knn nosol

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0.1 This is the k-nearest neighbors workbook for ECE C147/C247 Assignment #2

Please follow the notebook linearly to implement k-nearest neighbors.

Please print out the workbook entirely when completed.

The goal of this workbook is to give you experience with the data, training and evaluating a simple classifier, k-fold cross validation, and as a Python refresher.

0.2 Import the appropriate libraries

```
[2]: # Set the path to the CIFAR-10 data
cifar10_dir = '/home/andrea/git/UCLA/UCLA_ECE147/Homework2/HW2_code/
cifar-10-batches-py' # You need to update this line
X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

# As a sanity check, we print out the size of the training and test data.
print('Training data shape: ', X_train.shape)
print('Training labels shape: ', y_train.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

Training data shape: (50000, 32, 32, 3)

Training labels shape: (50000,)

```
Test data shape: (10000, 32, 32, 3)
Test labels shape: (10000,)
```

```
[3]: # Visualize some examples from the dataset.
     # We show a few examples of training images from each class.
    classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse',

     num_classes = len(classes)
    samples_per_class = 7
    for y, cls in enumerate(classes):
        idxs = np.flatnonzero(y_train == y)
        idxs = np.random.choice(idxs, samples_per_class, replace=False)
        for i, idx in enumerate(idxs):
            plt_idx = i * num_classes + y + 1
            plt.subplot(samples_per_class, num_classes, plt_idx)
            plt.imshow(X_train[idx].astype('uint8'))
            plt.axis('off')
            if i == 0:
                plt.title(cls)
    plt.show()
```



```
[4]: # Subsample the data for more efficient code execution in this exercise
num_training = 5000
mask = list(range(num_training))
X_train = X_train[mask]
y_train = y_train[mask]
```

```
num_test = 500
mask = list(range(num_test))
X_test = X_test[mask]
y_test = y_test[mask]

# Reshape the image data into rows
X_train = np.reshape(X_train, (X_train.shape[0], -1))
X_test = np.reshape(X_test, (X_test.shape[0], -1))
print(X_train.shape, X_test.shape)
```

(5000, 3072) (500, 3072)

1 K-nearest neighbors

In the following cells, you will build a KNN classifier and choose hyperparameters via k-fold cross-validation.

```
[5]: # Import the KNN class
from nndl import KNN
```

```
[6]: # Declare an instance of the knn class.
knn = KNN()

# Train the classifier.
# We have implemented the training of the KNN classifier.
# Look at the train function in the KNN class to see what this does.
knn.train(X=X_train, y=y_train)
```

1.1 Questions

- (1) Describe what is going on in the function knn.train().
- (2) What are the pros and cons of this training step?

1.2 Answers

- (1) knn.train() is loading the data into the KNN object.
- (2) The pros are that it is a very fast, O(1) training step. The cons are that no processing is actually done, and no additional structure or information is gained by the training step. Also, it is very memory intensive, since a lot of data needs to be stored.

1.3 KNN prediction

In the following sections, you will implement the functions to calculate the distances of test points to training points, and from this information, predict the class of the KNN.

Time to run code: 22.351867198944092

Frobenius norm of L2 distances: 7906696.077040902

Really slow code Note: This probably took a while. This is because we use two for loops. We could increase the speed via vectorization, removing the for loops.

If you implemented this correctly, evaluating np.linalg.norm (dists_L2, 'fro') should return: $\sim\!7906696$

1.3.1 KNN vectorization

The above code took far too long to run. If we wanted to optimize hyperparameters, it would be time-expensive. Thus, we will speed up the code by vectorizing it, removing the for loops.

Time to run code: 0.19461321830749512 Difference in L2 distances between your KNN implementations (should be 0): 0.0

Speedup Depending on your computer speed, you should see a 10-100x speed up from vectorization. On our computer, the vectorized form took 0.36 seconds while the naive implementation took 38.3 seconds.

1.3.2 Implementing the prediction

Now that we have functions to calculate the distances from a test point to given training points, we now implement the function that will predict the test point labels.

0.726

If you implemented this correctly, the error should be: 0.726.

This means that the k-nearest neighbors classifier is right 27.4% of the time, which is not great, considering that chance levels are 10%.

2 Optimizing KNN hyperparameters

In this section, we'll take the KNN classifier that you have constructed and perform cross-validation to choose a best value of k, as well as a best choice of norm.

2.0.1 Create training and validation folds

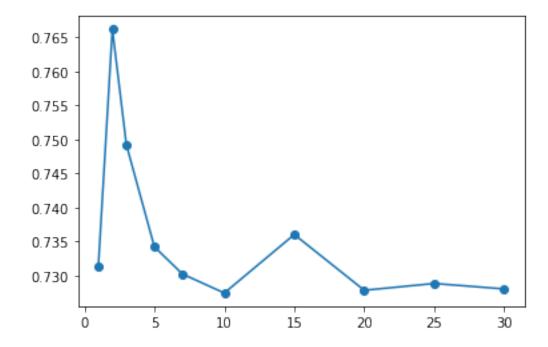
First, we will create the training and validation folds for use in k-fold cross validation.

2.0.2 Optimizing the number of nearest neighbors hyperparameter.

In this section, we select different numbers of nearest neighbors and assess which one has the lowest k-fold cross validation error.

```
[12]: %matplotlib inline
     import matplotlib.pyplot as plt
     time start =time.time()
     ks = [1, 2, 3, 5, 7, 10, 15, 20, 25, 30]
                           ----- #
     # YOUR CODE HERE:
        Calculate the cross-validation error for each k in ks, testing
       the trained model on each of the 5 folds. Average these errors
        together and make a plot of k vs. cross-validation error. Since
       we are assuming L2 distance here, please use the vectorized code!
        Otherwise, you might be waiting a long time.
     # ----- #
     err_data = np.zeros((len(ks), num_folds))
     for i in range(0, num_folds):
        knn2 = KNN()
        knn2.train(X_train[~split_mat[:,i]], y_train[~split_mat[:,i]])
        dists = knn2.compute_L2_distances_vectorized(X_train_folds[i])
         # print("i-th fold:", X_train_folds[i].shape)
         # print("dists.shape:", dists.shape)
         # print(np.unique(dists, return_counts=True))
        for j, k in enumerate(ks):
```

[0.7314 0.7662 0.7492 0.7342 0.7302 0.7274 0.736 0.7278 0.7288 0.728] Computation time: 4.12



2.1 Questions:

- (1) What value of k is best amongst the tested k's?
- (2) What is the cross-validation error for this value of k?

2.2 Answers:

- (1) The best value of k was 10,
- (2) The cross validation error for k = 10 was 0.7274.

2.2.1 Optimizing the norm

Next, we test three different norms (the 1, 2, and infinity norms) and see which distance metric results in the best cross-validation performance.

```
[13]: time_start =time.time()
     L1_norm = lambda x: np.linalg.norm(x, ord=1)
     L2_norm = lambda x: np.linalg.norm(x, ord=2)
     Linf_norm = lambda x: np.linalg.norm(x, ord= np.inf)
     norms = [L1_norm, L2_norm, Linf_norm]
     # ----- #
     # YOUR CODE HERE:
         Calculate the cross-validation error for each norm in norms, testing
        the trained model on each of the 5 folds. Average these errors
        together and make a plot of the norm used us the cross-validation error
         Use the best cross-validation k from the previous part.
      #
         Feel free to use the compute_distances function. We're testing just
         three norms, but be advised that this could still take some time.
         You're welcome to write a vectorized form of the L1- and Linf- norms
         to speed this up, but it is not necessary.
     err_data = np.zeros((len(norms), num_folds))
     for i in range(0, num_folds):
         knn2 = KNN()
         knn2.train(X_train[~split_mat[:,i]], y_train[~split_mat[:,i]])
         for j, norm in enumerate(norms):
             dists = knn2.compute_distances(X_train_folds[i], norm)
             predictions = knn2.predict_labels(dists, k=15)
             error = (predictions != y_train_folds[i]).mean()
             # print(error)
             # print(predictions)
             # print(y_train_folds[i])
             err_data[j, i] = error
     # print(err_data)
     mean_err = err_data.mean(axis=1)
     print(mean_err)
     plt.bar(["L1 norm", "L2 norm", "L-inf norm"], mean_err)
```

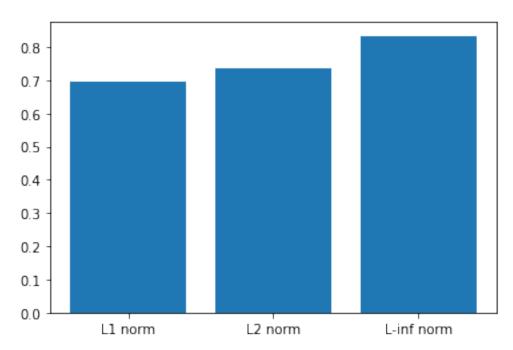
```
# ----- #

# END YOUR CODE HERE

# ------ #

print('Computation time: %.2f'%(time.time()-time_start))
```

[0.6944 0.736 0.834] Computation time: 525.52



2.3 Questions:

- (1) What norm has the best cross-validation error?
- (2) What is the cross-validation error for your given norm and k?

2.4 Answers:

- (1) The L1 norm had the best cross-validation error for k=10.
- (2) The cross validation error it achieved is 0.6944.

3 Evaluating the model on the testing dataset.

Now, given the optimal k and norm you found in earlier parts, evaluate the testing error of the k-nearest neighbors model.

```
[27]: error = 1
```

Error rate achieved: 0.722

3.1 Question:

How much did your error improve by cross-validation over naively choosing k = 1 and using the L2-norm?

3.2 Answer:

Very little. The error rate fell from 0.726 to 0.722, a whopping 1.5% improvement in success rate.