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DEPARTMENT OF

# INDUSTRIAL ENGINEERING



## Renewable Energy Conversion Systems

Lecture 13

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MSc Degree in Mechatronic Engineering,

Academic Year 2024-2025

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e Scienza dell'Informazione  
*Department of Info-  
Engineering*



## Lecture 13: Outline



Main topic:

### Ocean Wave Energy Conversion Systems

Wave energy: **why?**

Resource amount

Wave energy: **when?**

Ocean energy roadmap

Wave energy: **where?**

Geographical availability  
of the resource

Wave energy: **what?**

Origin of wave energy

Wave energy: **how?**

Exploitation mechanisms  
(concepts and basics of control)

Conclusions



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# Introduction to wave energy

**The sea is part of our lives**

**In one way...**



**...Or in the other!...**



# Introduction to wave energy

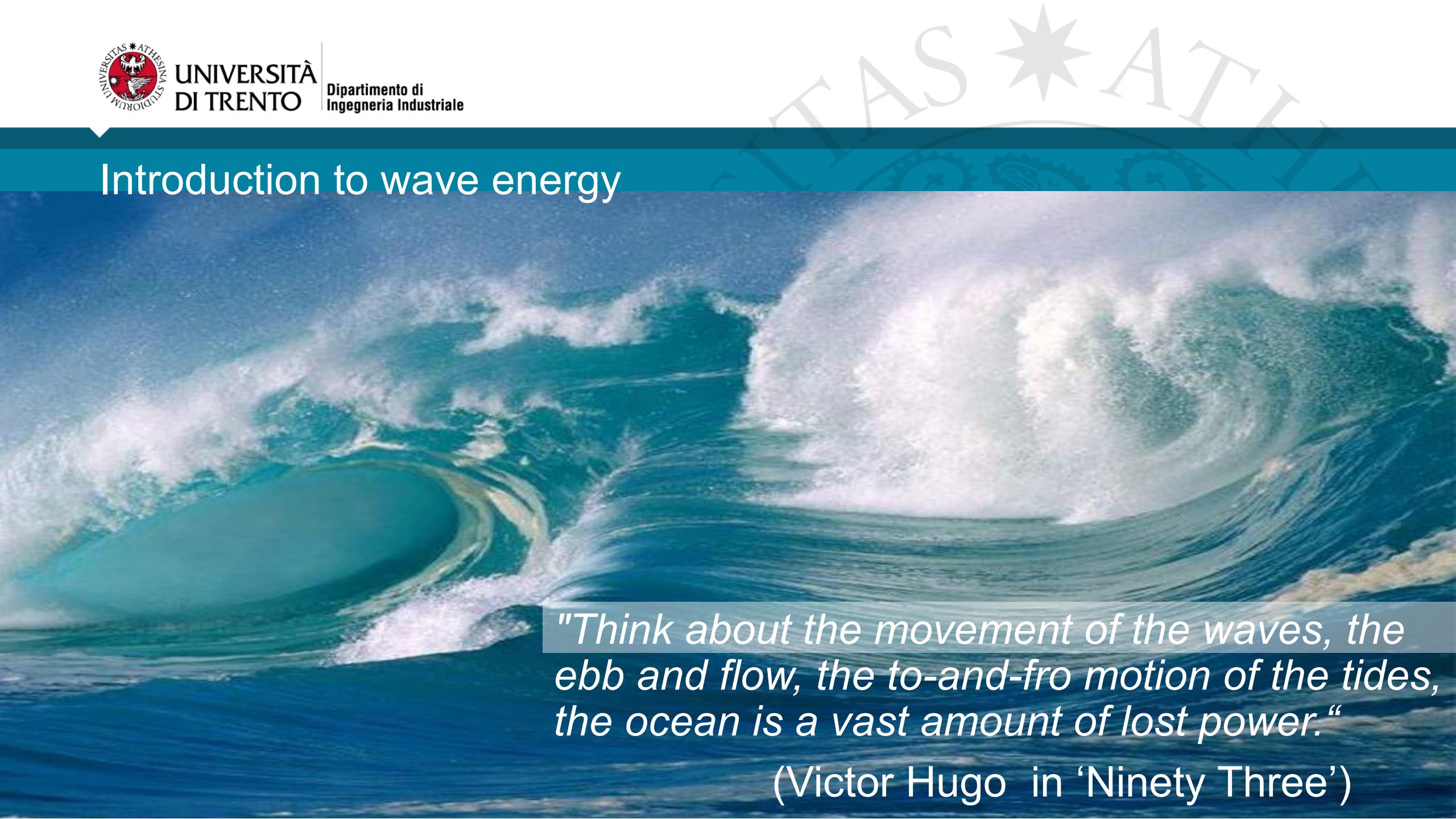
# Challenging...



...With alternating fortunes...



# Introduction to wave energy



*"Think about the movement of the waves, the ebb and flow, the to-and-fro motion of the tides, the ocean is a vast amount of lost power."*

(Victor Hugo in 'Ninety Three')



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# Introduction to wave energy

**Why?**

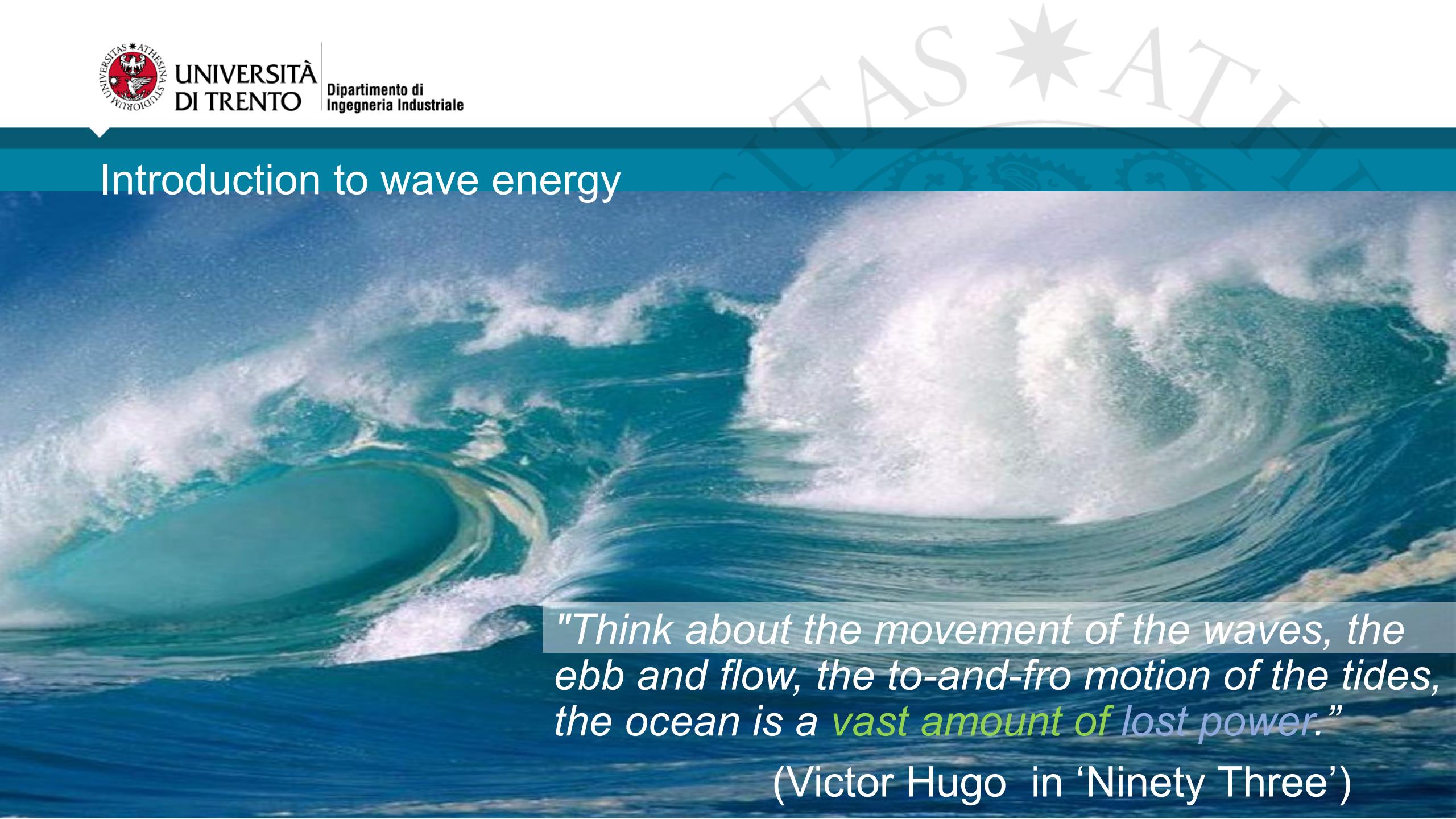




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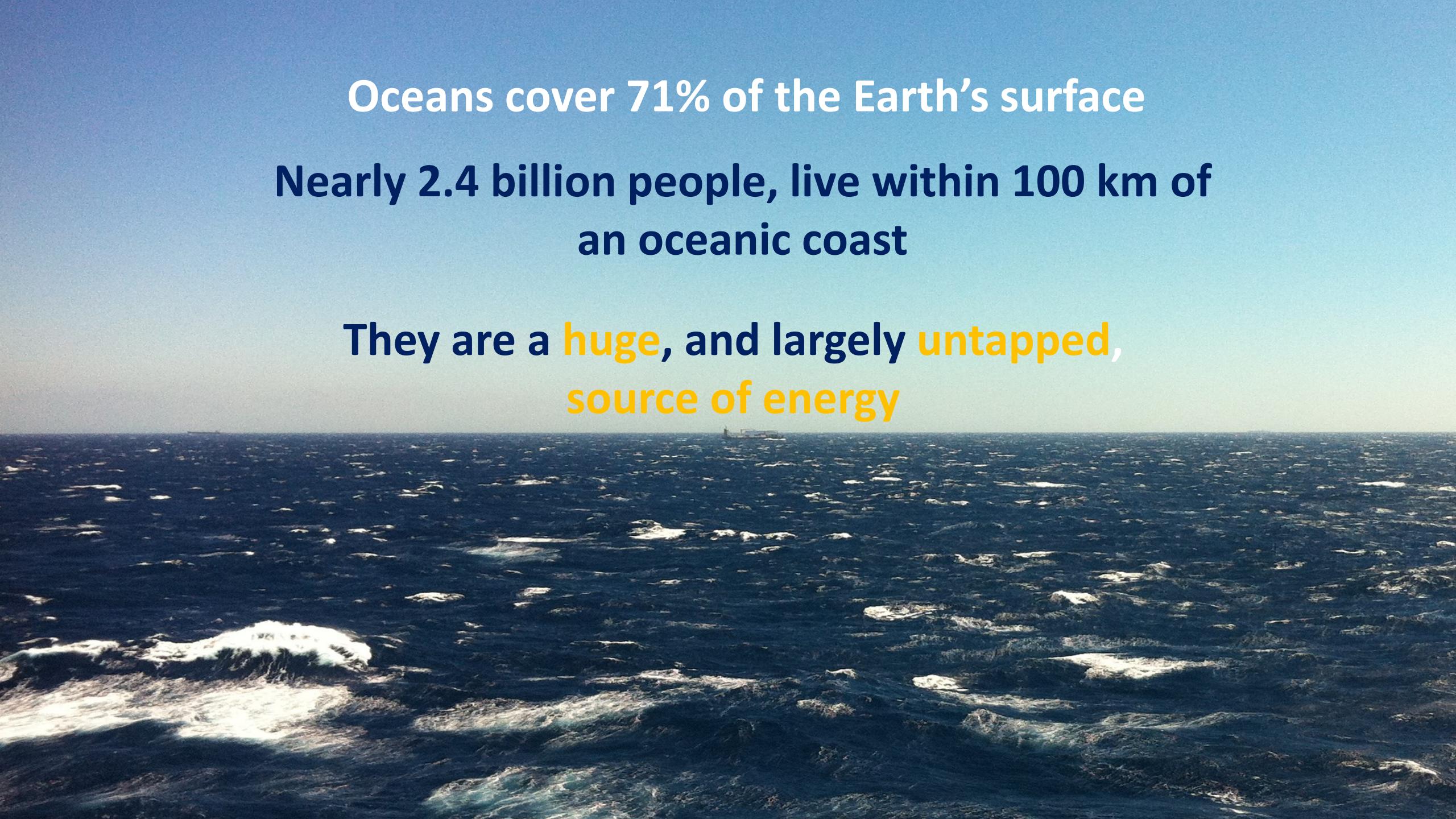
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# Introduction to wave energy



*"Think about the movement of the waves, the ebb and flow, the to-and-fro motion of the tides, the ocean is a vast amount of lost power."*

(Victor Hugo in 'Ninety Three')

The background image shows a vast, dark blue ocean with numerous small white-capped waves. The horizon is flat, and the sky above is a clear, pale blue.

Oceans cover 71% of the Earth's surface

Nearly 2.4 billion people, live within 100 km of  
an oceanic coast

They are a **huge**, and largely **untapped**,  
**source of energy**



## Introduction to wave energy

### Offshore renewable energy portfolio

It includes many different ways of extracting energy from the sea:

- Tidal energy: (range and currents): exploits the 12h periodic tides due to moon gravity
- Salinity gradient: pressure differential between salt water and fresh water
- Ocean thermal: temperature differential between deep water and surface water
- Wave Energy: surface and subsurface motion of the waves

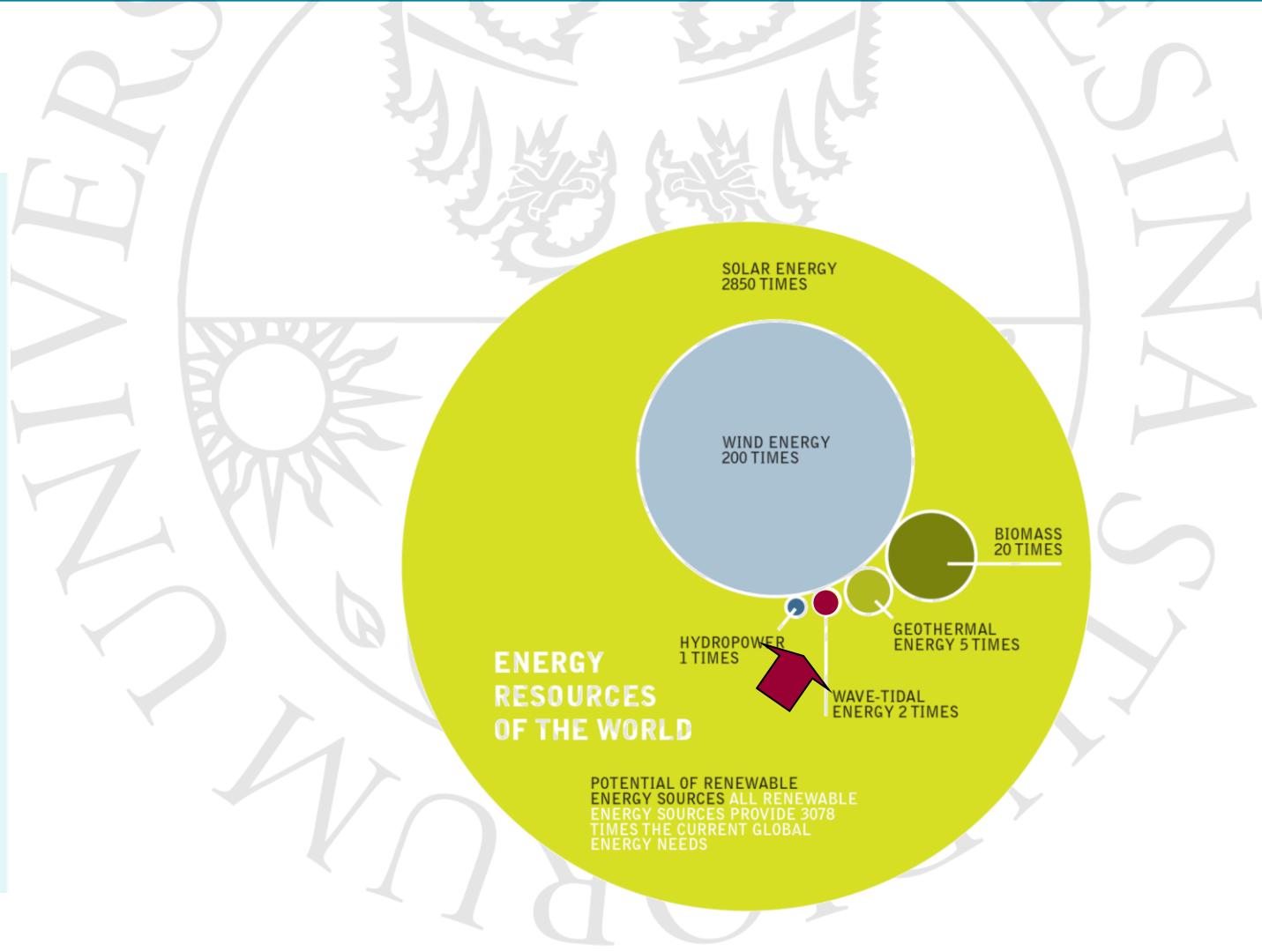
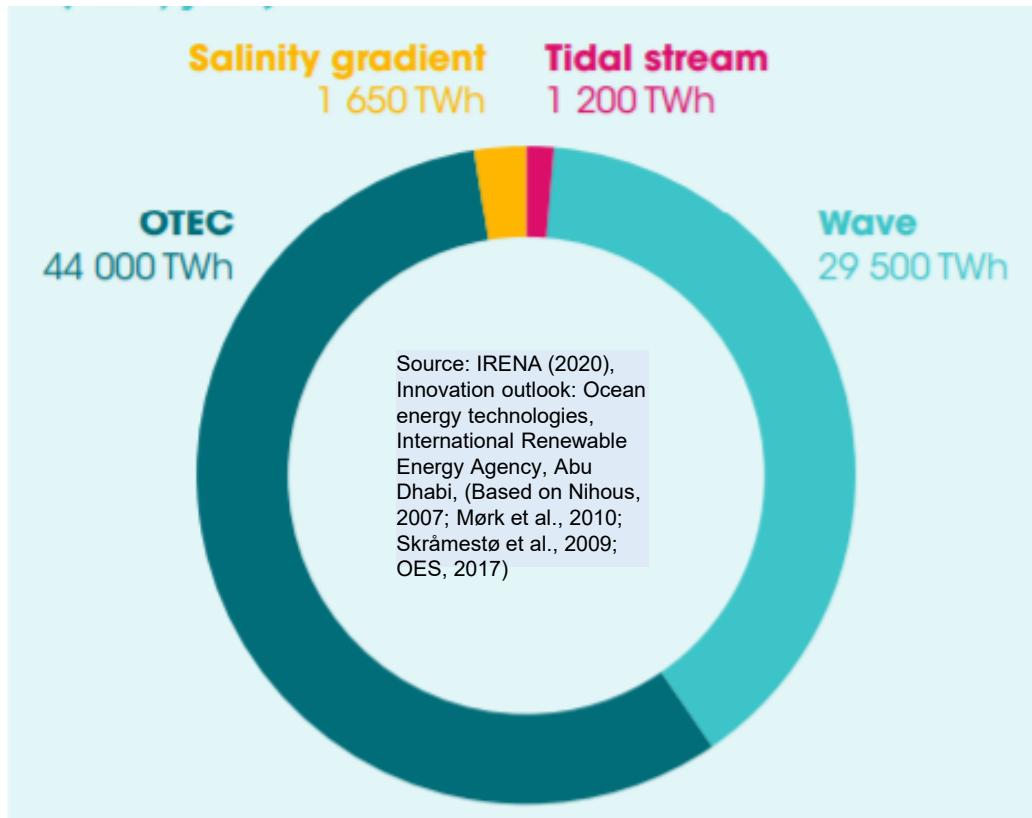
### Theoretical resource potential





# Introduction to wave energy

## Ocean energy perspectives





# Introduction to wave energy

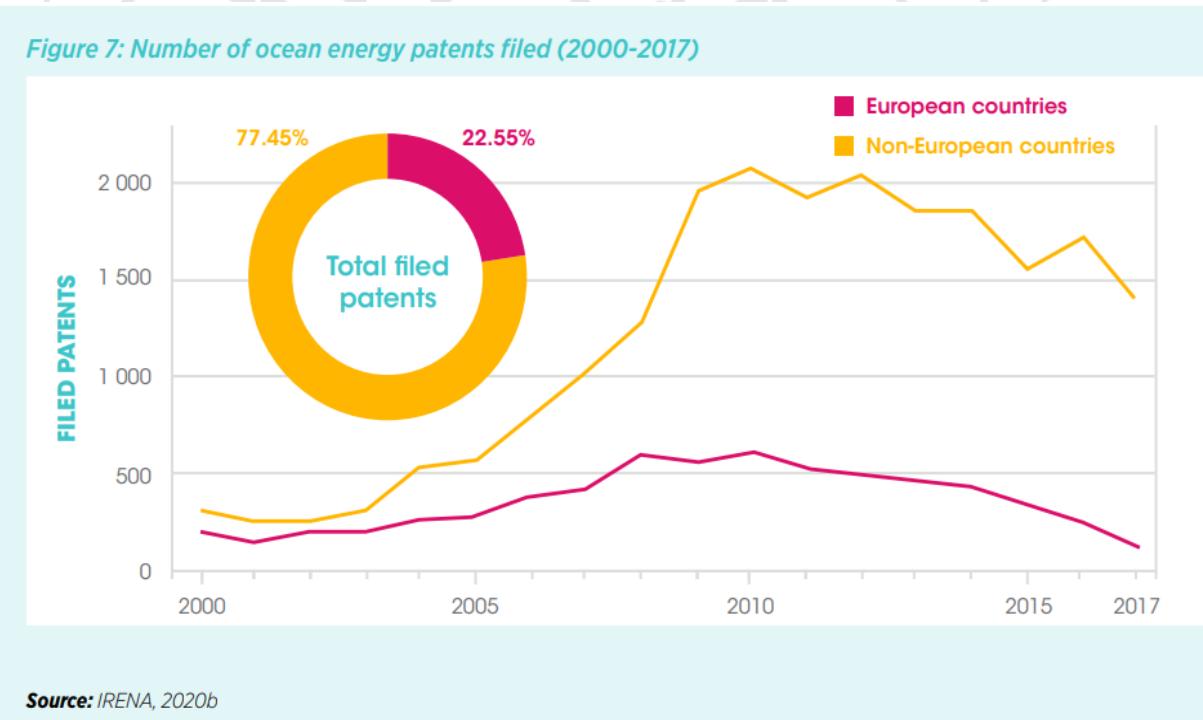
**When?**





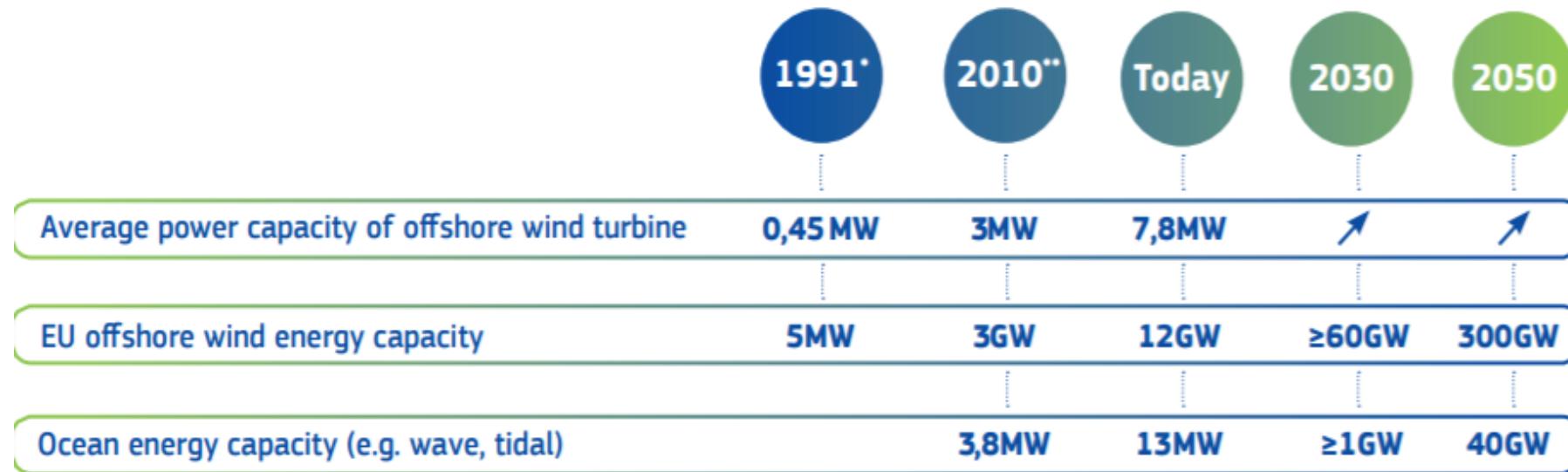
## Brief history of wave energy

- First patent filed in 1799
- Intense research in wave energy in the 1970s, many devices proposed
- More than 1000 patents followed
- Lack of interest at the end of the oil crisis
- Slow development till 2000
- New interest due to the European quest for renewable energy production
- Contribution to the goals set by the Paris Agreement



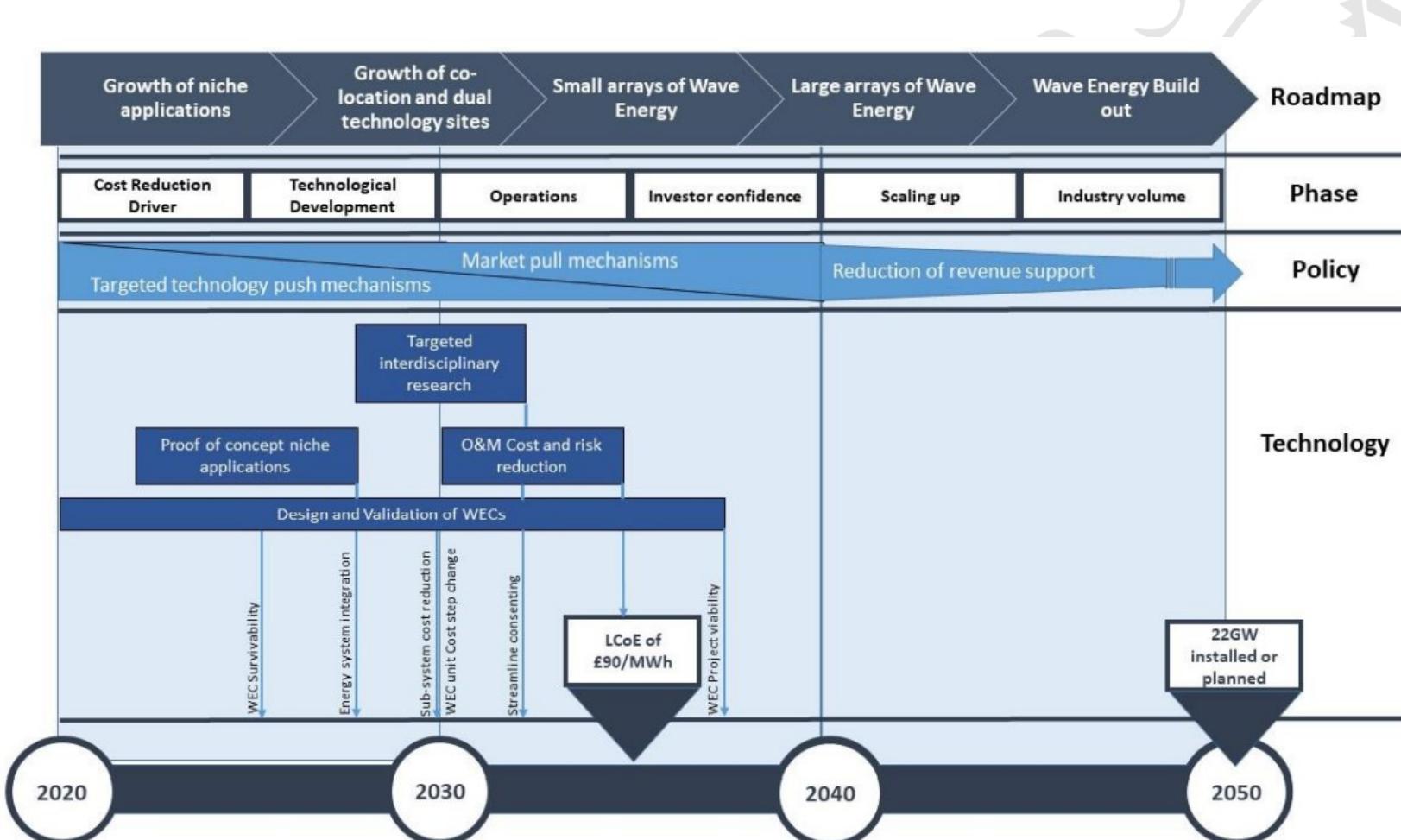


## Ocean energy roadmap





# Wave energy (UK) roadmap



**2020-2025**

Alternative technology, novel Wave Energy Converters (WECs)  
Survivability and reliability. Innovative materials. Power Take-Offs (PTOs) and control systems

**2025-2030**

Mooring and connection systems.  
Foundation design and installation for bottom fixed devices  
Demonstration of WECs in real sea conditions.

**2030-2038**

Demonstration of pilot WEC farm in real sea conditions



# Ocean energy outlook

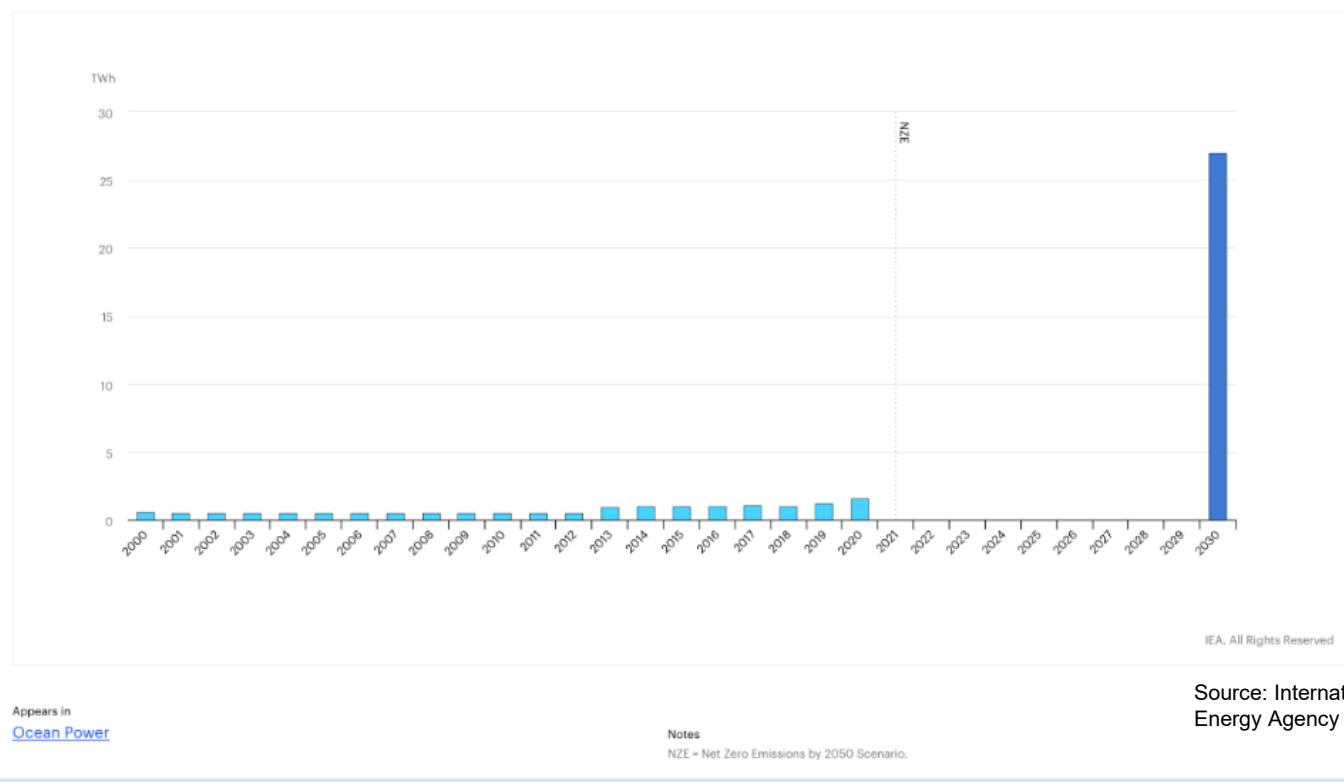
## Ocean power generation in the NetZero Scenario, 2000-2030

Last updated 2 Nov 2021

Download chart ↓

x

Cite Share



Ocean power generation needs to grow 33% a year to achieve net zero by 2050

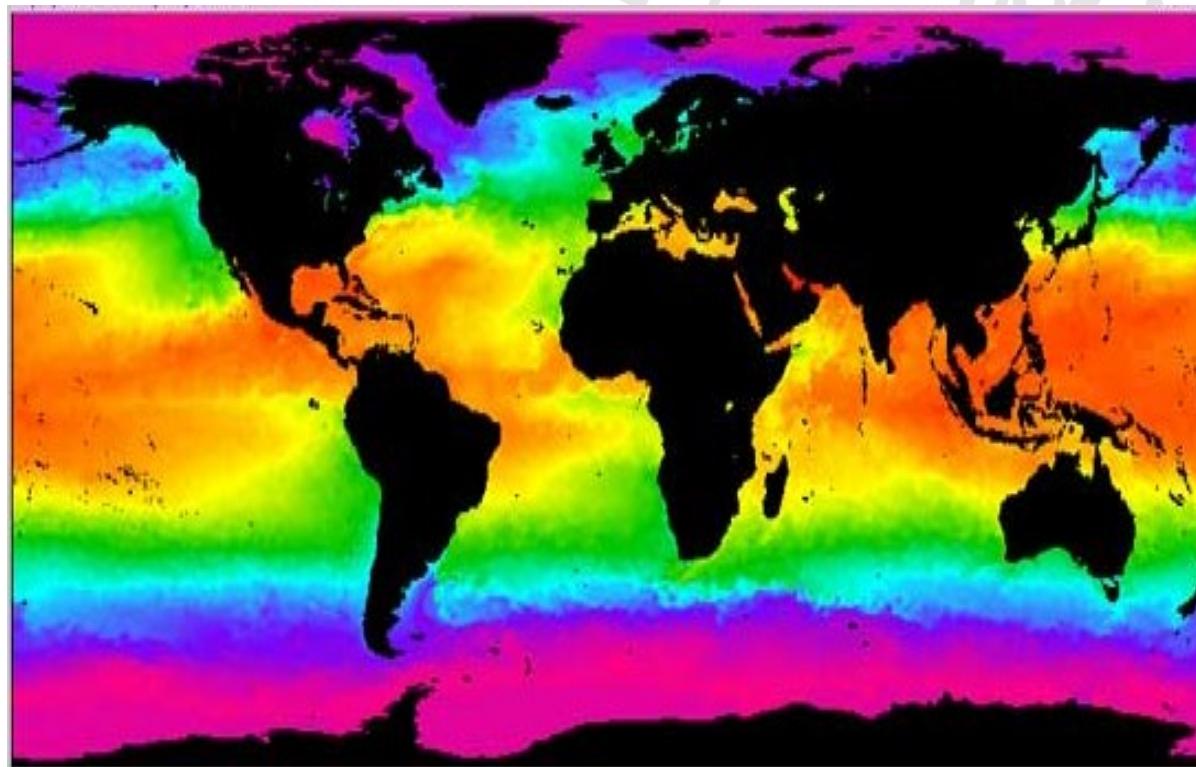


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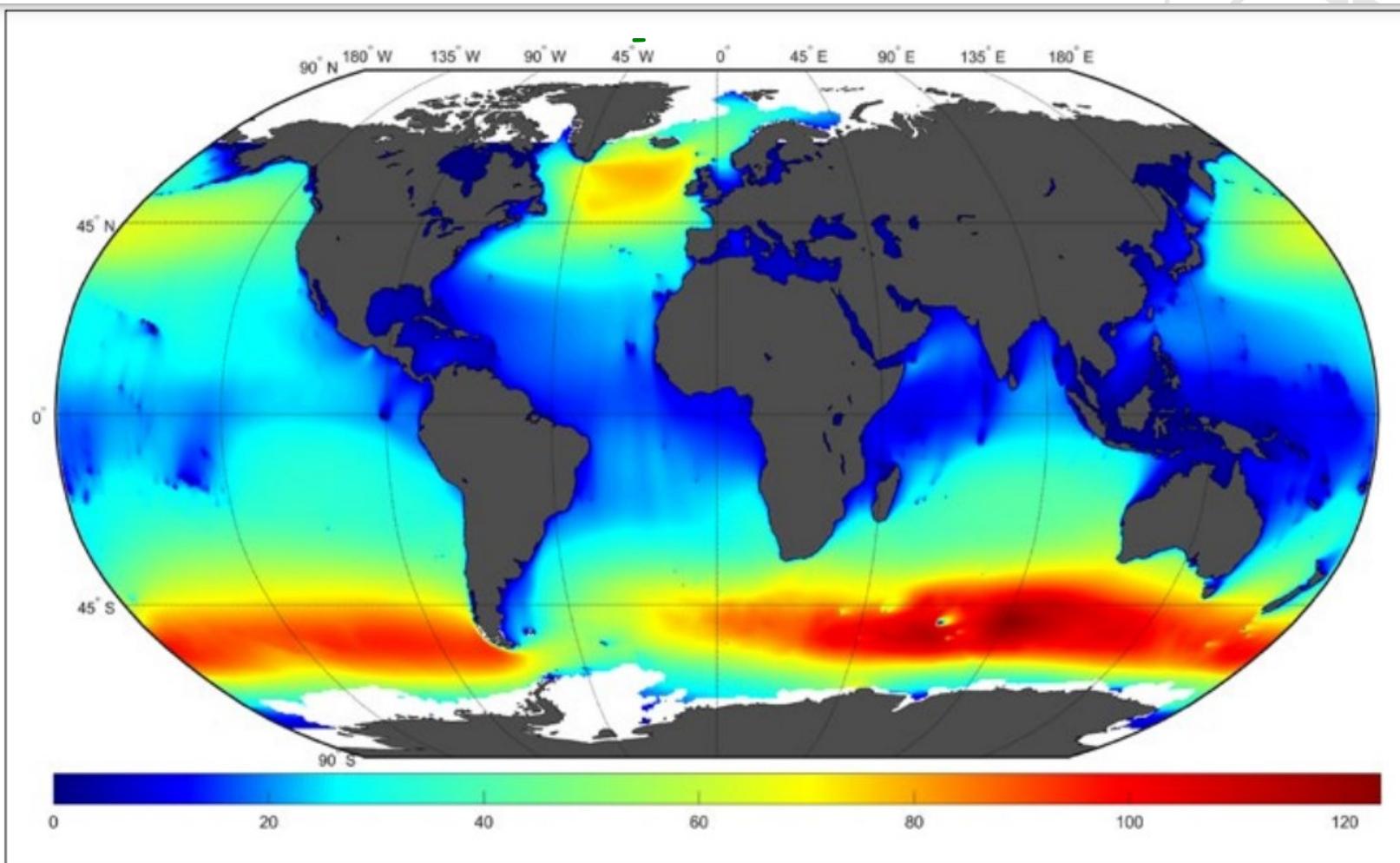
# Introduction to wave energy

**Where?**





## Availability of the resource



Highest wave energy transport at latitudes between **40°** and **60°**

Higher waves on the **west coasts**

Europe as the most favored continent for wave energy exploitation

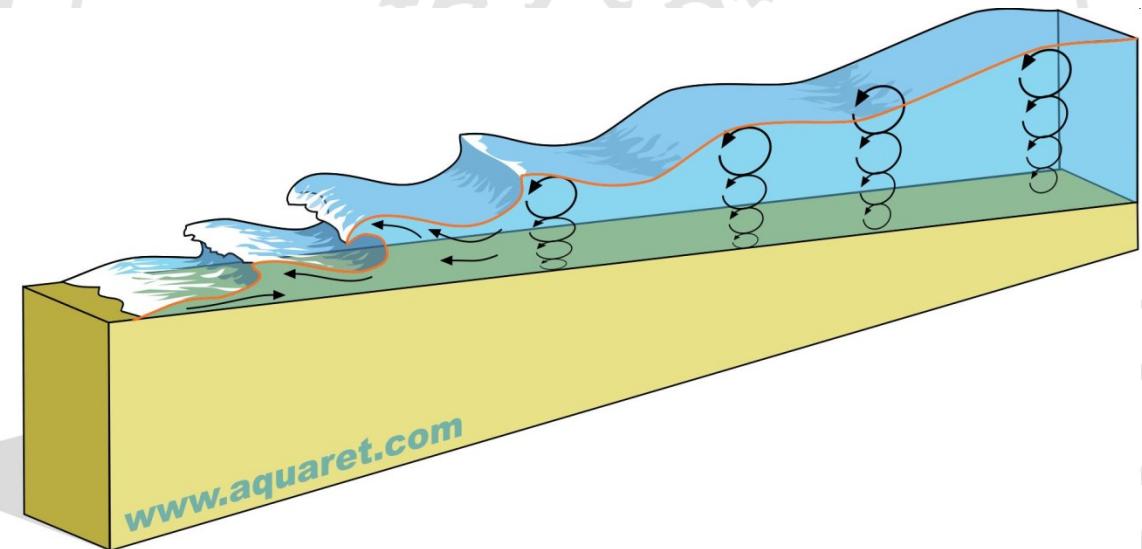
High potential also in America and Oceania



## Wave propagation

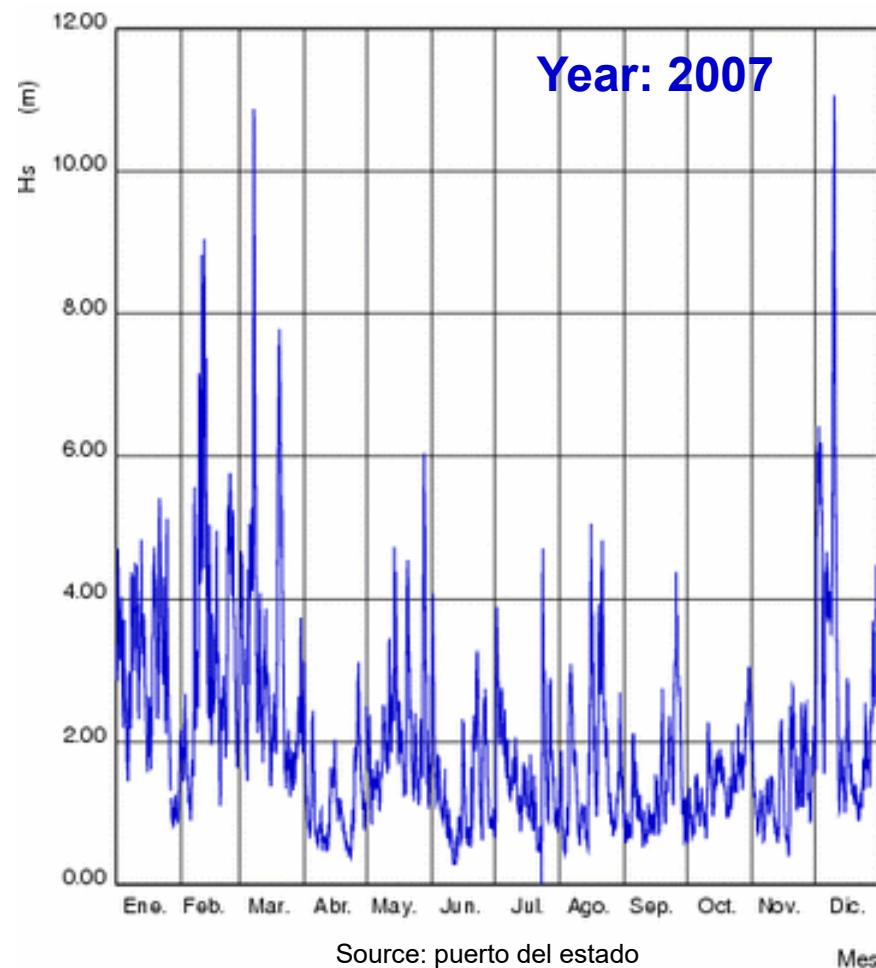
Waves **travel a lot** without loosing energy in **deep waters**

They rapidly loose their  
**energy close to shore** due  
to interaction with seabed





## Variability of the resource



Waves show a **seasonal variability**,  
being **more energetic during winter**  
**Such variability can be of a factor two**  
**or more**  
Data recorded from an offshore buoy  
located close to Bilbao, Spain



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# Introduction to wave energy

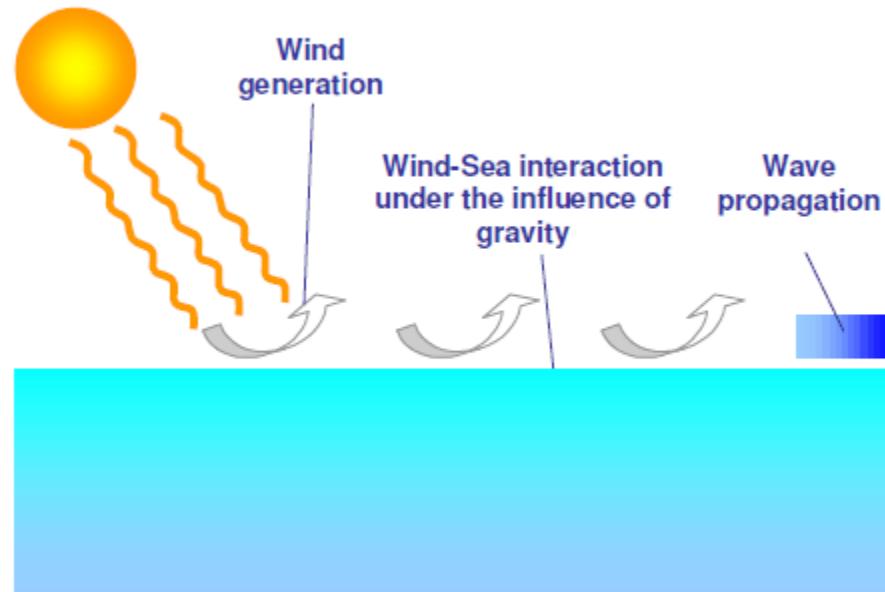
**What?**





## Origin of the energy

**Waves are created by winds and act as a concentrated storage of wind energy below the sea surface**



Actually, **waves** are a concentrated form of **solar energy**



## Comparison with other renewables

**Just below the sea level, wave energy flow is typically 5 times denser than the wind energy flow 20 m above the sea surface**



**Just below the sea level, wave energy flow is typically 20-30 times denser than the solar energy flow**

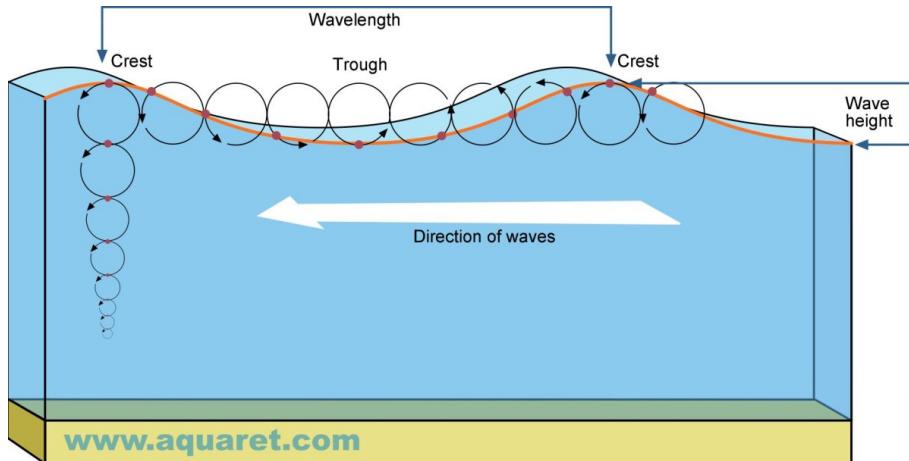


## Comparison with other renewables

ENERGY TYPE	CAPACITY FACTOR
	(The average absorbed power (or electricity) divided by the maximum power (or electricity) that a device can produce)
Offshore wind	0.3-0.6
Wave energy	0.25-0.32
Tidal current	0.5-0.7
Floating solar	0.1-0.3
Thermal gradient	0.9-0.95
Salinity gradient	0.8-0.84



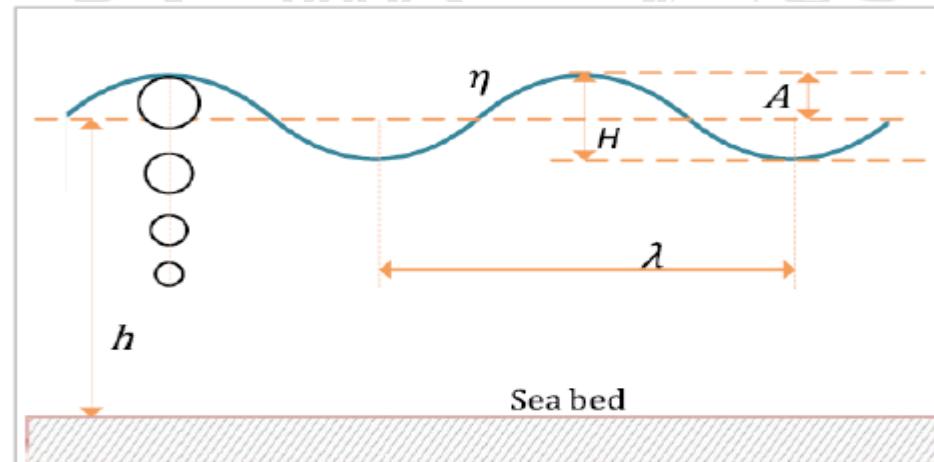
## Origin of the energy



**Sinusoidal (i.e. regular wave) approximation for sea waves is often used in the first instance**

**Due to wind action, water particles move in small circles**

**Most of the energy is concentrated just below the sea surface**

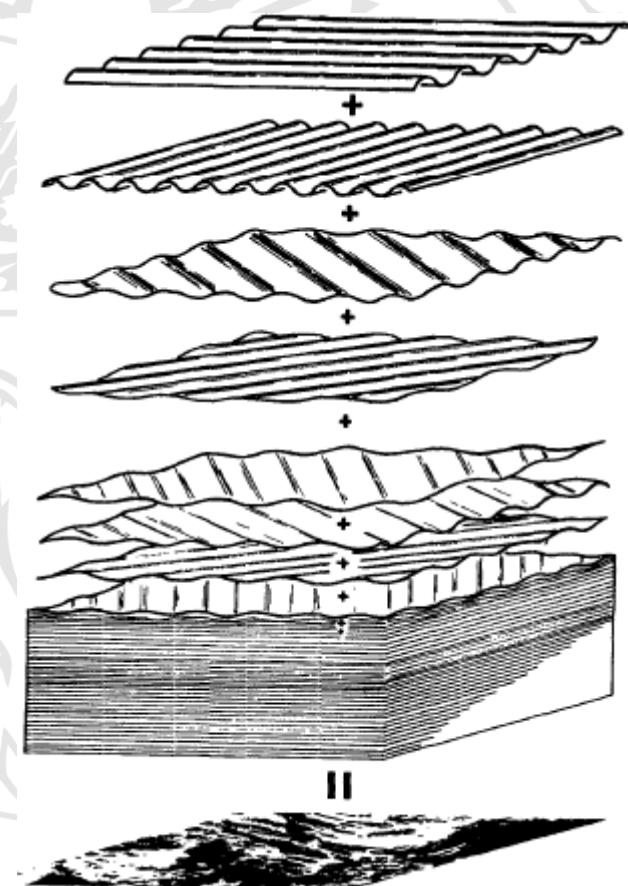


$\lambda$  = wavelength  
 $A$  = wave amplitude  
 $H$  = wave height  
 $h$  = water depth  
 $\eta$  = wave elevation



## Nature of irregular waves

**Intuitive description of an irregular sea:**  
**“A collection of a great number of simple regular waves of different lengths, all of small height and all mixed together with no apparent relation to each other except that they are all there and are travelling in the same direction”**

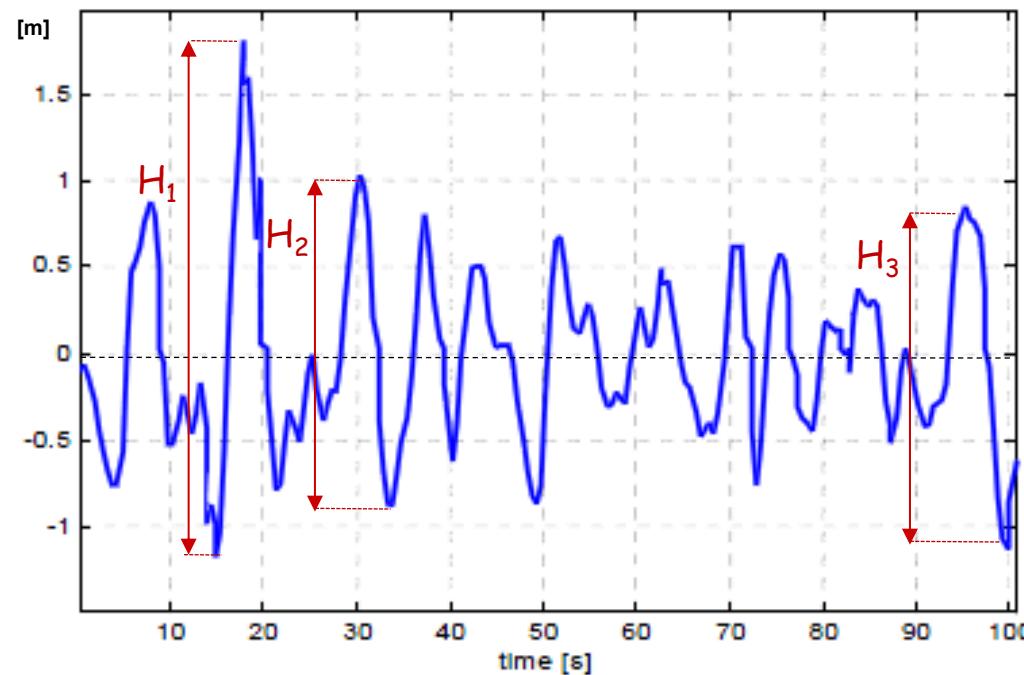


After Willard J. Pierson *et al.*, with permission  
of the US. Naval Hydrographic Office



# Significant wave height

Wave profile: example recorded in the  
North Atlantic



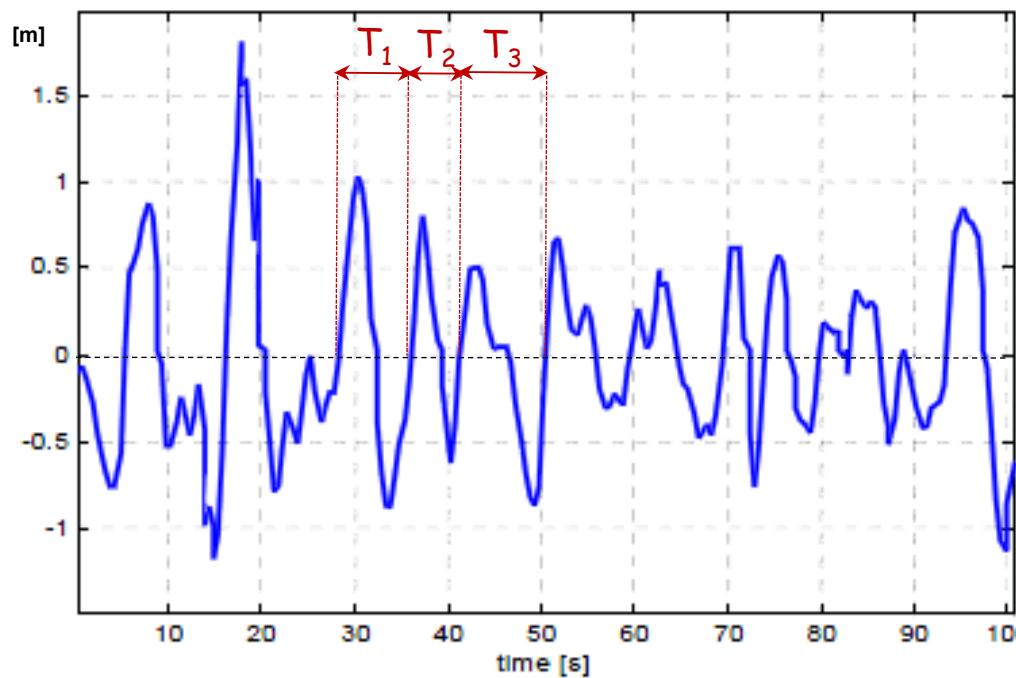
**Significant wave height** is the average of the highest one third of the individual trough-to-crest heights  $H_i$  ( $i=1,2,3,\dots$ ), and is denoted by  $H_{1/3}$  or often  $H_s$

$$H_s = H_{1/3} = \frac{H_1 + H_2 + \dots + H_{N/3}}{N/3}$$



## Average zero up-crossing time

Wave profile: example recorded in the  
North Atlantic



The individual **zero up-cross time  $T_i$**  ( $i=1,2,3\dots$ ) is the time interval between two consecutive instants where the wave elevation crosses the zero level in the upward direction. An **average** of these over a certain time provides a useful measure of the real-sea wave period.

$$T_z = \frac{T_1 + T_2 + \dots + T_N}{N}$$



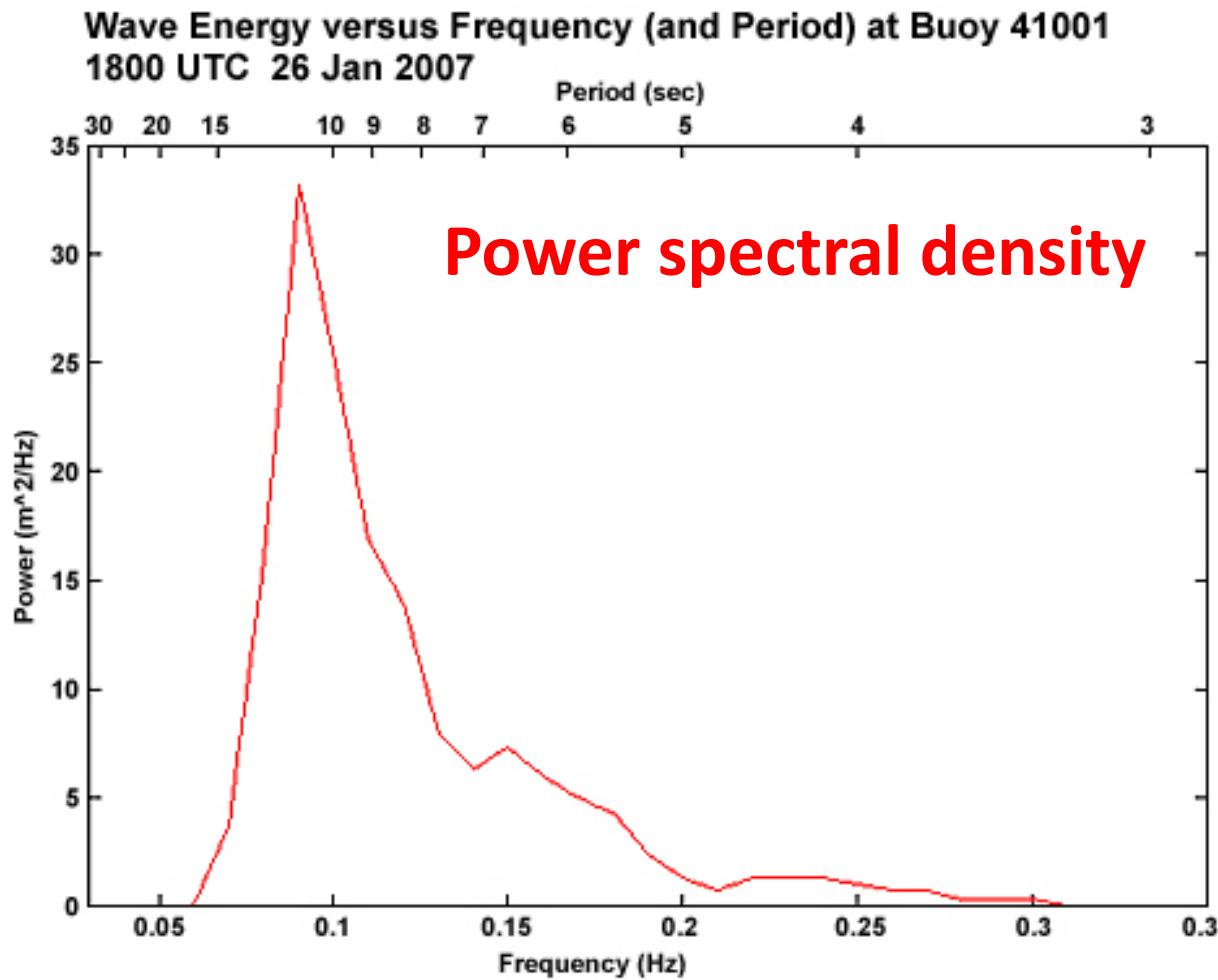
## Energy spectrum

- The intensity of the sea is characterized by its total energy, and we can show the individual contribution made by each of its component waves
- With each component waves of different height and frequency, we can show how the total energy of the sea is distributed according to the frequencies of the various wave components
- Such distribution is the energy spectrum of the sea, or simply, sea spectrum

(J.H. Michels, Sea Spectra Revisited)



## Energy spectrum



Power spectral density

From real sea measurements, the sea spectrum can be derived

Bretschneider Spectrum

$$S_f(f) = 0.08 H_s^2 T_z^{-4} f^{-5} \exp\left(-\frac{0.318}{T_z^4} f^{-4}\right)$$

Pierson-Moskowitz spectrum

$$S_f(f) = 5 \cdot 10^{-4} f^{-5} \exp\left(-\frac{2 \cdot 10^{-3}}{H_s^2} f^4\right)$$



## Wave power per meter length

- The wave power of linear regular (sinusoidal) waves per unit length of wave front in deep water is:

$$P_{\text{sin}} = \frac{\rho g^2 H^2 T}{32 \pi} \quad [\text{W/m}]$$

- The wave power of linear irregular waves per unit length of wave front in deep water is:

$$P_{\text{irr}} = \frac{\rho g^2 H_s^2 T_e}{64 \pi} \quad [\text{W/m}]$$

$$T_e \square [1.15 - 1.25] T_z$$

depending on sea spectrum



## Wave resource characterization at a specific site

Significant wave height, Hs (m)	Te (s)																						
	<5.0	5.5	6.0	6.5	7.0	7.5	8.0	8.5	9.0	9.5	10.0	10.5	11.0	11.5	12.0	12.5	13.0	13.5	14.0	14.5	15.0	15.5	16.0
14.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.00	0.00
13.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.00	0.00
13.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.02	0.00	0.01	0.00	0.00	0.00	0.00
12.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
12.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00
11.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.01	0.00	0.00	0.00	0.00	0.00	0.00	0.00
11.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.02	0.01	0.00	0.00	0.00	0.00	0.00	0.00
10.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
10.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.02	0.03	0.00	0.00	0.00	0.00	0.00	0.00	0.00
9.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.03	0.01	0.00	0.00	0.02	0.02	0.00	0.00	0.00
9.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.02	0.00	0.01	0.01	0.02	0.04	0.00	0.01	0.00
8.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.02	0.00	0.02	0.00	0.02	0.01	0.01	0.00	0.01	0.00	0.00
8.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.01	0.00	0.02	0.03	0.05	0.01	0.01	0.00	0.00	0.00	0.00	0.00
7.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.02	0.02	0.05	0.05	0.02	0.00	0.01	0.02	0.02	0.00	0.00
7.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.02	0.04	0.09	0.09	0.06	0.02	0.01	0.01	0.03	0.00	0.00	0.00
6.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.04	0.09	0.13	0.11	0.09	0.01	0.02	0.02	0.01	0.00	0.00	0.00	0.00
6.0	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.02	0.02	0.07	0.14	0.14	0.12	0.03	0.02	0.02	0.00	0.00	0.00	0.00	0.00
5.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.02	0.07	0.14	0.24	0.21	0.14	0.11	0.03	0.02	0.00	0.00	0.00	0.00	0.00	0.00	0.00
5.0	0.00	0.00	0.00	0.00	0.00	0.06	0.11	0.28	0.34	0.35	0.31	0.22	0.14	0.05	0.02	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
4.5	0.00	0.00	0.00	0.00	0.01	0.08	0.12	0.52	0.60	0.72	0.47	0.27	0.20	0.12	0.08	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
4.0	0.00	0.00	0.00	0.00	0.04	0.16	0.50	0.83	0.95	0.86	0.55	0.52	0.37	0.10	0.03	0.00	0.05	0.01	0.01	0.00	0.00	0.00	0.00
3.5	0.00	0.00	0.00	0.00	0.07	0.11	0.52	0.89	1.49	2.06	1.57	1.05	0.68	0.51	0.34	0.10	0.08	0.05	0.00	0.00	0.00	0.00	0.00
3.0	0.00	0.00	0.00	0.09	0.21	0.74	1.15	2.14	2.61	2.58	1.58	1.14	0.90	0.56	0.39	0.26	0.09	0.10	0.02	0.01	0.00	0.00	0.01
2.5	0.00	0.01	0.02	0.17	0.57	1.71	2.03	2.15	2.42	1.87	1.53	1.18	0.68	0.36	0.21	0.14	0.15	0.13	0.09	0.03	0.02	0.02	0.02
2.0	0.00	0.11	0.67	1.08	1.74	1.93	2.81	3.43	3.71	2.68	1.79	1.15	0.49	0.20	0.17	0.10	0.03	0.02	0.00	0.01	0.02	0.00	0.01
1.5	0.02	0.46	1.34	0.92	1.50	2.18	2.38	3.12	2.25	2.27	1.74	1.02	0.55	0.20	0.03	0.05	0.05	0.00	0.00	0.00	0.00	0.00	0.00
1.0	0.09	0.14	0.55	0.30	0.71	0.95	0.79	0.49	0.33	0.40	0.14	0.06	0.03	0.02	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
0.5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

At a specific site, the wave resource is often characterized by the % occurrence of each different couple of wave height/wave period and represented through a scatter diagramme

Source: AMETS scatter diagram (2010)



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# Introduction to wave energy

How?





# Introduction to wave energy

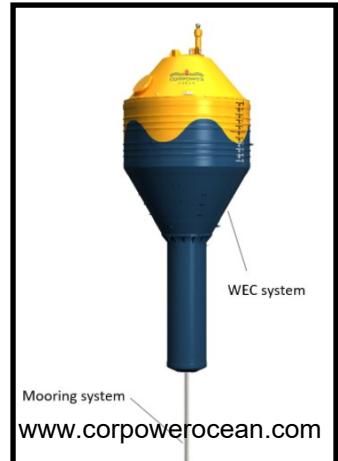
WAVEROLLER



WELLO-PENGUIN



CORPOWER



MARMOK



**High concept diversification  
Frequent need of tailor-made  
solutions**

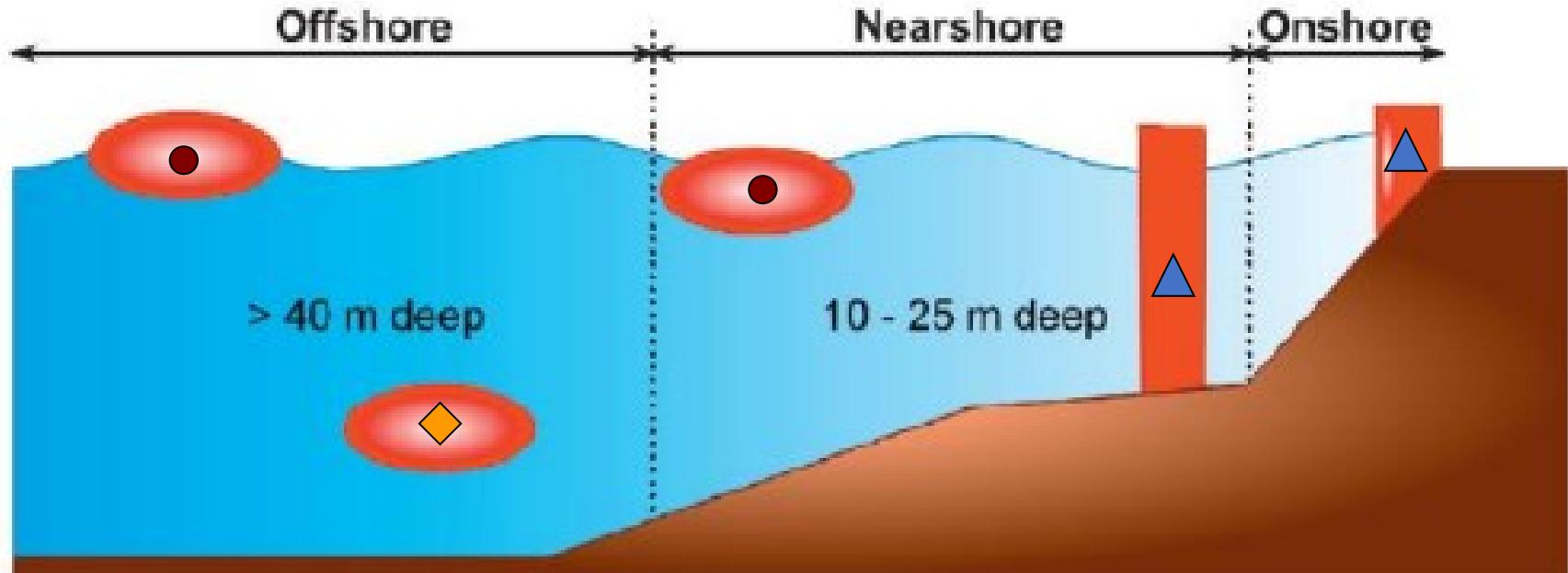


## Classification of devices

- **Location**
- **Depth of installation**
- **Size and orientation**
- **Primary conversion mechanism**



## Location and depth of installation

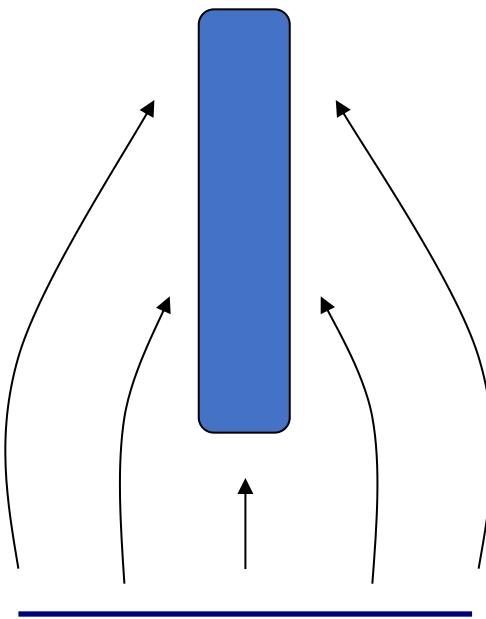


- **Floating**
- ◆ **Submerged**
- ▲ **Bottom standing**

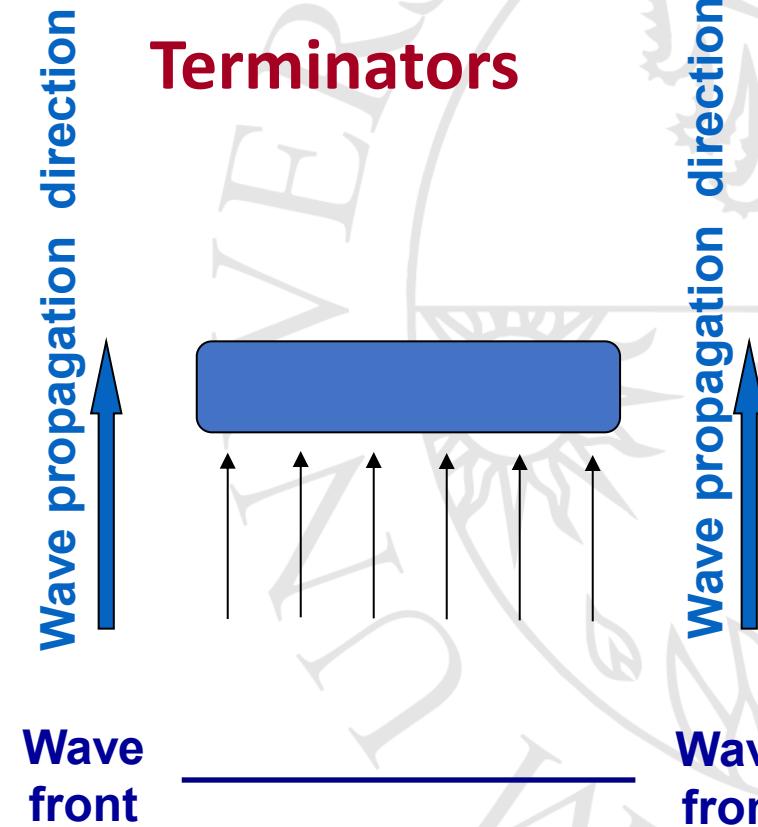


## Size and orientation

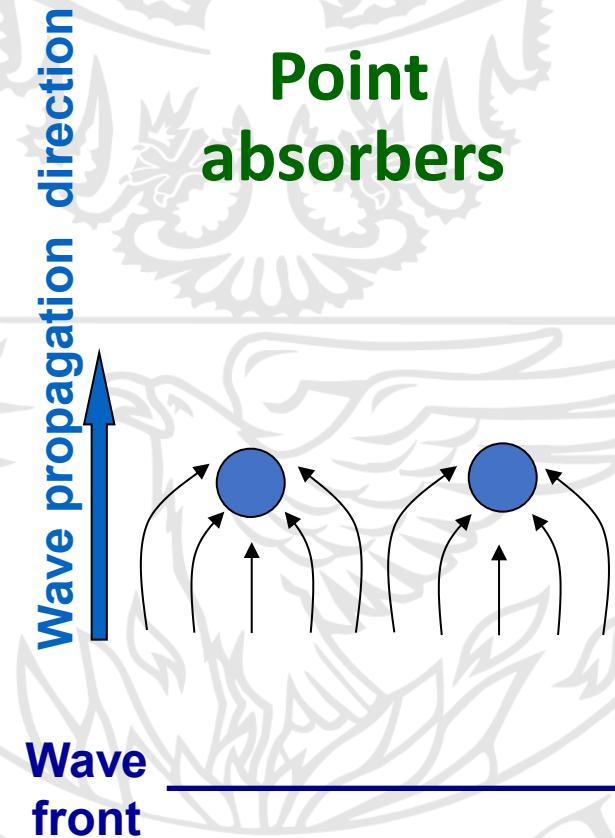
### Attenuators



### Terminators

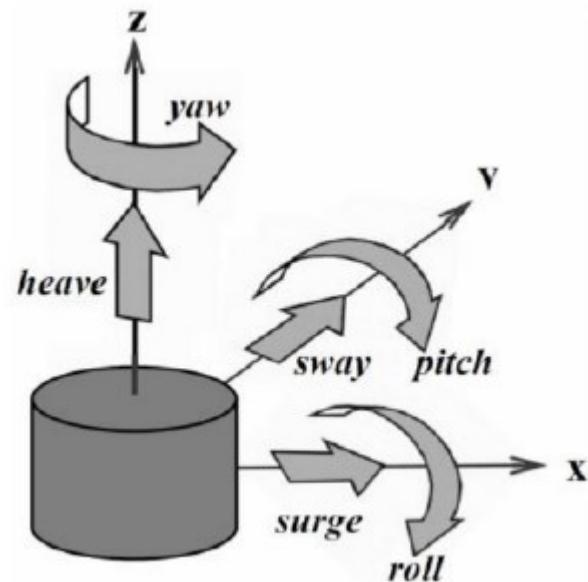


### Point absorbers





# Motion of a rigid body subject to waves



Source: W. Sheng (2010)

## Translational degrees of motion:

**SURGE** – Forward and backward moving along the longitudinal horizontal axis.

**SWAY** – Left and right motion along the lateral horizontal axis.

**HEAVE** – Up and down motion along the vertical axis is.

## Rotational degrees of motion:

**ROLL** – Rotating motion about the longitudinal horizontal axis.

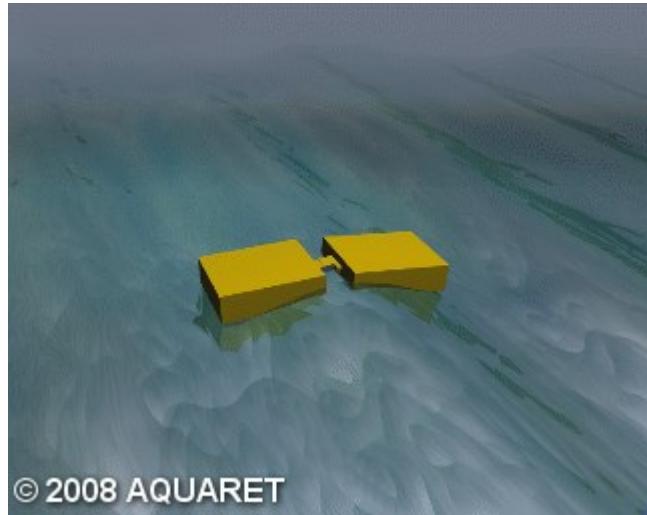
**PITCH** – Rotating motion about the lateral horizontal axis.

**YAW** – Rotating motion about the vertical axis.



## Working principle

### Attenuator

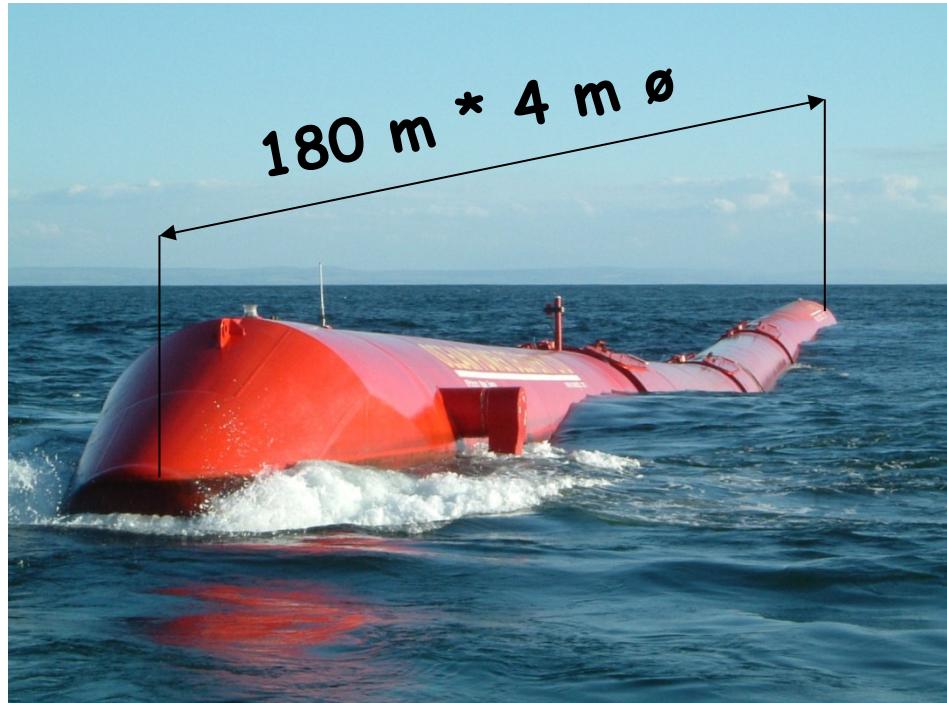


An **attenuator** Wave Energy Converter (WEC) is a line absorber operating parallel to the wave propagation direction. The device is usually not physically fixed in place. This device captures energy from the relative motion of the two arms as the wave passes them.



## Example

### Attenuator



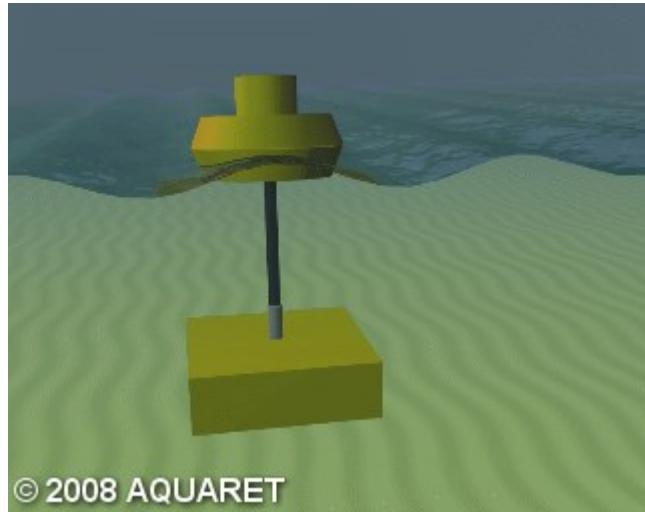
Source: [www.pelamiswave.com](http://www.pelamiswave.com)

- PELAMIS was the first attenuator to be deployed offshore and grid-connected (2004)
- 5 modules for **750 kW**
- 180 m long and **4 m** in diameter
- Annual production around 25-40% of full rated power
- Hydraulic rams
- High pressure fluid
- Smoothing accumulators
- **Hydraulic motors + electrical generators**



## Working principle

### Point Absorber



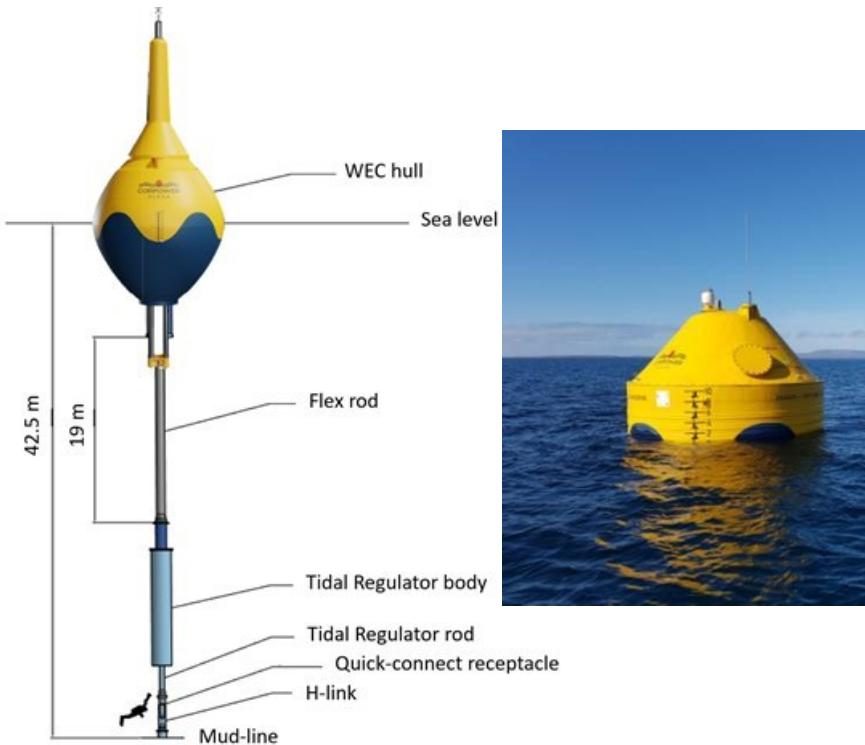
A **point absorber** is a device with small dimensions compared to the incident wavelength and because of that, wave direction is irrelevant for the system.

Point absorbers are most often used in offshore locations, and they mainly utilize heave motion for wave energy extraction



## Working principle

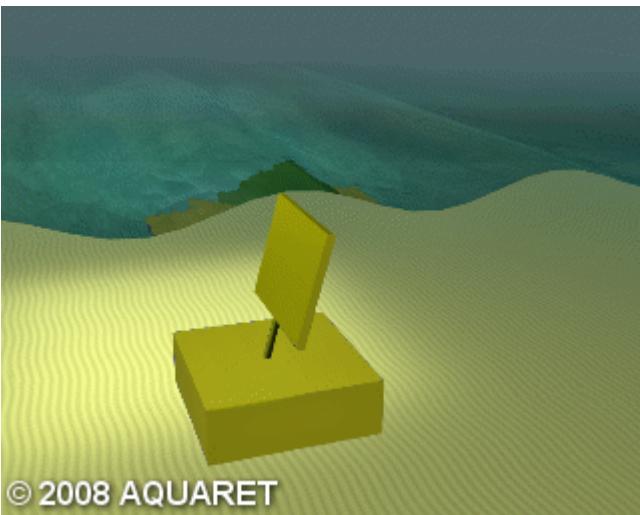
### Point Absorber



- CORPOWER point absorber concept
- 300 kW power rating of the buoy
- 9 m diameter, 18 m high buoy
- Exploitation of waves between 0.5 m and 8 m
- Capacity factor between 40% and 60%
- Suitable for offshore installations, including array deployment



## Working principle



### Oscillating Water Surge Converter

An **oscillating water surge converter (OWSC)** is positioned perpendicular to the wave direction and extracts energy from wave surges, exploiting the horizontal particle velocity of the waves. The arm oscillates as a pendulum around a pivot axis in response to the movement of water in the waves.



## Example

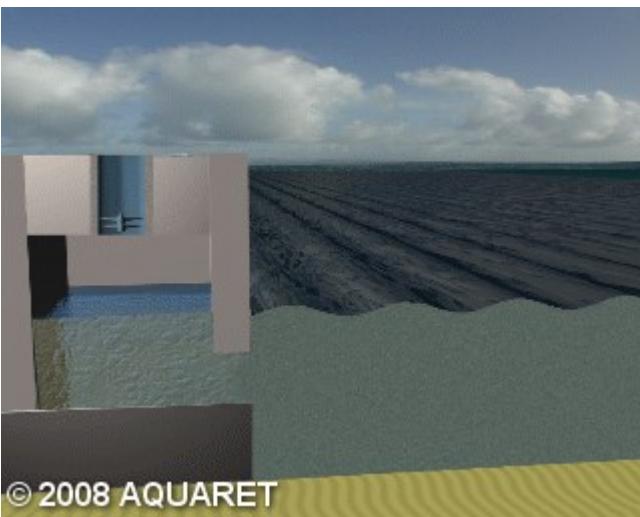


### Oscillating Water Surge Converter

- WAVEROLLER is a buoyant, hinged flap (OWSC)
- Deployed in near shore areas (8-20 m water depth)
- A single WaveRoller unit (one panel and Power Take Off system combination) is rated at **between 350kW and 1000kW**
- Capacity factor **between 25% and 50%**



## Working principle



### Oscillating Water Column

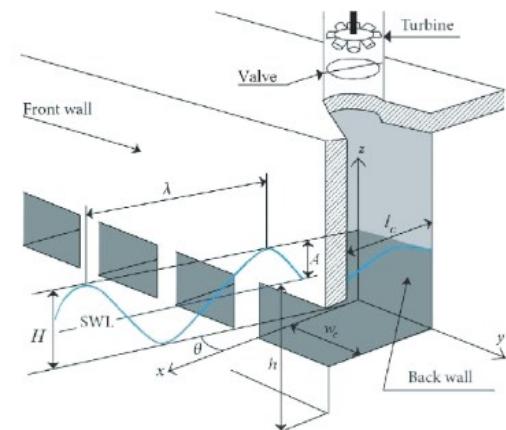
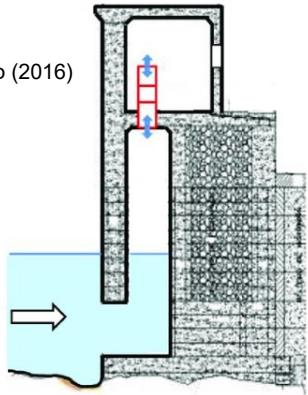
An **oscillating water column (OWC)** consists of a semi-submerged and hollow structure with an underwater opening that allows water to enter and leave the device. The structure encloses an air column on top of a water column. Water is forced into a chamber as soon as waves move towards the device and the trapped air, compressed and decompressed, drives the air turbine. So OWCs use the different wave-induced water level to force air to flow through an air turbine to extract energy



## Example

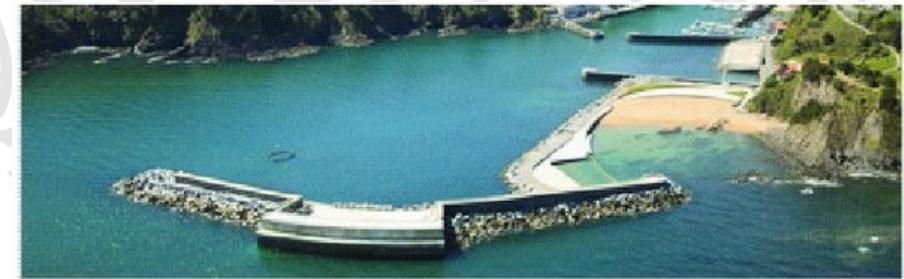
### Oscillating Water Column

Source:  
A. Falcao (2016)



- NEREIDA power plant in Mutriku
- **16 OWC** integrated in the breakwater
- Total installed capacity: **296 kW**
- Each OWC has a **Wells turbine**
- Each Wells turbine drives an **18.5 kW Doubly Fed Induction Generator (DFIG)**

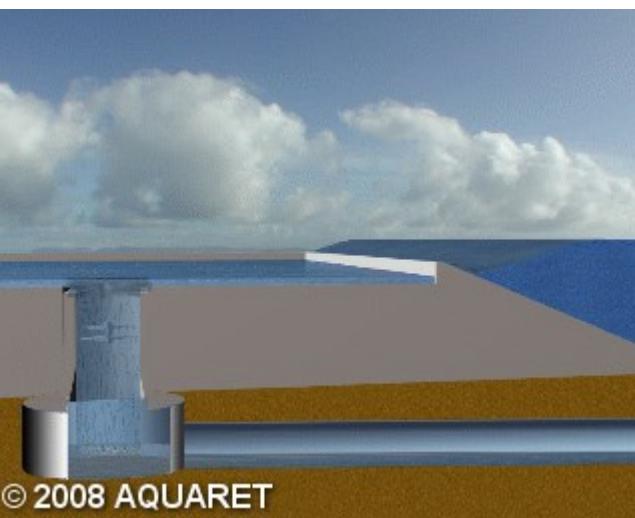
Source: Fares M'zoughi (2019)



Source: Fares M'zoughi (2019)



## Working principle



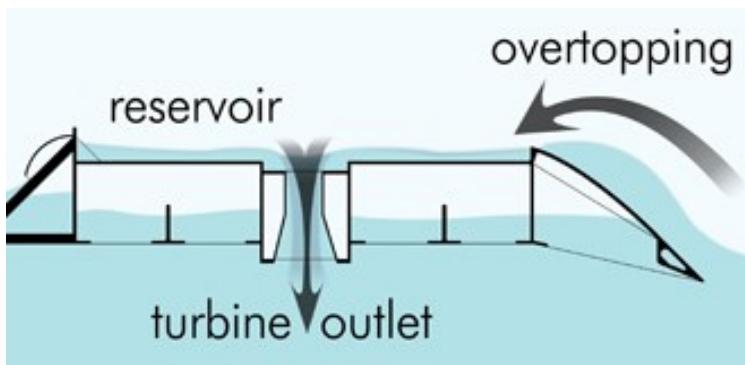
### Overtopping device

An **overtopping device** is a partially submerged terminator with a reservoir above the sea level for capturing sea waves. A ramp allows the incident waves to pass over the structure and then to return to the ocean falling through low-head water turbines to generate electricity



## Working principle

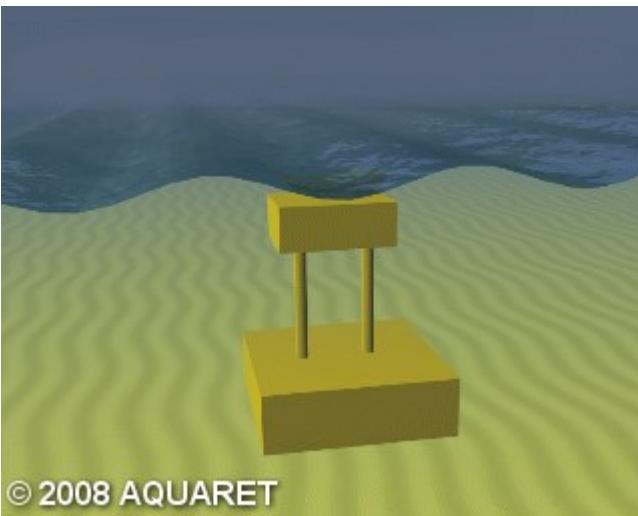
### Overtopping device



- WAVEDRAGON overtopping device
- Floating, slack moored with curved ramp and wave deflector
- Reservoir above the sea level
- Kaplan turbines + PM generators
- Total width and length: 390 m \* 220 m (for a 4MW device)
- Tested in small scale (20 kW) between 2003-2005 and 2006-2011



## Working principle



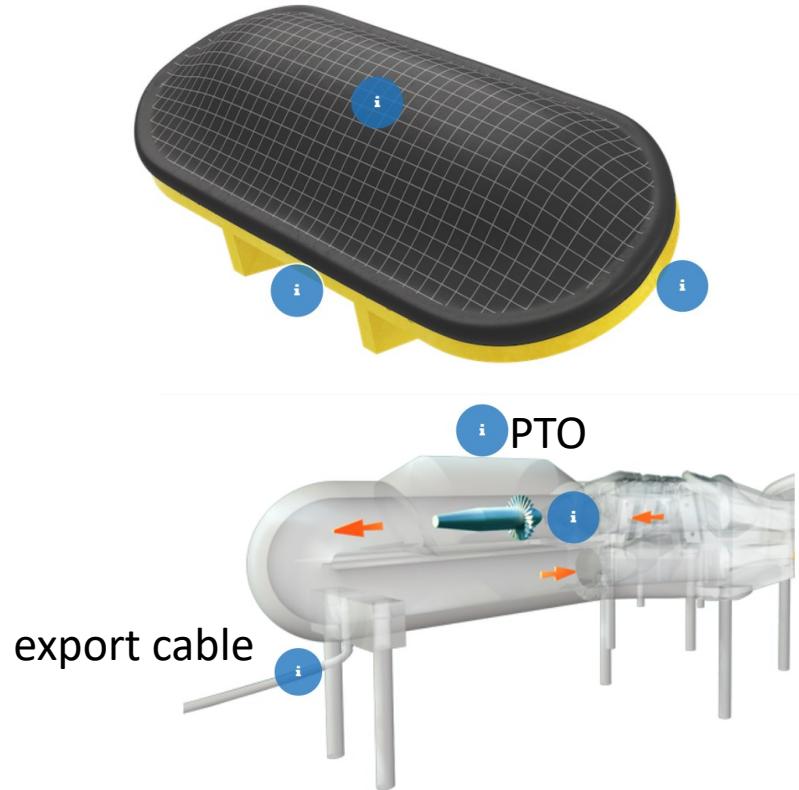
### Submerged pressure differential

A **submerged pressure differential device** exploits the sea level rise and fall above the device, due to sea waves, which induces a pressure differential in the device. The alternating pressure pumps fluid through a system to generate electricity. It's typically installed near shore.



## Working principle

### Submerged pressure diff.

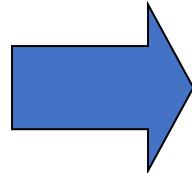


- BOMBORA mWave
- Concave cells covered by air-inflated rubber membranes
- High speed unidirectional turbine + PM generators
- Full scale (1.25 MW) demo tested in 2020
- Modular for scalability and coupling with other renewables



## Wave energy conversion chain

### Waves



**Primary en. conversion:** from waves to pressurized air, water or hydraulic oil

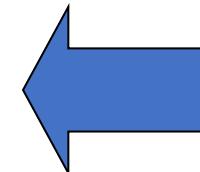


**Secondary en. conversion:** from the fluid to a turbine or motor converting it into mechanical energy



**Tertiary en. conversion:** from mechanical into electrical by electric generator

### Electricity

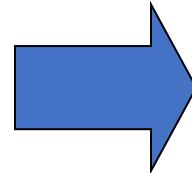


Can be merged for «direct-drive» solutions



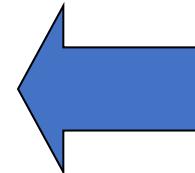
# Wave energy conversion chain

## Waves



**First conversion stage:**  
from waves to mechanical energy  
(Direct-drive solution)

## Electricity



**Second conversion stage:**  
from mechanical into electrical by  
electric generator



## Power Take-Off systems for Wave Energy Converters

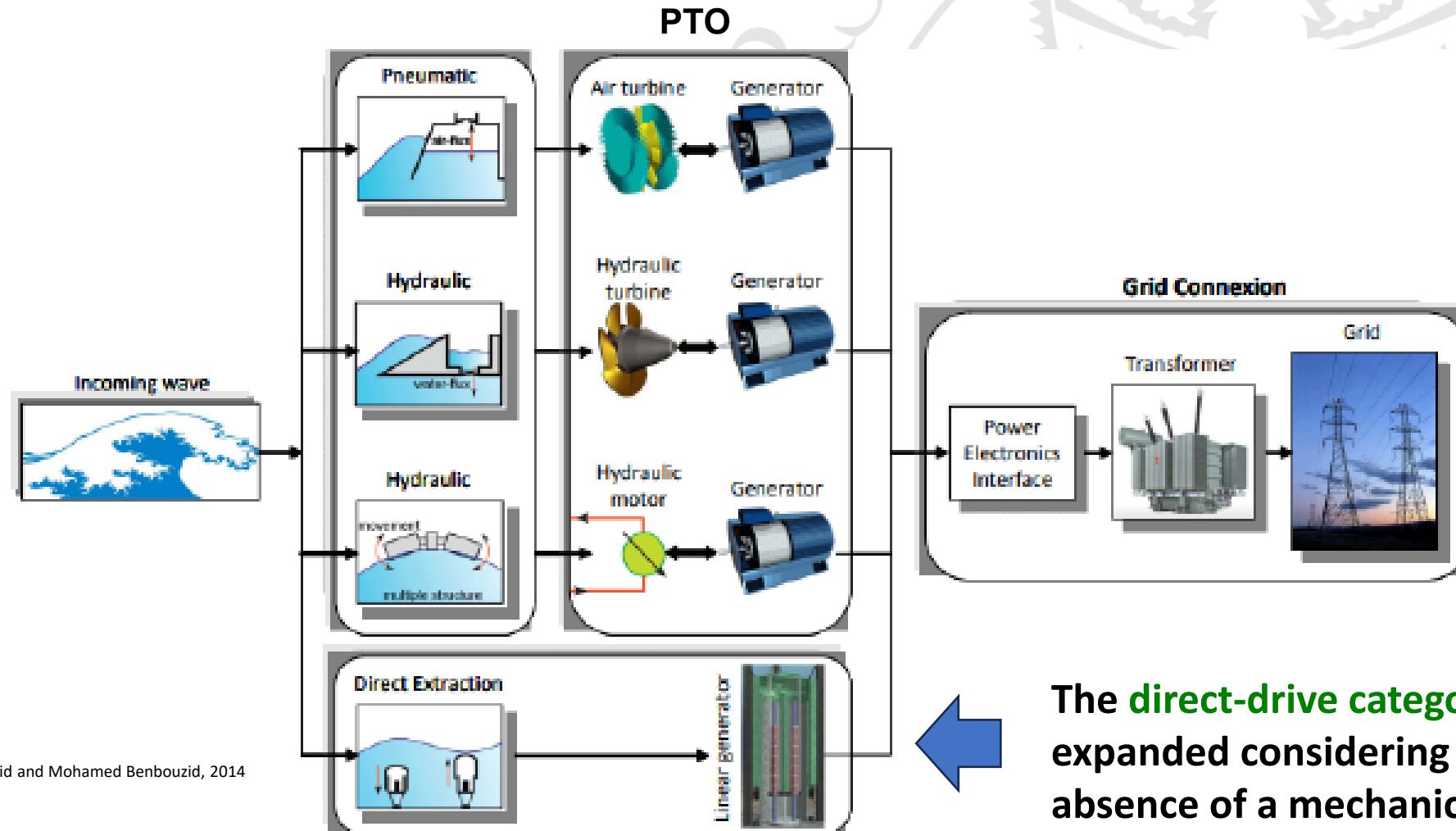
The **Power Take-Off (PTO) system** of a wave energy converter is the mechanism with which the absorbed energy by the primary converter is transformed into useable electricity

High PTO concept diversification and frequent need of tailor-made solutions characterize the wave energy industry

***"The limited amount of electricity generated by wave energy converters suggests that designs still need to be optimized; and that conversion technologies, in particular reliable Power Take Offs (PTO) need still to be validated"***

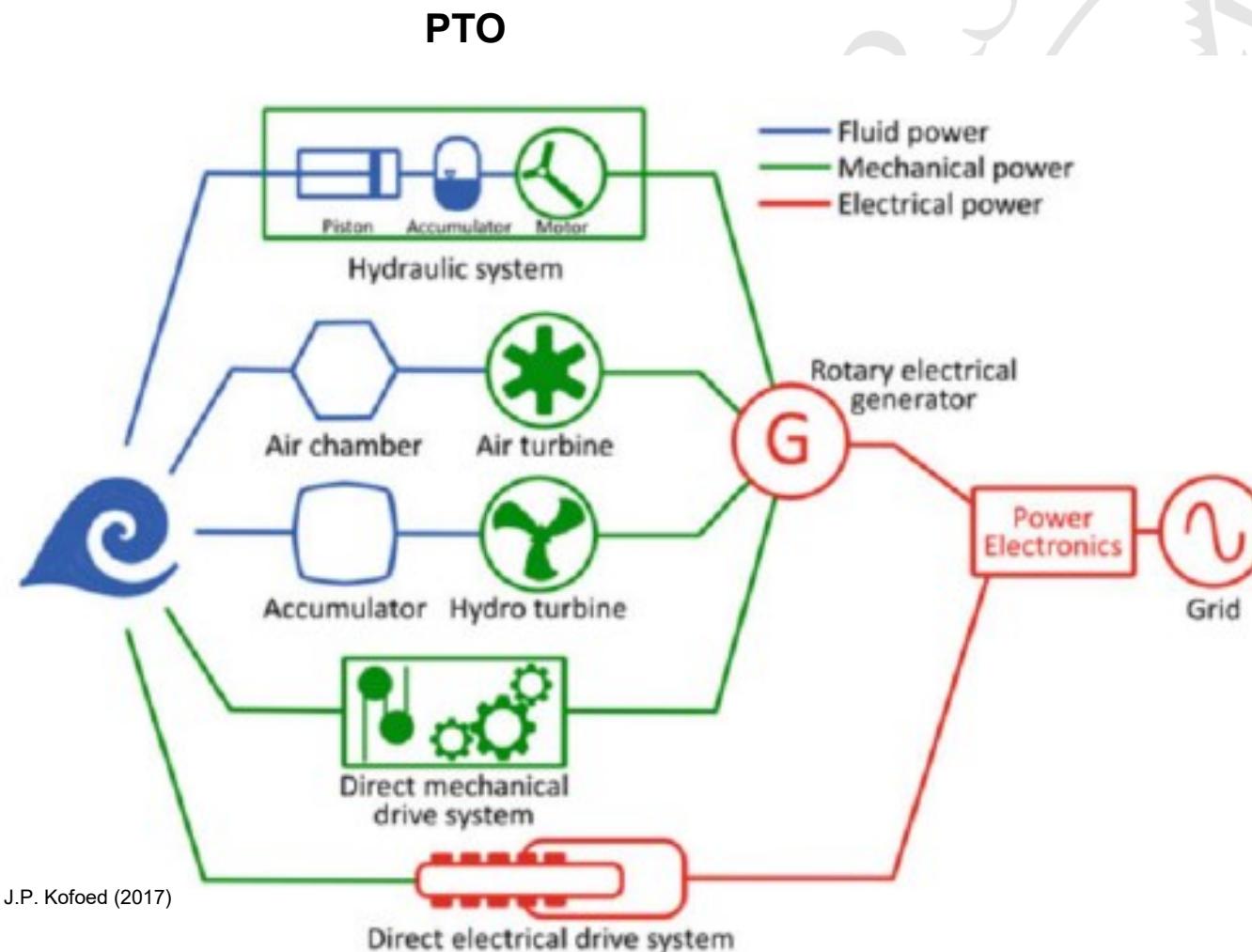


# Power Take-Off systems for Wave Energy Converters





# Power Take-Off systems for Wave Energy Converters

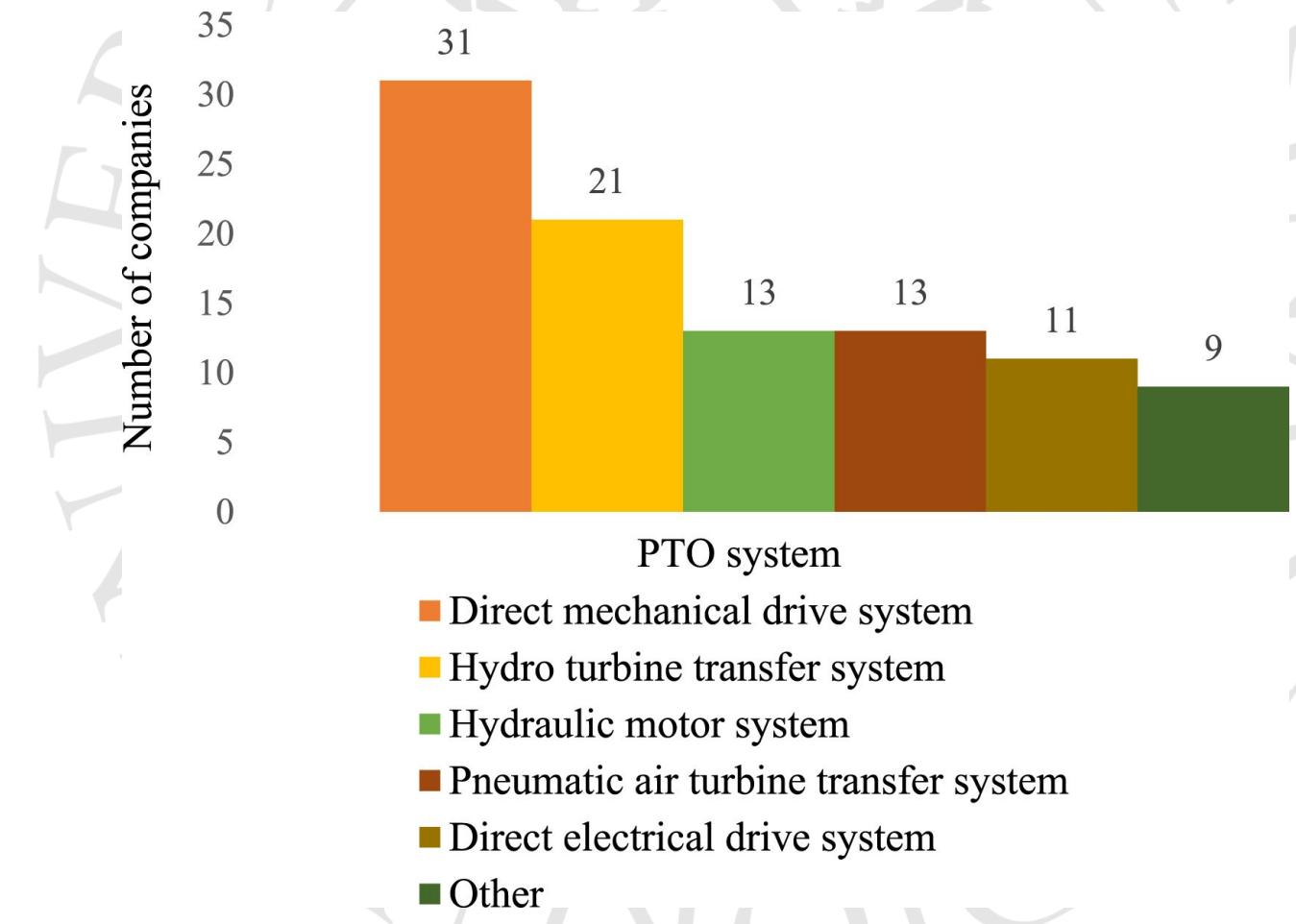




## Market share

**WEC developers  
based on PTO system**

**The largest number of  
WEC developers are  
from Europe (63%) and  
North America (25%)**





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Dipartimento di  
Ingegneria Industriale

# Control of Wave Energy Converters



## Basis of wave energy capture mechanism

**Wave energy absorption is based on an apparent paradox:**

**“To absorb a wave means to generate a wave”**

**or in other words:**

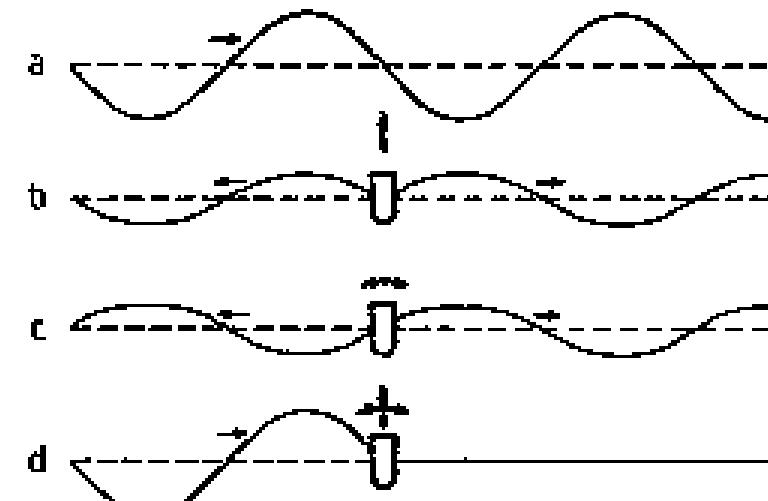
**“To destroy a wave is to create a wave”**



## Control of wave energy converters

**Wave energy exploitation is based on a destructive interference between sea waves and buoy oscillation**

**Active control of the buoy movement is needed to maximize power extraction from the sea**



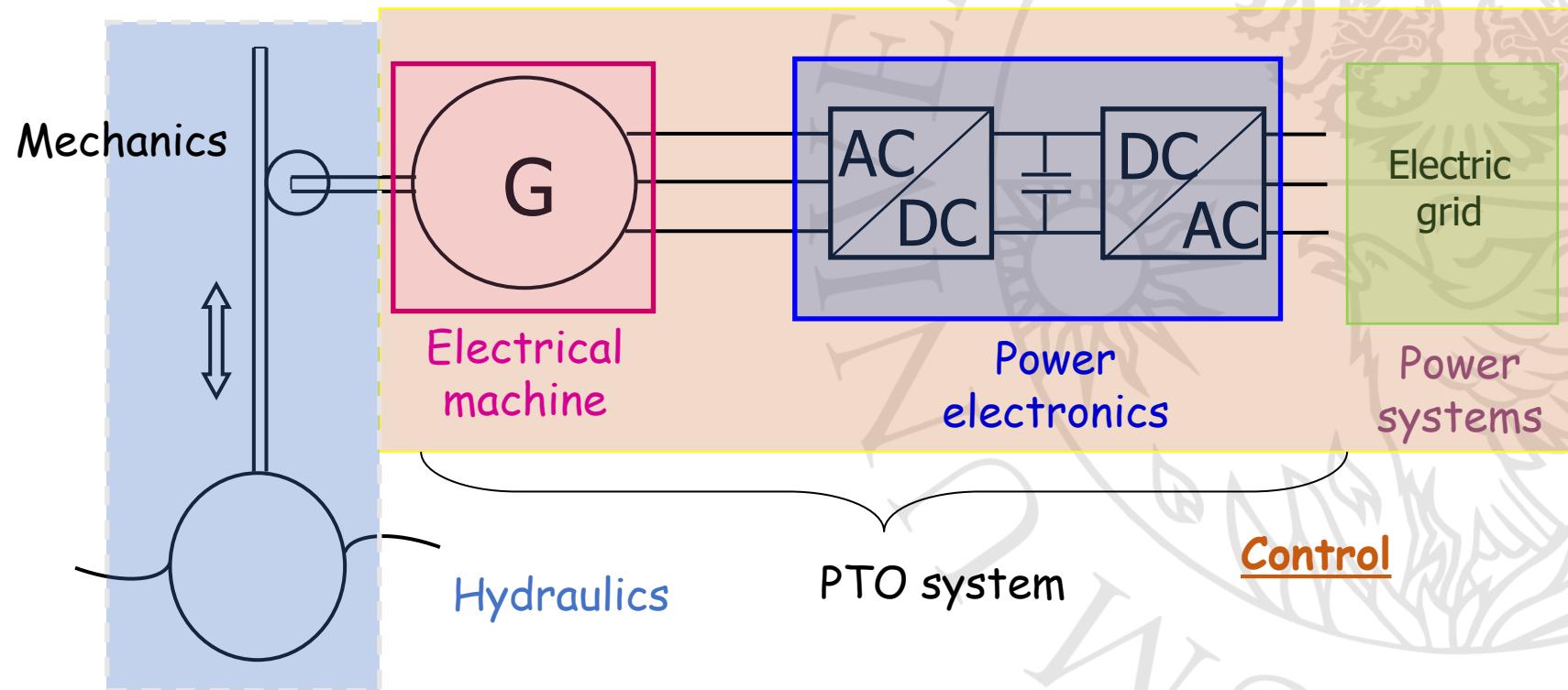
Source: Falnes (2000)

**The first goal of WEC control is to maximize such extraction**



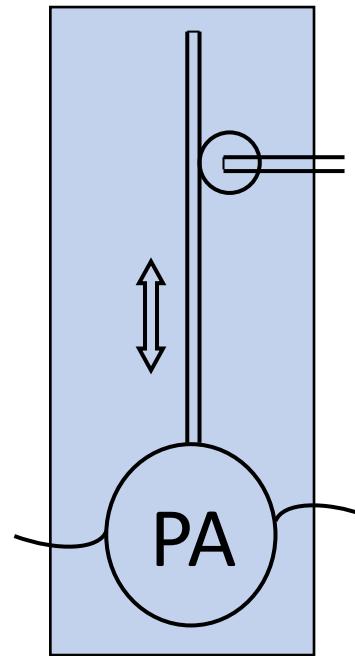
# Multidisciplinary approach to wave energy

Reference system for control discussion





## Control of wave energy converters

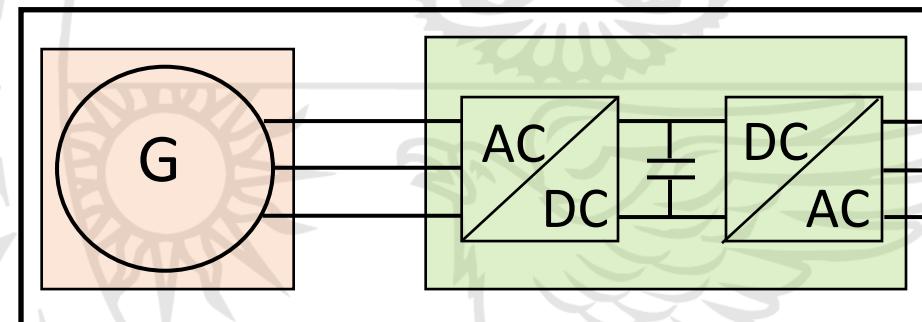


**WEC control goal:**

**Set  $F_L$**

WEC control is the bridge between the hydrodynamic domain and the electrical domain

**POWER TAKE-OFF**

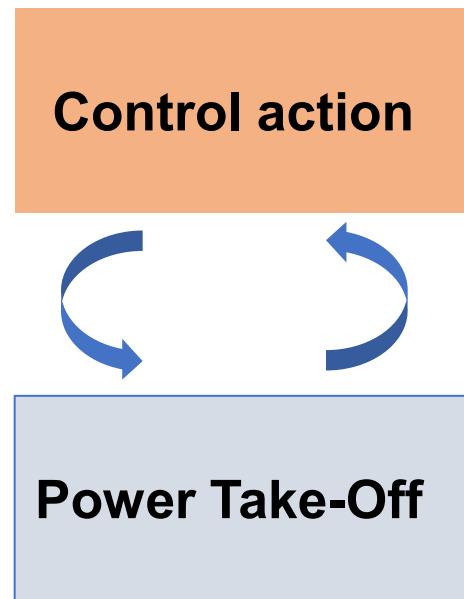


**Interaction of subsystems through control is the basis of power conversion, delivery and conditioning**



## Control of wave energy converters

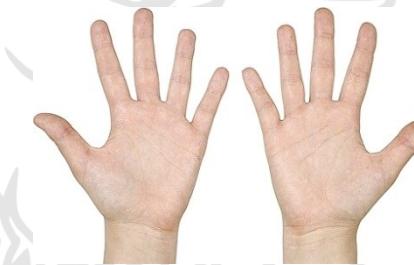
**The PTO is the component that actuates of the control action**



**How we want the system to behave and what reference signals we consequently need to generate**



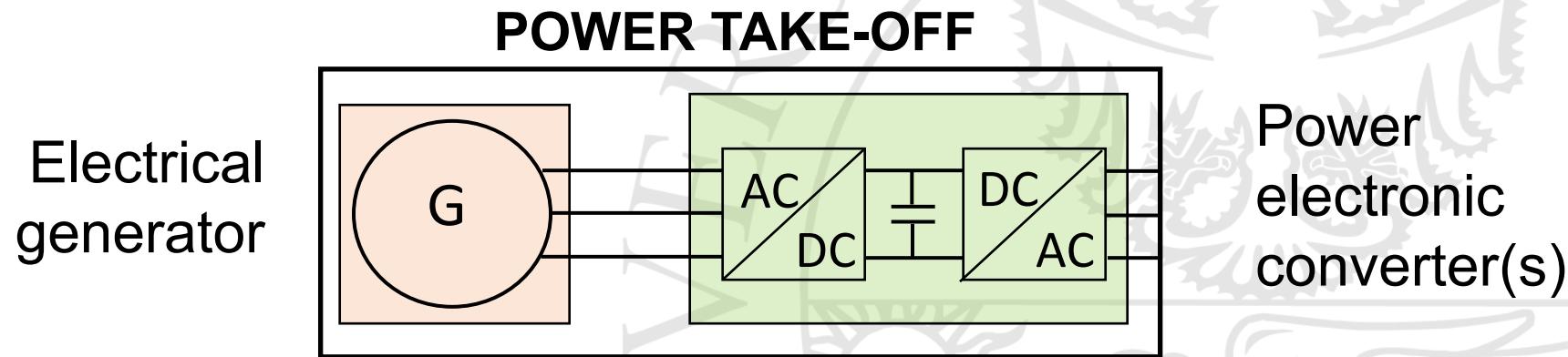
**How we practically apply the (control) reference signals in the real system**



**There is a strong, mutual interaction between control strategies and the Power Take-Off system**



## The Power Take-Off (PTO) system



To transform the mechanical energy extracted from the buoy into electrical energy

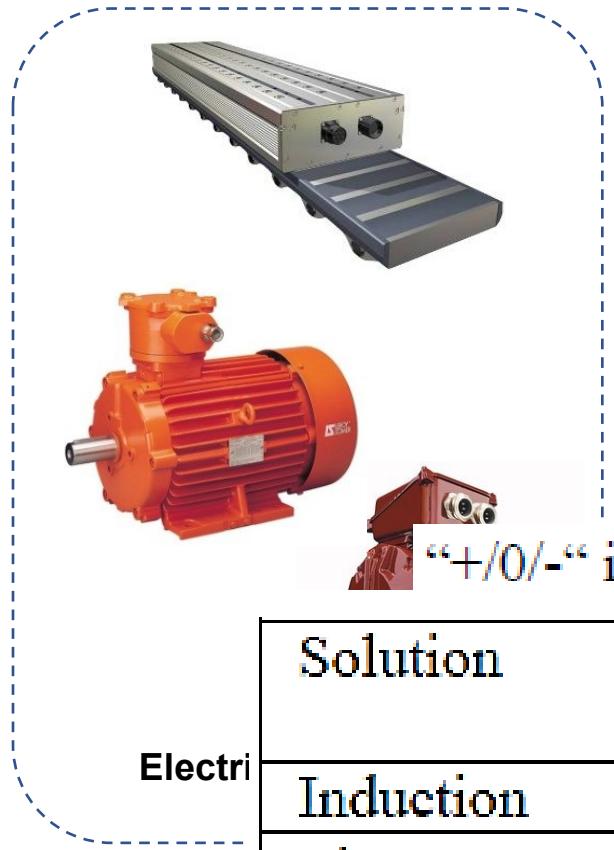
power conversion      ->      Electrical machine

Control and inject electrical power into the local power system respecting the conditions imposed by utilities

power conditioning      ->      Power electronics interface



## Electrical machine selection



Permanent  
magnet linear  
generator

Asynchronous  
generator

### Typical requirements:

- low speed
- high torque/force

“+/-“ is favorable/neutral/less advantageous.

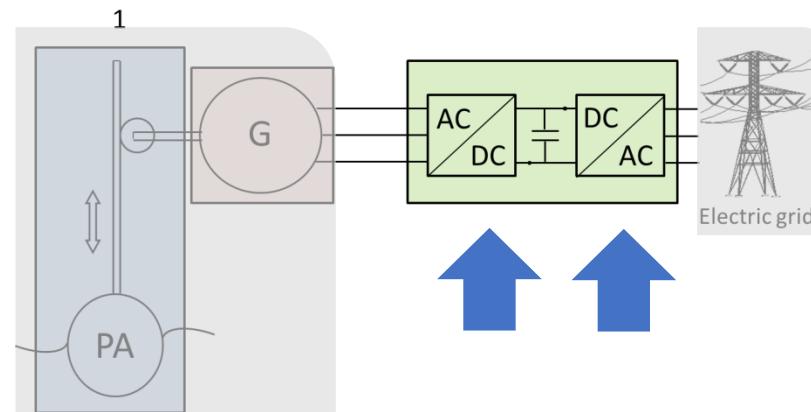
Solution	kg	$\eta$	Robustness	Converter size	Cost
Induction	+	0,90	+	0	+
Linear PM	-	0,93	-	0	-
Rotating PM	-	0,95	0	+	0



## Control of wave energy converters

**Control of wave energy converters (WECs) has a twofold function:**

- “WEC side” control
- “Grid side” control



Improve the power absorption from the waves

Control the quality of the power delivered to the electric grid

Power electronics is crucial in both of them

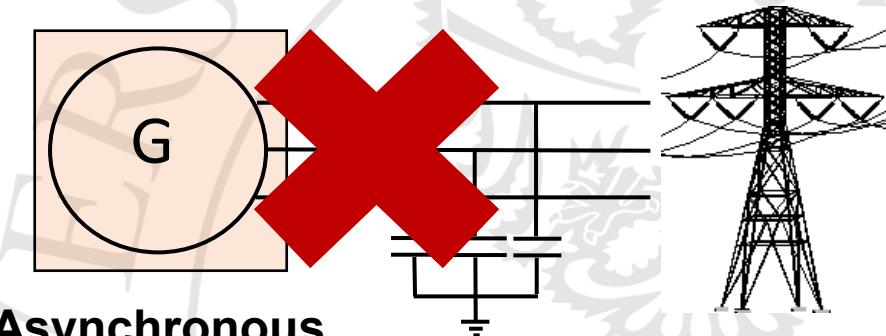
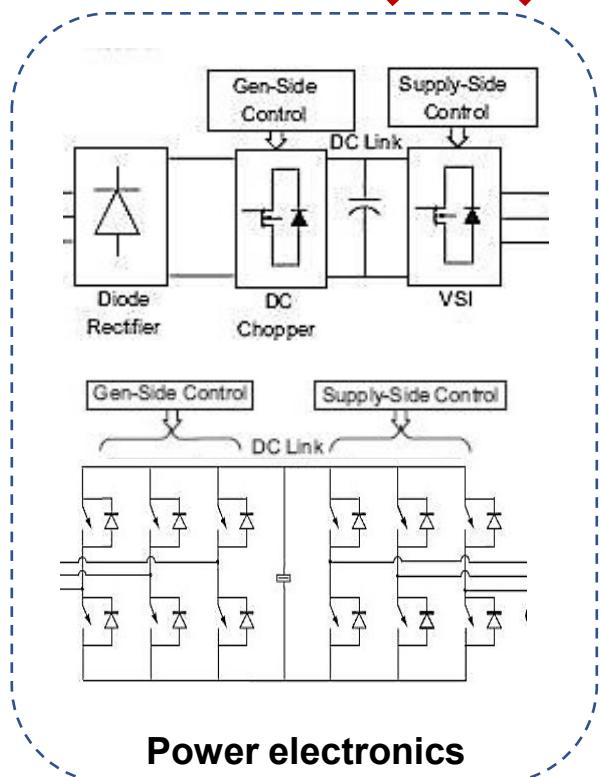
- The power electronic interface is used to properly control the electrical generator
- It is also used to regulate the power injection into the local power system



## Power electronics selection

**Direct connection to the grid**

**No power electronics interface**



Asynchronous  
machine

**Discouraged solution!**

**Diode rectifier +  
DC/DC converter +  
inverter**

**Controlled rectifier +  
inverter =  
Back-to-back converter**

**Selection of one  
or the other  
topology affects  
the degree of  
controllability  
of the system**

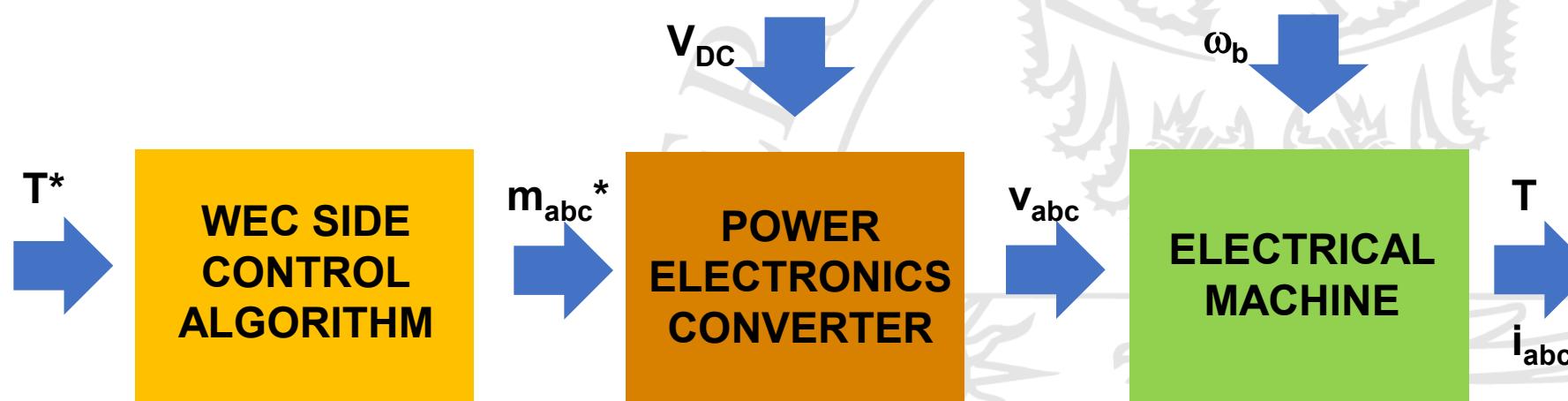
Similar to Type 1  
& Type 2 wind  
turbines

Similar to Type 4  
wind turbines



## Low level control of a WEC generator

The control force  $F_L$  is turned into a torque signal,  $T$ . In the case of rotating machines



Similar to low level control of a wind turbine

$T^*$ ,  $T$  = Torque reference, actual torque of the electrical machine

$m_{abc}^*$  = Switching signals for the power electronics converter ( $v_{abc}^* = V_{DC} * m_{abc}^*$ )

$V_{DC}$  = Voltage of the DC link

$V_{abc}$  = Voltages at the terminals of the electrical machine

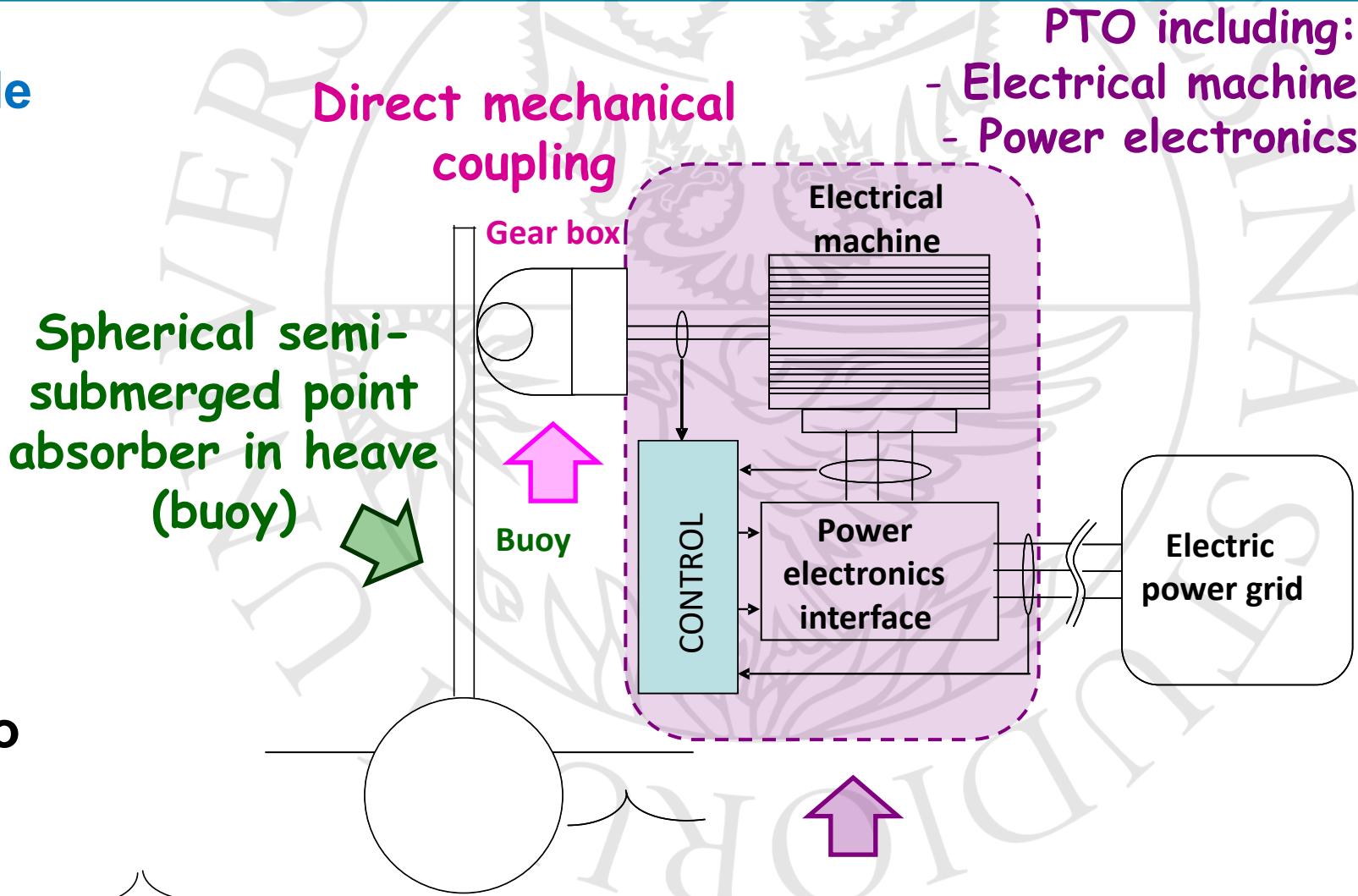
$\omega_b$  = Electric rotating speed of the electrical machine

$i_{abc}$  = Currents at the terminals of the electrical machine



## High level control of a WEC generator

- A key point is **how to provide the torque (or equivalently, force) reference** to the low-level controller to optimize the power extraction from the ocean waves
- Such task is accomplished by the high-level controller, whose operation can be better explained with reference to a simple (**point absorber**) system, subject to regular (**sinusoidal**) waves





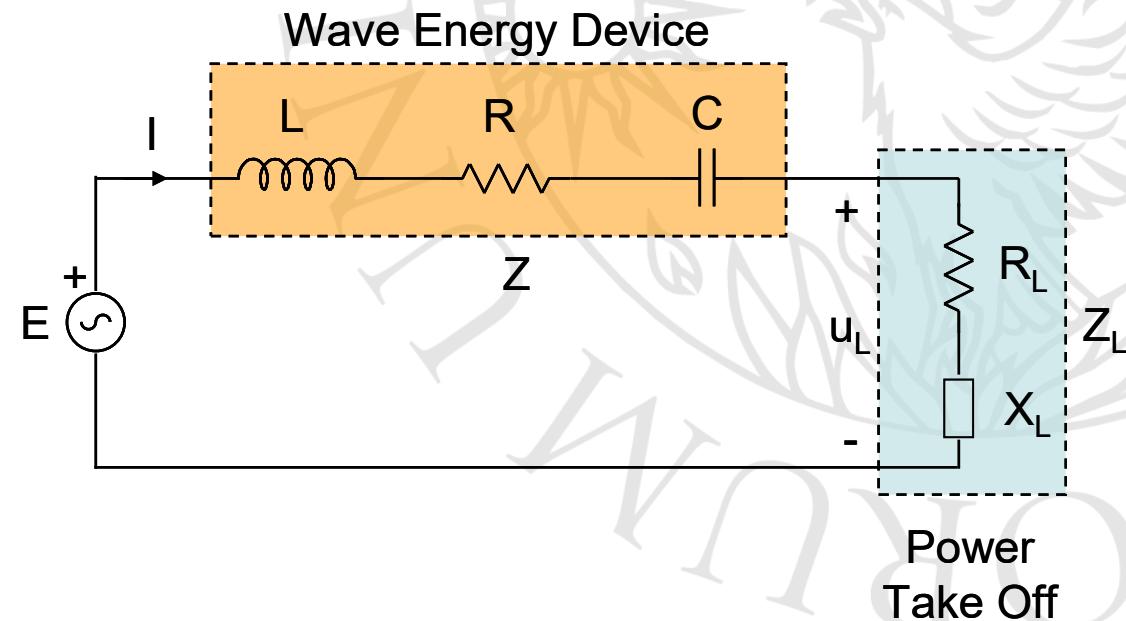
## Modeling of a point absorber WEC – frequency domain

**Assumption of sinusoidal (i.e. regular) waves, of angular freq.  $\omega$**

**Equation describing the buoy hydrodynamic model (mass-spring-damper system):**

$$-\omega^2(M + a(\omega))\hat{X} + j\omega B(\omega)\hat{X} + K\hat{X} = \hat{F}_E + \hat{F}_L$$

- $F_E$  = Excitation force
- $F_L$  = Control Force
- $M$  = Mass of the device
- $a$  = "Added mass"
- $B$  = Mechanical damping
- $K$  = Hydrostatic stiffness
- $X$  = position of the buoy

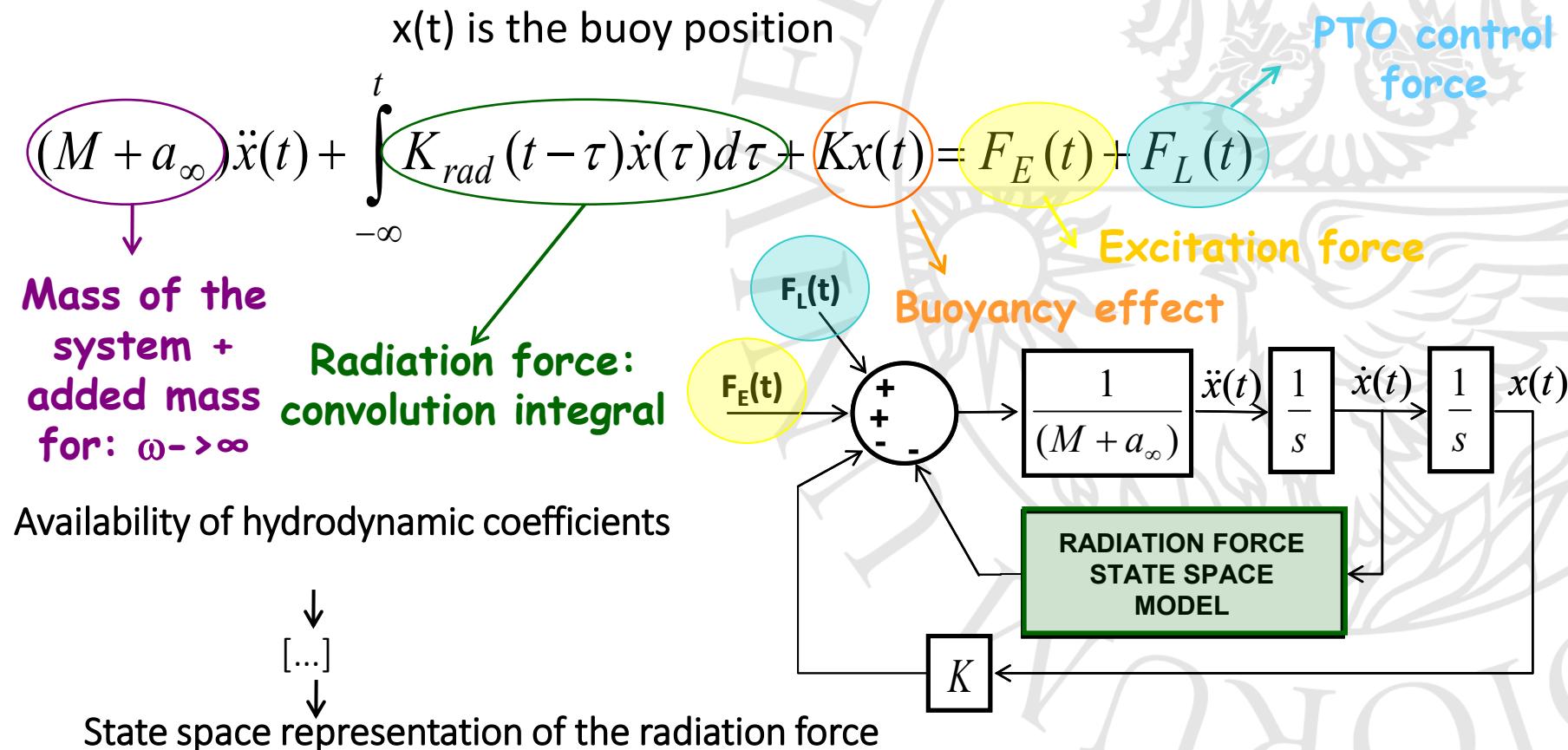


The «hat» sign indicates phasors



## Modeling of a point absorber WEC – time domain

**Cummins equation** to deal with irregular waves:



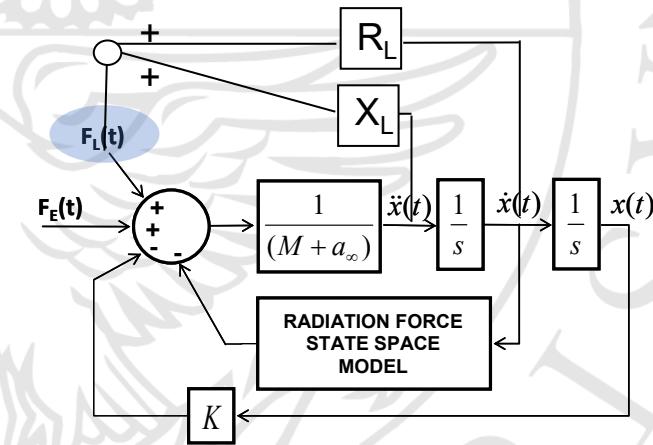


## High level control of a WEC generator

Most widespread **control techniques** are the **linear** ones, whose effect is well-established under sinusoidal conditions

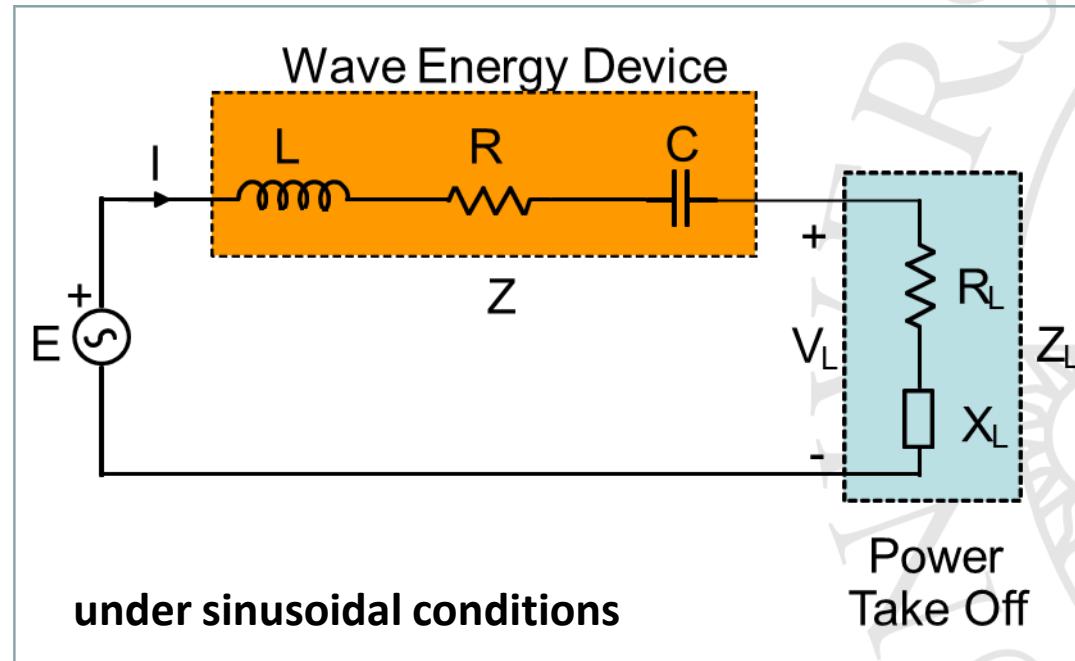
Passive loading: **force applied by to Power Take Off (PTO) is proportional to the buoy velocity**

Optimum (complex-conjugate/reactive) control:  
**force applied by the PTO has a component proportional to the buoy velocity and another to the buoy acceleration**





## High level control of a WEC generator



Mechanical-Electrical equivalence

Mechanical domain		Electrical domain	
Quantity	Symbol	Quantity	Symbol
Excitation force	$F_E$	Source voltage	$e$
Buoy velocity	$u$	Current	$i$
Buoy position	$x$	Charge	$q$
WEC total mass	$M+a$	Inductance	$L$
Spring constant	$K$	Capacitance <sup>-1</sup>	$C^{-1}$
Total buoy damping	$B$	Resistance	$R$
PTO force	$F_L$	Load voltage	$v_L$
PTO damping	$B_L$	Load resistance	$R_L$
PTO spring constant/PTO added mass	$K_L/\omega$ or $\omega M_L$	Load reactance	$X_L$

The control problem corresponds to the suitable tuning of "load" parameters:  $R_L$  and  $X_L$

Optimum control:  $R_L = R$     $X_L = \omega L_L - \frac{1}{\omega C_L} = -(\omega L - \frac{1}{\omega C})$     $F_L = -R_L \dot{x}(t) - L_L \ddot{x}(t) - \frac{1}{C_L} x(t)$

Passive loading:  $R_L = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$     $X_L = 0$     $F_L = -R_L \dot{x}(t)$



## High level control of a WEC generator

**The choice of the high-level control strategy has implications on the equipment required, in particular:**

- Optimum control produces a **bidirectional power flow**, between the point absorber and the grid, hence it requires a **reversible electrical machine** and (current-) **bidirectional power electronic converters**
- Passive loading produces a **unidirectional power flow**, so an electrical generator with unidirectional power electronics would be potentially sufficient, but it is **suboptimal** in terms of wave energy harvesting



## High level control of a WEC generator

**Under sinusoidal conditions (i.e., regular waves) it is possible to exactly define control parameters for the maximization of the average extracted power...**

**...Under irregular waves this is not trivial...**

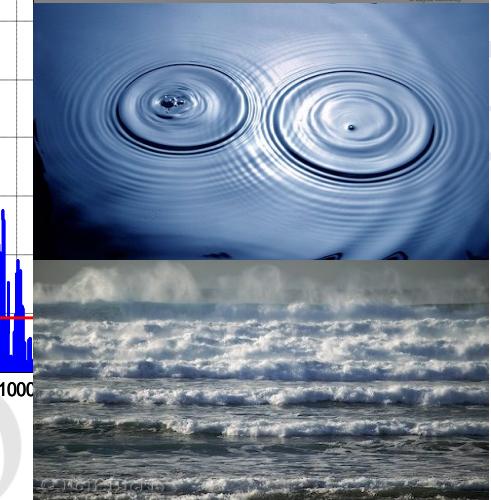
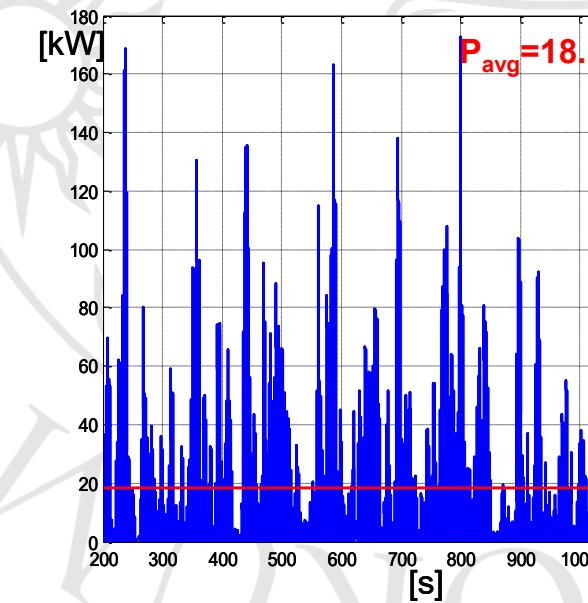
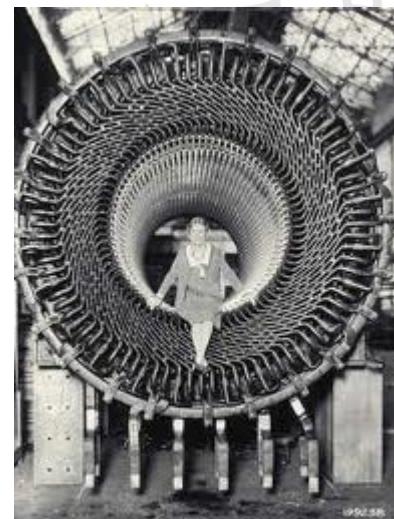
**...And in real seas this is even more difficult!**



## High level control of a WEC generator

### Main **problems** for control implementation:

- Very **intermittent** operation
- High **peak to average** extracted power
- **Oversized PTO**  
**required**





## Conclusions

- Wave energy has **enormous potential** that is still mostly **unexploited**
- **High concept diversification** (primary converter, PTO, etc.) has hampered the development of the wave energy industry
- **The PTO system** is still recognized as a **critical component** in the power conversion chain
- **Control is critical** to achieve high energy harvesting in compliance with equipment physical limits



## Lecture 13: Reference material

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- Michel, Walter H. "Sea spectra revisited." *Mar Technol* 36.4 (1999): 211-227.
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- European Commission, Offshore Renewable Energy Strategy, 19/11/2020
- H. Lendenmann *et al*, "Direct generation wave energy converters for optimized electrical power production" Proc. of the 7th European Wave and Tidal Energy Conference (EWTEC07), Porto, 11-13 September 2007