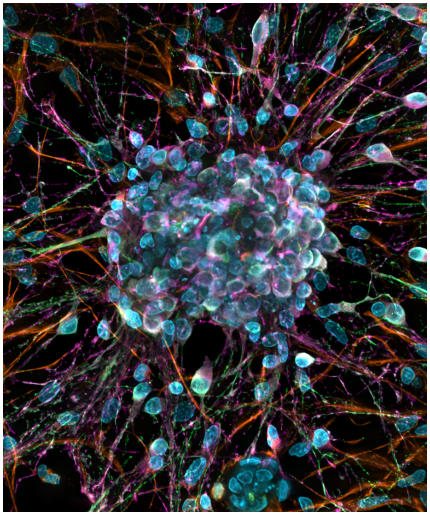
January 9 & 14, 2020



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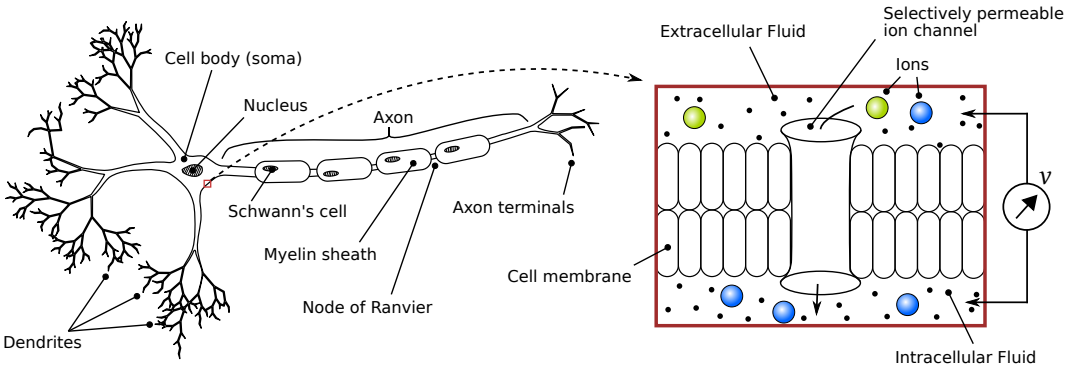
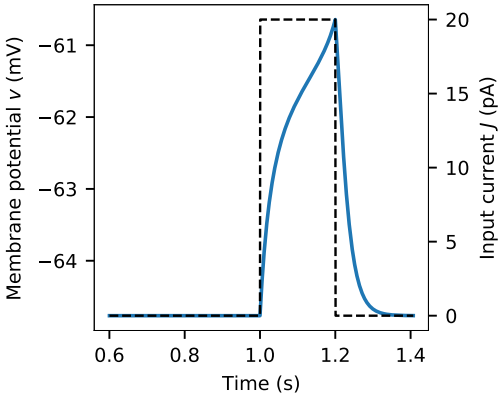
# Textbook Neuron and Cell Membrane



# Injecting a Current Into a Detailed Neuron Model




Computer simulation of an Hodgkin-Huxley type neuron with Traub kinematics (Roger D. Traub and Richard Miles, *Neuronal Networks of the Hippocampus*, Cambridge University Press, 1991)

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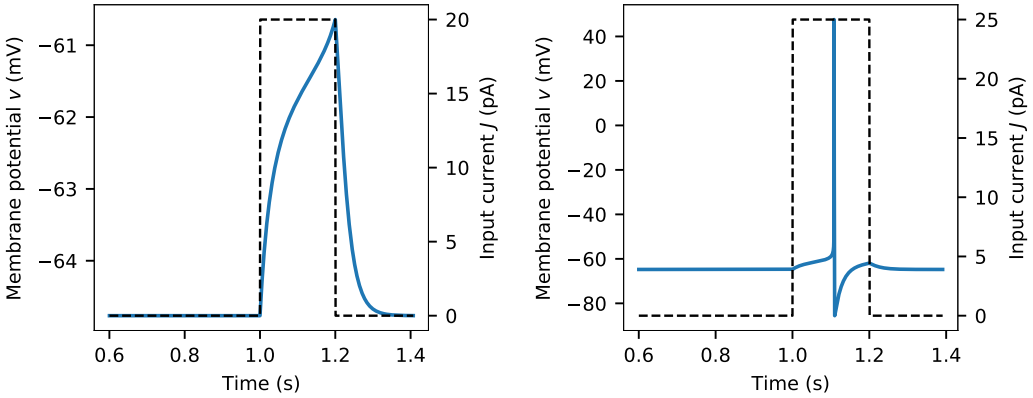


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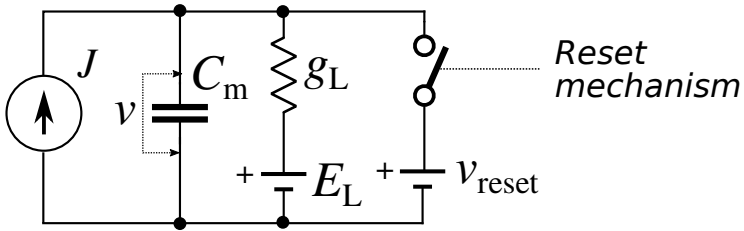
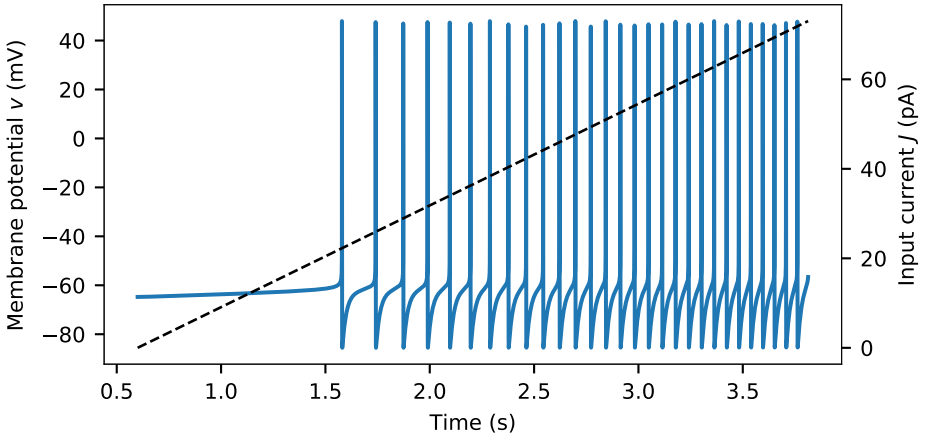
# The Leaky Integrate-and-Fire Equivalent Circuit



# Injecting a Current Ramp into a Detailed Neuron Model

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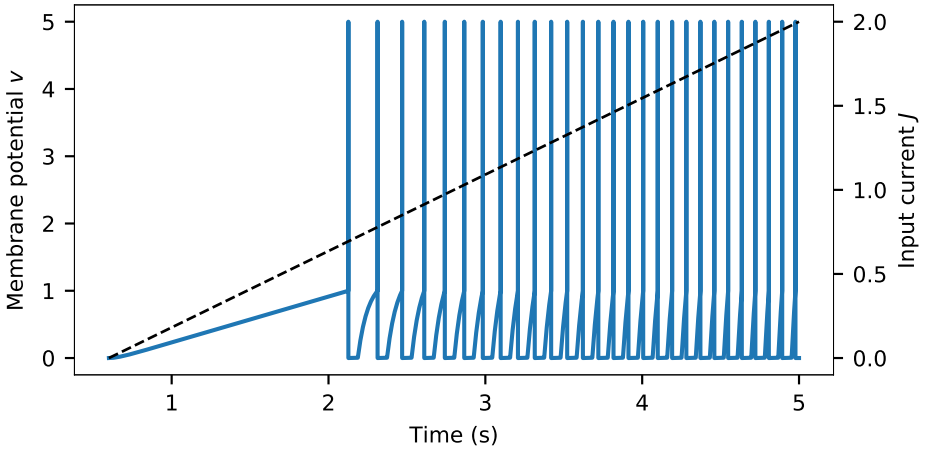
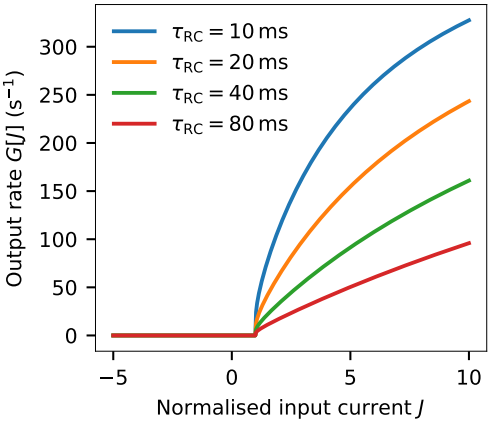
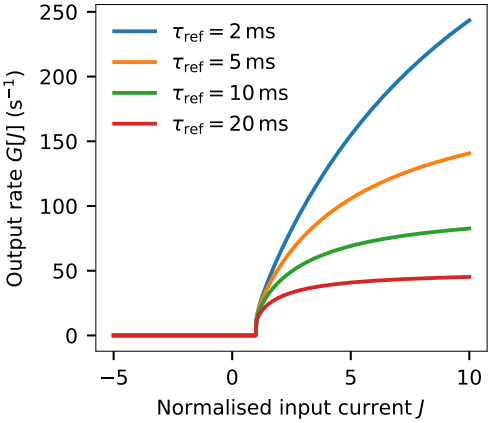
# Injecting a Current Ramp into a LIF Neuron Model

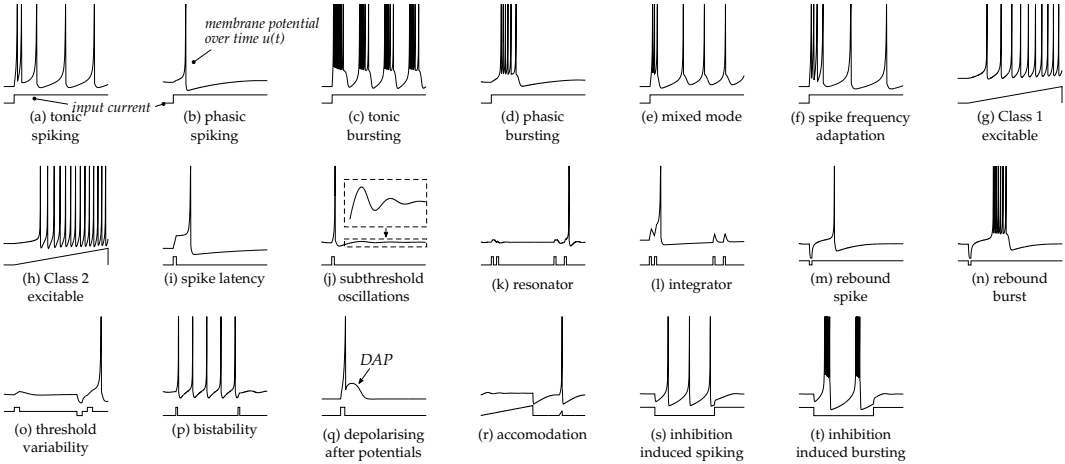


# Exploring the LIF Rate Approximation



# Limitations of the LIF Neuron Model



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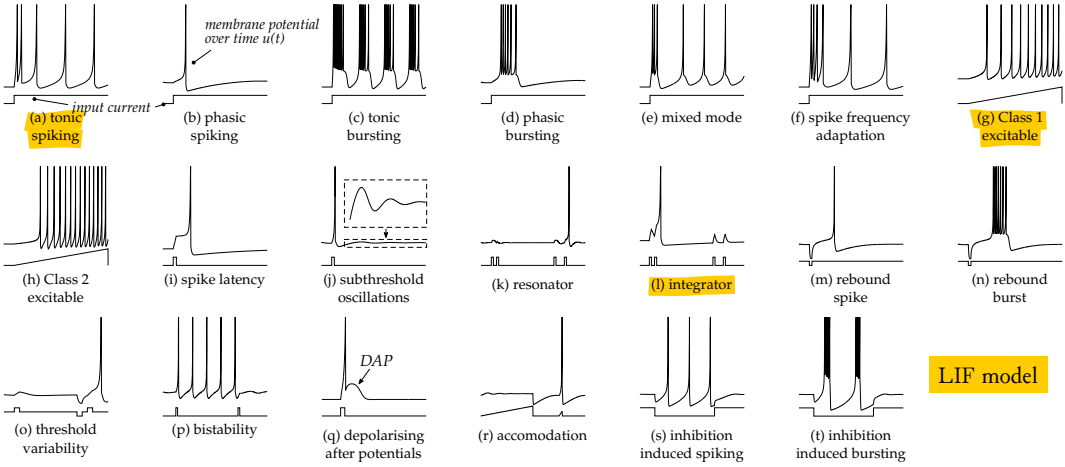
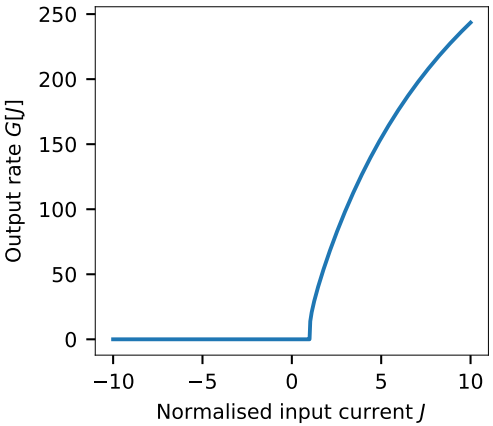


# Artifical Rate Neurons: LIF

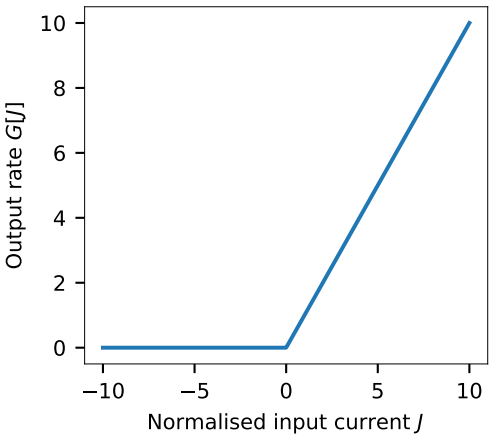



$$G[J] = \frac{1}{\tau_{\text{ref}} - \tau_{\text{RC}} \log\left(1 - \frac{1}{J}\right)}$$

**Usefulness to neurobiological systems modellers:**

- ⊕ Biologically motivated
- ⊕ Captures saturation effects
- ● Relatively slow to evaluate numerically (for machine-learning people)
- ⊖ Spike onset is smooth in noisy systems

# Artifical Rate Neurons: ReLU

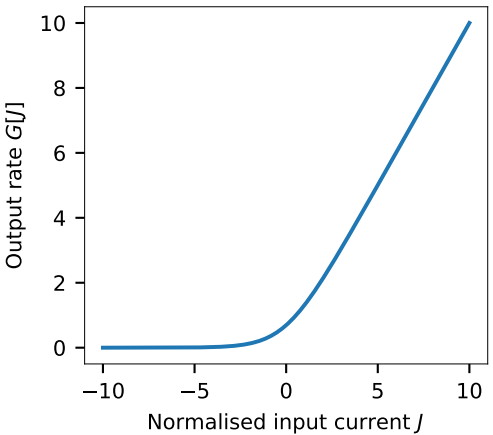



$$G[J] = \max\{0, J\}$$

**Usefulness to neurobiological systems modellers:**

- ⊕ Fast to evaluate
- ● Rough approximation of the LIF response curve
- ⊖ Does not capture saturation effects
- ⊖ Spike onset is smooth in noisy systems

# Artifical Rate Neurons: Smooth ReLU (Softplus)

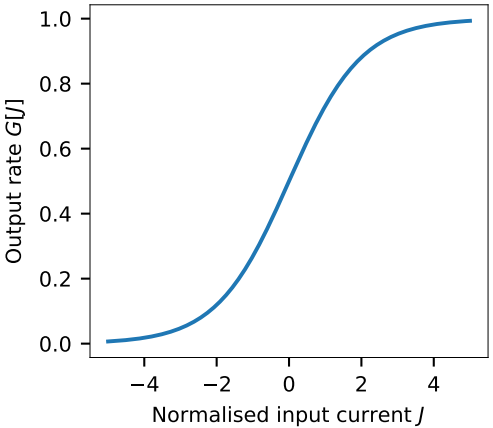



$$G[J] = \log(1 + \exp(J))$$

**Usefulness to neurobiological systems modellers:**

- ⊕ Models smooth spike onset
- ● Rough approximation of the LIF response curve
- ⊖ Does not capture saturation effects

# Artifical Rate Neurons: Logistic Function

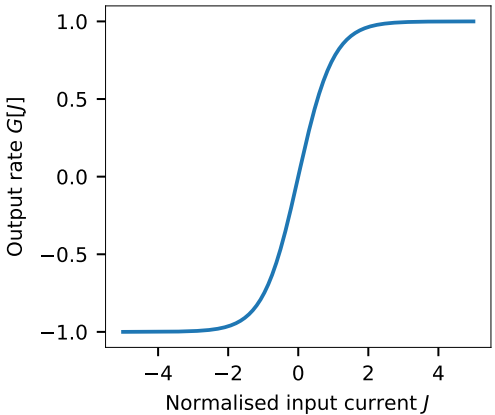



$$G[J] = \frac{1}{1 + e^{-J}}$$

**Usefulness to neurobiological systems modellers:**

- Models smooth spike onset and saturation (?)

# Artifical Rate Neurons: Hyperbolic Tangent




$$G[J] = \tanh(J) = \frac{e^{J} - e^{-J}}{e^{J} + e^{-J}}$$

**Usefulness to neurobiological systems modellers:**

- Models smooth spike onset and saturation (?)
- Negative rates

# Image sources

**Title slide**
Image of rat primary cortical neurons in culture.
Author: ZEISS Microscopy, `http://www.zeiss.com/celldiscoverer`.
From Wikimedia.