CHAPTER 5

Conditionals and Recursion

The main topic of this chapter is the `if` statement, which executes different code depending on the state of the program. But first I want to introduce two new operators: floor division and modulus.

Floor Division and Modulus

The **floor division** operator, `//`, divides two numbers and rounds down to an integer. For example, suppose the run time of a movie is 105 minutes. You might want to know how long that is in hours. Conventional division returns a floating-point number:

```
>>> minutes = 105
>>> minutes / 60
1.75
```

But we don't normally write hours with decimal points. Floor division returns the integer number of hours, dropping the fraction part:

```
>>> minutes = 105
>>> hours = minutes // 60
>>> hours
1
```

To get the remainder, you could subtract off one hour in minutes:

```
>>> remainder = minutes - hours * 60
>>> remainder
45
```

An alternative is to use the **modulus operator**, `%`, which divides two numbers and returns the remainder:

```
>>> remainder = minutes % 60
>>> remainder
45
```

The modulus operator is more useful than it seems. For example, you can check whether one number is divisible by another—if `x % y` is zero, then `x` is divisible by `y`.

Also, you can extract the right-most digit or digits from a number. For example, `x % 10` yields the right-most digit of `x` (in base 10). Similarly `x % 100` yields the last two digits.

If you are using Python 2, division works differently. The division operator, `/`, performs floor division if both operands are integers, and floating-point division if either operand is a `float`.

Boolean Expressions

A **boolean expression** is an expression that is either true or false. The following examples use the operator `==`, which compares two operands and produces `True` if they are equal and `False` otherwise:

```
>>> 5 == 5
True
>>> 5 == 6
False
```

`True` and `False` are special values that belong to the type `bool`; they are not strings:

```
>>> type(True)
<class 'bool'>
>>> type(False)
<class 'bool'>
```

The `==` operator is one of the **relational operators**; the others are:

```
x != y               # x is not equal to y
x > y                # x is greater than y
x < y                # x is less than y
x >= y               # x is greater than or equal to y
x <= y               # x is less than or equal to y
```

Although these operations are probably familiar to you, the Python symbols are different from the mathematical symbols. A common error is to use a single equal sign (`=`) instead of a double equal sign (`==`). Remember that `=` is an assignment operator and `==` is a relational operator. There is no such thing as `=<` or `=>`.

Logical Operators

There are three **logical operators**: `and`, `or`, and `not`. The semantics (meaning) of these operators is similar to their meaning in English. For example, `x > 0 and x < 10` is true only if `x` is greater than 0 *and* less than 10.

`n%2 == 0 or n%3 == 0` is true if *either or both* of the conditions is true, that is, if the number is divisible by 2 *or* 3.

Finally, the `not` operator negates a boolean expression, so `not (x > y)` is true if `x > y` is false, that is, if `x` is less than or equal to `y`.

Strictly speaking, the operands of the logical operators should be boolean expressions, but Python is not very strict. Any nonzero number is interpreted as `True`:

```
>>> 42 and True
True
```

This flexibility can be useful, but there are some subtleties to it that might be confusing. You might want to avoid it (unless you know what you are doing).

Conditional Execution

In order to write useful programs, we almost always need the ability to check conditions and change the behavior of the program accordingly. **Conditional statements** give us this ability. The simplest form is the `if` statement:

```
if x > 0:
    print('x is positive')
```

The boolean expression after `if` is called the **condition**. If it is true, the indented statement runs. If not, nothing happens.

`if` statements have the same structure as function definitions: a header followed by an indented body. Statements like this are called **compound statements**.

There is no limit on the number of statements that can appear in the body, but there has to be at least one. Occasionally, it is useful to have a body with no statements (usually as a place keeper for code you haven't written yet). In that case, you can use the `pass` statement, which does nothing.

```
if x < 0:
    pass          # TODO: need to handle negative values!
```

Alternative Execution

A second form of the `if` statement is "alternative execution", in which there are two possibilities and the condition determines which one runs. The syntax looks like this:

```
if x % 2 == 0:
    print('x is even')
else:
    print('x is odd')
```

If the remainder when `x` is divided by 2 is 0, then we know that `x` is even, and the program displays an appropriate message. If the condition is false, the second set of statements runs. Since the condition must be true or false, exactly one of the alternatives will run. The alternatives are called **branches**, because they are branches in the flow of execution.

Chained Conditionals

Sometimes there are more than two possibilities and we need more than two branches. One way to express a computation like that is a **chained conditional**:

```
if x < y:
    print('x is less than y')
elif x > y:
    print('x is greater than y')
else:
    print('x and y are equal')
```

`elif` is an abbreviation of "else if". Again, exactly one branch will run. There is no limit on the number of `elif` statements. If there is an `else` clause, it has to be at the end, but there doesn't have to be one.

```
if choice == 'a':
    draw_a()
elif choice == 'b':
    draw_b()
elif choice == 'c':
    draw_c()
```

Each condition is checked in order. If the first is false, the next is checked, and so on. If one of them is true, the corresponding branch runs and the statement ends. Even if more than one condition is true, only the first true branch runs.

Nested Conditionals

One conditional can also be nested within another. We could have written the example in the previous section like this:

```
if x == y:
    print('x and y are equal')
else:
    if x < y:
        print('x is less than y')
    else:
        print('x is greater than y')
```

The outer conditional contains two branches. The first branch contains a simple statement. The second branch contains another `if` statement, which has two branches of its own. Those two branches are both simple statements, although they could have been conditional statements as well.

Although the indentation of the statements makes the structure apparent, **nested conditionals** become difficult to read very quickly. It is a good idea to avoid them when you can.

Logical operators often provide a way to simplify nested conditional statements. For example, we can rewrite the following code using a single conditional:

```
if 0 < x:
    if x < 10:
        print('x is a positive single-digit number.')
```

The `print` statement runs only if we make it past both conditionals, so we can get the same effect with the `and` operator:

```
if 0 < x and x < 10:
    print('x is a positive single-digit number.')
```

For this kind of condition, Python provides a more concise option:

```
if 0 < x < 10:
    print('x is a positive single-digit number.')
```

Recursion

It is legal for one function to call another; it is also legal for a function to call itself. It may not be obvious why that is a good thing, but it turns out to be one of the most magical things a program can do. For example, look at the following function:

```
def countdown(n):
    if n <= 0:
        print('Blastoff!')
    else:
        print(n)
        countdown(n-1)
```

If `n` is 0 or negative, it outputs the word, "Blastoff!" Otherwise, it outputs `n` and then calls a function named `countdown`—itself—passing `n-1` as an argument.

What happens if we call this function like this?

```
>>> countdown(3)
```