

1. Ex. 1: Give a context-free grammar to generate the following language  $\mathcal{L}$ :

$$\mathcal{L} = \{w \in \{0,1\}^* \mid w \text{ contains at least four } 1\}$$

2. Ex. 2: Give a context-free grammar to generate the following language  $\mathcal{L}$ :

$$\mathcal{L} = \{w \in \{0,1\}^* \mid w = \text{reverse}(w) \wedge |w| \text{ is odd}\}$$

3. Ex. 3: Give a context-free grammar to generate the following language  $\mathcal{L}$ :

$$\mathcal{L} = \{w \in \{0,1\}^* \mid w = \text{reverse}(w)\}$$

4. Ex. 4: Give a context-free grammar to generate the following language  $\mathcal{L}$ :

$$\mathcal{L} = \{a^i b^j c^k \mid i, j, k \in \mathbb{N} \wedge i + j = k\}$$

5. Ex. 5: Give a context-free grammar to generate the following language  $\mathcal{L}$ :

$$\mathcal{L} = \{0^n 1^n \mid n \in \mathbb{N}\} \cup \{0^n 1^{2n} \mid n \in \mathbb{N}\}$$