Question 1

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1. Work = Time on one processor (T_1)

Here, we are dividing the array in two at each step.

We can calculate T_1 by summing two parts together: The upper and lower

Upper half =
$$2^0 + 2^1 + ... + 2^{n-1} + 2^n$$

halves. Upper half =
$$2^0 + 2^1 + \dots + 2^{n-1} + 2^n$$

Lower half = $2^{n-1} + 2^{n-2} + \dots + 2^0$
 $T_1 = 2 * \sum_{i=0}^{n-1} 2^i + 2^n = 2 * (2^n - 1) + 2^n$

2. Critical Path = Time on ∞ processors (T_{∞})

In this case, we can use as many processors as we like.

$$T_{\infty} = 2 * \log_2(n) + 1$$

3. Parallelism = $\frac{T_1}{T_{\infty}} = \frac{2*(2^n-1)+2^n}{2*\log_2(n)+1}$