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## **Template**

```
#include <bits/stdc++.h>
#define ff first
#define ss second
#define mp make_pair
#define mt make_tuple
#define pb push_back
#define eb emplace_back
#define ep emplace
#define MOD 1000000007LL
#define all(x) (x).begin(), (x).end()
#define forn(i, n) for(int i = 0; i < int(n); i++)
#define for1(i, n) for(int i = 1; i <= int(n); i++)
#define ford(i, n) for(int i = int(n) - 1; i \ge 0; i--)
#define fore(i, a, b) for(int i = int(a); i <= int(b); i++)
#define debug(x) cerr << #x << "_=_" << x << endl
using namespace std;
typedef long long 11;
const 11 oo = 1000000000000000000000;
const int N = 100005;
int main(){
   return 0;
.vimrc
set statusline+=%F
set number
set showcmd
set cindent
set smarttab
set autoindent
set smartindent
set tabstop=4
set shiftwidth=4
set softtabstop=4
set expandtab
set smartcase
```

## Ad hoc

## Go up for ultras

```
struct Segtree{
  int n;
  vector<int> st;
  void build(int p, int L, int R, const int v[]) {
     if(L == R) { st[p] = v[L]; return; }
     int mid = (L + R) / 2;
     build(2*p, L, mid, v);
     build(2*p+1, mid+1, R, v);
     st[p] = max(st[2*p], st[2*p+1]);
   int findL(int p, int i, int L, int R, int v) {
     if(i <= L || v >= st[p]) return -1;
     if(L == R) return L;
     int mid = (L + R) / 2;
     int ret = -1;
     if(i > mid+1 && st[2*p+1] > v)
         ret = findL(2*p+1, i, mid+1, R, v);
     if(ret != -1) return ret;
      return findL(2*p, i, L, mid, v);
  int findR(int p, int i, int L, int R, int v) {
     if(i > R || v >= st[p]) return -1;
     if(L == R) return L;
     int mid = (L + R) / 2;
     int ret = -1;
     if(i < mid && st[2*p] > v)
        ret = findR(2*p, i, L, mid, v);
     if(ret != -1) return ret;
      return findR(2*p+1, i, mid+1, R, v);
   Segtree (int sz, const int v[]) : n(sz), st(4*sz, 0) {
     build(1, 0, n-1, v);
   int findR(int i, int v) {
      return findR(1, i, 0, n-1, v);
   int findL(int i, int v) {
      return findL(1, i, 0, n-1, v);
};
```

## Small to Large

```
void cnt_sz(int u, int p = -1) {
   sz[u] = 1;
   for (int v : q[u]) if (v != p)
      cnt_sz(v, u), sz[u] += sz[v];
void add(int u, int p, int big = -1) {
   // Update info about this vx in global answer
   for(int v : g[u]) if(v != p && v != big)
      add(v, u);
void dfs(int u, int p, int keep) {
   int big = -1, mmx = -1;
   for(int v : q[u]) if(v != p && sz[v] > mmx)
      mmx = sz[v], big = v;
   for(int v : g[u]) if(v != p && v != big)
      dfs(v, u, 0);
   if (big !=-1) dfs (big, u, 1);
   add(u, p, big);
   for(auto x : q[u]) {
      // answer all queries for this vx
   if(!keep){
      // Remove data from this subtree
```

## Estrutura de Dados

## Segtree

```
struct Segtree{
   int n;
   vector<1l> st, lazy;

void prop(int p, int L, int R){
   if(lazy[p]){
```

```
st[p] += lazy[p] * (R - L + 1);
         if (L != R) lazy[2*p] += lazy[p], lazy[2*p+1] += lazy[p];
         lazy[p] = 0;
     }
  void update(int p, int L, int R, int i, int j, ll v){
      prop(p, L, R);
     if(L > j || R < i) return;
     if(L >= i && R <= j) {
         lazy[p] = v;
         prop(p, L, R);
         return;
      int mid = (L+R)/2;
      update(2*p, L, mid, i, j, v);
      update(2*p+1, mid+1, R, i, j, v);
      st[p] = st[2*p] + st[2*p+1];
  11 query(int p, int L, int R, int i, int j){
      prop(p, L, R);
     if(L > j || R < i) return 0;
     if(L >= i && R <= j) return st[p];</pre>
     int mid = (L+R)/2;
      return query(2*p, L, mid, i, j) + query(2*p+1, mid+1, R, i, j);
public:
   Segtree(int sz = 0) : n(sz), st(4*sz, 0), lazy(4*sz, 0){}
  // sum v to every element in range [i, j]
  void update(int i, int j, ll v){
      update(1, 1, n, i, j, v);
  11 query(int i, int j){
      return query(1, 1, n, i, j);
};
```

## Contra Ataque Ramsay

```
#include <iostream>
#include <cstdio>
#include <cstring>
#include <liist>
#include <vector>

#define LADO 800
#define SEG_LADO 1400000

using namespace std;
```

```
class Sqtree{
                                                                                           tmp2 = max(arv[(p<<2)+3], arv[(p<<2)+4]);
   private:
                                                                                           arv[p] = max(tmp1, tmp2);
      int arv[SEG_LADO];
   public:
      int query(int L, int R, int D, int U, int 1, int r, int d, int u, int p);
      void update(int L, int R, int D, int U, int pos_x, int pos_y, int num, int p);
      Sqtree() {memset(arv, 0, SEG_LADO<<2);};</pre>
                                                                                     vector<int> G[50001];
}tipo_segtree;
                                                                                     Sqtree *tree;
                                                                                     tipo_soldado soldado[50001];
                                                                                     bool is_root[50001];
typedef struct _sold{
                                                                                     int ans = 1;
   int x,y;
                                                                                     void dfs(int no){
   bool pai;
                                                                                        int tmp = tree->query(0, LADO, 0, LADO, 0, soldado[no].x-1, 0, soldado[no].y-1, 0);
}tipo_soldado;
                                                                                        tmp++;
                                                                                        tree->update(0, LADO, 0, LADO, soldado[no].x, soldado[no].y, tmp, 0);
int Sqtree::query(int L, int R, int D, int U, int l, int r, int d, int u, int p) {
                                                                                        ans = max(ans, tmp);
   if(r < L || 1 > R || d > U || u < D)
                                                                                        for(int j : G[no])
      return 0;
                                                                                           dfs(j);
   if(L >= 1 && R <= r && U <= u && D >= d) {
                                                                                        tree->update(0, LADO, 0, LADO, soldado[no].x, soldado[no].y, 0, 0);
      return arv[p];
   int tmp1, tmp2, tmp3, tmp4;
   tmp1 = query(L, (L+R)>>1, D, (U+D)>>1, l, r, d, u, (p<<2)+1);
                                                                                     int main() {
                                                                                        int N, M, i, j, no_pai, no_filho;
   tmp2 = query(L, (L+R)>>1, ((U+D)>>1) + 1, U, 1, r, d, u, (p<<2)+2);
   tmp3 = query(((L+R)>>1) + 1, R, D, (U+D)>>1, 1, r, d, u, (p<<2)+3);
                                                                                        tree = new Sgtree();
   tmp4 = query(((L+R)>>1) + 1, R, ((U+D)>>1) + 1, U, 1, r, d, u, (p<<2)+4);
                                                                                        scanf("%d, %d", &N, &M);
   tmp1 = max(tmp1, tmp2);
                                                                                        for(i = 1; i <= N; i++) {
   tmp1 = max(tmp1, tmp3);
                                                                                           scanf("%d", &soldado[i].x);
   return max(tmp1, tmp4);
                                                                                           scanf("%d", &soldado[i].y);
                                                                                           soldado[i].x += 400;
                                                                                           soldado[i].y += 400;
void Sgtree::update(int L, int R, int D, int U, int pos_x, int pos_y, int num, int p){}
   if (L == R && U == D) {
      arv[p] = num;
                                                                                        for(i = 1; i <= N; i++) is_root[i] = 1;</pre>
                                                                                        for(i = 1; i <= M; i++) {</pre>
   else
                                                                                           scanf("%d.%d", &no_filho, &no_pai);
      if(pos_x <= (L+R)>>1) {
                                                                                           G[no_pai].push_back(no_filho);
         if(pos_y <= (U+D)>>1)
                                                                                           is_root[no_filho] = 0;
            update(L, (L+R)>>1, D, (U+D)>>1, pos_x, pos_y, num, (p<<2)+1);
            update(L, (L+R)>>1, ((U+D)>>1) + 1, U, pos_x, pos_y, num, (p<<2)+2);
                                                                                        for(i = 1; i <= N; i++) {</pre>
                                                                                           if(!is_root[i]) continue;
      else{
                                                                                           if(!G[i].empty())
         if(pos_y <= (U+D)>>1)
                                                                                              dfs(i);
            update(((L+R)>>1) + 1, R, D, (U+D)>>1, pos_x, pos_y, num, (p<<2)+3);
            update(((L+R)>>1) + 1, R, ((U+D)>>1) + 1, U, pos_x, pos_y, num, (p<<2)+4); printf("%d\n", ans);
                                                                                        return 0;
      int tmp1, tmp2;
      tmp1 = max(arv[(p<<2)+1], arv[(p<<2)+2]);
```

## Sparse Table

```
#include <bits/stdc++.h>
#define mp make_pair
#define ff first
#define ss second
using namespace std;
typedef long long 11;
int st1[200005][20], st2[200005][20];
void build(int n) {
   int i, j;
   for (j = 1; 1 << j <= n; j++) {
      for(i = 0; i +(1<<j) <= n; i++) {
         st1[i][j] = max(st1[i][j-1], st1[i+(1<<(j-1))][j-1]);
         st2[i][j] = min(st2[i][j-1], st2[i+(1<<(j-1))][j-1]);
int getA(int 1, int r){
   int num = r-1+1, k=0;
   while (num>=2) num/=2, k++;
   return max(st1[1][k], st1[r-(1<<k)+1][k]);
int getB(int 1, int r) {
   int num = r-1+1, k=0;
   while (num>=2) num/=2, k++;
   return min(st2[1][k], st2[r-(1<<k)+1][k]);
int bsearch1(int i, int n) {
   int mid, l=i-1, r=n;
   while (1+1 < r) {
      mid = (l+r) >> 1;
      int a = getA(i, mid);
      int b = getB(i, mid);
      if(a < b) l = mid;
      else r = mid;
   return r;
int bsearch2(int i, int n){
   int mid, l=i-1, r=n;
   while (1+1 < r) {
```

```
mid = (1+r) >> 1;
      int a = getA(i, mid);
      int b = getB(i, mid);
      if(a <= b) l = mid;
      else r = mid;
   return r;
int main(){
   int n,i,j;
   scanf("%d", &n);
   for(i = 0; i < n; i++) scanf("%d", &st1[i][0]);</pre>
   for(i = 0; i < n; i++) scanf("%d", &st2[i][0]);
  build(n);
  11 \text{ ans} = 0;
   for(i = 0; i < n; i++) {
     int x = bsearch1(i,n);
      int y = bsearch2(i,n);
      if(y > x)
         ans += (y-x);
  printf("%lld\n", ans);
   return 0;
```

## Merge Sort Tree

```
#include <bits/stdc++.h>
using namespace std;
struct MergeTree {
  int n;
  vector<vector<int> > st;
  void build(int p, int L, int R, const int v[]) {
     if (L == R) {
         st[p].push_back(v[L]);
         return:
     int mid = (L+R)/2;
     build(2*p, L, mid, v);
     build(2*p+1, mid+1, R, v);
     st[p].resize(R-L+1);
     merge(st[2*p].begin(), st[2*p].end(),
            st[2*p+1].begin(), st[2*p+1].end(),
            st[p].begin());
```

```
int update_cf (int a, int v) {
                                                                                            for (int i = a; i < n; i += (i & -i)) ft[i] += v;</pre>
   int query(int p, int L, int R, int i, int j, int x) const{
      if(L > j || R < i) return 0;
                                                                                            return 0; }
      if(L >= i && R <= j) {
         int id = lower_bound(st[p].begin(), st[p].end(), x) - st[p].begin();
                                                                                      };
         return int(st[p].size()) - id;
      int mid = (L+R)/2;
                                                                                      class ft invert {
      return query(2*p, L, mid, i, j, x) +
                                                                                      public:
         query (2*p+1, mid+1, R, i, j, x);
                                                                                         vector<int> ft_inv;
                                                                                         int n;
   public:
                                                                                         ft_invert (int size) : n(size), ft_inv(n, 0){}
   MergeTree(int sz, const int v[]): n(sz), st(4*sz) {
      build(1, 1, n, v);
                                                                                         int query_cf_inv(int a) const{ int resp = 0;
                                                                                            for (int i = a; i < n; i += (i & -i)) resp += ft_inv[i];</pre>
                                                                                            return resp; }
   //number of elements >= x on segment [i, j]
                                                                                         int update cf inv (int a, int v) {
   int query(int i, int j, int x) const{
                                                                                            for (int i = a; i; i -= (i & -i)) ft_inv[i] += v;
      if(i > j) swap(i, j);
                                                                                            return 0; }
      return query(1, 1, n, i, j, x);
                                                                                      };
};
                                                                                      /* bit diferente -> range minimum query*/
int n, v[100005];
                                                                                      class ft_diff {
                                                                                      public:
int main(){
                                                                                         int n;
                                                                                         vector<int> ft;
   scanf("%d", &n);
                                                                                         vector<int> ft inv;
                                                                                         vector<int> vet:
   for(int i = 1; i <= n; i++)</pre>
      scanf("%d", v+i);
                                                                                         ft_diff(int size) : n(size), ft(n, 0), ft_inv(n, 0), vet(n, 0){
                                                                                            for (int i = 1; i < n; i++) ft[i] = ft_inv[i] = i; }</pre>
  MergeTree mst(n, v);
                                                                                         int query_rmq (int a, int b) const{
                                                                                            int i, mini = a;
   return 0;
                                                                                            //bit normal
                                                                                            for (i = a; i <= b; i += (i & -i))
                                                                                               if (i + (i & -i) <= b)
                                                                                                  mini = vet[mini] < vet[ft_inv[i]] ? mini : ft_inv[i];</pre>
Bit bolada
                                                                                               else mini = vet[mini] < vet[i] ? mini : i;</pre>
                                                                                            //bit invertida
                                                                                            for (i = b; i >= a; i -= (i & -i))
/* bit normal -> cumulative frequency */
                                                                                               if (i - (i & -i) >= a)
class ft_normal {
                                                                                                  mini = vet[mini] < vet[ft[i]] ? mini : ft[i];</pre>
public:
                                                                                            return mini;
   vector<int> ft;
   int n;
                                                                                         int upd (int a, int v) {
                                                                                            put_value(a, v);
   ft_normal (int size) : n(size), ft(n, 0){}
                                                                                            update_rmq(a, v);
   int query_cf(int a) const{ int resp = 0;
                                                                                            return 0;
      for (int i = a; i; i -= (i & -i)) resp += ft[i];
```

return resp; }

```
#include <algorithm>
                                                                             #include <vector>
   int put_value (int a, int v) {
     vet[a] = v;
                                                                             #include <set>
     return 0;
                                                                             #include <map>
                                                                             #include <string>
  int update_rmq (int a, int v) const{
                                                                             #include <utility>
     int mini_l = a, mini_r = a;
                                                                             #include <cstring>
     for (int i = a; i < n; i += (i \& -i)) {
                                                                             #include <cassert>
        if (ft[i] != a) ft[i] = v < vet[ft[i]] ? a : ft[i];</pre>
                                                                             #include <cmath>
                                                                             #include <stack>
           ft[i] = vet[mini_l] < vet[mini_r] ?</pre>
                                                                             #include <queue>
              (vet[mini_1] < v ? mini_1 : a) : (vet[mini_r] < v ? mini_r : a);</pre>
           if (i >= a + 1)
                                                                             using namespace std;
             mini_r = vet[mini_r] < vet[ft_inv[i]] ? mini_r : i;</pre>
           if (i - (i & -i) + 1 <= a - 1)
                                                                             const int MAXN = 105000;
             mini_l = vet[mini_l] < vet[ft[i - (i & -i) + 1]]?
                mini_l : i - (i \& -i) + 1;
                                                                             struct node {
                                                                               int next[26];
                                                                               int len:
     mini_l = a, mini_r = a;
                                                                               int sufflink;
     //bit invertida
                                                                                int num;
     for (int i = a; i; i -= (i & -i)) {
                                                                             };
        if (ft_inv[i] != a) ft_inv[i] = v < vet[ft_inv[i]] ? a : ft_inv[i];</pre>
        else {
                                                                             int len;
           ft_inv[i] = vet[mini_l] < vet[mini_r] ?</pre>
                                                                             char s[MAXN];
              (vet[mini_1] < v ? mini_1 : a) : (vet[mini_r] < v ? mini_r : a);</pre>
                                                                             node tree[MAXN];
                                                                             int num; // node 1 - root with len -1, node 2 - root with len 0
           if (i + (i \& -i) - 1 >= a + 1)
             mini_r = vet[mini_r] < vet[ft_inv[i + (i & -i) - 1]]?
                                                                             int suff; // max suffix palindrome
                mini_r : (i + (i \& -i) - 1);
                                                                             long long ans;
           if (i <= a - 1)
             mini_l = vet[mini_l] < vet[ft[i]] ? mini_l : i;</pre>
                                                                             bool addLetter(int pos) {
                                                                               int cur = suff, curlen = 0;
                                                                               int let = s[pos] - 'a';
     return 0;
                                                                               while (true) {
                                                                                  curlen = tree[cur].len;
};
                                                                                  if (pos - 1 - curlen >= 0 && s[pos - 1 - curlen] == s[pos])
Palindromic Tree
                                                                                  cur = tree[cur].sufflink;
                                                                               if (tree[cur].next[let]) {
return false:
 This code counts number of palindrome substrings of the string.
 Based on problem 1750 from informatics.mccme.ru:
                                                                               num++;
http://informatics.mccme.ru/moodle/mod/statements/view.php?chapterid=1750
                                                                                suff = num;
 tree[cur].next[let] = num;
#include <iostream>
                                                                               if (tree[num].len == 1) {
#include <cstdio>
```

#include <cstdlib>

tree[num].sufflink = 2;

```
tree[num].num = 1;
      return true;
   while (true) {
     cur = tree[cur].sufflink;
      curlen = tree[cur].len;
     if (pos - 1 - curlen >= 0 && s[pos - 1 - curlen] == s[pos]) {
         tree[num].sufflink = tree[cur].next[let];
         break;
   tree[num].num = 1 + tree[tree[num].sufflink].num;
   return true;
void initTree() {
  num = 2; suff = 2;
  tree[1].len = -1; tree[1].sufflink = 1;
   tree[2].len = 0; tree[2].sufflink = 1;
int main() {
   //assert(freopen("input.txt", "r", stdin));
   //assert(freopen("output.txt", "w", stdout));
   gets(s);
   len = strlen(s);
   initTree();
   for (int i = 0; i < len; i++) {</pre>
     addLetter(i);
      ans += tree[suff].num;
   cout << ans << endl;
   return 0;
```

# Paradigmas

### FFT

```
// typedef complex<double> base;
struct base{
```

```
double r, i;
   base(double r = 0, double i = 0) : r(r), i(i) {}
   base operator*(const base &o) {
      return base(r*o.r - i*o.i, r*o.i + o.r*i);
  base& operator *= (const base &o) {
      double newr = r*o.r - i*o.i, newi = r*o.i + o.r*i;
      r = newr, i = newi;
      return *this;
  base& operator+= (const base &o) {
      r += o.r, i += o.i;
      return *this;
  base& operator/=(const double &o) {
      r /= o, i /= o;
      return *this;
  base& operator-= (const base &o) {
      r -= o.r, i -= o.i;
      return *this:
  base operator+(const base &o) {
      return base(r + o.r, i + o.i);
  base operator-(const base &o) {
      return base(r - o.r, i - o.i);
};
double PI = acos(-1);
void fft(vector<base> &a, bool inv) {
   int n = (int)a.size();
   for (int i = 1, j = 0; i < n; i++) {
     int bit = n >> 1:
      for(; j >= bit; bit >>= 1)
         j -= bit;
     j += bit;
      if(i < j)
         swap(a[i], a[j]);
   for(int len = 2; len <= n; len <<= 1) {</pre>
      double ang = 2*PI/len * (inv ? -1 : 1);
```

```
base wlen(cos(ang), sin(ang));
      for(int i = 0; i < n; i += len) {</pre>
         base w(1);
         for (int j = 0; j < len/2; j++) {
            base u = a[i+j], v = a[i+j+len/2] * w;
            a[i+j] = u + v;
            a[i+j+len/2] = u - v;
            w \star = wlen;
   if (inv)
      for(int i = 0; i < n; i++)</pre>
         a[i] /= n;
void multiply(const vector<int> &a, const vector<int> &b, vector<int> &res) {
   vector<base> fa(a.begin(), a.end()), fb(b.begin(), b.end());
   size t n = 1;
   while(n < a.size()) n <<= 1;
   while(n < b.size()) n <<= 1;
   n <<= 1;
   fa.resize(n), fb.resize(n);
   fft(fa, false), fft (fb, false);
   for(size_t i = 0; i < n; i++)</pre>
      fa[i] \star = fb[i];
   fft(fa, true);
   res.resize (n);
   for(size_t i = 0; i < n; ++i)</pre>
      res[i] = int(fa[i].real() + 0.5);
NTT
const int mod = 7340033:
const int root = 5;
const int root_1 = 4404020;
const int root_pw = 1<<20;</pre>
void fft (vector<int> & a, bool invert) {
   int n = (int) a.size();
   for (int i=1, j=0; i<n; ++i) {</pre>
      int bit = n >> 1;
      for (; j>=bit; bit>>=1)
         j -= bit;
      j += bit;
      if (i < j)
```

swap (a[i], a[j]);

```
for (int len=2; len<=n; len<<=1) {
    int wlen = invert ? root_1 : root;
    for (int i=len; i<root_pw; i<<=1)
        wlen = int (wlen * 111 * wlen % mod);
    for (int i=0; i<n; i+=len) {
        int w = 1;
        for (int j=0; j<len/2; ++j) {
            int u = a[i+j], v = int (a[i+j+len/2] * 111 * w % mod);
            a[i+j] = u+v < mod ? u+v : u+v-mod;
            a[i+j+len/2] = u-v >= 0 ? u-v : u-v+mod;
            w = int (w * 111 * wlen % mod);
        }
    }
}
if (invert) {
    int nrev = reverse (n, mod);
    for (int i=0; i<n; ++i)
        a[i] = int (a[i] * 111 * nrev % mod);
}</pre>
```

## Matemática

### Euclides Extendido

```
// a*x + b*y = gcd(a, b), <gcd, <x, y>>
typedef tuple<int, int, int> tiii;
tiii euclidesExt(int a, int b) {
    if(b == 0) return tiii(a, 1, 0);
    tiii ret = euclidesExt(b, a % b);

    int q, w, e;
    tie(q, w, e) = ret;

    get<1>(ret) = e;
    get<2>(ret) = w - e*(a / b);

    return ret;
}

// a*b = 1 (mod c) <-> a*b + c*k = 1
int invmult(int a, int b) {
    return (get<1>(euclidesExt(a, b)) + b) % b;
}
```

## Função totiente

```
1l totiente(ll n) {
    ll ans = n;
    for(ll i = 2; i*i <= n; i++) {
        if(n % i == 0) {
            ans = (ans / i) * (i-1);
            while(n % i == 0) n /= i;
        }
    }
    if(n > 1) ans = (ans / n) * (n - 1);
    return ans;
}
```

## Eliminação Gaussiana

```
// Gaussian elimination
//
// Solves systems of linear equations.
// To use, build a matrix of coefficients and call run(mat, R, C).
// If the i-th variable is free, row[i] will be -1, otherwise it's value will
// be ans[i].
// Time complexity: O(R * C^2)
// Constants to configure:
// - MAXC is the number of columns
// - eps is the epsilon value
namespace Gauss {
 const int MAXC = 1001;
 int row[MAXC];
 double ans[MAXC];
 void run(double mat[][MAXC], int R, int C) {
  REP(i, C) row[i] = -1;
   int r = 0;
   REP(c, C) {
    int k = r:
    FOR(i, r, R) if (fabs(mat[i][c]) > fabs(mat[k][c])) k = i;
    if (fabs(mat[k][c]) < eps) continue;</pre>
    REP(j, C+1) swap(mat[r][j], mat[k][j]);
    REP(i, R) if (i != r) {
      double w = mat[i][c] / mat[r][c];
      REP(j, C+1) mat[i][j] -= mat[r][j] * w;
    row[c] = r++;
```

```
REP(i, C) {
  int r = row[i];
  ans[i] = r == -1 ? 0 : mat[r][C] / mat[r][i];
}
```

## Grafos

### LCA

```
int p[N], L[N], vis[N], dp[N][MAXL], pw[N], dp2[N][MAXL];
vector<vector<ii> > g;
void dfs(int u) {
   vis[u] = 1;
   for(ii &v : g[u]){
      if(!vis[v.ff]){
         p[v.ff] = u;
         L[v.ff] = L[u]+1;
         pw[v.ff] = v.ss;
         dfs(v.ff);
     }
int f(int u, int j) {
   if(j == 0) return p[u];
   if (dp[u][j] != -1) return dp[u][j];
   return dp[u][j] = f(f(u, j-1), j-1);
ll h(int u, int j) {
   if(j == 0) return pw[u];
   if (dp2[u][j] != -1) return dp2[u][j];
   return dp2[u][j] = h(u, j-1) + h(f(u, j-1), j-1);
int LCA(int u, int v) {
   if(L[u] < L[v]) swap(u, v);
   for(int i = MAXL-1; i >= 0; i--)
     if(L[u] - (1 << i) >= L[v])
         u = f(u, i);
   if(u == v) return v;
```

```
for (int i = MAXL-1; i >= 0; i--)
      if(L[u] - (1 << i) && f(u, i) != f(v, i))
         u = f(u, i), v = f(v, i);
   return p[u];
long long DIST(int u, int v) {
   if(L[u] < L[v]) swap(u, v);
   11 \text{ ans} = 0:
   for(int i = MAXL-1; i >= 0; i--)
      if(L[u] - (1 << i) >= L[v])
         ans += h(u, i), u = f(u, i);
   if(u == v) return ans;
   for(int i = MAXL-1; i >= 0; i--)
      if(L[u] > (1 << i) && f(u, i) != f(v, i))
         ans += h(u, i) + h(v, i), u = f(u, i), v = f(v, i);
   ans += pw[u] + pw[v];
   return ans;
int KTH(int a, int b, int c){
   int lca = LCA(a, b);
   int u = a, v = b;
   if(c > L[a] - L[lca] + 1) {
      c = L[a] - L[lca] + 1;
      for(int i = MAXL-1; i >= 0; i--)
         if(L[v] - (1 << i) - L[lca] >= c)
            v = f(v, i);
      return v;
   else{
      for(int i = MAXL-1; i >= 0; i--)
         if(L[a] - (L[u] - (1 << i)) + 1 <= c)
            u = f(u, i);
      return u;
   return 0;
```

### Fluxo Máximo

### Batalha Naval

```
#include <bits/stdc++.h>
using namespace std;
int pX[200200], pY[200200], distX[200200], distY[200200];
int n, ptrx = 1, ptry = 100100;
vector<vector<int> > g(200200);
bool bfs(){
   bool found = false;
   queue<int> Q;
   for(int i = 1; i < ptrx; i++)
      if(pX[i] == -1)
         Q.push(i);
   memset(distX, 0, sizeof distX);
   memset(distY, 0, sizeof distY);
   while(!Q.empty()){
      int u = Q.front(); Q.pop();
      for(int i = 0; i < (int)g[u].size(); i++){</pre>
         int v = g[u][i];
         if(distY[v] == 0){
            distY[v] = distX[u]+1;
            if(pY[v] == -1) found = true;
            else{
               distX[pY[v]] = distY[v]+1;
               Q.push(pY[v]);
   return found;
bool dfs(int u) {
   for(int i = 0; i < (int)g[u].size(); i++){</pre>
     int v = q[u][i];
      if(distX[u]+1 == distY[v]){
         distY[v] = 0; // "apaga" o vertice para a dfs
         if(pY[v] == -1 || dfs(pY[v])){
            pX[u] = v, pY[v] = u;
            return true;
   return false;
int f(){
```

```
int ans = 0;
   memset(pX, -1, sizeof pX);
   memset (pY, -1, sizeof pY);
   while (bfs())
      for(int i = 1; i < ptrx; i++)
         if(pX[i] == -1 \&\& dfs(i)) // eh possivel escolher um par para i
   return ans;
int main(){
   int x, y;
   map<int, int> mapx;
   map<int, int> mapy;
   while (scanf ("%d", &n) == 1) {
      g.assign(200200, vector<int>());
      for(int i = 0; i < n; i++) {</pre>
         scanf("%d, %d", &x, &y);
         if(mapx.find(x) == mapx.end()) mapx[x] = ptrx++;
         if(mapy.find(y) == mapy.end()) mapy[y] = ptry++;
         x = mapx[x];
         y = mapy[y];
         g[x].push_back(y);
         q[y].push_back(x);
      printf("%d\n", f());
   return 0;
Circulation
```

```
// Circulation
// Given a directed weighted graph, computes the minimum cost to run the maximum
// amount of circulation flow through the graph.
// Configure: MAXV
// Configure: MAXE (at least 2 * calls_to_edge)
// Functions:
// - init(n) initializes the algorithm with the given number of nodes
```

```
// - edge(x, y, c, w) adds an edge x->y with capacity c and weight w
// - run() runs the algorithm and returns total cost
// Time complexity: No idea, but it should be fast enough to solve any problem
// where V and E are up to around 1000.
//
// Constants to configure:
// - MAXV is the maximum number of vertices
// - MAXE is the maximum number of edges (i.e. twice the calls to function edge)
namespace Circu {
 const int MAXV = 1000100;
 const int MAXE = 1000100;
 int V, E;
 int how[MAXV], good[MAXV], bio[MAXV], cookie = 1; llint dist[MAXV];
 int from[MAXE], to[MAXE]; llint cap[MAXE], cost[MAXE];
 void init(int n) { V = n; E = 0; }
 void edge(int x, int y, llint c, llint w) {
  from [E] = x; to [E] = y; cap [E] = c; cost [E] = +w; ++E;
  from [E] = y; to [E] = x; cap [E] = 0; cost [E] = -w; ++E;
 void reset() {
  REP(i, V) dist[i] = 0;
  REP(i, V) how[i] = -1;
 bool relax() {
  bool ret = false;
  REP(e, E) if (cap[e]) {
    int x = from[e];
    int y = to[e];
    if (dist[x] + cost[e] < dist[y]) {</pre>
     dist[y] = dist[x] + cost[e];
     how[y] = e;
     ret = true;
   return ret:
 llint cycle(int s, bool flip = false) {
   int x = s;
  llint c = cap[how[x]];
    int e = how[x];
    c = min(c, cap[e]);
    x = from[e];
```

```
} while (x != s);
   llint sum = 0;
    int e = how[x];
    if (flip) {
     cap[e] -= c;
     cap[e^1] += c;
    sum += cost[e] * c;
    x = from[e];
   } while (x != s);
   return sum;
 llint push (int x) {
   for (++cookie; bio[x] != cookie; x = from[how[x]]) {
    if (!good[x] || how[x] == -1 || cap[how[x]] == 0) return 0;
    bio[x] = cookie;
    good[x] = false;
   return cycle(x) >= 0 ? 0 : cycle(x, true);
 llint run() {
   reset();
  llint ret = 0;
   REP(step, 2*V) {
    if (step == V) reset();
    if (!relax()) continue;
    REP(i, V) good[i] = true;
    REP(i, V) if (llint w = push(i)) ret += w, step = 0;
   return ret;
Dinic
const int N = 205, int E = 30006;
vector<int> g[N];
int ne;
struct Edge{
  int from, to;
   ll cap;
} edge[E];
```

int lvl[N], vis[N], pass, source, target, px[N];

```
ll run(int s, ll minE) {
   if(s == target) return minE;
   ll ans = 0;
   for(; px[s] < q[s].size(); px[s]++) {</pre>
      int e = g[s][ px[s] ];
      auto &v = edge[e], &rev = edge[e^1];
      if(lvl[v.to] != lvl[s]+1 || !v.cap) continue;
      11 tmp = run(v.to, min(minE, v.cap));
      v.cap -= tmp, rev.cap += tmp;
      ans += tmp, minE -= tmp;
      if (minE == 0) break;
   return ans;
int bfs(){
   queue<int> q;
   q.push(source);
   lvl[source] = 1;
   vis[source] = ++pass;
   while(!q.empty()){
      int u = q.front(); q.pop();
      px[u] = 0;
      for(int e : q[u]){
         auto v = edge[e];
         if(v.cap <= 0 || vis[v.to] == pass) continue;</pre>
         vis[v.to] = pass;
         lvl[v.to] = lvl[u]+1;
         q.push(v.to);
     }
   return vis[target] == pass;
ll flow(){
   ll ans = 0;
   while(bfs()) ans += run(source, oo);
   return ans;
void addEdge(int u, int v, ll c){
   edge[ne] = \{u, v, c\};
   q[u].pb(ne++);
```

### Min Cost Max Flow

```
#include <bits/stdc++.h>
#define forn(i, n) for(int i = 0; i < int(n); i++)
#define fore(i, a, b) for(int i = int(a); i <= int(b); i++)
#define ff first
#define ss second
#define mp make_pair
#define mt make_tuple
#define pb push_back
#define eb emplace_back
using namespace std;
typedef long long 11;
const 11 oo = 1e18;
const int N = 505;
const int E = 30006;
vector<int> q[N];
int ne:
struct Edge{
   int from, to;
   11 cap, cost;
} edge[E];
int lvl[N], vis[N], pass, source, target, p[N], px[N];
ll d[N];
11 back(int s, ll minE) {
   if(s == source) return minE;
   int e = p[s];
   ll f = back(edge[e].from, min(minE, edge[e].cap));
   edge[e].cap -= f;
   edge[e^1].cap += f;
   return f:
int dijkstra() {
   forn(i, N) d[i] = oo;
   priority_queue<pair<ll, int> > q;
   d[source] = 0;
```

```
q.emplace(0, source);
   while(!q.empty()){
      ll dis = -q.top().ff;
      int u = q.top().ss; q.pop();
      if(dis > d[u]) continue;
      for(int e : q[u]){
         auto v = edge[e];
         if(v.cap <= 0) continue;</pre>
         if(d[u] + v.cost < d[v.to]) {
            d[v.to] = d[u] + v.cost;
            p[v.to] = e;
            q.emplace(-d[v.to], v.to);
      }
   return d[target] != oo;
pair<ll, ll> mincost() {
   ll ans = 0, mf = 0;
   while(dijkstra()){
     11 f = back(target, oo);
     mf += f;
     ans += f * d[target];
   return {mf, ans};
void addEdge(int u, int v, ll c, ll cost){
   edge[ne] = \{u, v, c, cost\};
   g[u].pb(ne++);
char s[55][55];
int main(){
   int n, m;
   for(int tc = 1; scanf("%d,%d", &n, &m) == 2; tc++){
      ne = 0;
      int a, b, c;
      forn(i, m) {
         scanf("%d_%d_%d", &a, &b, &c);
         addEdge(a, b, 0, c);
         addEdge(b, a, 0, -c);
         addEdge(b, a, 0, c);
         addEdge(a, b, 0, -c);
```

```
int d, k;
scanf("%d_%d", &d, &k);
forn(i, ne) if(i % 2 == 0) edge[i].cap = k;
source = 0, target = n;
addEdge(0, 1, d, 0);
addEdge(1, 0, 0, 0);

pair<11, ll> ans = mincost();
printf("Instancia_%d\n", tc);
if(ans.ff < d) printf("impossivel\n");
else printf("%lld\n", ans.ss);

printf("\n");
forn(i, N) g[i].clear();
}</pre>
```

### Junior e Falta de Ideias

```
#include <bits/stdc++.h>
#define ff first
#define ss second
#define mp make_pair
using namespace std;
typedef long long 11;
vector<pair<int,int>> G[500005];
int subtree[500005], treesize, k;
bool vis[500005];
11 dist[500005], ans;
int dfs(int v, int p){
   subtree[v] = 1;
   for(pair<int,int> x : G[v])
     if (x.ff != p \&\& !vis[x.ff]) subtree[v] += dfs(x.ff,v);
   return subtree[v];
int centroid(int v, int p){
   for(pair<int, int> x : G[v]) {
     if(x.ff == p || vis[x.ff]) continue;
      if(subtree[x.ff]*2 > treesize) return centroid(x.ff,v);
```

```
return v:
void procurar_ans(int v, int p, int d_atual, ll custo) {
   ans = min(ans, dist[k-d atual] + custo);
  if(d_atual == k) return;
   for(pair<int, int> x : G[v]) {
      if(!vis[x.ff] && x.ff != p)
         procurar_ans(x.ff, v, d_atual+1, custo+x.ss);
void atualiza_distancia(int v, int p, int d_atual, ll custo) {
   dist[d_atual] = min(dist[d_atual], custo);
   if(d_atual == k) return;
   for(pair<int, int> x : G[v]) {
      if(!vis[x.ff] && x.ff != p)
         atualiza distancia (x.ff, v, d atual+1, custo+x.ss);
void decomp(int v, int p){
  treesize = dfs(v,v);
   // if(treesize < k) return;</pre>
  int cent = centroid(v, v);
  vis[cent] = 1;
   for(int i = 1; i <= treesize; i++)
      dist[i] = 1e18;
   for(pair<int, int> x : G[cent]) {
      if(!vis[x.ff]){
         procurar_ans(x.ff,cent,1,x.ss);
         atualiza_distancia(x.ff,cent,1,x.ss);
   }
   for(pair<int,int> x : G[cent]){
     if(!vis[x.ff])
         decomp(x.ff, cent);
int main(){
  int n,i,a,b;
   scanf("%d%d", &n,&k);
   for(i = 2; i <= n; i++) {
      scanf("%d%d", &a,&b);
      G[i].push_back(mp(a,b));
      G[a].push_back(mp(i,b));
```

```
ans = 1e18;
decomp(1,-1);
printf("%lld\n", ans == 1e18 ? -1 : ans);
return 0;
```

## Componentes Fortemente Conexas

## Kosaraju

```
vector<int> g[N], gt[N], S;
int vis[N], cor[N], tempo = 1;
void dfs(int u) {
   vis[u] = 1;
   for(int v : g[u]) if(!vis[v])
      dfs(v);
   S.push_back(u);
int e;
void dfst(int u) {
   cor[u] = e;
   for(int v : gt[u]) if(!cor[v])
      dfst(v);
int main(){
   memset (vis, 0, sizeof vis);
   memset(cor, 0, sizeof color);
   for(int i = 1; i <= n; i++) if(!vis[i])</pre>
      dfs(i);
   e = 0;
   for(int u : S) if(!cor[u])
      e++, dfst(u);
   return 0;
```

## Tarjan

```
int num[N], low[N], vis[N], cor[N];
```

```
vector<int> q[N], S;
int t, e;
void dfs(int u) {
  low[u] = num[u] = t++;
  S.push_back(u);
  vis[u] = 1;
   for(int v : g[u]) {
      if(num[v] == -1) dfs(v);
      if(vis[v]) low[u] = min(low[u], low[v]);
  if(low[u] == num[u]){
      e++;
      int v;
         v = s.back(), s.pop_back();
         vis[v] = 0, cor[v] = e;
      }while(v != u);
int main(){
  memset (num, -1, sizeof num);
  memset(vis, 0, sizeof vis);
  memset(low, 0, sizeof low);
   for(int i = 1; i <= n; i++) if(num[i] == -1)</pre>
      dfs(i);
```

## **Strings**

### **YATG**

```
#include <bits/stdc++.h>
#define ff first
#define ss second
#define mp make_pair
#define oo 1000000000

using namespace std;

int n, k, mat[300005][26], ans;

int dfs(int u) {
   int ret = oo;
   ans++;

   for(int i = 0; i < 26; i++) {
      if(mat[u][i]) {</pre>
```

```
ret = min(ret, dfs(mat[u][i]));
      }
   if(ret == 00) {
      ret = 0;
      ans++;
   ret++;
   if(ret > k) {
      ans++;
      ret = 1;
   return ret;
int main(){
   scanf("%d,%d", &n, &k);
   char s[100005];
   int ptr = 1;
   for(int i = 0; i < n; i++) {</pre>
      scanf(",%s", s);
      int node = 0;
      for (int j = 0; s[j]; j++) {
         int letra = s[j]-'a';
         if(!mat[node][letra])
            mat[node][letra] = ptr++;
         node = mat[node][letra];
   for(int i = 0; i < 26; i++)
      if (mat[0][i])
         dfs(mat[0][i]);
   ans += n;
   printf("%d\n", ans);
   return 0:
```

### Trie ponteiro

```
#include <bits/stdc++.h>
using namespace std;
```

```
typedef long long 11;
struct node {
  bool is_end;
  int prefixes, words, maxsize;
  struct node* edge[26];
  //initialize()
  //addword(vertex, word)
  //countPrefixes(vertex, prefix)
  //countWords(vertex, word)
  node(){
     maxsize = 0;
     prefixes = 0;
     words = 0;
     is_end = false;
     for(int i = 0; i < 26; i++) edge[i] = NULL;</pre>
  void addWord(string word, int tam) {
     maxsize = max(tam, maxsize);
     if(word.empty()){
         prefixes++;
         words++;
     else{
         prefixes++;
        int k = word[0] - 'a';
        if(edge[k] == NULL){
           node *p1 = new node();
           p1->addWord(word.substr(1,word.size()-1), tam);
           edge[k] = p1;
         else
            edge[k]->addWord(word.substr(1,word.size()-1), tam);
  int countWords(string word) {
     if(word.empty())
         return words;
     int k = word[0] - 'a';
     if(edge[k] == NULL)
         return 0;
     return edge[k]->countWords(word.substr(1,word.size()-1) );
  int countPrefixes(string word) {
     if(word.empty())
         return prefixes;
     int k = word[0] - 'a';
     if(edge[k] == NULL)
```

```
return 0;
      return edge[k]->countPrefixes(word.substr(1,word.size()-1) );
   int countSize(string word) {
      if(word.empty())
         return maxsize;
      int k = word[0] - 'a';
      if (edge[k] == NULL)
         return 0;
      return edge[k]->countSize(word.substr(1,word.size()-1) );
};
int main() {
   int n,m;
   string s;
   while(scanf("%d", &n) != EOF) {
      node *trie = new node();
      while (n--) {
         cin >> s;
         trie->addWord(s, s.size());
      scanf("%d", &m);
      while (m--) {
         cin >> s;
         int x = trie->countPrefixes(s);
         if(x == 0)
            cout << "-1\n";
         else
            cout << x << "_" << trie->countSize(s) << endl;
   return 0;
Trie
#include <bits/stdc++.h>
#define oo 1000000000000000000000
using namespace std;
int mat[6400640][2];
int cnt[6400640][2];
int main(){
```

```
int n, x, ptr, next = 1;
char c;
scanf("%d", &n);
ptr = 0;
for(int i = 30; i >= 0; i--) {
   if(!mat[ptr][0]) mat[ptr][0] = next++;
   cnt[ptr][0]++;
   ptr = mat[ptr][0];
for(int i = 0; i < n; i++) {</pre>
   scanf(" %c %d", &c, &x);
   if(c == '+'){
      ptr = 0;
      for (int i = 30; i >= 0; i--) {
         if((1 << i) & x){
            if(!mat[ptr][1]) mat[ptr][1] = next++;
            cnt[ptr][1]++;
            ptr = mat[ptr][1];
         else
            if(!mat[ptr][0]) mat[ptr][0] = next++;
            cnt[ptr][0]++;
            ptr = mat[ptr][0];
   else if(c == '-') {
      ptr = 0;
      for(int i = 30; i >= 0; i--) {
         if((1 << i) & x){
            cnt[ptr][1]--;
            ptr = mat[ptr][1];
         else{
            cnt[ptr][0]--;
            ptr = mat[ptr][0];
   else{
      int ans = 0;
      ptr = 0;
      for(int i = 30; i >= 0; i--){
         if((1 << i) & x){
            if(cnt[ptr][0] > 0){
               ans += (1 << i);
               ptr = mat[ptr][0];
```

```
else ptr = mat[ptr][1];
            else
               if(cnt[ptr][1] > 0){
                  ans += (1 << i);
                  ptr = mat[ptr][1];
               else ptr = mat[ptr][0];
        printf("%d\n", ans);
   return 0;
Aho Corasick
#include <bits/stdc++.h>
#define ff first
#define ss second
#define mp make_pair
using namespace std;
typedef long long 11;
int trie[1000005][52], fn[1000005];
int ptr;
bool passou[1000005];
vector<int> final vec;
int insert(char *str){
   int v = 0;
   for(int i = 0; str[i]; i++){
     int to = str[i] >= 'a' ? str[i]-'a'+26 : str[i]-'A';
     if(trie[v][to])
        v = trie[v][to];
     else
        v = trie[v][to] = ptr++;
   return v;
void init_aho() {
   queue<int> Q;
```

```
Q.push(0);
  while(!Q.empty()){
      int t = Q.front(); Q.pop();
      for(int i = 0; i < 52; i++) {</pre>
         if(trie[t][i]){
            int x = trie[t][i];
            Q.push(x);
            if(t){
               fn[x] = fn[t];
               while (fn[x] \&\& trie[fn[x]][i] == 0) fn[x] = fn[fn[x]];
               if(trie[fn[x]][i]) fn[x] = trie[fn[x]][i];
               trie[x][i] = fn[x];
int main(){
   int t,q;
   char s[100005], s2[1005];
   scanf("%d", &t);
  while (t--) {
      scanf("_%s", s);
      memset(trie, 0, sizeof trie);
      memset (passou, 0, sizeof passou);
     memset (fn, 0, sizeof fn);
      final vec.clear();
      ptr = 1;
      scanf("%d", &q);
      // build trie
      while (q--) {
         scanf("_%s", s2);
         final_vec.push_back(insert(s2));
      // build failures
      init_aho();
      // simulate
      int v = 0;
      for(int i = 0; s[i]; i++){
         int to = s[i] >= 'a' ? s[i]-'a'+26 : s[i]-'A';
```

```
v = trie[v][to];
         else{
            while (v) {
               v = fn[v];
               passou[v] = 1;
               if(trie[v][to]) {
                  v = trie[v][to];
                  break;
         passou[v] = 1;
      for(int i = 0; i < final_vec.size(); i++){</pre>
         if(passou[final_vec[i]]) printf("y\n");
         else printf("n\n");
   return 0;
Suffix Array
char s[N];
int n, sa[N], tsa[N], lcp[N], r[N], nr[N], c[N];
void sort(int k, int mx){
   mx++;
   memset(c, 0, sizeof(int) * mx);
   forn(i, n) c[i + k < n ? r[i+k]+1 : 1]++;
   partial_sum(c, c+mx, c);
   int t;
   forn(i, n) t = sa[i]+k < n ? r[sa[i]+k] : 0,
           tsa[c[t]++] = sa[i];
   memcpy(sa, tsa, sizeof(int) * n);
void build_sa() {
   forn(i, n) sa[i] = i, r[i] = s[i];
   int t = 300, a, b;
   for (int sz = 1; sz < n; sz *= 2) {
      sort(sz, t), sort(0, t);
      t = nr[sa[0]] = 0;
      for(int i = 1; i < n; i++) {</pre>
         a = sa[i]+sz < n ? r[ sa[i]+sz ] : -1;
```

b = sa[i-1]+sz < n ? r[ sa[i-1]+sz ] : -1;

### Z Algorithm

```
vector<int> z_algo(const string &s) {
  int n = s.size(), L = 0, R = 0;
  vector<int> z(n, 0);
  for(int i = 1; i < n; i++) {
    if(i <= R) z[i] = min(z[i-L], R - i + 1);
    while(z[i]+i < n && s[ z[i]+i ] == s[ z[i] ]) z[i]++;
    if(i+z[i]-1 > R) L = i, R = i + z[i] - 1;
  }
  return z;
}
```

### Prefix function/KMP

```
vector<int> pf(const string &s) {
   int n = s.size();
   vector<int> b(n+1);
   b[0] = -1;
   int i = 0, j = -1;
   while(i < n) {
      while(j >= 0 && s[i] != s[j]) j = b[j];
      b[++i] = ++j;
   }
   return b;
}

void kmp(const string &t, const string &p) {
   vector<int> b = pf(p);
```

```
int n = t.size();
int j = 0;
for(int i = 0; i < n; i++){
    while(j >= 0 && t[i] != p[j]) j = b[j];
    j++;
    if(j == m) {
        //patern found
        j = b[j];
    }
}
```

### Min rotation

```
// Lexicographically minimum rotation of a sequence
//
// Given a sequence s of length N, min_rotation(s, N) returns the start index
// of the lexicographically minimum rotation.
//
// Note: array s must be of length of at least 2 * N.
//
// Time complexity: O(N)

int min_rotation(int *s, int N) {
   REP(i, N) s[N+i] = s[i];
   int a = 0;
   REP(b, N) REP(i, N) {
    if (a+i == b || s[a+i] < s[b+i]) { b += max(0, i-1); break; }
    if (s[a+i] > s[b+i]) { a = b; break; }
   return a;
}
```

### All palindrome

```
// Finds all palindromes in a string
//
// Given a string s of length N, finds all palindromes as its substrings.
//
// After calling manacher(s, N, rad), rad[x] will be the radius of the largest
// palindrome centered at index x / 2.
// Example:
// s = b a n a n a a
// rad = 0000102010010
//
// Note: Array rad must be of length at least twice the length of the string.
// Also, "invalid" characters are denoted by -1, therefore the string must not
// contain such characters.
//
// Time complexity: O(N)
```

```
//
// Constants to configure:
// - MAX is the maximum length of the string
void manacher(char *s, int N, int *rad) {
 static char t[2*MAX];
 int m = 2 * N - 1;
 REP(i, m) t[i] = -1;
 REP(i, N) t[2*i] = s[i];
 int x = 0:
 FOR(i, 1, m) {
  int &r = rad[i] = 0;
  if (i \le x + rad[x]) r = min(rad[x + x - i], x + rad[x] - i);
  while (i-r-1) = 0 \& \& i+r+1 < m \& \& t[i-r-1] == t[i+r+1] + +r;
  if (i+r >= x+rad[x]) x = i;
 REP(i, m) if (i-rad[i] == 0 || i+rad[i] == m-1) ++rad[i];
 REP(i, m) rad[i] \neq 2;
```

## Geometria

### Convex Hull

```
U.push_back(p);
}
L.pop_back();
U.pop_back();
L.reserve(L.size() + U.size());
L.insert(L.end(), U.begin(), U.end());
return L;
```

### **Nearest Points**

```
struct pt {
   int x, y, id;
};
inline bool cmp_x (const pt & a, const pt & b) {
   return a.x < b.x || a.x == b.x && a.y < b.y;
inline bool cmp_y (const pt & a, const pt & b) {
   return a.y < b.y;</pre>
pt a[MAXN];
double mindist;
int ansa, ansb;
inline void upd_ans (const pt & a, const pt & b) {
   double dist = sqrt ((a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y) + .0);
   if (dist < mindist)</pre>
      mindist = dist, ansa = a.id, ansb = b.id;
void rec (int 1, int r) {
   if (r - 1 \le 3) {
      for (int i=1; i<=r; ++i)</pre>
         for (int j=i+1; j<=r; ++j)</pre>
            upd_ans (a[i], a[j]);
      sort (a+1, a+r+1, &cmp_y);
      return;
   int m = (1 + r) >> 1;
   int midx = a[m].x;
   rec (1, m), rec (m+1, r);
   static pt t[MAXN];
```

### Determinante

```
const double EPS = 1E-9;
int n;
vector < vector<double> > a (n, vector<double> (n));
double det = 1;
for (int i=0; i<n; ++i) {</pre>
  int k = i;
   for (int j=i+1; j<n; ++j)
      if (abs (a[j][i]) > abs (a[k][i]))
         k = j;
  if (abs (a[k][i]) < EPS) {
      det = 0;
      break;
   swap (a[i], a[k]);
  if (i != k)
      det = -det;
   det *= a[i][i];
   for (int j=i+1; j<n; ++j)
      a[i][j] /= a[i][i];
   for (int j=0; j<n; ++j)
      if (j != i && abs (a[j][i]) > EPS)
         for (int k=i+1; k<n; ++k)</pre>
            a[j][k] = a[i][k] * a[j][i];
cout << det:
```

### Convex Hull Trick

#include <bits/stdc++.h>

```
#define ff first
#define ss second
#define pb push_back
#define eb emplace_back
#define mp make pair
using namespace std;
const int N = 100005;
const double EPS = 1e-9;
int n;
int h[N], ht[N], c[N], ct[N], erased[N], id[N];
pair<double, double> H[N], C[N];
double getx(int *h, int *hc, int i, int j){
   return 1.0*(h[i] - h[j])/(hc[j] - hc[i]);
void cht(int *h, int *hc, pair<double, double> *H) {
   for(int i = 0; i < n; i++) id[i] = i;</pre>
   sort(id, id+n, [=](int a, int b){
      if(hc[a] == hc[b]) return h[a] < h[b];</pre>
         return hc[a] < hc[b];</pre>
   });
   vector<int> v;
   for(int i = 0; i < n; i++) {</pre>
      while(v.size() >= 1){
         bool taken = 0;
         double x3 = getx(h, hc, v[v.size()-1], id[i]);
         if(x3 < EPS) taken = 1, v.pop_back();</pre>
         if(v.size() >= 2){
            double x1 = getx(h, hc, v[v.size()-1], v[v.size()-2]);
            double x2 = getx(h, hc, v[v.size()-2], id[i]);
            if(x2-EPS <= x1) v.pop_back();</pre>
            else break;
         else if(!taken) break;
      v.push_back(id[i]);
```

```
double last = 0;
   for(int i = 0; i < v.size(); i++) {</pre>
     H[v[i]].ff = last;
     if(i+1 < v.size()) last = H[ v[i] ].ss = getx(h, hc, v[i], v[i+1]);
     else H[ v[i] ].ss = 1e50;
  }
int main(){
  scanf("%d", &n);
   for(int i = 0; i < n; i++)</pre>
      scanf("%d,%d,%d,%d", h+i, ht+i, c+i, ct+i), c[i] *= -1, ct[i] *= -1;
      multiset<pair<int, int> > hh, cc;
      for(int i = 0; i < n; i++)</pre>
         hh.insert(mp(h[i], ht[i])),
         cc.count(mp(c[i], ct[i]));
      for(int i = 0; i < n; i++)
         if(hh.count(mp(h[i], ht[i])) > 1 \mid | cc.count(mp(c[i], ct[i])) > 1)
            erased[i] = 1;
   for(int i = 0; i < n; i++)</pre>
     H[i].ff = H[i].ss = C[i].ff = C[i].ss = -1;
   cht(h, ht, H);
   cht(c, ct, C);
  int ans = 0;
   for(int i = 0; i < n; i++) if(!erased[i]){</pre>
     if (H[i].ff == -1 || C[i].ff == -1) continue;
      double a = max(H[i].ff, C[i].ff);
      double b = min(H[i].ss, C[i].ss);
      if(a+EPS <= b){
         ans++;
  printf("%d\n", ans);
   return 0;
```