Getting started with the glmmTMB package

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1 Introduction/quick start

glmmTMB is an R package built on the Template Model Builder automatic differentiation engine, for fitting generalized linear mixed models and extensions. (Not-yet-implemented features are denoted *like this*)

- response distributions: Poisson, binomial, negative binomial (NB1 and NB2 parameterizations), Gamma, Beta, Gaussian; truncated Poisson and negative binomial; Student t; Tweedie
- link functions: log, logit, probit, complementary log-log, inverse, identity
- zero-inflation with fixed and random-effects components; *hurdle models* via truncated Poisson/NB
- single or multiple (nested or crossed) random effects
- offsets
- fixed-effects models for dispersion
- diagonal, compound-symmetric, or unstructured random effects variancecovariance matrices

In order to use glmmTMB effectively you should already be reasonably familiar with generalized linear mixed models (GLMMs), which in turn requires familiarity with (i) generalized linear models (e.g. the special cases of logistic, binomial, and Poisson regression) and (ii) 'modern' mixed models (those working via maximization of the marginal likelihood rather than by manipulating sums of squares). Bolker et al. (2009) and Bolker (2015) are reasonable starting points in this area (especially geared to biologists and less-technical readers), as are Zuur et al. (2009), Millar (2011), and Zuur et al. (2013).

In order to fit a model in glmmTMB you need to:

• specify a model for the conditional effects, in the standard R (Wilkinson-Rogers) formula notation (see ?formula or Section 11.1 of the Introduction to R. Formulae can also include offsets.

- specify a model for the random effects, in the notation that is common to the nlme and lme4 packages. Random effects are specified as x|g, where x is an effect and g is a grouping factor (which must be a factor variable, or a nesting of/interaction among factor variables). For example, the formula would be 1|block for a random-intercept model or time|block for a model with random variation in slopes through time across groups specified by block. A model of nested random effects (block within site) would be 1|site/block; a model of crossed random effects (block and year) would be (1|block)+(1|year).
- choose the error distribution by specifying the family
- optionally specify a zero-inflation model with fixed and/or random effects
- optionally specify a dispersion model with fixed effects

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```
## bbmle glmmTMB
## 1.0.18 0.0.2
```

The current citation for glmmTMB is:

Magnusson A, Skaug H, Nielsen A, Berg C, Kristensen K, Maechler M, van Bentham K, Bolker B and Brooks M (2015). *glmmTMB:* Generalized Linear Mixed Models using Template Model Builder. R package version 0.0.2, https://github.com/glmmTMB.

2 Preliminaries: packages and data

Load required packages:

```
library("glmmTMB")
library("bbmle") ## for AICtab
library("ggplot2")
## cosmetic
theme_set(theme_bw()+
   theme(panel.margin=grid::unit(0,"lines")))
```

The data, taken from Zuur et al. (2009) and ultimately from Roulin and Bersier (2007), quantify the number of negotiations among owlets (owl chicks) in different nests *prior* to the arrival of a provisioning parent as a function of food treatment (deprived or satiated), the sex of the parent, and arrival time. The total number of calls from the nest is recorded, along with the total brood size, which is used as an offset to allow the use of a Poisson response.

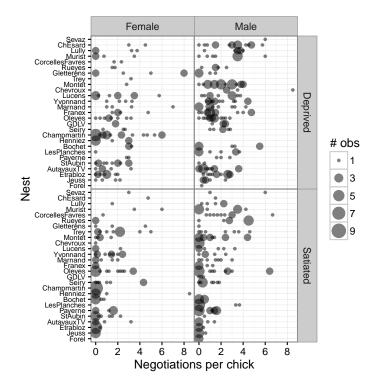


Figure 1: Basic view of owl data from Roulin and Bersier (2007).

Since the same nests are measured repeatedly, the nest is used as a random effect. The model can be expressed as a zero-inflated generalized linear mixed model (ZIGLMM).

First we draw a picture (Figure 1).

Various small manipulations of the data set: (1) reorder nests by mean negotiations per chick, for plotting purposes; (2) add log brood size variable (for offset); (3) rename response variable and abbreviate one of the input variables.

(If you were really using this data set you should start with summary(Owls) to explore the data set.)

We should explore the data further, e.g. by visualizing the effect of arrival time, but this is a vignette about glmmTMB, not data visualization ...

Now fit some models:

The basic glmmTMB fit — a zero-inflated Poisson model with a single zero-inflation parameter applying to all observations (zi~1). (Excluding zero-inflation is glmmTMB's default: to exclude it explicitly, use zi~0.)

```
summary(fit_zipoisson)
  Family: poisson (log)
## Formula:
## NCalls ~ (FT + ArrivalTime) * SexParent + offset(log(BroodSize)) +
##
     (1 | Nest)
     Data: Owls
##
##
       AIC
                   logLik deviance df.resid
##
               BIC
            4050.8 -1999.8
                            3999.6
##
    4015.6
##
## Random effects:
##
## Conditional model:
  Groups Name
                    Variance Std.Dev.
  Nest (Intercept) 0.1291
                             0.3593
## Number of obs: 599, groups: Nest, 27
##
## Conditional model:
                         Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                          2.53995
                                     0.35656
                                             7.123 1.05e-12 ***
                                     0.05961 -4.884 1.04e-06 ***
## FTSatiated
                          -0.29111
## ArrivalTime
                          0.44885
                                   0.45002
                                             0.997
## SexParentMale
                                                       0.319
## FTSatiated:SexParentMale 0.10473
                                     0.07286
                                              1.437
                                                       0.151
## ArrivalTime:SexParentMale -0.02140
                                   0.01835 -1.166
                                                       0.244
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Zero inflation:
             Estimate Std. Error z value Pr(>|z|)
## (Intercept) -1.05753
                      0.09412 -11.24 <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

We can also try a standard zero-inflated negative binomial model; the default is the "NB2" parameterization (variance = $\mu(1 + \mu/k)$: Hardin and Hilbe (2007)). To use families (Poisson, binomial, Gaussian) that are defined in R, you should specify them as in 'glm (as a string referring to the family function, as the family function itself, or as the result of a call to the family function: i.e. family="poisson", family=poisson, family=poisson(), and family=poisson(link="log") are all allowed and all equivalent (the log link is the default for the Poisson family). Some of the additional families that are not defined in base R (at this point nbinom2 and nbinom1) can be specified using the same format. Otherwise, for families that are implemented in glmmTMB but for which glmmTMB does not provide a function, you should specify the family argument as a list containing (at least) the (character) elements family and link, e.g. family=list(family="nbinom2",link="log"). (In order to be able to retrieve Pearson (variance-scaled) residuals from a fit, you also need to specify a variance component; see 'family_glmmTMB.)

```
fit_zinbinom <- update(fit_zipoisson,family=nbinom2)</pre>
```

Alternatively, we can use an "NB1" fit (variance = $\phi \mu$).

```
fit_zinbinom1 <- update(fit_zipoisson,family=nbinom1)</pre>
```

we should have a getFamily function: ideally it would also specify which are really implemented (although that's harder), and specify default links

Relax the assumption that total number of calls is strictly proportional to brood size (i.e. using log(brood size) as an offset):

Every change we have made so far improves the fit — changing distributions improves it enormously, while changing the role of brood size makes only a modest (-1 AIC unit) difference:

2.1 Hurdle models

In contrast to zero-inflated models, hurdle models treat zero-count and non-zero outcomes as two completely separate categories, rather than treating the

zero-count outcomes as a mixture of structural and sampling zeros.

glmmTMB includes truncated Poisson and negative binomial familes and hence can fit hurdle models. The two parts of the model have to be fitted separately, however. First we fit a truncated distribution to the non-zero outcomes:

Truncated families aren't there yet. Once they are, we might not actually need to fit two separate models – if we simply ignore zero values rather than giving them a 0 likelihood, we could fit a zero-inflated model and let the zero-inflation handle the zero/not-zero stuff automatically (should there be a flag to allow ignoring zeros for this purpose? Should we implement a control argument soon??)

3 Sample timings

To get a rough idea of glmmTMB's speed relative to lme4 (the most commonly used mixed-model package for R), we try a few standard problems, enlarging the data sets by cloning the original data set (making multiple copies and sticking them together).

Figure 2 shows the results of replicating the Contraception data set (1934 observations, 60 levels in the random effects grouping level) from 1 to 40 times. $\mathtt{glmmADMB}$ is sufficiently slow (≈ 1 minute for a single copy of the data) that we didn't try replicating very much. On average, $\mathtt{glmmTMB}$ is about 2.3 times faster than \mathtt{glmer} for this problem.

Figure 3 shows equivalent timings for the InstEval data set, although in this case since the original data set is large (73421 observations) we subsample the data set rather than cloning it: in this case, the advantage is reversed and lmer is about 5 times faster.

In general, we expect glmmTMB's advantages over lme4 to be (1) greater flexibility (zero-inflation etc.); (2) greater speed for GLMMs, especially those with large number of "top-level" parameters (fixed effects plus random-effects variance-covariance parameters). In contrast, lme4 should be faster for LMMs (for maximum speed, you may want to check the MixedModels.jl package for Julia); lme4 is more mature and at present has a wider variety of diagnostic checks and methods for using model results, including downstream packages.

References

Bolker, B. M. (2015). Linear and generalized linear mixed models. In G. A. Fox, S. Negrete-Yankelevich, and V. J. Sosa (Eds.), *Ecological Statistics: Contem*porary theory and application, Chapter 13. Oxford University Press.

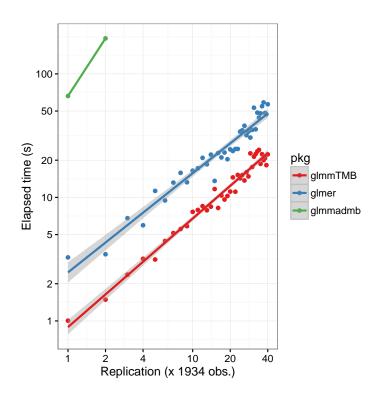


Figure 2: Timing for fitting the replicated Contraception data set.

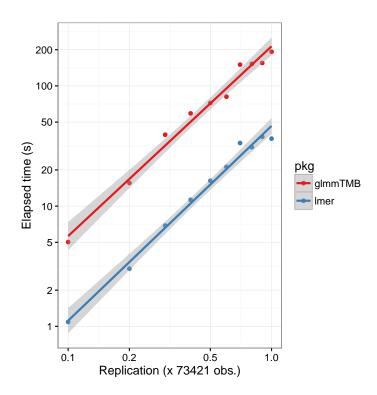


Figure 3: Timing for fitting subsets of the InstEval data set.

- Bolker, B. M., M. E. Brooks, C. J. Clark, S. W. Geange, J. R. Poulsen, M. H. H. Stevens, and J. S. White (2009). Generalized linear mixed models: a practical guide for ecology and evolution. *Trends in Ecology & Evolution* 24, 127–135.
- Hardin, J. W. and J. Hilbe (2007, February). Generalized linear models and extensions. Stata Press.
- Millar, R. B. (2011, July). Maximum Likelihood Estimation and Inference: With Examples in R, SAS and ADMB. John Wiley & Sons.
- Roulin, A. and L. Bersier (2007). Nestling barn owls beg more intensely in the presence of their mother than in the presence of their father. *Animal Behaviour* 74, 1099–1106.
- Zuur, A. F., J. M. Hilbe, and E. N. Leno (2013, May). A Beginner's Guide to GLM and GLMM with R: A Frequentist and Bayesian Perspective for Ecologists. Highland Statistics Ltd.
- Zuur, A. F., E. N. Ieno, N. J. Walker, A. A. Saveliev, and G. M. Smith (2009, March). *Mixed Effects Models and Extensions in Ecology with R* (1 ed.). Springer.