# Simplified Coherent Transceivers for Optical Communication Networks

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### **Theocratical Overview**

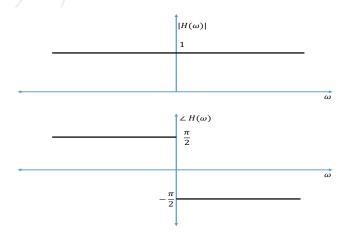
- Coherent optical transmission schemes are optimal from the stand point of spectral efficiency since they allow the encoding of information in both quadrature and polarization.
- However, such coherent optical schemes require two optical hybrids and four pairs of balanced photodetector. Therefore, it formulate a solution for medium-to-long-reach applications since cost of such receiver become an obstacle in short reach application like PON,inter-data-center communications and metropolitan network.





### 1. What is Hilbert transform?

If we consider a filter  $H(\omega)$  that has a unity magnitude response for all frequencies and the phase response is  $-\pi/2$  for all positive frequencies and  $\pi/2$  for negative frequencies.



Magnitude and phase of Hilbert transform filter



The transfer function of this filter is given by

$$H(\boldsymbol{\omega}) = -isgn(\boldsymbol{\omega}) \tag{1}$$

The inpulse response of this filter can be given as,

$$h(t) = \frac{1}{\pi t} \tag{2}$$

When this filter driven by an arbitrary signal s(t), the filter produces the output as,

$$\hat{s}(t) = s(t) * h(t) = \int_{-\infty}^{\infty} \frac{s(u)}{\pi(t - u)} du$$
(3)

The function  $\hat{s}(t)$  is called the Hilbert transform if s(t). Note that



$$\mathscr{F}[\hat{s}(t)] = H(\boldsymbol{\omega})S(\boldsymbol{\omega}) = -isgn(\boldsymbol{\omega})S(\boldsymbol{\omega})$$



## 2. What is the SSB signal and how it can be generated?

By definition, the SSB is the signal which contains either upper sideband or lower sideband and hence it reduces the spectral occupancy by half. In another words, SSB signal is the frequency translated version of an analytical signal.

• **Analytical Signal**: An analytic signal is a complex-valued signal that has no negative frequency components, and its real and imaginary parts are related to each other by the Hilbert transform.

$$s_a(t) = s(t) + i\hat{s}(t) \tag{5}$$

where,  $s_a(t)$  is an analytical signal and  $\hat{s}(t)$  is the Hilbert transform of the signal s(t). Such analytical signal can be used to generate Single Sideband Signal (SSB) signal.





Since a SSB signal is the frequency translated version of an analytical signal, it can be generated as,

$$s_{ssb}(t) = Re\{s_a(t)e^{i2\pi f_0 t}\}\$$

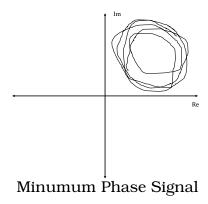
$$= Re\{[s(t) + i\hat{s}(t)][cos(2\pi f_0 t) + isin(2\pi f_0 t)]\}\$$

$$= s(t)cos(2\pi f_0 t) - \hat{s}(t)sin(2\pi f_0 t)$$
(6)



## 3. What is minimum phase signal?

- ullet A necessary and sufficient condition for a complex signal A(t) to be minimum phase is that the curve described in a complex plane by A(t) when  $t \to -\infty$  to  $t \to \infty$  does not encircle the origin.
- A minimum-phase signal has an useful property that the natural logarithm of the magnitude of the frequency response is related to the phase angle of the frequency response by the Hilbert transform.







# 4. How we can use these signals and profit from them?

### Analytical Signal:

If we denote an analytic signal  $A_s(t)$  as,

$$A_s(t) = A_{s,r}(t) + iA_{s,i}(t)$$
 (7)

then in the equation 7, the real and imaginary parts  $A_{s,r}(t)$  and  $A_{s,i}(t)$  are related through the Kramers-Kronig relation with each other as,

$$A_{s,r}(t) = -\frac{1}{\pi} p.v. \int_{-\infty}^{\infty} \frac{A_{s,i}(t')}{t - t'} dt'$$

$$A_{s,i}(t) = \frac{1}{\pi} p.v. \int_{-\infty}^{\infty} \frac{A_{s,r}(t')}{t - t'} dt'$$
(8)



#### Minimum Phase Signal:

Given function  $A(t) = A_s(t) + \bar{E}$  never encircles the origin for  $t \in (-\infty, \infty)$ .

$$G(t) = log \left[ \frac{A(t)}{\bar{A}} \right] \tag{9}$$

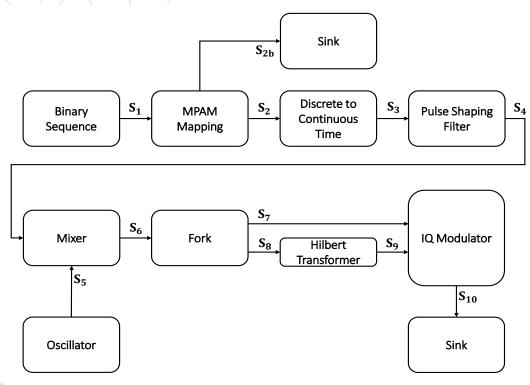
Under the hypothesis of signal being minimum phase, the phase information can be reconstructed by from its intensity as,

$$\phi(t) = \bar{\phi} + \frac{1}{2\pi} p.v. \int_{-\infty}^{\infty} \frac{\log|A(t)|^2}{t - t'} dt'$$
 (10)



## Simulation setup

#### Transmitter setup

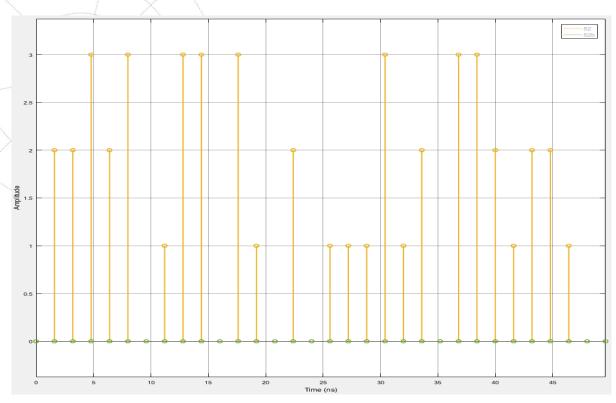




Transmitter simulation setup



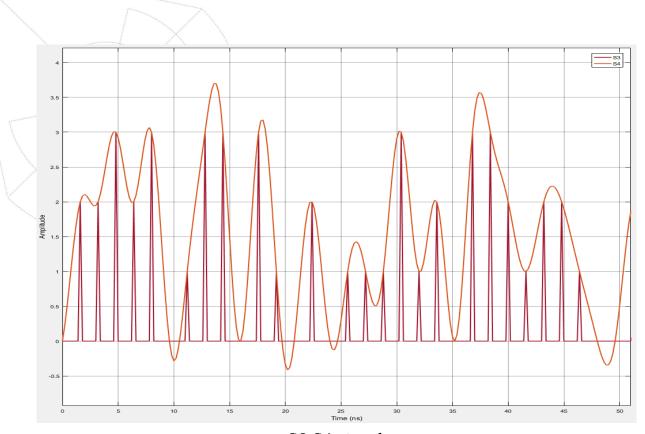
## **Simulation Results**



S2 and S2b signals



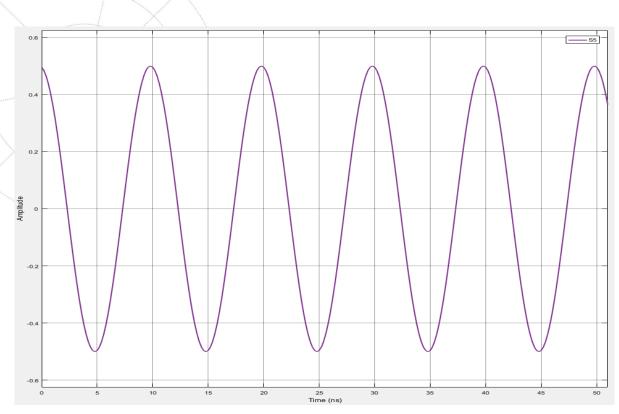




S3 S4 signals



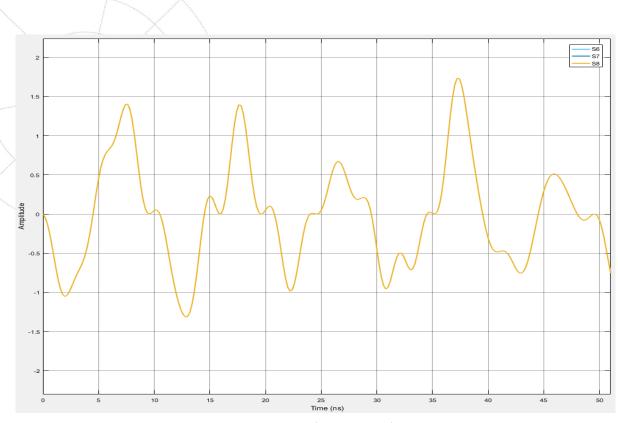




S5 signal







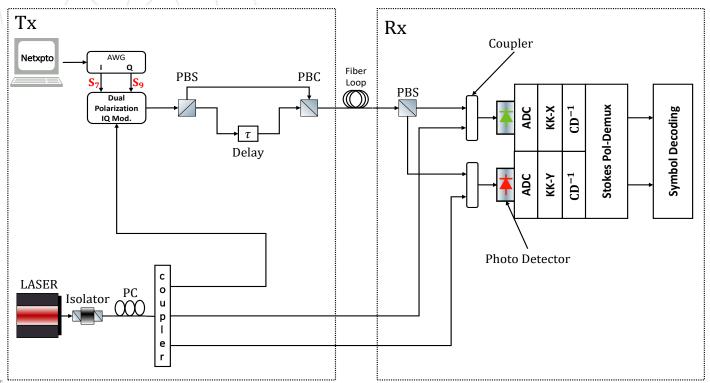
S6, S7 and S8 signals





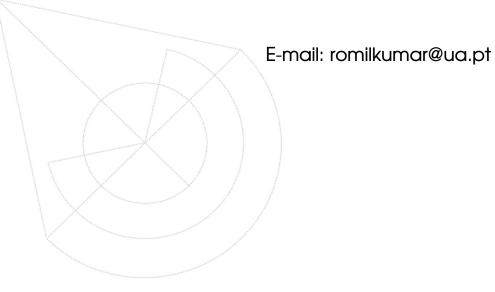
## **Experimental setup**

### Envisioned lab setup









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