### **Tutorial 09, Michaelmas Term**

Research Methods for Political Science (PO3600)

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#### **Session Outline**

- 1. Chi Square Test
- 2. Correlations in SPSS
- $3. \ {\sf Research\ proposal/paper}$

#### Chi Square Test

- A Chi Square Test determines if a sample data matches a population.
- Formula:  $\chi^2 = \sum \frac{(O_i E_i)^2}{E_i}$
- O: observed value; E: expected value
- ullet Problem: calculation by hand takes long  $\longleftrightarrow$  SPSS!

$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$

Category	Observed	Expected	Residual= (Obs-Exp)	(Obs-Exp)^2	Component = (Obs- Exp)^2 / Exp
Aries	29				
Taurus	24				
Gemini	22				
Cancer	19				
Leo	21				
Virgo	18				
Libra	19				
Scorpio	20				
Sagittarius	23				
Capricorn	18				
Aquarius	20				
Pisces	23				

Figure: Source:

http://www.statisticshowto.com/probability-and-statistics/chi-square/.

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$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$

Category	Observed	Expected	Residual= (Obs-Exp)	(Obs-Exp)^2	Component = (Obs- Exp)^2 / Exp
Aries	29	21.333			
Taurus	24	21.333			
Gemini	22	21.333			
Cancer	19	21.333			
Leo	21	21.333			
Virgo	18	21.333			
Libra	19	21.333			
Scorpio	20	21.333			
Sagittarius	23	21.333			
Capricorn	18	21.333			
Aquarius	20	21.333			
Pisces	23	21.333			

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$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$

Category	Observed	Expected	Residual= (Obs-Exp)	(Obs-Exp)^2	Component = (Obs- Exp)^2 / Exp
Aries	29	21.333	7.667		
Taurus	24	21.333	2.667		
Gemini	22	21.333	0.667		
Cancer	19	21.333	-2.333		
Leo	21	21.333	-0.333		
Virgo	18	21.333	-3.333		
Libra	19	21.333	-2.333		
Scorpio	20	21.333	-1.333		
Sagittarius	23	21.333	1.667		
Capricorn	18	21.333	-3.333		
Aquarius	20	21.333	-1.333		
Pisces	23	21.333	1.667		

$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$

Category	Observed	Expected	Residual= (Obs-Exp)	(Obs-Exp)^2	Component = (Obs- Exp)^2 / Exp
Aries	29	21.333	7.667	58.782889	
Taurus	24	21.333	2.667	7.112889	
Gemini	22	21.333	0.667	0.44889	
Cancer	19	21.333	-2.333	5.442889	
Leo	21	21.333	-0.333	0.110889	
Virgo	18	21.333	-3.333	11.108889	
Libra	19	21.333	-2.333	5.442889	
Scorpio	20	21.333	-1.333	1.776889	
Sagittarius	23	21.333	1.667	2.778889	
Capricorn	18	21.333	-3.333	11.108889	
Aquarius	20	21.333	-1.333	1.776889	
Pisces	23	21.333	1.667	2.778889	

$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$

Category	Observed	Expected	Residual= (Obs-Exp)	(Obs-Exp)^2	Component = (Obs- Exp)^2 / Exp
Aries	29	21.333	7.667	58.782889	2.755490976
Taurus	24	21.333	2.667	7.112889	0.333421882
Gemini	22	21.333	0.667	0.44889	0.021042048
Cancer	19	21.333	-2.333	5.442889	0.255139408
Leo	21	21.333	-0.333	0.110889	0.005198003
Virgo	18	21.333	-3.333	11.108889	0.520737308
Libra	19	21.333	-2.333	5.442889	0.255139408
Scorpio	20	21.333	-1.333	1.776889	0.083292973
Sagittarius	23	21.333	1.667	2.778889	0.130262457
Capricorn	18	21.333	-3.333	11.108889	0.520737308
Aquarius	20	21.333	-1.333	1.776889	0.083292973
Pisces	23	21.333	1.667	2.778889	0.130262457
					5.094017203

### Test Chi Square Hypothesis: Steps

Question: Difference in sample, can we generalise this to the population?

- 1. 11 Degrees of Freedom; Chi square test statistic of 5.094
- 2. Take the chi-square statistic and find value in chi-square table
- 3. closest value for df=11 and 5.094 is between .900 and .950.
- Decide whether this p-value supports or rejects the null hypothesis.
   This very large p-value means that the null hypothesis cannot be rejected.

### Research Proposal

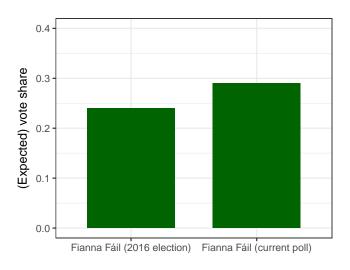
Team up and discuss (some of) the following aspects:

- 1. Research question + relevance
- 2. Theoretical argument + hypothesis
- 3. Type of data + operationalisation of variables
- 4. Ways of analysing your data

### Research Proposal

#### Discuss with your neighbour:

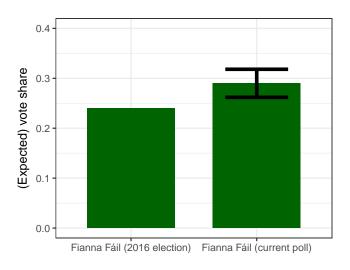
- 1. What is the puzzle you address?
- 2. Why is the question relevant?
- 3. What are your key dependent and independent variables?
- 4. What data will you use?



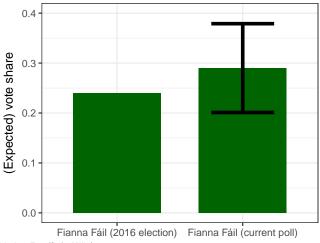
Is there a statistically significance in support for FF in December 2017 compared to the election in February 2016?

#### What we know:

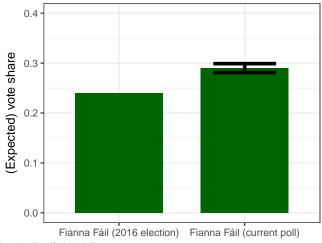
- 2016 FF election result: 24%; FF standing in latest poll (p) = 29%; number of respondents in poll = 1001; 95 percent confidence interval (z) = 1.96
- $CI = p \pm z * \sqrt{(p \times (1-p)/N)}$
- $CI_{low} = 0.29 + 1.96 * \sqrt{(0.29 \times (1 0.29)/1001} = 0.26$
- $CI_{high} = 0.29 1.96 * \sqrt{(0.29 \times (1 0.29)/1001} = 0.31$



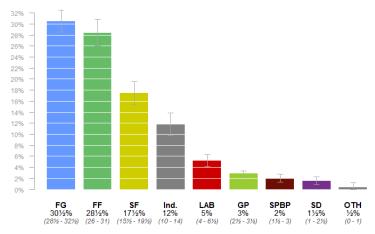
How does plot look like when we only ask 30 Irish voters?



...and for 10,000 respondents?



### **Irish Polling Indicator**



 $Mean\ estimates\ and\ 95\%\ uncertainty\ margins.\ Figures\ rounded\ to\ \%\ a\ per\ cent.\ (c)\ Tom\ Louwerse,\ Leiden\ University$ 



			Owner o	or tenant	Total
			Owner	Tenant	IOLAI
Vote in 2007	Did vote	Count	938	119	1057
election	Did not vote	Count	99	42	141
Total		Count	1037	161	1198
Total (%)			0.87%	0.13%	100%

How likely is it that we obtained these numbers by chance?

That is: if there was no relationship between ownership and voting in the population, how likely is it we get numbers which are so far away from what we would expect (or more extreme)?

	or tenant	Total	Total (0/)			
			Owner	Tenant	Total	Total (%)
Vote in 2007	Did vote	Count	Α	С	1057	88%
election	Did not vote	Count	В	D	141	12%
Total		Count	1037	161	1198	100%
Total (%)			0.87%	0.13%	100%	

 If ownership and vote were not related, how many respondents should we expect in cell A?

			Owner o	or tenant	Takal	Tatal (0/)
			Owner	Tenant	Total	Total (%)
Vote in 2007	Did vote	Count	A = 88%*0.87%	C = 88%*0.13%	1057	88%
election	Did not vote	Count	B = 12%*0.87%	D = 12%*0.13%	141	12%
Total		Count	1037	161	1198	100%
Total (%)			0.87%	0.13%	100%	

- If ownership and vote were not related, how many respondents should we expect in cell A?
  - If among all voters, 88% did vote, we would expect that among owners, also 88% would vote.
  - If among all owners, 87% did vote, we would expect that among voters, also 87% would vote.

			or tenant	Total	T-+-1 (0/)	
			Owner	Owner Tenant		Total (%)
Vote in 2007	Did vote	Count	Α	С	1057	88%
election	Did not vote	Count	В	D	141	12%
Total		Count	1037	161	1198	100%
Total (%)			0.87%	0.13%	100%	

- If ownership and vote were not related, how many respondents should we expect in cell A?
- Expected frequency  $(f_e)$ = row margin\*  $\frac{\text{column margin}}{\text{total}}$
- $f_e = 1037 * \frac{1057}{1198}$
- $f_e = 1037 * 0.88 = 914.9$

			Owner o	or tenant	Takal
			Owner	Tenant	Total
Vote in 2007	Did vote	Count	Α	С	1057
election	Did not vote	Count	В	D	141
Total		Count	1037	161	1198

Expected frequency 
$$(f_e) = \frac{\text{row margin} * \text{colum margin}}{\text{total}}$$

			Owner o	or tenant	Takal
			Owner	Tenant	Total
Vote in 2007	Did vote	Count	Α	С	1057
election	Did not vote	Count	В	D	141
Total		Count	1037	161	1198

• B: 
$$f_e$$
 = 1037 \* 141 / 1198 = 122.1

• C: 
$$f_e$$
 = 1057\* 161 / 1198 = 142.1

• D: 
$$f_e = 141 * 161 / 1198 = 18.9$$

			Owner o		
			Owner Tenant		Total
Vote in 2007 election	Did vote	Count	914.9	142.1	1057
	Did not vote	Count	122.1	18.9	141
Total		Count	1037	161	1198

			Owner o	Total	
			Owner	Tenant	iotai
Vote in 2007	Did vote	Count	938	119	1057
election	Did not vote	Count	99	42	141
Total		Count	1037	161	1198
		Expected	I frequencies		
			Owner o	T-1-1	
			Owner	Tenant	Total
Vote in 2007	Did vote	Count	914.9	142.1	1057
election	Did not vote	Count	122.1	18.9	141

Count

1037

161

1198

Total

			Owner o	Total	
			Owner	Tenant	iotai
Vote in 2007	Did vote	Count	938	119	1057
election	Did not vote	Count	99	42	141
Total		Count	1037	161	1198
		Expected	I frequencies		
			Owner or tenant		Total
			Owner	Tenant	iotai
Vota in 2007	Did vote	Count	914.9	142.1	1057

Vote in 2007

election

Total

Did not

vote

$$\chi^2 = \sum \frac{(f_o - f_e)^2}{f_o}$$

122.1

1037

18.9

161

141

1198

Cell A: 
$$\frac{(f_o - f_e)^2}{f_e} = \frac{(938 - 914.9)^2}{914.9} = \frac{533.61}{914.9} = 0.58$$

Count

Count

			Owner o	Total	
			Owner	Tenant	iotai
Vote in 2007	Did vote	Count	938	119	1057
election	Did not vote	Count	99	42	141
Total		Count	1037	161	1198
		Evportod	l fraguancias		

			Owner or tenant		Total
			Owner	Tenant	Total
Vote in 2007	Did vote	Count	914.9	142.1	1057
election	Did not vote	Count	122.1	18.9	141
Total	Vote	Count	1037	161	1198

Cell B: 
$$\frac{(f_o - f_e)^2}{f_e} = \frac{(99 - 122.1)^2}{122.1} = \frac{533.61}{122.1} = 4.37$$

Cell C:  $\frac{(f_o - f_e)^2}{f_e} = \frac{(119 - 142.1)^2}{142.1} = \frac{533.61}{142.1} = 3.76$ 

Cell D:  $\frac{(f_o - f_e)^2}{f_e} = \frac{(42 - 18.9)^2}{18.9} = \frac{533.61}{18.9} = 28.23$ 

### Chi squared

$$\chi^2 = \sum \frac{(f_o - f_e)^2}{f_e}$$

$$\chi^2 = .58 + 4.37 + 3.76 + 28.23 = 36.94$$

Interesting, but what does that mean?

## Chi squared

 We need to compare the chi squared we obtained with the critical value for chi squared.

• If  $\chi^2_{\text{obtained}} > \chi^2_{\text{critical}}$  we can conclude that it is unlikely that the relationship we found is just due to sampling error.

### The cricical value

- First, we need to set a confidence level, normally 95%
- This corresponds to a *p* value of 0.05 (1 95/100).
- Second, we need to know the degrees of freedom: df = (c-1)(r-1)

### The critical value

### In our example:

- The degrees of freedom:
  - -2 rows
  - 2 columns
  - -df = (2-1)\*(2-1) = 1\*1 = 1
- The critical value corresponding df = 1 and p = 0.05 is found in Field, appendix A.4:

## A.4. Critical values of the chi-square distribution

			p			
0.05	df	0.01	0.05			
37.68	25	6.63	3.84	<b>→</b> 1		
38.89	26	9.21	5.99	2		
40.1	27	11.34	7.81	3		
41.34	28	13.28	9.49	4		
42.56	29	15.09	11.07	5		
43.77	30	16.81	12.59	6		
49.80	35	18.48	14.07	7		

### Comparing obtained and critical value

- $\chi^2_{\text{obtained}} = 36.94$
- $\chi^2_{critical} = 3.84$

• As  $\chi^2_{\text{obtained}} > \chi^2_{\text{critical}}$  we conclude that there is a statistically significant relationship.