ML course, 2019 fall

What you should know:

Week 1, 2: Basic issues in Probabilities

Read: Chapter 2 (section 2.1) from the Foundations of Statistical Natural Language Processing book by Christopher Manning and Hinrich Schütze, MIT Press, 2002.¹

Week 1:

PART I: A brief introduction to Machine Learning

(slides 0-9, 20-24 from https://profs.info.uaic.ro/~ciortuz/SLIDES/ml0.pdf)

PART II: Random events

(slides 3-6 from https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf)

Concepts/definitions:

- sample space, random event, event space
- probability function
- conditional probabilities
- independent random events (2 forms); conditionally independent random events (2 forms)

Theoretical results/formulas:

- elementary probability formula:
 # favorable cases
 # all possible cases
- the "multiplication" rule; the "chain" rule
- "total probability" formula (2 forms)
- Bayes formula (2 forms)

Exercises illustrating the above concepts/definitions and theoretical results/formulas, in particular: proofs for certain properties derived from the definition of the probability function for instance: $P(\emptyset) = 0$, $P(\bar{A}) = 1 - P(A)$, $A \subseteq B \Rightarrow P(A) \le P(B)$

Ciortuz et al.'s exercise book (2019) ch. Foundations, ex. 1-5 [6-7], 8, 61-64 [65-66], 67

Advanced issues:

o Similar tests:

 $\label{lem:http://www.cs.cmu.edu/} $$ http://www.cs.cmu.edu/~ninamf/courses/601sp15/hw/homework1.pdf (CMU, 2015 spring, N. Balcan) $$ http://curtis.ml.cmu.edu/w/courses/images/8/88/Homework1.pdf (CMU, 2016 spring, W. Cohen, N. Balcan) $$$

 $\label{eq:http://www.cs.cmu.edu/} $$ http://www.cs.cmu.edu/\sim mgormley/courses/10601b-f16/files/hw1_questions.pdf (CMU, 2016 fall, N. Balcan, M. Gormley) $$$

¹For a more concise / formal introductory text, see *Probability Theory Review for Machine Learning*, Samuel Ieong, November 6, 2006 (https://see.stanford.edu/materials/aimlcs229/cs229-prob.pdf) and/or *Review of Probability Theory*, Arian Maleki, Tom Do, Stanford University.

Week 2: Random variables [and a few basic probabilistic distributions]

(slides 7-16 from https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf)

Concepts/definitions:

- random variables; random variables obtained through function composition
- discrete random variables; probability mass function (p.m.f.) examples: Bernoulli, binomial [geometric, Poisson] distributions
- expectation (mean), variance, standard variation; covariance. (See definitions!)
- multi-valued random functions; joint, marginal, conditional distributions
- independence of random variables; conditional independence of random variables

Theoretical results/formulas:

• for any discrete variable X: $\sum_{x} p(x) = 1$, where p is the pmf of X

for any continuous variable X: $\int p(x) dx = 1$, where p is the pdf of X

Corollary: the *liniarity* of expectation: $E[\sum_{i=1}^{n} a_i X_i] = \sum_{i=1}^{n} a_i E[X_i].$

 $\begin{aligned} &Var[aX] = a^2 \, Var[X] \\ &Var[X] = E[X^2] - (E[X])^2 \\ &Cov(X,Y) = E[XY] - E[X]E[Y] \\ &Var[X+Y] = Var[X] + Var[Y] + 2 \, Cov(X,Y) \end{aligned}$

- X, Y independent variables $\Rightarrow Var[X + Y] = Var[X] + Var[Y]$
- X, Y independent variables \Rightarrow Cov(X, Y) = 0, i.e. E[XY] = E[X]E[Y]

Exercises illustrating the above concepts/definitions and theoretical results/formulas, concentrating especially on:

- computing probabilities
- computing means / expected values of random variables
- verifying the [conditional] independence of two or more random variables
- identifying in a given problem's text the underlying probabilistic distribution: either a basic one (e.g., Bernoulli, binomial, categorial etc.), or one derived [by function composition or] by summation of identically distributed random variables

Ciortuz et al.'s exercise book: ch. Foundations, ex. 9-15, 19, 20-21, [22] 68-75, 81, 82-83

Advanced issues (I):

Concepts/definitions:

- cumulative function distribution
- continuous random variables; probability density function (p.d.f.) examples: Gaussian, exponential, [Gamma, Beta, Laplace] distributions

Ciortuz et al.'s exercise book: ch. Foundations, ex. 25-28, 76-78

Theoretical result:

 For any vector of random variables, the covariance matrix is symmetric and positive semi-definite.

Ciortuz et al.'s exercise book: ch. Foundations, ex. 18

Advanced issues (II):

- the *likelihood function* (see *Estimating Probabilities*, additional chapter to the *Machine Learning* book by Tom Mitchell, 2016)
- the Bernoulli distribution: MLE and MAP estimation of the parameter

Week $3.\frac{1}{2}$: Introduction to Information Theory

Read: Chapter 2 (section 2.2) from the Foundations of Statistical Natural Language Processing book by Christopher Manning and Hinrich Schütze, MIT Press, 2002. (slides 28-31 [32-33] from https://profs.info.uaic.ro/~ciortuz/SLIDES/foundations.pdf)

Theoretical results/formulas:

•
$$0 \le H(X) \le H(\underbrace{1/n, 1/n, \dots, 1/n}_{n \text{ times}}) = \log_2 n$$

Concepts/definitions:

• entropy; specific conditional entropy; average conditional entropy; information gain (mutual information) joint entropy;

- IG(X;Y) = H(X) H(X|Y) = H(Y) H(Y|X)
- $IG(X;Y) \geq 0$
- IG(X;Y) = 0 iff X and Y are independent
- IG(X;X) = H(X)
- H(X,Y) = H(X) + H(Y|X) = H(Y) + H(X|Y)(generalisation: the chain rule, $H(X_1, ..., X_n) = H(X_1) + H(X_2 \mid X_1) + ... + H(X_n \mid X_1, ..., X_{n-1})$) • H(X,Y) = H(X) + H(Y) iff X and Y are indep.

Exercises illustrating the above concepts/definitions and theoretical results/formulas, concentrating especially on:

- computing different types of entropies: Ciortuz et al.'s exercise book: ch. Foundations, ex. 35-36, 39, 92;
- proof of some basic properties:
 Ciortuz et al.'s exercise book: ch. Foundations, ex. [33] 34, 40, 93-94 [95], 96, 98.

Advanced issues:

• cross-entropy

Ciortuz et al.'s exercise book: ch. Foundations, ex. 41-42, 97;

• relative entropy (Kullback-Leibler divergence)

Ciortuz et al.'s exercise book: ch. Foundations, ex. 38.

Weeks $3.\frac{2}{2}$, 4 and 5: Decision Trees

Read: Chapter 3 from Tom Mitchell's Machine Learning book.

Important Note:

See (i.e., do *not* skip!) the Overview (rom.: "Sumar") section for the *Decision Trees* chapter in Ciortuz et al.'s exercise book. It is in fact a "road map" for what we will be doing here. (This *note* applies also to all chapters.)

Week 3.
$$\frac{2}{2}$$
:

Decision trees and the ID3 algorithm:

applications;

analysis of the ID3 algorithm (as an algorithm per se);

properties of ID3 trees:

Ciortuz et al.'s exercise book, ch. Decision trees, ex. 1-9, 22.a, 29-40, 52 [53]

• decision trees:

seen as data structures: ex. 1, 7.b, 29 and as logic programs: ex. 2.e, 36.bc

• ID3 algorithm:

simple applications: ex. 2-3, 5, 34-35, 37-38

• analysis of ID3 as an algorithm per se:

recursive, divide-et-impera greedy: ex. 4, 22.a, 36 search algorithm: ex. 3, 35

• properties of ID3 trees: ex. 2-4, 7-9, 22.a, 30, 35-36 [39] 52

• implementation exercises: ex. 32 [53]

Important Note:

Some of the exercises listed above would be done in class (i.e., at seminaries) in an easier / nicer way if students would priorily do at home the exercise 32, which asks for the **implementation** of the **information gain** (and also entropy, specific conditional entropy and average conditional entropy), starting form the counts (more precisely, from the data partitions) associated to the leaf nodes of a **decision stump**.² Alternatively, the exercise 33 advises the student on how to conveniently use a **pocket calculator** in order to calculate the above mentioned entropies and the information gain.

Implementation exercises:

CMU, 2012 spring, Roni Rosenfeld, HW3

- Complete a given C (incomplete) implementation for ID3.
- Work firstly on a simple example (Play Tennis from Tom Mitchell's *Machine Learning* book) and secondly on a real dataset (Agaricus-Lepiota Mushrooms).
- Perform reduced-error (top-down vs. bottom-up) pruning to cope with overfitting.³

Note: CMU, 2011 spring, Roni Rosenfeld, HW3 – a similar problem to the above one — uses a *chess* dataset generated by Alen Shapiro (see *Structured Induction in Expert Systems*, 1983, 1987).

²This implementation could be later extanded to an implementation of ID3 algorithm (the basic form); see ex. 53. 3 CMU, 2011 spring, T. Mitchell, A. Singh, HW1, pr. 3 is similar to the above problem, except that *pruning* a node is conditioned on getting at least an ε increase in accuracy. (Dataset: mushrooms.)

Week 4:

extensions of the ID3 algorithm;

analysis of ID3 as a Machine Learning algorithm;

Ciortuz et al.'s ex. book, ch. *Decision trees*, ex. 10-12, 14-17 [18-19] 20 [21] 22, 42-45, [48-49] 50 [51]

• extensions of the ID3 algorithm

- handling of continuous attributes: ex. 10-12, 42-45
- decision surfaces, decision boundaries: ex. 10, 42, and ch. Instance-based learning, ex. 11.b

o other extensions to the ID3 algorithm

- handling of attributes with many values: ex. 14
- handling of attributes with costs: ex. 15
- using other impurity neasures as local optimality criterion in ID3: ex. 16
- reducing the greedy behaviour of the ID3 algorithm: ex. 18-19 [48-49]
- other splitting criteria (optional): ex. 13, 46-47

• analysis: ID3 as a Machine Learning algorithm

- inductive bias for ID3:

[LC: a hierarchical structure of the model, compatibility/consistency with the data, and] compactness of the resulting decision tree;

- -error analysis/computation: training error, validation error, n-fold cross-validation, CVLOO: ex. 6-8, 10, 22.d, 39-40, 43, 44.d
- ID3 as "eager" learner: ex. 17
- ID3 and [non-]robustness to noises, and overfitting: ex. 10, 22.bc, 43
- pruning strategies for decision trees: ex. 20 [21] [49] 50 [51]

Implementation exercises:

CMU, 2011 fall, T. Mitchell, A. Singh, HW1, pr. 2

- Working with continuous attributes on a real dataset: Breast Cancer.
- Complete a given a Matlab/Octave implementation for ID3.
- Perform reduced-error pruning.
- Implement another splitting criterion: the weighted misclassification rate.

Week 5: The AdaBoost Algorithm

Weeks 6-7: Bayesian Classifiers

Read

Chapter 6 from T. Mitchell's *Machine Learning* book (except subsections 6.11 and 6.12.2); (slides #3-5, 11-12, 14 in https://profs.info.uaic.ro/~ciortuz/SLIDES/ml6.pdf)

Week 8: midterm

Week 9: Instance-Based Learning

Read: Chapter 8 from Tom Mitchell's Machine Learning book.

Weeks 10-14: Clustering

Weeks 10-12: Hierarchical and Partitional Clustering

Read: Chapter 14 from Manning and Schütze' Foundations of Statistical Natural Language Processing book.

Week 13:

The likelihood function, and the Maximum Likelihood method for estimating parameters of probabilistic distributions (abbrev., MLE)

Read: Estimating Probabilities, additional chapter to the Machine Learning book by Tom Mitchell, 2016.

Week 14: Model-based Clustering

Using the EM algorithm to solve GMMs (Gaussian Mixture Models), the uni-variate case.

Read: Tom Mitchell, *Machine Learning*, sections 6.12.1 and 6.12.3; see section 3 in the *overview* of the *Clustering* chapter in Ciortuz et al.'s exercise book;

Weeks 15-16: [final] EXAM