# **Tutorial 06, Hilary Term**

Research Methods for Political Science (PO3600)

Stefan Müller

6 March 2018

Trinity College Dublin http://muellerstefan.net/research-methods

# **Multivariate Regression**

What predicts wealth (measured as GDP per capita)?

# **Multivariate Regression**

What predicts wealth (measured as GDP per capita)?

Dependent variable: GDP per capita (US\$) 2002 (UNDP 2004)

Independent variables:

- FM\_Lit2002: Adult illiteracy rate (% ages 15 and above) 2002 (UNDP 2004)
- F\_Work2002: Female economic activity rate (% ages 15 and above)
   2002 (UNDP 2004)
- SDI: Social Diversity Index, primary data source 2001 (Okediji 2005)

# **Regression Coefficients**

#### Coefficientsa

		Unstandardize	d Coefficients	Standardized Coefficients		
Model		В	Std. Error	Beta	t	Sig.
1	(Constant)	-1052.329	3854.899		273	.786
	Adult literacy rate (female rate as % of male rate) 2002 (UNDP 2004)	72.153	28.127	.276	2.565	.012
	Female economic activity rate (% ages 15 and above) 2002 (UNDP 2004)	-89.083	34.071	302	-2.615	.011
	Social Diversity Index, primary data source 2001 (Okediji 2005)	3266.519	2976.317	.126	1.098	.276

a. Dependent Variable: GDP per capita (US\$) 2002 (UNDP 2004)

#### Residuals Statistics<sup>a</sup>

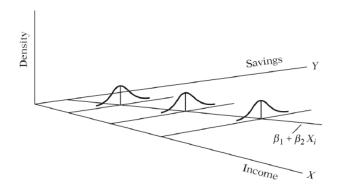
	Minimum	Maximum	Mean	Std. Deviation	N
Predicted Value	-1615.23	6343.40	2927.33	2056.694	84
Residual	-5941.399	23353.250	.000	4386.110	84
Std. Predicted Value	-2.209	1.661	.000	1.000	84
Std. Residual	-1.330	5.227	.000	.982	84

a. Dependent Variable: GDP per capita (US\$) 2002 (UNDP 2004)

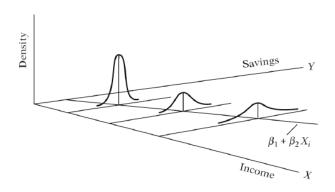
# **Regression Diagnostics**

- 1. Influential data points/outliers
- Independence/autocorrelation (errors associated with one observation not correlated with errors in any other observation)
- 3. Linearity (relationship should be linear)
- 4. Homoscedasticity (constant error variance)
- 5. Normality (errors should be normally distributed)
- 6. Model specification
- 7. Multicollinearity (predictors are highly correlated)
- 8. Leverage (extent to which predictor differs from mean of predictor)

# **Recap: Homoscedasticity**



# **Recap: Heteroscedasticity**

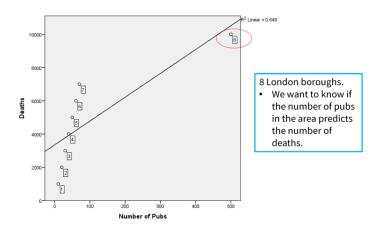


# **Recap: Homoscedasticity**

**Homoscedasticity**: Variance of the residuals is homogeneous across levels of the predicted values.

- Plot of ZRESID and ZPRED
- Interpret the plot

## **Outliers vs. Influential Points**



# **Outliers vs. Influential Points**

pubs	mortality	ZRE_1	COO_1
10	1000	-1.33839	.21328
20	2000	87895	.08530
30	3000	41950	.01814
40	4000	.03995	.00015
50	5000	.49940	.02294
60	6000	.95885	.08092
70	7000	1.41830	.17107
500	10000	27966	227.14286
	But it has a BIG influence (the		
	computation for Cook's distance is huge).		

# **Diagnostics: Influential points**

#### Cook's Distance

- How much the predicted scores for other observations would differ if the observation in question were not included?
- Cook's Distance: influence of an observation and is proportional to the sum of the squared differences between predictions made with all observations in the analysis and predictions made leaving out the observation in question.
- A common rule of thumb is that an observation with a value of Cook's D over 1.0 has too much influence.

# Check for influential points

Residuals Statistics<sup>a</sup>

	Minimum	Maximum	Mean	Std. Deviation	N
Predicted Value	-1615.23	6343.40	2927.33	2056.694	84
Std. Predicted Value	-2.209	1.661	.000	1.000	84
Standard Error of Predicted Value	515.610	1654.260	947.708	230.056	84
Adjusted Predicted Value	-1793.46	6830.28	2909.38	2076.405	84
Residual	-5941.399	23353.250	.000	4386.110	84
Std. Residual	-1.330	5.227	.000	.982	84
Stud. Residual	-1.383	5.337	.002	1.005	84
Deleted Residual	-6428.279	24339.891	17.951	4594.516	84
Stud. Deleted Residual	-1.391	6.608	.025	1.113	84
Mahal. Distance	.117	10.392	2.964	2.007	84
Cook's Distance	.000	.301	.012	.040	84
Centered Leverage Value	.001	.125	.036	.024	84

a. Dependent Variable: GDP per capita (US\$) 2002 (UNDP 2004)

# **Diagnostics: Autocorrelation**

- Assumption: observations are independent
- Durbin-Watson statistic should be between 1.5 and 2.5

# **Diagnostics: Multicollinearity**

- Perfect multicollinearity: SPSS will remove one predictor
- High multicollinearity when two of the independent variables are highly correlated
- Standard errors will be large: more uncertainty in the model
- Check multicollinearity by calculating Variance Inflation Factor (VIF): VIF > 5 is definitely cause for concern!

# **Exercise: Categorical Predictors and Interaction Terms**

- 1. Use the ANES 2016 pilot dataset (available on Blackboard)
- 2. Download the codebook: https://tinyurl.com/anescodebook
- Create summary statistics of the following variables: pid1d educ, gender
- 4. Create new variable called piddem which is based on pidid and coded binary: 1: Democrat; 0: Not Democrat. Pay attention to missing values and recode them as system missing

```
ftohama
                                                                       Feeling thermometer - Barack Obama
                              numeric (byte)
ftobama, but 92 nonmissing values are not labeled
                     type:
label:
                              [0, 100]
                                                                  units: 1
                    range:
                                                           missing .: 0/1,200
missing .*: 2/1,200
          unique values:
                              101
        uni que my codes:
                 examples:
                              3
31
                              70
                                     70 - Fairly warm or favorable feeling
                              90
```

```
Party ID - Republican first
         type: numeric (byte)
label: pidld
                [1,4]
                                                units: 1
          range:
 unique values: 4
                                           missing .: 0/1,200
unique my codes:
                                           missing .*: 612/1,200
     tabulation:
                  Freq.
                           Numeric Label
                    229
                                   Democrat
                    123
                                2 Republican
                               3 Independent
                    195
                     41
                                   Something else
                    612
                               .b [9] Not Asked
```

```
educ
                                                                                   Education
                 type: numeric (byte)
                label: educ
                 range:
                        [1,6]
                                                      units: 1
         unique values:
                                                  missing .: 0/1,200
           tabulation:
                        Freq.
                                Numeric Label
                           102
                                          No HS
                           411
                                       2 High school graduate
                           257
                                       3 Some college
                                       4 2-year
                           106
                           202
                                          4-year
                           122
                                          Post - grad
```

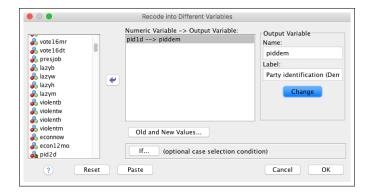
```
type: numeric (byte) label: gender

range: [1,2] units: 1
unique values: 2 missing .: 0/1,200

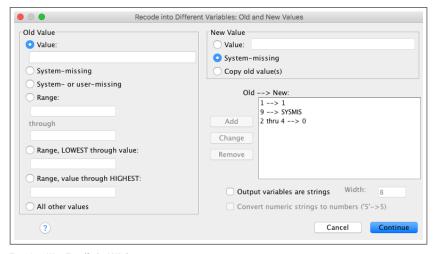
tabulation: Freq. Numeric Label
570 1 Male
630 2 Female
```

# Create a New Variable (I)

#### Transform → Recode into Different Variable



# Create a New Variable (II)



# **Exercise: Categorical Predictors and Interaction Terms**

- 1. Dependent variable: ftobama (feeling thermometer for Obama)
- 2. Independent variables: piddem, educ, gender
- 3. Explain the coding of these variables
- 4. Interpret these coefficients (in substantive terms!)

# **Regression Results**

# Model Summary Adjusted R Square R Square 1 .626<sup>a</sup> .392 .389

 a. Predictors: (Constant), educ, Party identification (Democrat), gender

Sum of

#### ANOVA<sup>a</sup>

Model		Squares	df	Mean Square	F	Sig.
1	Regression	335341.201	3	111780.400	125.312	.000 <sup>b</sup>
	Residual	520045.641	583	892.017		
	Total	855386.842	586			

a. Dependent Variable: ftobama

b. Predictors: (Constant), educ, Party identification (Democrat), gender

#### Coefficientsa

Std. Error of

the Estimate

29.867

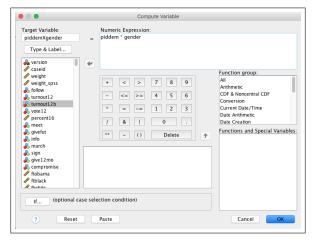
		Unstandardize	d Coefficients	Standardized Coefficients		
Model		В	Std. Error	Beta	t	Sig.
1	(Constant)	19.456	4.807		4.047	.000
	Party identification (Democrat)	47.872	2.551	.611	18.763	.000
	gender	5.400	2.490	.071	2.169	.031
	educ	.968	.818	.038	1.184	.237

# **Exercise: Categorical Predictors and Interaction Terms**

- Generate variable called piddemXgender which is an interaction of gender and piddem
- 2. Re-run the model and add piddemXgender
- 3. Interpret the coefficient of the interaction

## Interaction Effect

### Transform → Compute Variable



# **Regression Results with Interaction**

#### **Model Summary**

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.627ª	.394	.390	29.851

 Predictors: (Constant), piddemXgender, educ, gender, Party identification (Democrat)

#### ANOVA<sup>a</sup>

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	336759.705	4	84189.926	94.477	.000b
	Residual	518627.136	582	891.112		
	Total	855386.842	586			

- a. Dependent Variable: ftobama
- b. Predictors: (Constant), piddemXgender, educ, gender, Party identification (Democrat)

#### Coefficientsa

		Unstandardize	Unstandardized Coefficients			
Mode	el .	В	Std. Error	Beta	t	Sig.
1	(Constant)	15.712	5.647		2.782	.006
	Party identification (Democrat)	57.867	8.322	.739	6.953	.000
	gender	7.866	3.165	.103	2.486	.013
	educ	1.010	.818	.040	1.234	.218
	piddemXgender	-6.465	5.124	142	-1.262	.208

a. Dependent Variable: ftobama

# **Useful Explanation**

SPSS Regression Diagnostics: https://stats.idre.ucla.edu/spss/seminars/introduction-to-regression-with-spss/introreg-lesson2/

Doing it all in R:  $https://github.com/stefan-mueller/research-methods/blob/master/code/ht05/ht_05\_replicate\_spss.R$