

# **EduElevators with Standard Bank**



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# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

**NATIONAL  
SENIOR CERTIFICATE/  
NASIONALE  
SENIOR SERTIFIKAAT**

**GRADE/GRAAD 12**

**MATHEMATICS P2/WISKUNDE V2**

**NOVEMBER 2018**

**MARKING GUIDELINES/NASIENRIGLYNE**

**MARKS/PUNTE: 150**

**These marking guidelines consist of 24pages.  
Hierdie nasienriglyne bestaan uit 24 bladsye.**

**NOTE:**

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent accuracy applies in ALL aspects of the marking memorandum. Stop marking at the second calculation error.
- Assuming answers/values in order to solve a problem is NOT acceptable.

**NOTA:**

- As 'n kandidaat 'n vraag TWEE KEER beantwoord, sien slegs die EERSTE poging na.
- As 'n kandidaat 'n antwoord van 'n vraag doodtrek en nie oordoen nie, sien die doodgetrekte poging na.
- Volgehoue akkuraatheid word in ALLE aspekte van die nasienriglyne toegepas. Hou op nasien by die tweede berekeningsfout.
- Om antwoorde/waardes te aanvaar om 'n probleem op te los, word NIE toegelaat NIE.

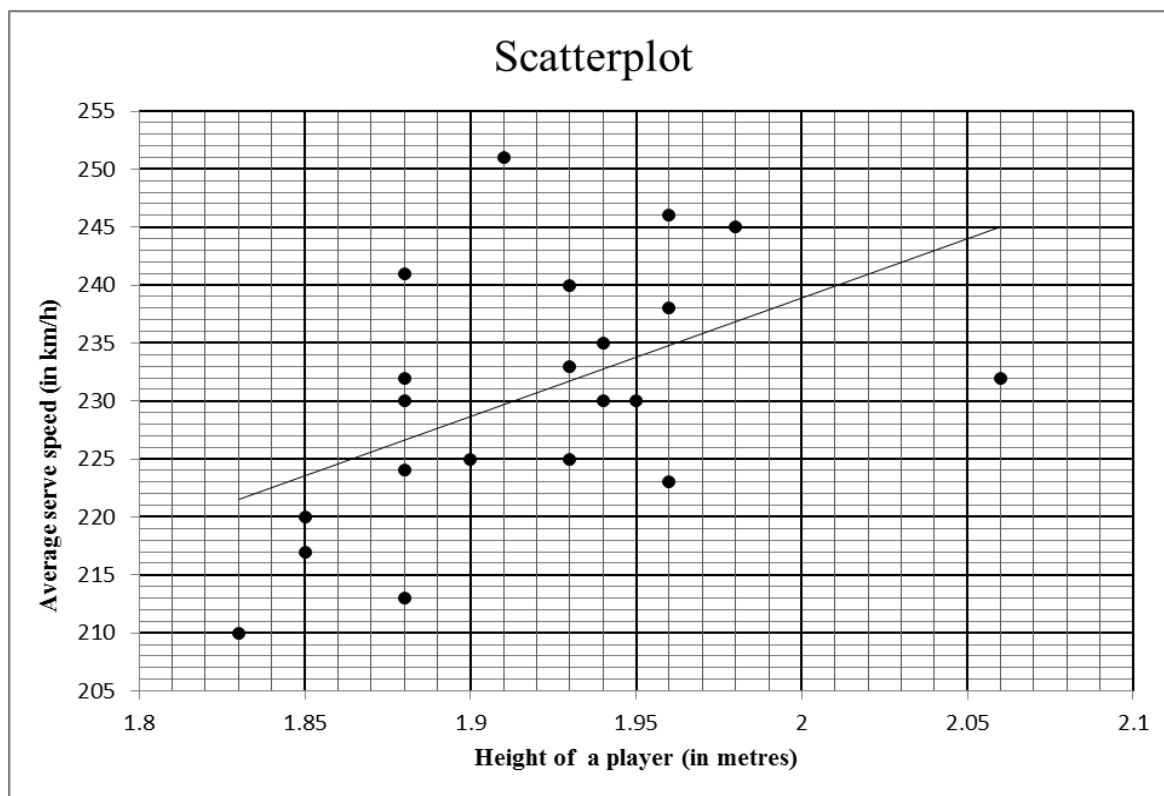
<b>GEOMETRY • MEETKUNDE</b>	
<b>S</b>	<b>A mark for a correct statement (A statement mark is independent of a reason)</b>
	<i>'n Punt vir 'n korrekte bewering ( 'n Punt vir 'n bewering is onafhanklik van die rede)</i>
<b>R</b>	<b>A mark for the correct reason (A reason mark may only be awarded if the statement is correct)</b>
	<i>'n Punt vir 'n korrekte rede ( 'n Punt word slegs vir die rede toegeken as die bewering korrek is)</i>
<b>S/R</b>	<b>Award a mark if statement AND reason are both correct</b>
	<i>Ken 'n punt toe as die bewering EN rede beide korrek is</i>

**QUESTION/VRAAG 1**

1.1.1	140 items	✓ answer (1)
1.1.2	Modal class/modale klas: $20 < x \leq 30$ minutes <b>OR/OF</b> $20 \leq x < 30$ minutes	✓ answer (1) ✓ answer (1)
1.1.3	Number of minutes taken = 20 minutes	✓ answer (1)
1.1.4	140 – 126 [Accept: 124 to 128] 14 orders (12 to 16) <div>Answer only: Full marks</div>	✓ 126 ✓ answer (2)
1.1.5	75 <sup>th</sup> percentile is at 105 items =37 minutes [accept 36 – 38 minutes] <div>Answer only: Full marks</div>	✓ 105 ✓ answer (2)
1.1.6	Lower quartile is at 35 items =21,5 min [accept 21 – 23 min] IQR = 37 – 21,5 = 15,5 min [accept 13 – 17 min] <div>Answer only: Full marks</div>	✓ lower quartile ( $Q_1$ ) ✓ answer (2)

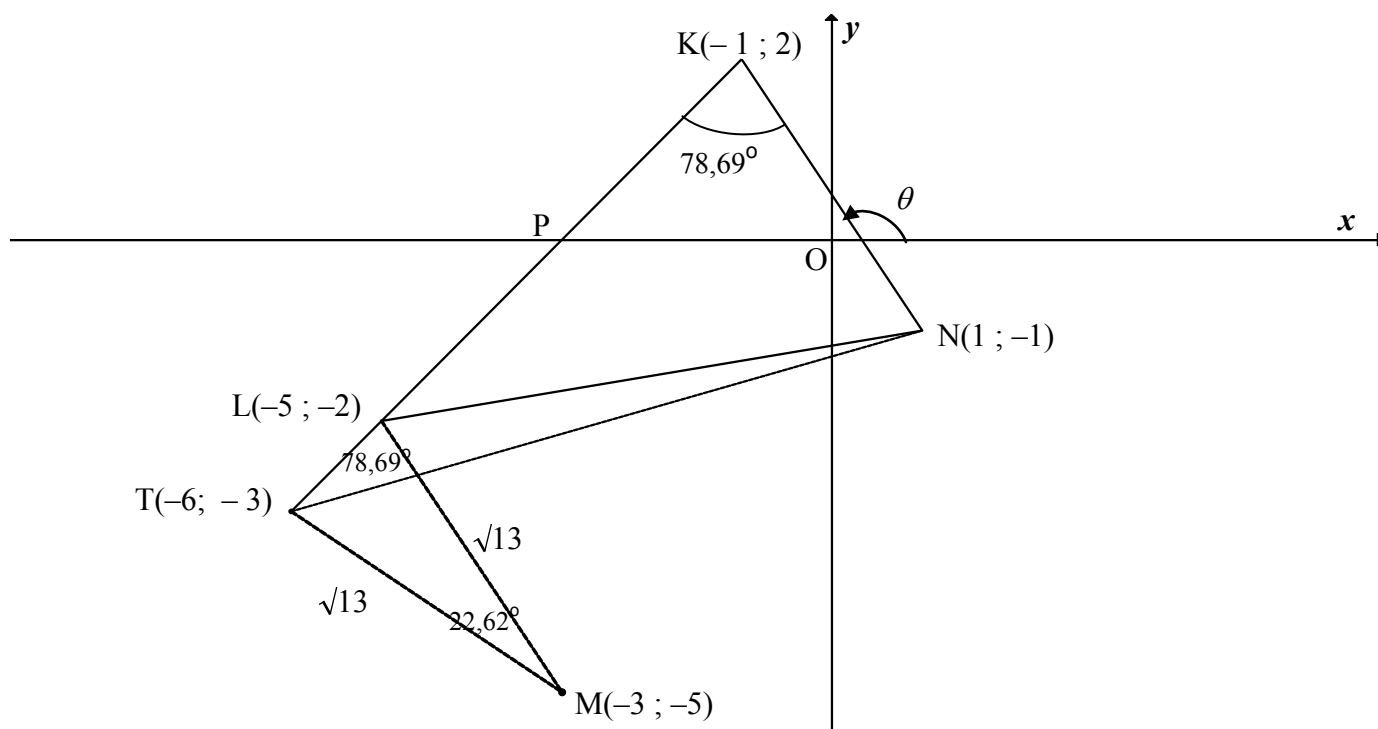
35	70	75	80	80
90	100	100	105	105
110	110	115	120	125

1.2.1(a)	$\bar{x} = \frac{1420}{15}$ = R94,666.. = R94,67 <div>Answer only: Full marks</div>	✓ 1420 ✓ answer (2)
1.2.1(b)	$\sigma = R22,691... = R22,69$	✓✓ answer (2)
1.2.2(a)	They both collected the <b>same (equal) amount</b> in tips, i.e. R1 420 over the 15-day period.  <i>Hulle albei het dieselfde bedrag met footjies ontvang, nl. R1 420 oor die 15 dae-tydperk</i>	✓ answer (1)
1.2.2(b)	Mary's standard deviation is smaller than Reggie's which suggests that there was <b>greater variation in the amount of tips that Reggie collected</b> each day compared to the number of tips that Mary collected each day.  <i>Marie se standaardafwyking is kleiner as Reggie s'n wat beteken dat daar groter variasie/verspreiding in die footjies was wat Reggie elke dag ontvang het in vergelyking met die getal footjies wat Marie elke dag ontvang het.</i>	✓ explanation (1)
<b>[15]</b>		

**QUESTION/VRAAG 2**

2.1	251 km/h	✓ answer (1)
2.2.1	$r = 0,52$ OR C	✓ answer (1)
2.2.2	<p>The points are <b>fairly scattered</b> and the least squares regression line is increasing.</p> <p><i>Die punte is <b>redelik verspreid</b> en die kleinste kwadrate-regressielyn neem toe.</i></p>	✓ reason (1)
2.3	<p>There is a weak positive relation hence the height could have an influence</p> <p><i>Daar is 'n swak positiewe verband, tog kan die lengte 'n invloed hê.</i></p> <p><b>OR/OF</b></p> <p>There is no conclusive evidence that the height of a player will influence his/her tennis serve speed.</p> <p><i>Daar is geen duidelike bewys dat die lengte van die speler sy/haar afslaanspoed kan beïnvloed nie.</i></p> <p><b>OR/OF</b></p> <p>There is no conclusive evidence that a taller person will serve faster than a shorter person.</p> <p><i>Daar is geen duidelike bewys dat 'n langer speler vinniger sal afslaan as 'n korter een nie.</i></p>	<p>✓ answer (1)</p> <p>✓ answer (1)</p> <p>✓ answer (1)</p>

2.4	<p>For <math>(0 ; 27,07)</math>, it means that the player has a height of 0 m but can serve at a speed of 27,07 km/h.  <b>It is impossible for a person to have a height of 0 m.</b></p> <p><i>(0 ; 27,07) beteken dat 'n speler 'n lengte van 0 m kan hê en teen 'n spoed van 27,07 km/h kan afslaan. <b>Dit is onmoontlik om 'n lengte van 0 m te hê.</b></i></p> <p><b>OR/OF</b></p> <p>This means that the <b>player does not exist and therefore cannot serve and have a serve speed.</b></p> <p><i>Dit beteken dat die speler nie bestaan nie en daarom nie kan afslaan en 'n afslaanspoed hê nie.</i></p>	<p>✓ explanation (1)</p> <p>✓ explanation (1)</p>
<b>[5]</b>		

**QUESTION/VRAAG 3**

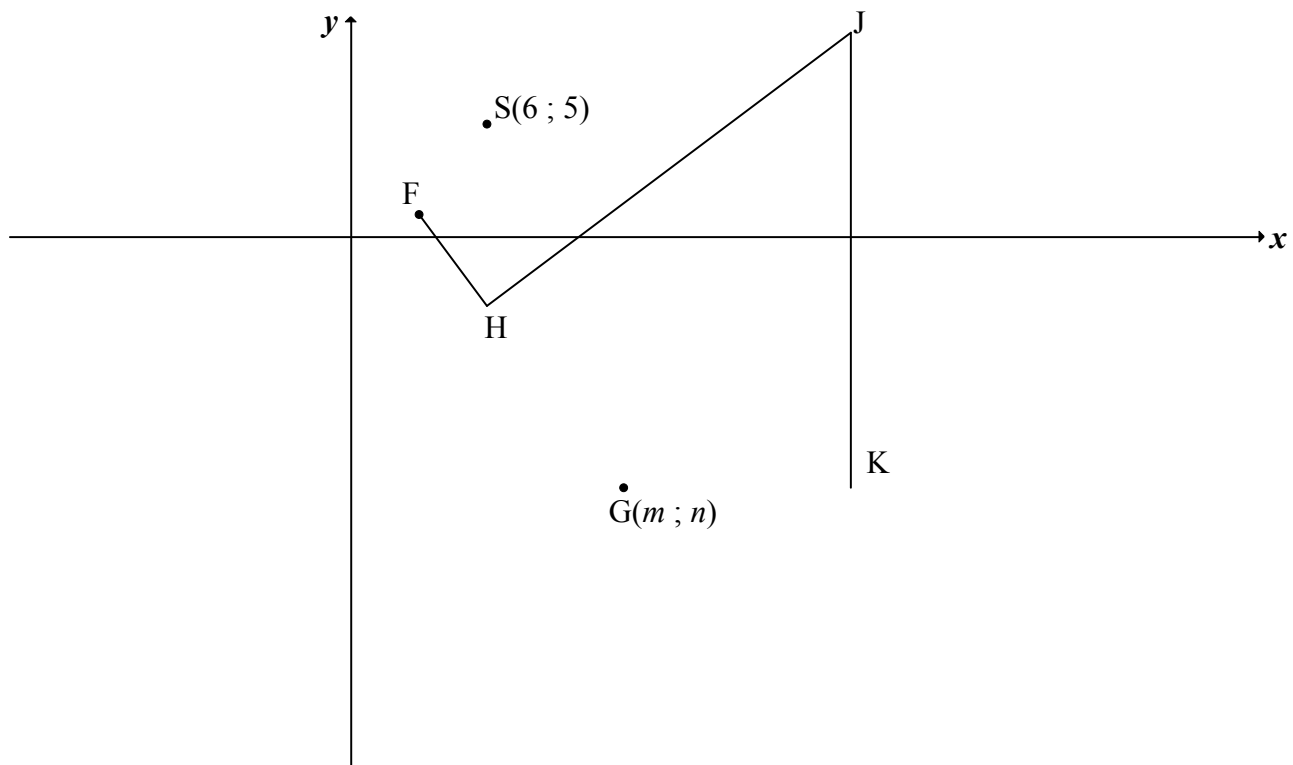
3.1.1	$m_{KN} = \frac{y_2 - y_1}{x_2 - x_1}$ $m_{KN} = \frac{2 - (-1)}{-1 - 1}$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: Full marks</div> $= -\frac{3}{2}$	✓ correct substitution ✓ answer (2)
3.1.2	$\tan \theta = m_{KN} = -\frac{3}{2}$ $\theta = 180^\circ - 56,31^\circ$ $\theta = 123,69^\circ$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: Full marks</div>	✓ $\tan \theta = m_{KN} = -\frac{3}{2}$ ✓ answer (2)
3.2	Inclination $KL = 123,69^\circ - 78,69^\circ = 45^\circ$ [ext $\angle \Delta$ ] $\tan 45^\circ = m_{KL} = 1$	✓ S ✓ $\tan 45^\circ = m_{KL} = 1$ (2)
3.3	$y = x + c$ $2 = -1 + c$ $c = 3$ $y = x + 3$ <b>OR/OF</b> $y - y_1 = 1(x - x_1)$ $y - 2 = 1(x - (-1))$ $y = x + 3$	✓ substitute $(-1; 2)$ and $m$ ✓ equation (2)  ✓ substitute $(-1; 2)$ and $m$ ✓ equation (2)

3.4	$KN = \sqrt{(1+1)^2 + (-1-2)^2}$ $KN = \sqrt{13}$ or 3,61 <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div>	✓ substitute K and N into distance formula ✓ answer (2)
3.5.1	$(x+3)^2 + (y+5)^2 = 13$ ... (1) L is a point on KL $y = x + 3$ ... (2) (2) in (1): $(x+3)^2 + (x+3+5)^2 = 13$ $x^2 + 6x + 9 + x^2 + 16x + 64 = 13$ $2x^2 + 22x + 60 = 0$ $x^2 + 11x + 30 = 0$ $(x+5)(x+6) = 0$ $x = -5$ or $x = -6$ $y = -2$ or $y = -3$ L(-5 ; -2) or (-6 ; -3)  <b>OR/OF</b> $(x+3)^2 + (y+5)^2 = 13$ ... (1) L is a point on KL $y = x + 3 \quad \therefore x = y - 3$ ... (2) (2) in (1): $(y-3+3)^2 + (y+5)^2 = 13$ $y^2 + y^2 + 10y + 25 = 13$ $2y^2 + 10y + 12 = 0$ $y^2 + 5y + 6 = 0$ $(y+2)(y+3) = 0$ $y = -2$ or $y = -3$ $x = -5$ or $x = -6$ L(-5 ; -2) or (-6 ; -3)	✓ equation (1)   ✓ substituting eq (2)  ✓ standard form  ✓ x-values ✓ y-values (5)  ✓ equation (1)  ✓ substituting eq (2)  ✓ standard form ✓ y-values (both) ✓ x-values (both) (5)
3.5.2	Midpoint of KM: (-2 ; -1,5) $\therefore \frac{x_L + 1}{2} = -2$ and $\frac{y_L - 1}{2} = -\frac{3}{2}$ $\therefore L(-5 ; -2)$ <b>OR/OF</b> $m_{KN} = m_{LM}$ $\frac{y - (-5)}{x - (-3)} = -\frac{3}{2}$ $2(x+3+5) = -3(x+3)$ $2x+16 = -3x-9$ $5x = -25$ $x = -5$ $\therefore L(-5 ; -2)$ <div style="border: 1px solid black; padding: 2px; display: inline-block;">Answer only: Full marks</div>	✓ midpoint of KM  ✓ x value ✓ y value (3)  ✓ $m_{LM} = m_{KN}$  ✓ x value ✓ y value (3)



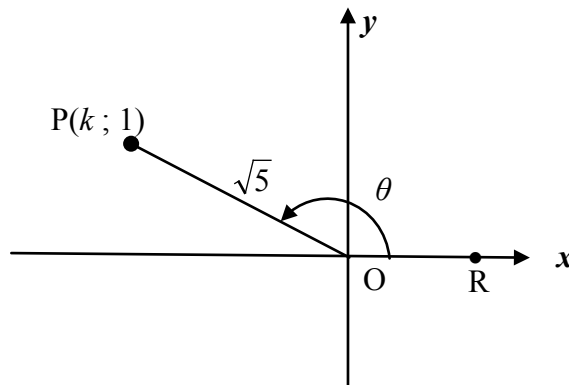
	<p><b>OR/OF</b></p> <p>N→M: <math>(x; y) \rightarrow (x - 4; y - 4)</math>  <math>\therefore L(-1 - 4; 2 - 4)</math>  <math>\therefore L(-5; -2)</math></p> <p>N→K: <math>(x; y) \rightarrow (x - 2; y + 3)</math>  <math>\therefore L(-3 - 2; -5 + 3)</math>  <math>\therefore L(-5; -2)</math></p>	
	<p><b>OR/OF</b></p> <p>N→M: <math>(x; y) \rightarrow (x - 4; y - 4)</math>  <math>\therefore L(-1 - 4; 2 - 4)</math>  <math>\therefore L(-5; -2)</math></p> <p>N→K: <math>(x; y) \rightarrow (x - 2; y + 3)</math>  <math>\therefore L(-3 - 2; -5 + 3)</math>  <math>\therefore L(-5; -2)</math></p>	
	<p><b>OR/OF</b></p> <p>N→M: <math>(x; y) \rightarrow (x - 4; y - 4)</math>  <math>\therefore L(-1 - 4; 2 - 4)</math>  <math>\therefore L(-5; -2)</math></p> <p>N→K: <math>(x; y) \rightarrow (x - 2; y + 3)</math>  <math>\therefore L(-3 - 2; -5 + 3)</math>  <math>\therefore L(-5; -2)</math></p>	
	<p><b>OR/OF</b></p> <p>N→M: <math>(x; y) \rightarrow (x - 4; y - 4)</math>  <math>\therefore L(-1 - 4; 2 - 4)</math>  <math>\therefore L(-5; -2)</math></p> <p>N→K: <math>(x; y) \rightarrow (x - 2; y + 3)</math>  <math>\therefore L(-3 - 2; -5 + 3)</math>  <math>\therefore L(-5; -2)</math></p>	
	<p><b>OR/OF</b></p> <p>N→M: <math>(x; y) \rightarrow (x - 4; y - 4)</math>  <math>\therefore L(-1 - 4; 2 - 4)</math>  <math>\therefore L(-5; -2)</math></p> <p>N→K: <math>(x; y) \rightarrow (x - 2; y + 3)</math>  <math>\therefore L(-3 - 2; -5 + 3)</math>  <math>\therefore L(-5; -2)</math></p>	<p>✓ transformation</p> <p>✓ x value ✓ y value</p> <p>(3)</p>
3.6	<p>T(-6; -3) (from Question 3.5.1)</p> <p><math>KT = \sqrt{(-1 - (-6))^2 + (2 - (-3))^2}</math>  <math>= \sqrt{50}</math></p> <p><math>KN = \sqrt{13}</math> (CA from 3.4)</p> <p>Area of <math>\Delta KTN = \frac{1}{2} KT \cdot KN \sin \hat{LKN}</math>  <math>= \frac{1}{2} \sqrt{50} \cdot \sqrt{13} \sin 78,69^\circ</math>  <math>= 12,50 \text{ square units}</math></p>	<p>✓ coordinates of T</p> <p>✓ length of KT</p> <p>✓ substitution into area rule</p> <p>✓ answer</p> <p>(4)</p>



**QUESTION/VRAAG 4**

4.1	$F(3;1)$	✓ $x$ value ✓ $y$ value (2)
4.2	$FS = \sqrt{(6-3)^2 + (5-1)^2}$ $FS = 5$	✓ substitution of F & S ✓ answer (2)
4.3	$FH(FS) : HG = 1 : 2$ $\therefore HG = 2 FH$ $= 10$	✓ $HG = 10$ (1)
4.4	Tangents from common/same point / <i>Raaklyne vanaf gemeenskaplike of dieselfde punt</i>	✓ answer (1)
4.5.1	$\hat{F}HJ = 90^\circ$ [tan $\perp$ radius / <i>rkl</i> $\perp$ radius] $FJ^2 = 20^2 + 5^2$ [Pyth theorem/ <i>stelling</i> ] $FJ = \sqrt{425}$ or $5\sqrt{17}$ or 20,62	✓ S ✓ R ✓ S ✓ answer (4)
4.5.2	$(x-m)^2 + (y-n)^2 = 100$	✓ answer (1)

4.5.3	<p> <math>K(22; n)</math>  <math>GK = HG = 10</math>  <math>FH = FS = 5</math>  <math>m = 22 - 10</math>  <math>m = 12</math>  F, H and G are collinear  <i>F, H en G is saamlynig</i>  <math>FG^2 = (12 - 3)^2 + (n - 1)^2</math>  <math>15^2 = 81 + (n - 1)^2</math>  <math>(n - 1)^2 = 144</math>  <math>n - 1 = \pm 12</math>  <math>n \neq 13</math> or <math>n = -11</math>  <math>\therefore G(12; -11)</math>   <b>OR/OF</b>   <math>K(22; n)</math>  <math>GK = HG = 10</math>  <math>FH = FS = 5</math>  <math>m = 22 - 10</math>  <math>m = 12</math>  Let <math>J(22; y)</math>:  <math>FJ^2 = (22 - 3)^2 + (y - 1)^2</math>  <math>425 = 361 + y^2 - 2y + 1</math>  <math>0 = y^2 - 2y - 63</math>  <math>0 = (y - 9)(y + 7)</math>  <math>\therefore y = 9</math> or/of <math>y \neq -7</math>  <math>\therefore n = 9 - 20 = -11</math>  <math>\therefore G(12; -11)</math> </p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> <p>[radius <math>\perp</math> tangent] [radii] [radii]</p> <p>[HJ is a common tangent] [HJ is 'n gemeenskaplike raaklyn]</p> </div> <div style="border: 1px solid black; padding: 5px;"> <math>n^2 - 2n - 143 = 0</math>  <math>(n + 11)(n - 13) = 0</math>  <math>n = -11</math> or <math>n \neq 13</math> </div> </div>	<p>✓ <math>K(22; n)</math></p> <p>✓ value of <math>m</math></p> <p>✓ subst. of F and G in distance formula</p> <p>✓ <math>FG = 15</math></p> <p>✓ simplification/standard form</p> <p>✓ value of <math>n</math></p> <p>✓ coordinates of G (7)</p> <p>✓ <math>K(22; n)</math></p> <p>✓ value of <math>m</math></p> <p>✓ subst. of F and J in distance formula</p> <p>✓ <math>FJ = \sqrt{425}</math></p> <p>✓ standard form</p> <p>✓ value of <math>n</math></p> <p>✓ coordinates of G (7)</p>
<b>[18]</b>		

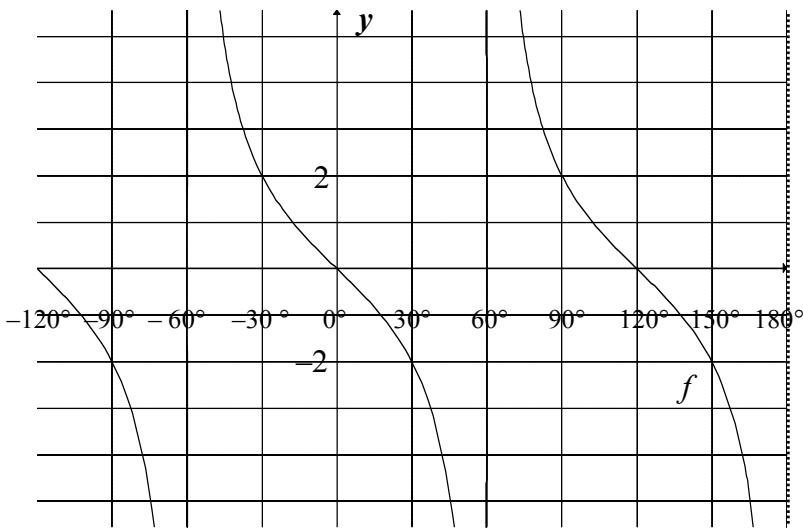
**QUESTION/VRAAG 5**

5.1.1	$k^2 = (\sqrt{5})^2 - 1^2$ $= 4$ $k = -2$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: full marks</div>	✓ substitution into theorem of Pythagoras ✓ answer (2)
5.1.2(a)	$\tan \theta = -\frac{1}{2}$	✓ answer (1)
5.1.2(b)	$\cos(180^\circ + \theta) = -\cos \theta$ $= \frac{2}{\sqrt{5}}$ <div style="border: 1px solid black; padding: 5px; display: inline-block;">Answer only: full marks</div>	✓ reduction ✓ answer (2)
5.1.2(c)	$\sin(\theta + 60^\circ) = \frac{a+b}{\sqrt{20}}$ LHS = $\sin \theta \cos 60^\circ + \cos \theta \sin 60^\circ$ $= \left(\frac{1}{\sqrt{5}}\right)\left(\frac{1}{2}\right) + \left(-\frac{2}{\sqrt{5}}\right)\left(\frac{\sqrt{3}}{2}\right)$ $= \frac{1-2\sqrt{3}}{2\sqrt{5}}$ $= \frac{1-2\sqrt{3}}{\sqrt{20}}$	✓ expansion ✓ subst of $\sin \theta$ ✓ subst of $\cos \theta$ ✓ both special $\angle$ s ✓ $\frac{1-2\sqrt{3}}{2\sqrt{5}}$ (5)
5.1.3	$\tan \theta = -\frac{1}{2}$ $\therefore \theta = 180^\circ - 26,57^\circ$ $\therefore \theta = 153,43^\circ$ $\tan(2\theta - 40^\circ) = \tan[(2 \times 153,43^\circ) - 40^\circ]$ $= \tan 266,87^\circ$ $= 18,3$	✓ $\theta$ ✓ substitution ✓ answer (3)

5.2	<p> <math display="block">\text{LHS} = \frac{\cos x + \sin x}{\cos x - \sin x} - \frac{\cos x - \sin x}{\cos x + \sin x} \quad \text{RHS} = 2 \tan 2x</math> <math display="block">= \frac{(\cos x + \sin x)^2 - (\cos x - \sin x)^2}{(\cos x - \sin x)(\cos x + \sin x)}</math> <math display="block">= \frac{\cos^2 x + 2 \sin x \cos x + \sin^2 x - \cos^2 x + 2 \sin x \cos x - \sin^2 x}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{2(2 \sin x \cos x)}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{2 \sin 2x}{\cos 2x}</math> <math display="block">= 2 \tan 2x</math> <math display="block">= \text{RHS}</math> <p><b>OR/OF</b></p> <math display="block">\text{LHS} = \frac{\cos x + \sin x}{\cos x - \sin x} - \frac{\cos x - \sin x}{\cos x + \sin x} \quad \text{RHS} = 2 \tan 2x</math> <math display="block">= \frac{(\cos x + \sin x)^2 - (\cos x - \sin x)^2}{(\cos x - \sin x)(\cos x + \sin x)}</math> <math display="block">= \frac{(\cos x + \sin x + \cos x - \sin x)(\cos x + \sin x - \cos x + \sin x)}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{(2 \cos x)(2 \sin x)}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{2(2 \sin x \cos x)}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{2 \sin 2x}{\cos 2x}</math> <math display="block">= 2 \tan 2x</math> <math display="block">= \text{RHS}</math> <p><b>OR/OF</b></p> <math display="block">\text{RHS} = 2 \tan 2x</math> <math display="block">= \frac{2 \sin 2x}{\cos 2x}</math> <math display="block">= \frac{2(2 \sin x \cdot \cos x)}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{4 \sin x \cdot \cos x}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{1 + 2 \sin x \cdot \cos x - (1 - 2 \sin x \cdot \cos x)}{\cos^2 x - \sin^2 x}</math> <math display="block">= \frac{(\cos x + \sin x)^2 - (\cos x - \sin x)^2}{(\cos x + \sin x)(\cos x - \sin x)}</math> <math display="block">= \frac{(\cos x + \sin x)^2}{(\cos x + \sin x)(\cos x - \sin x)} - \frac{(\cos x - \sin x)^2}{(\cos x + \sin x)(\cos x - \sin x)}</math> <math display="block">= \frac{\cos x + \sin x}{\cos x - \sin x} - \frac{\cos x - \sin x}{\cos x + \sin x} = \text{LHS}</math> </p>	<p>✓ single fraction</p> <p>✓ expansion</p> <p>✓ simplification (both)</p> <p>✓ double ∠ identity</p> <p>✓ double ∠ identity</p> <p>(5)</p> <p>✓ single fraction</p> <p>✓ difference of two squares</p> <p>✓ simplification (both)</p> <p>✓ double ∠ identity</p> <p>✓ double ∠ identity</p> <p>(5)</p> <p>✓ double ∠ identity</p> <p>✓ double ∠ identity</p> <p>✓ identity &amp; method</p> <p>✓ factorising numerator and denominator</p> <p>✓ writing as 2 terms</p> <p>(5)</p>
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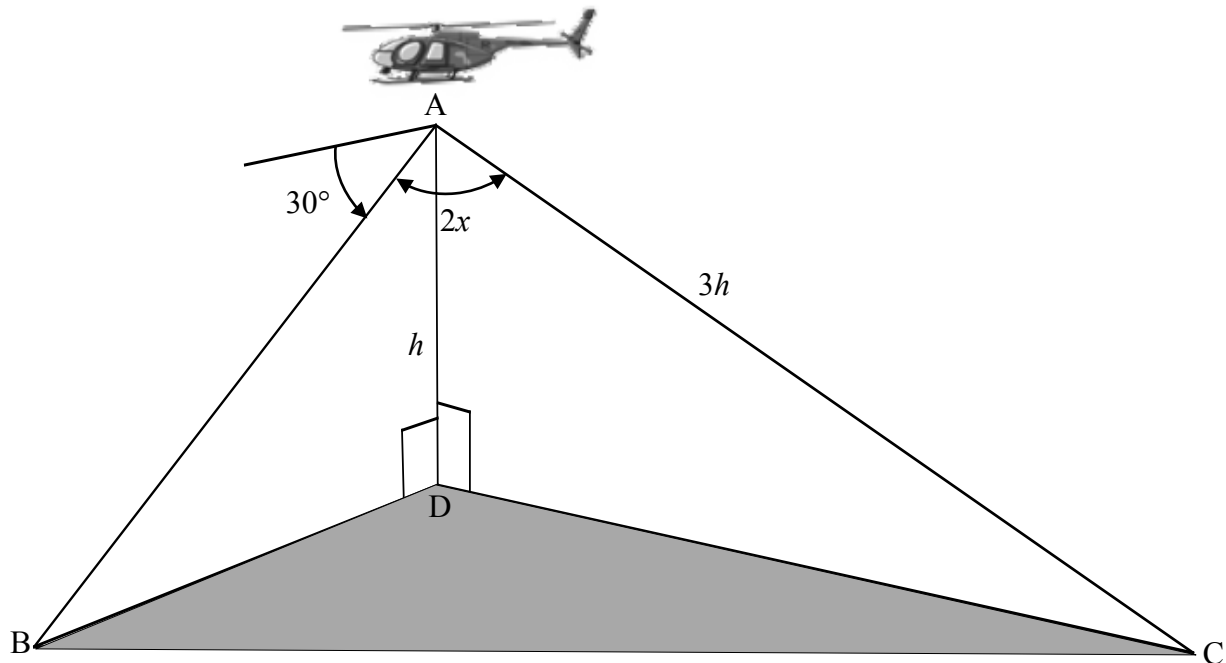
5.3	$\sum_{A=38^{\circ}}^{52^{\circ}} \cos^2 A$ $= \cos^2 38^{\circ} + \cos^2 39^{\circ} + \cos^2 40^{\circ} + \dots + \cos^2 51^{\circ} + \cos^2 52^{\circ}$ $= \sin^2 52^{\circ} + \sin^2 51^{\circ} + \sin^2 50^{\circ} + \dots + \cos^2 51^{\circ} + \cos^2 52^{\circ}$ $= 7(1) + \cos^2 45^{\circ}$ $= 7 + \left(\frac{\sqrt{2}}{2}\right)^2 \quad \text{or} \quad = 7 + \left(\frac{1}{\sqrt{2}}\right)^2$ $= 7\frac{1}{2}$ <p><b>OR/OF</b></p> $\sum_{A=38^{\circ}}^{52^{\circ}} \cos^2 A$ $= \cos^2 38^{\circ} + \cos^2 39^{\circ} + \cos^2 40^{\circ} + \dots + \cos^2 51^{\circ} + \cos^2 52^{\circ}$ $= (\cos^2 38^{\circ} + \sin^2 52^{\circ}) + (\cos^2 39^{\circ} + \sin^2 51^{\circ}) \dots + \cos^2 45^{\circ}$ $= 7(1) + \cos^2 45^{\circ}$ $= 7 + \left(\frac{\sqrt{2}}{2}\right)^2 \quad \text{or} \quad = 7 + \left(\frac{1}{\sqrt{2}}\right)^2$ $= 7\frac{1}{2}$	<p>✓ expansion ✓ co ratio ✓ <math>\cos^2 45^{\circ}</math> ✓ <math>7 \times</math> identity</p> <p>✓ answer (5)</p> <p>✓ expansion ✓ pairing ✓ <math>\cos^2 45^{\circ}</math> ✓ <math>7 \times</math> identity</p> <p>✓ answer (5)</p>
<b>[23]</b>		

**QUESTION/VRAAG 6**

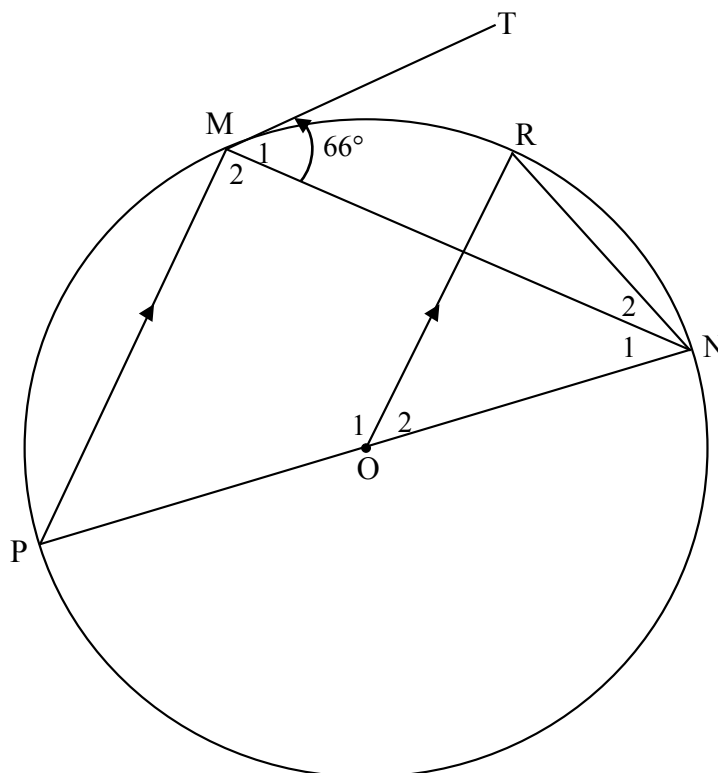
6.1	Period = $120^\circ$	✓ answer (1)
6.2	$2 = -2 \tan \frac{3}{2}x$ $\tan \left( \frac{3}{2}t \right) = -1$ $\frac{3}{2}t = 135^\circ + k.180^\circ \quad \text{OR/OR} \quad \frac{3}{2}t = -45^\circ + k.180^\circ$ $t = 90^\circ + k.120^\circ ; k \in \mathbb{Z} \quad \quad \quad t = -30^\circ + k.120^\circ ; k \in \mathbb{Z}$ <p><b>OR/OR</b></p> $2 = -2 \tan \frac{3}{2}x$ $\tan \left( \frac{3}{2}t \right) = -1$ $\frac{3}{2}t = 135^\circ + k.360^\circ \text{ or/of } \frac{3}{2}t = 315^\circ + k.360^\circ$ $t = 90^\circ + k.240^\circ \text{ or/of } t = 210^\circ + k.240^\circ ; k \in \mathbb{Z}$	✓ equating  ✓ general solution of $\frac{3}{2}t$ ✓ general solution of $t$ (3)  ✓ equating  ✓ general solution of $\frac{3}{2}t$ ✓ general solution of $t$ (3)
6.3		✓ asymptotes: $x = \pm 60^\circ ; x = 180^\circ$ ✓ x-intercepts $0^\circ ; \pm 120^\circ$ ✓ negative shape ✓ $(90^\circ ; 2)$ or $(-30^\circ ; 2)$ or $(30^\circ ; -2)$ or $(-90^\circ ; -2)$ (4)
6.4	$x \in (-60^\circ ; -30^\circ] \text{ or } (60^\circ ; 90^\circ]$ <p><b>OR/OR</b></p> $-60^\circ < x \leq -30^\circ \text{ or } 60^\circ < x \leq 90^\circ$	✓ interval ✓ interval ✓ notation (3) ✓ interval ✓ interval ✓ notation (3)
6.5	$g(x) = -2 \tan \left[ \frac{3}{2}(x + 40^\circ) \right] = f(x + 40^\circ)$ <p>Translation of <math>40^\circ</math> to the left / skuif met <math>40^\circ</math> links</p>	✓ Translation of $40^\circ$ ✓ to the left (2)
<b>[13]</b>		



## QUESTION/VRAAG 7

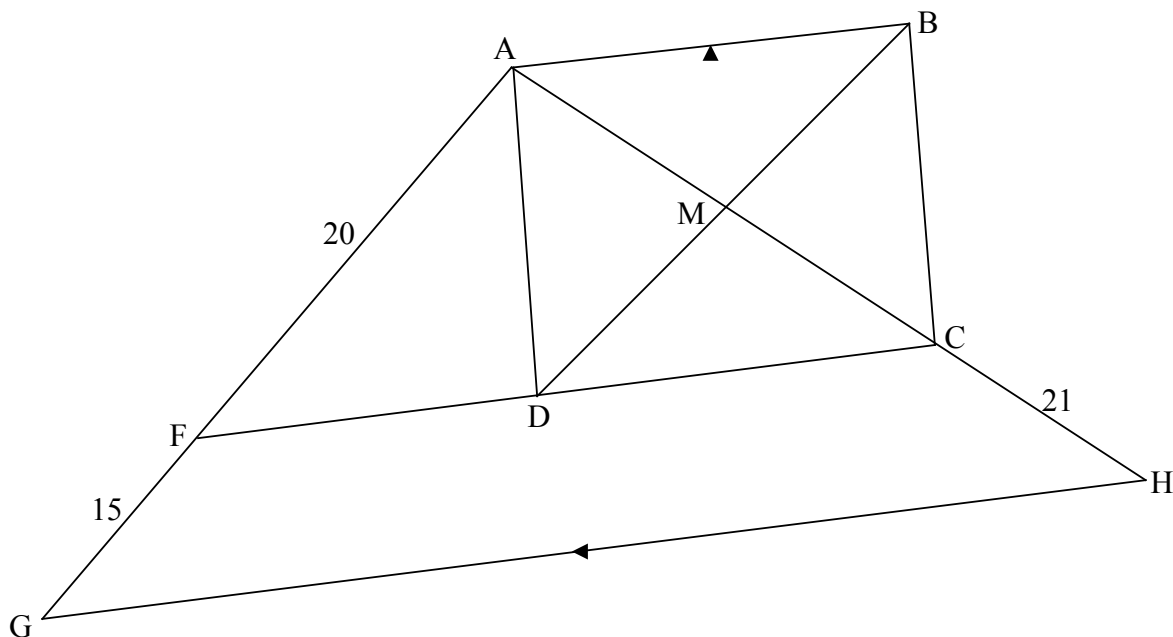


7.1	$\hat{A}BD = 30^\circ$ $\sin 30^\circ = \frac{h}{AB}$ $AB = \frac{h}{\sin 30^\circ}$ <b>OR</b> $AB = \frac{h}{\frac{1}{2}}$ <b>OR</b> $AB = 2h$  <b>OR/OF</b> $\hat{B}AD = 60^\circ$ $\cos 60^\circ = \frac{h}{AB}$ $AB = \frac{h}{\cos 60^\circ}$ <b>OR</b> $AB = \frac{h}{\frac{1}{2}}$ <b>OR</b> $AB = 2h$	$\checkmark \hat{A}BD = 30^\circ$  $\checkmark$ answer (2)  $\checkmark \hat{B}AD = 60^\circ$  $\checkmark$ answer (2)
7.2	$BC^2 = AB^2 + AC^2 - 2AB \cdot AC \cos \hat{B}AC$ $= (2h)^2 + (3h)^2 - 2(2h)(3h) \cos 2x$ $= 13h^2 - 12h^2 (2 \cos^2 x - 1)$ $= 13h^2 - 24h^2 \cos^2 x + 12h^2$ $= 25h^2 - 24h^2 \cos^2 x$ $BC = h\sqrt{25 - 24 \cos^2 x}$	$\checkmark$ use of cosine rule in $\triangle ABC$ $\checkmark$ substitution $\checkmark$ double angle identity $\checkmark 25h^2 - 24h^2 \cos^2 x$ (4)
<b>[6]</b>		

**QUESTION/VRAAG 8**

8.1.1	$\hat{P} = \hat{M}_1 = 66^\circ$ [tan chord theorem/raaklyn koordst]	✓S ✓R (2)
8.1.2	$\hat{M}_2 = 90^\circ$ [ $\angle$ in semi circle/ $\angle$ in halfsirkel]	✓S ✓R (2)
8.1.3	$\hat{N}_1 = 180^\circ - (90^\circ + 66^\circ) = 24^\circ$ [sum of $\angle$ s of/som van $\angle$ e $\triangle MNP$ ]	✓S (1)
8.1.4	$\hat{O}_2 = \hat{P} = 66^\circ$ [corres. $\angle$ s;/ooreenk $\angle$ e, $PM \parallel OR$ ]	✓S ✓R (2)
8.1.5	$\hat{R} + \hat{N}_1 + \hat{N}_2 = 180^\circ - 66^\circ = 114^\circ$ [sum of $\angle$ s of/som van $\angle$ e $\triangle RNO$ ] $\hat{R} = \hat{N}_1 + \hat{N}_2 = 57^\circ$ [ $\angle$ s opposite = radii/ $\angle$ e teenoor = radii] $\therefore \hat{N}_2 = 33^\circ$  <b>OR/OF</b> $\hat{POR} = 114^\circ$ [ $\angle$ s on straight line/ $\angle$ e op reguitlyn] $\hat{PNR} = 57^\circ$ [ $\angle$ at centre = twice $\angle$ at circumference/ midpts $\angle = 2 \times$ omtreks $\angle$ ] $\therefore \hat{N}_2 = 33^\circ$	✓S ✓S/R ✓S  ✓S ✓S/R  ✓S  (3)

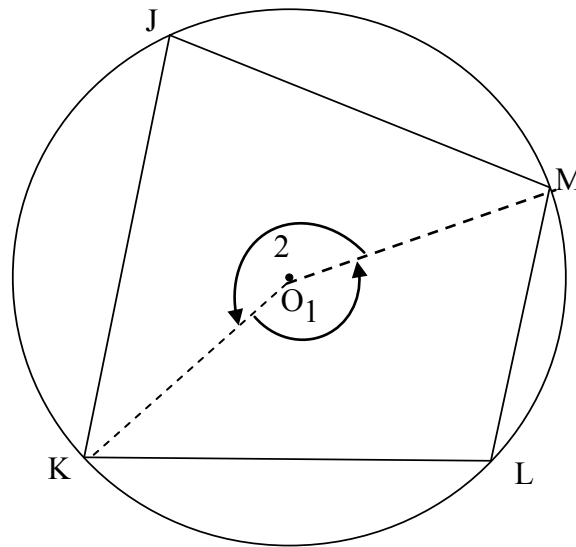
8.2



8.2.1	FC $\parallel$ AB $\parallel$ GH [opp sides of <b>rectangle</b> /teenoorst sye v reghoek]	✓ R (1)
8.2.2	$\frac{AC}{CH} = \frac{AF}{FG}$ [line $\parallel$ one side of $\Delta$ ] <b>OR</b> [prop theorem; FC $\parallel$ GH] [lyn $\parallel$ een sy van $\Delta$ ] <b>OF</b> [eweredighst; FC $\parallel$ GH] $\frac{AC}{21} = \frac{20}{15}$ $AC = \frac{20 \times 21}{15}$ $= 28$ DB = AC = 28 [diags of rectangle =/hoeklyne v reghoek =] $DM = \frac{1}{2}DB = 14$ [diags of rectangle bisect/hoekl v reghoek halveer]	✓ S ✓ R      ✓ AC ✓ S ✓ S (5)
<b>[16]</b>		

**QUESTION/VRAAG 9**

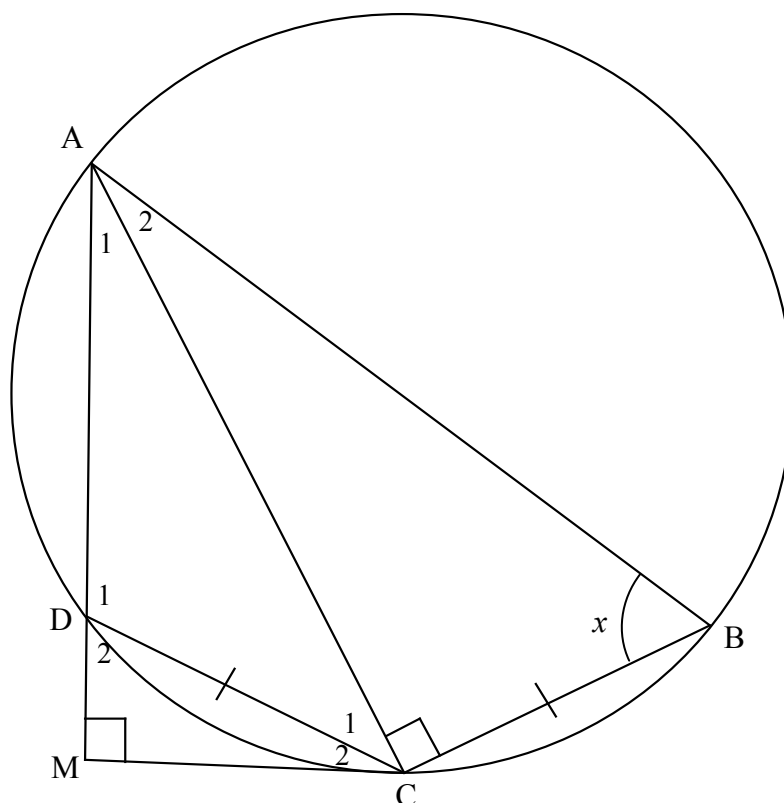
9.1



9.1	<p>Constr/Konstr.: Draw KO and MO/Trek KO en MO</p> <p>Proof:</p> $\hat{O}_1 = 2\hat{J} \quad [\angle \text{ at centre} = \text{twice } \angle \text{ at circumference}]$ $[\text{midpts } \angle = 2 \times \text{omtreks } \angle]$ $\hat{O}_2 = 2\hat{L} \quad [\angle \text{ at centre} = \text{twice } \angle \text{ at circumference}]$ $\hat{O}_1 + \hat{O}_2 = 360^\circ \quad [\angle \text{ s around a point / } \angle \text{ e om 'n punt}]$ $\therefore 2\hat{J} + 2\hat{L} = 360^\circ$ $\therefore 2(\hat{J} + \hat{L}) = 360^\circ$ $\therefore \hat{J} + \hat{L} = 180^\circ$ <p><b>OR/OF</b></p> <p>Constr/Konstr.: Draw KO and MO/Trek KO en MO</p> <p>Proof:</p> <p>Let <math>\hat{J} = x</math></p> $\hat{O}_1 = 2x \quad [\angle \text{ at centre} = \text{twice } \angle \text{ at circumference}]$ $[\text{midpts } \angle = 2 \times \text{omtreks } \angle]$ $\hat{O}_2 = 360^\circ - 2x \quad [\angle \text{ s around a point / } \angle \text{ e om 'n punt}]$ $\therefore \hat{L} = 180^\circ - x \quad [\angle \text{ at centre} = \text{twice } \angle \text{ at circumference}]$ $\therefore \hat{J} + \hat{L} = 180^\circ$	<p>✓ construction</p> <p>✓ S/R</p> <p>✓ S</p> <p>✓ S/R</p> <p>✓ S</p> <p>(5)</p> <p>✓ construction</p> <p>✓ S ✓ R</p> <p>✓ S/R</p> <p>✓ S</p> <p>(5)</p>
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**QUESTION/VRAAG 10**

10.1.1	<p> <math>\hat{A}_2 = \hat{A}_1 = 90^\circ - x</math> [= chords subtend = <math>\angle s</math> = <i>kde onderspan</i> = <math>\angle e</math>]  <math>\hat{D}_2 = x</math> [exterior angle of cyclic quad/<i>buite <math>\angle</math> koordevh.</i>]  <math>\therefore \hat{C}_2 = 90^\circ - x</math> [sum of <math>\angle s</math> of/<i>som v <math>\angle e</math>, <math>\triangle DCM</math></i>]  <math>\therefore \hat{C}_2 = \hat{A}_1 = 90^\circ - x</math>  <math>\therefore MC</math> is a tangent to the circle at C [converse: tan chord th]  <i>MC is 'n raaklyn by C [omgekeerde raakl koordst]</i> </p> <p><b>OR/OF</b></p> <p> <math>\hat{A}_2 = \hat{A}_1 = 90^\circ - x</math> [= chords subtend = <math>\angle s</math>/ = <i>kde onderspan</i> = <math>\angle e</math>]  <math>\hat{C}_1 + \hat{C}_2 = x</math> [sum of <math>\angle s</math> of/<i>som v <math>\angle e</math>, <math>\triangle ACM</math></i>]  <math>\therefore \hat{C}_1 + \hat{C}_2 = \hat{B} = x</math>  <math>\therefore MC</math> is a tangent to the circle at C [converse : tan chord th]  <i>MC is 'n raaklyn by C [omgekeerde raakl koordst]</i> </p> <p><b>OR/OF</b></p> <p>In <math>\triangle AMC</math> and <math>\triangle ACB</math>:</p> <p> <math>\hat{A}_2 = \hat{A}_1 = 90^\circ - x</math> [= chords subtend = <math>\angle s</math>/ = <i>kde onderspan</i> = <math>\angle e</math>]  <math>\hat{AMC} = \hat{ACB} = 90^\circ</math> [given]  <math>\therefore \hat{C}_1 + \hat{C}_2 = \hat{B} = x</math> </p>	<p> <math>\checkmark S \checkmark R</math>  <math>\checkmark S/R</math>  <math>\checkmark \hat{C}_2 = 90^\circ - x</math>  <math>\checkmark R</math> (5) </p> <p> <math>\checkmark S \checkmark R</math>  <math>\checkmark \checkmark \hat{C}_1 + \hat{C}_2 = x</math>  <math>\checkmark R</math> (5) </p> <p> <math>\checkmark S \checkmark R</math>  <math>\checkmark \checkmark \hat{C}_1 + \hat{C}_2 = x</math> </p>
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	$\therefore MC$ is a tangent to the circle at C [converse : tan chord th] <i>MC is 'n raaklyn by C [omgekeerde raakl koordst]</i>	✓ R (5)
	In $\triangle ACB$ and/en $\triangle CMD$ $\hat{B} = \hat{D}_2 = x$ [proved <b>OR</b> exterior $\angle$ of cyclic quad.] <i>[bewys <b>OF</b> buite <math>\angle</math> v koordevh]</i> $\hat{A}_2 = \hat{C}_2 = 90^\circ - x$ [proved <b>OR</b> sum of $\angle$ s in $\triangle$ ] <i>[Bewys <b>OF</b> som v <math>\angle</math>e in <math>\triangle</math>]</i> $\triangle ACB \parallel \triangle CMD$ [ $\angle, \angle, \angle$ ] <b>OR/OF</b> In $\triangle ACB$ and/en $\triangle CMD$ $\hat{B} = \hat{D}_2 = x$ [proved <b>OR</b> exterior $\angle$ of cyclic quad.] <i>[bewys <b>OF</b> buite <math>\angle</math> v koordevh]</i> $\hat{ACB} = \hat{AMC} = 90^\circ$ [given/gegee] $\triangle ACB \parallel \triangle CMD$ [ $\angle, \angle, \angle$ ] <b>OR/OF</b> In $\triangle ACB$ and/en $\triangle CMD$ $\hat{B} = \hat{D}_2 = x$ [proved <b>OR</b> exterior $\angle$ of cyclic quad] <i>[bewys <b>OF</b> buite <math>\angle</math> v koordevh]</i> $\hat{A}_2 = \hat{C}_2 = 90^\circ - x$ [proved <b>OR</b> sum of $\angle$ s in $\triangle$ ] <i>[Bewys <b>OF</b> som v <math>\angle</math>e in <math>\triangle</math>]</i> $\hat{ACB} = \hat{AMC} = 90^\circ$ [given <b>OR</b> sum of $\angle$ s in $\triangle$ ] <i>[gegee <b>OF</b> som v <math>\angle</math>e in <math>\triangle</math>]</i> $\triangle ACB \parallel \triangle CMD$	✓ S ✓ S ✓ R (3)  ✓ S ✓ S ✓ R (3)  ✓ S ✓ S ✓ S (3)
10.2.1	$\frac{BC}{MD} = \frac{AB}{DC}$ [ $\triangle ACB \parallel \triangle CMD$ ] $\frac{DC}{MD} = \frac{AB}{DC}$ [ $BC = DC$ ] $\therefore DC^2 = AB \times MD$ In $\triangle AMC$ and/en $\triangle CMD$ $\hat{M}$ is common/ <i>gemeen</i> $\hat{A}_1 = \hat{C}_2$ [tan chord th / <i>raaklyn koordst</i> ] <b>OR/OF</b> $\hat{C}_1 + \hat{C}_2 = \hat{B} = \hat{D} = x$ [tan chord th / <i>raaklyn koordst</i> <b>OR/OF</b> exterior $\angle$ of cyclic quad/ <i>buite <math>\angle</math> v kdvh</i> ] $\triangle AMC \parallel \triangle CMD$ [ $\angle, \angle, \angle$ ] $\frac{AM}{CM} = \frac{CM}{MD}$ $\therefore CM^2 = AM \times MD$ $\therefore \frac{CM^2}{DC^2} = \frac{AM \times MD}{AB \times MD}$ $= \frac{AM}{AB}$	✓ $\frac{BC}{MD} = \frac{AB}{DC}$  ✓ $DC^2 = AB \times MD$  ✓ S ✓ S  ✓ $CM^2 = AM \times MD$  ✓ $\frac{AM \times MD}{AB \times MD}$ (6)



	<p><b>OR/OF</b></p> $\frac{AC}{MC} = \frac{AB}{DC} \quad [\triangle ACB \parallel \triangle CMD]$ $\therefore CM \times AB = AC \times DC$ <p>In <math>\triangle AMC</math> and/en <math>\triangle ACB</math>  <math>\hat{C} = \hat{M} = 90^\circ</math> [given]  <math>\hat{A}_1 = \hat{A}_2</math> [proven]  <b>OR/OF</b>  <math>\hat{A}\hat{C}M = \hat{B} = x</math> [proven]  <math>\triangle AMC \parallel \triangle ACB</math> [<math>\angle, \angle, \angle</math>]  <math display="block">\frac{AC}{AM} = \frac{BC}{MC}</math> <math display="block">\therefore AC \times MC = AM \times BC</math> <math display="block">\therefore AC = \frac{BC \cdot AM}{MC}</math> <math display="block">CM \times AB = \frac{BC \cdot AM}{MC} \times DC</math> <math display="block">CM^2 = \frac{DC \cdot AM}{AB} \times DC \quad [BC = DC]</math> <math display="block">\frac{CM^2}{DC^2} = \frac{AM}{AB}</math></p>	<p>✓ <math>\frac{AC}{MC} = \frac{AB}{DC}</math></p> <p>✓ S</p> <p>✓ S</p> <p>✓ <math>AC \cdot MC = AM \cdot BC</math></p> <p>✓ equating</p> <p>✓ S</p> <p>(6)</p>
10.2.2	<p>In <math>\triangle DMC</math>:  <math display="block">\frac{CM}{DC} = \sin x</math> <math display="block">\frac{CM^2}{DC^2} = \sin^2 x \quad \frac{AC}{AB} = \frac{CM}{DC}</math> <math display="block">\therefore \frac{AM}{AB} = \sin^2 x</math></p> <p><b>OR/OF</b></p> <p>In <math>\triangle ABC</math>:  <math display="block">\sin x = \frac{AC}{AB}</math> <p>In <math>\triangle AMC</math>:  <math display="block">\sin x = \frac{AM}{AC}</math> <math display="block">\sin x \cdot \sin x = \frac{AC}{AB} \times \frac{AM}{AC} = \frac{AM}{AB}</math></p> </p>	<p>✓ trig ratio</p> <p>✓ square both sides</p> <p>(2)</p> <p>✓ 2 equations for <math>\sin x</math></p> <p>✓ product</p> <p>(2)</p>
<b>[16]</b>		

**TOTAL/TOTAAL: 150**