

Seminario 1

Andoni Latorre Galarraga

1.

a)

$$RE_{x \cdot y} \approx \frac{y}{xy} \frac{\partial xy}{\partial y} RE_y + \frac{x}{xy} \frac{\partial xy}{\partial x} RE_x = RE_x + RE_y$$

b)

$$RE_{x/y} \approx \frac{x}{x/y} \frac{\partial x/y}{\partial x} RE_x + \frac{y}{x/y} \frac{\partial x/y}{\partial y} RE_y = RE_x - RE_y$$

c)

$$RE_{x+y} \approx \frac{x}{x+y} \frac{\partial x+y}{\partial x} RE_x + \frac{y}{x+y} \frac{\partial x+y}{\partial y} RE_y = \frac{x}{x+y} RE_x + \frac{y}{x+y} RE_y$$

d)

$$RE_{\sqrt{x}} \approx \frac{x}{\sqrt{x}} \frac{\partial \sqrt{x}}{\partial x} RE_x = \frac{1}{2} RE_x$$

2.

$$\begin{aligned} RE_{\sqrt{3+\lg^2 x}} &\approx \frac{1}{2} RE_{3+\lg^2 x} \approx \frac{3}{6+2\lg^2 x} RE_3 + \frac{\lg^2 x}{6+2\lg^2 x} RE_{\lg^2 x} \\ &\approx \frac{3}{6+2\lg^2 x} \varepsilon + \frac{\lg^2 x}{6+2\lg^2 x} 2RE_{\lg x} \approx \frac{3}{6+2\lg^2 x} \varepsilon + \frac{\lg^2 x}{6+2\lg^2 x} 10\varepsilon \\ &\quad \frac{3+10\lg^2 x}{6+2\lg^2 x} \varepsilon \end{aligned}$$