

# Simplified Coherent Transceivers for Optical Communication Networks

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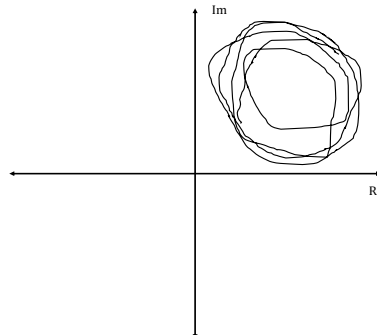
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# Theoretical Overview

- Coherent optical schemes require two optical hybrids and four pairs of balanced photodetector. It formulate a solution for medium-to-long-reach applications, however, cost of such receiver become an obstacle in short reach application like PON, inter-data-center communications and metropolitan network.
- Kramers-Kronig transceiver provides a solution for such short links. It allows the reconstruction of complex constellation from an intensity measurement using a single-photo-diode.
- The kramers-Kronig scheme relies on identifying a condition which ensures that the received signal is minimum phase.
- The following few slides would give a comprehensive overview about the working principle Kramers-Kronig receiver.

# 1. What is minimum phase signal?

- A necessary and sufficient condition for a complex signal  $A(t) = A_s(t) + \bar{A}$  to be minimum phase is that the curve described in a complex plane by  $A(t)$  when  $t \rightarrow -\infty$  to  $t \rightarrow \infty$  **does not encircle the origin**.  
where,  $A_t \rightarrow$  Single sideband (SSB) signal &  $\bar{A} \rightarrow$  DC value.
- A minimum-phase signal has an useful property that the **natural logarithm** of the magnitude related to the phase angle by the Hilbert transform.



Minumum Phase Signal

## 2. How we can use these signals and profit from them?

- **SSB Signal:**

If we denote a SSB signal  $A_s(t)$  as,

$$A_s(t) = A_{s,r}(t) + iA_{s,i}(t) \quad (1)$$

then in the equation 1, the real and imaginary parts  $A_{s,r}(t)$  and  $A_{s,i}(t)$  are related through the Kramers-Kronig relation with each other as,

$$\begin{aligned} A_{s,r}(t) &= -\frac{1}{\pi} p.v. \int_{-\infty}^{\infty} \frac{A_{s,i}(t')}{t - t'} dt' \\ A_{s,i}(t) &= \frac{1}{\pi} p.v. \int_{-\infty}^{\infty} \frac{A_{s,r}(t')}{t - t'} dt' \end{aligned} \quad (2)$$

**Note :** Single sideband signal is the frequency translated version of an analytical signal as,

$$A_s(t) = \text{Re}\{[s(t) + i\hat{s}(t)]e^{i2\pi f_0 t}\}$$

- **Minimum Phase Signal:**

Given function  $A(t) = A_s(t) + \bar{A}$  never encircles the origin for  $t \in (-\infty, \infty)$ .

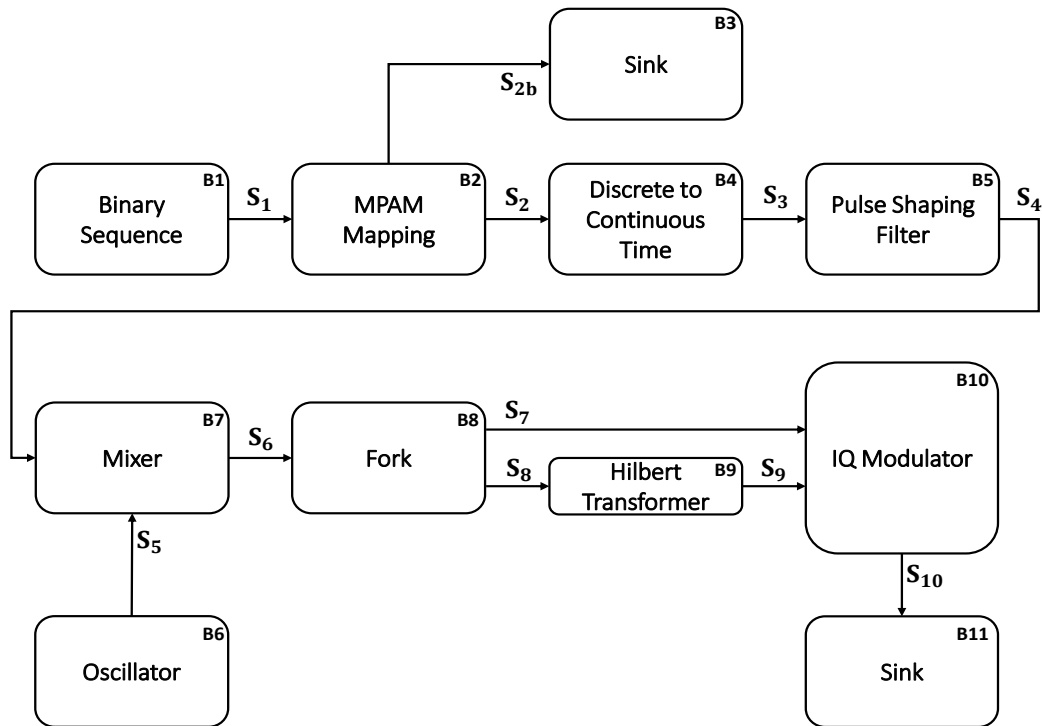
$$G(t) = \ln \left[ \frac{A(t)}{\bar{A}} \right] \quad (3)$$

Under the hypothesis of signal being minimum phase, the phase information can be reconstructed by from its intensity as,

$$\phi(t) = \bar{\phi} + \frac{1}{2\pi} p.v. \int_{-\infty}^{\infty} \frac{\ln|A(t')|^2}{t - t'} dt' \quad (4)$$

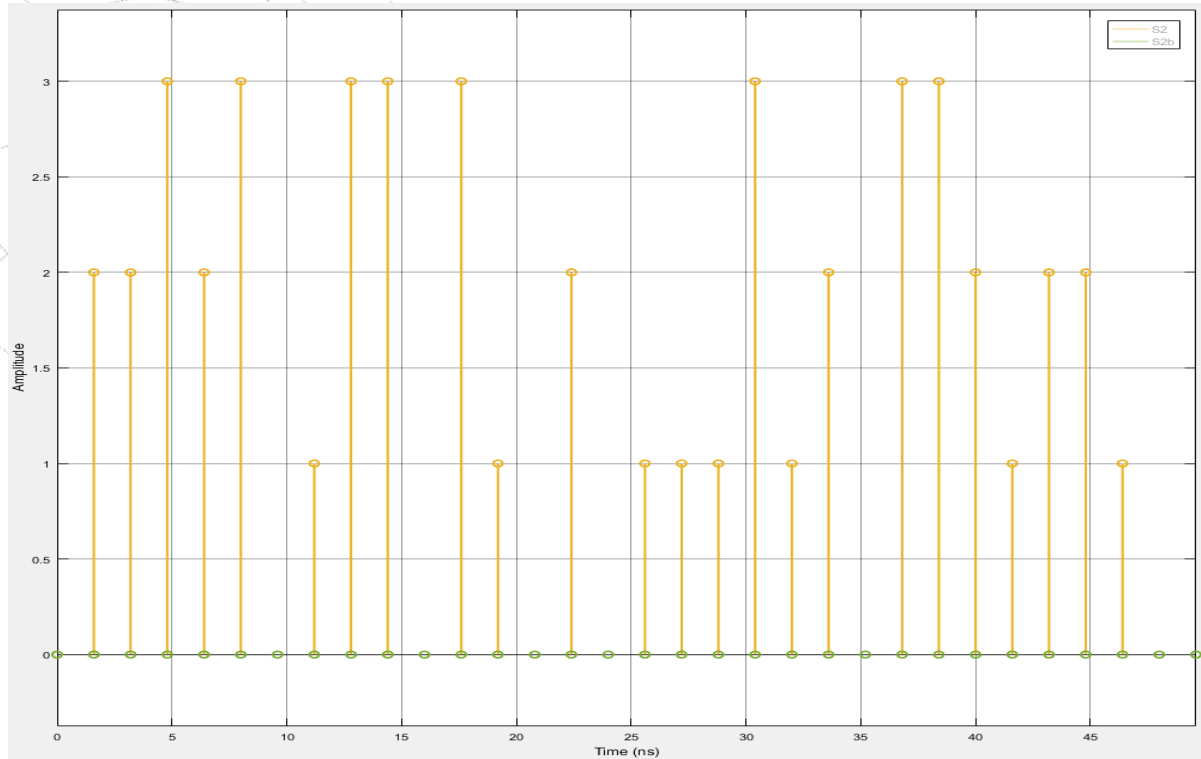
# Simulation setup

- Transmitter setup

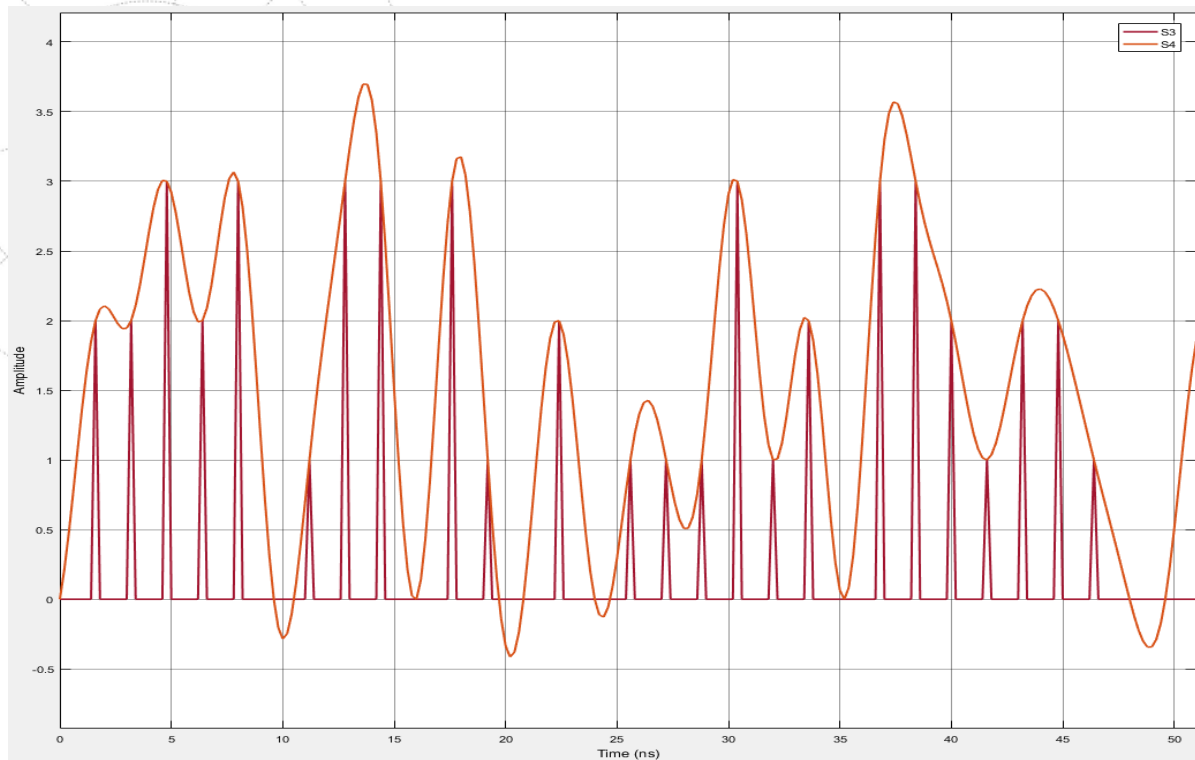


Transmitter simulation setup

# Simulation Results

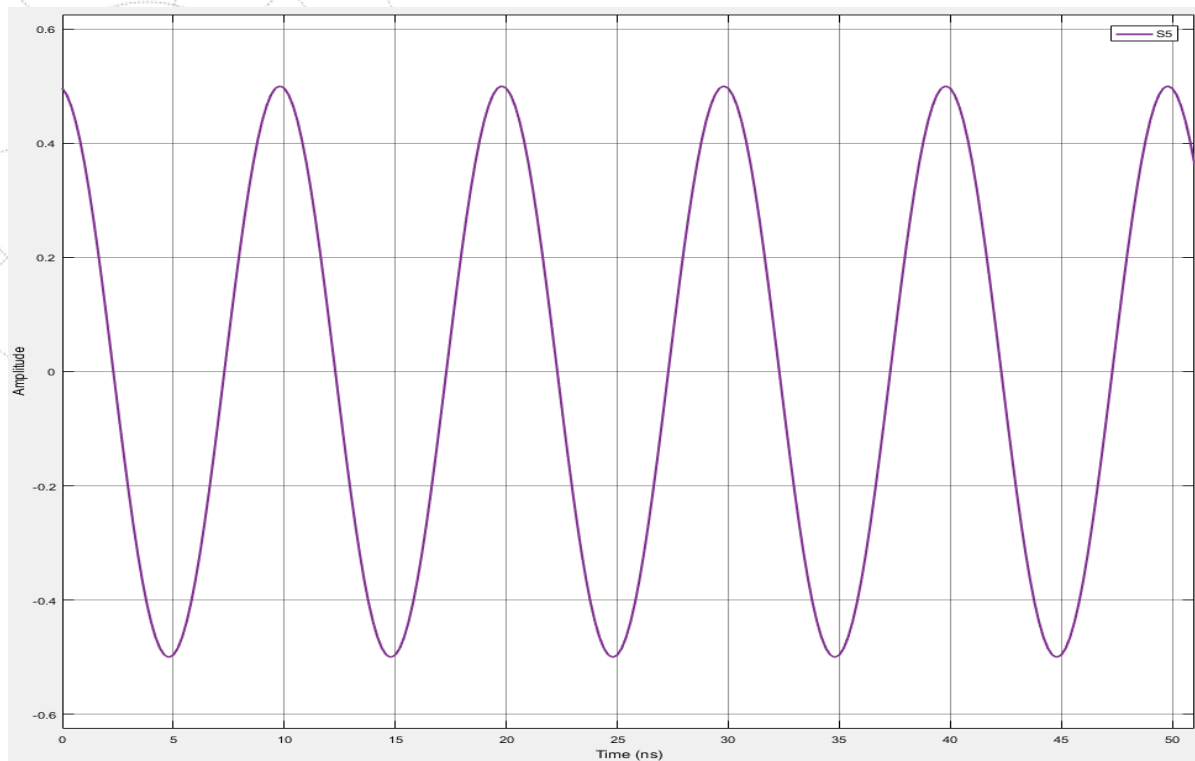


S2 and S2b signals

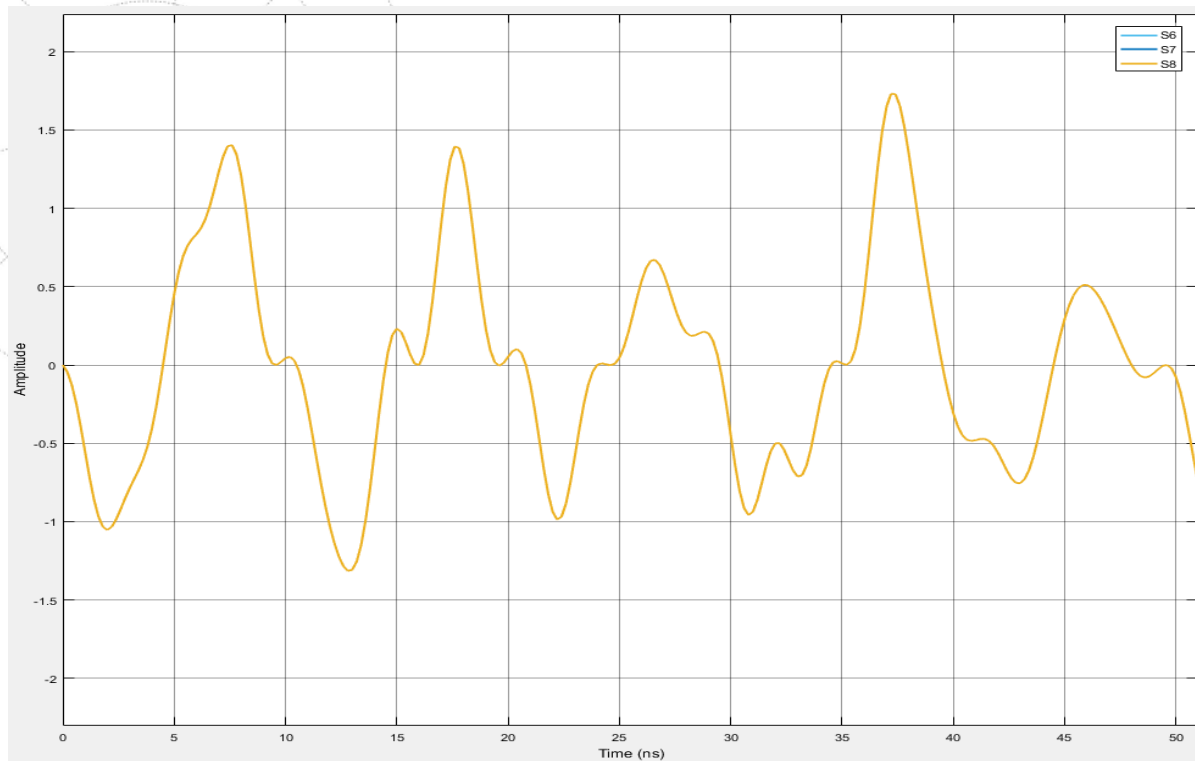


S3 S4 signals





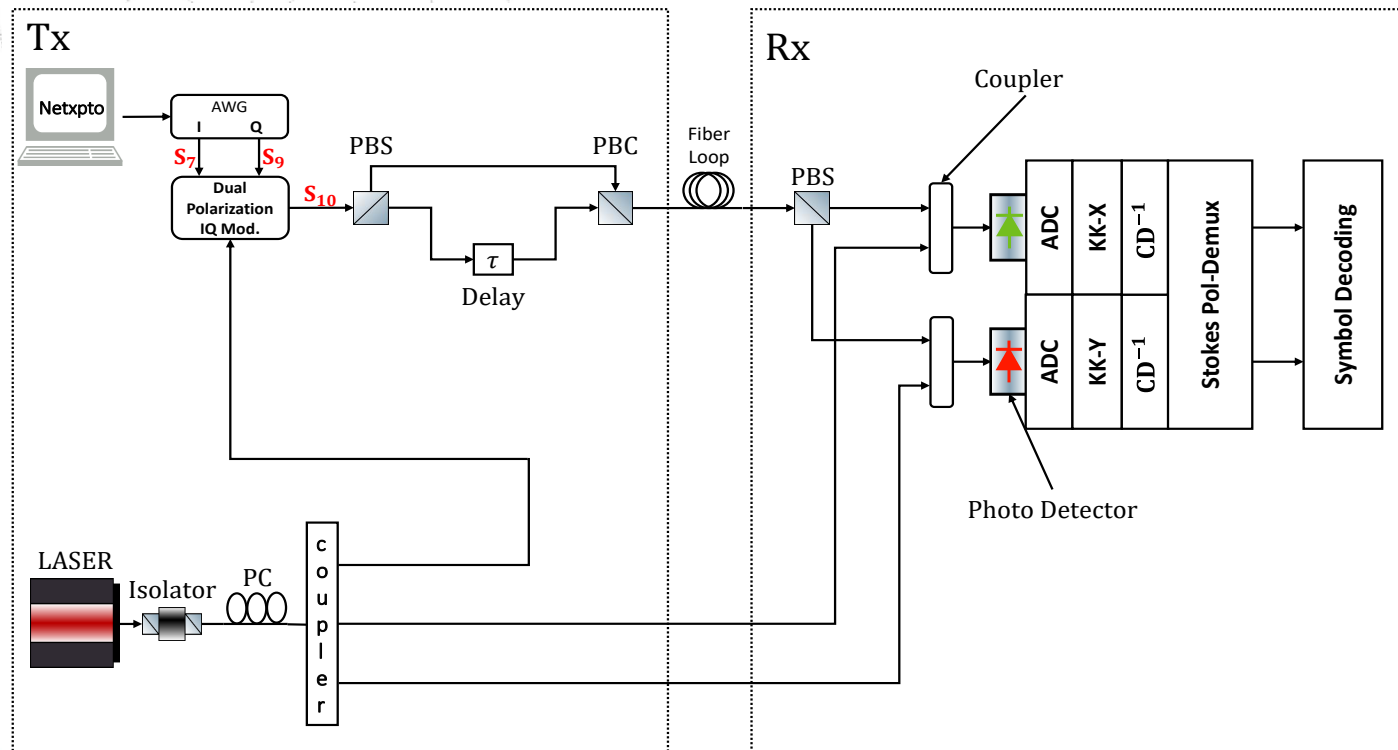
S5 signal



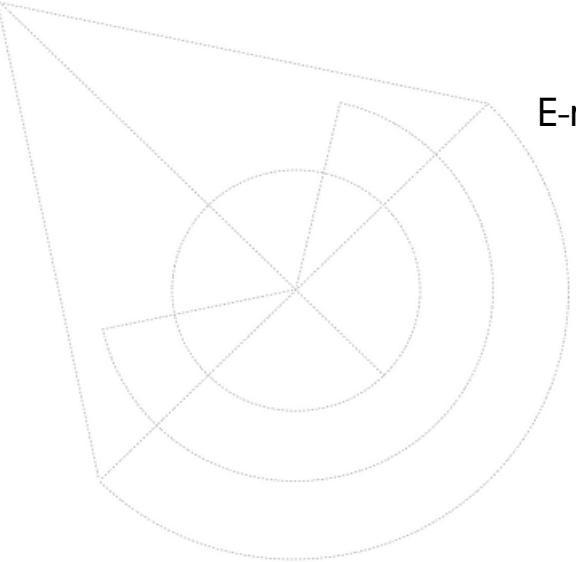
S6, S7 and S8 signals

# Experimental setup

- Envisioned lab setup



PDM Kramers-Kronig receiver experimental setup



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