# Visual\_Inspection\_of\_Motorcycle\_Connecting\_Rods

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# 1 Visual Inspection of Motorcycle Connecting Rods

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Students should develop a software system aimed at visual inspection of motorcycle connecting rods. The system should be able to analyse the dimensions of two different types of connecting rods to allow a vision-guided robot to pick and sort rods based on their type and dimensions. The two rod types are characterized by a different number of holes: Type A rods have one hole whilst Type B rods have two holes.

```
[1]: import cv2
import numpy as np
import math
import matplotlib.pyplot as plt
from matplotlib.patches import Rectangle
%matplotlib inline
```

```
[2]: def path_to_dic(img_name_list, folder_path):
    image_dict = {}

    for img_name in img_name_list:
        img = cv2.imread(folder_path+img_name, cv2.IMREAD_GRAYSCALE)
        image_dict[img_name] = img

    return image_dict

def plot_figure_dict(img_dict):
    for k in img_dict:
        plt.title(k)
        plt.imshow(img_dict[k], cmap = 'gray')
        plt.show()

def plot_figures(img_list, title_img = 'fig -', cmap='viridis', figsize=(10,10)):
    plt.figure(figsize=figsize)
    for num, img in enumerate(img_list, start = 1):
```

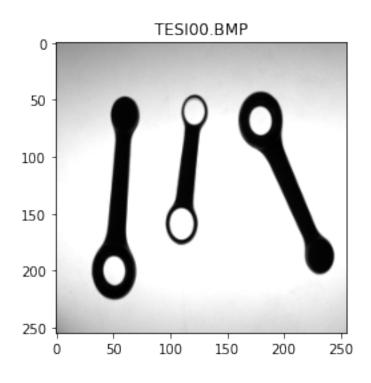
The images are loaded in two groupd per each task: \* A list of image paths \* A dictionary with the form of {"file name" : []}

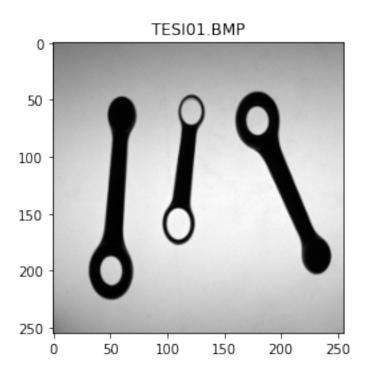
#### 4 First Task

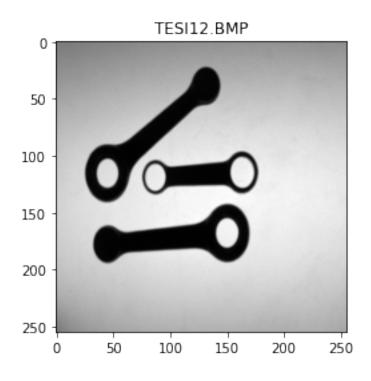
#### • Image characteristics

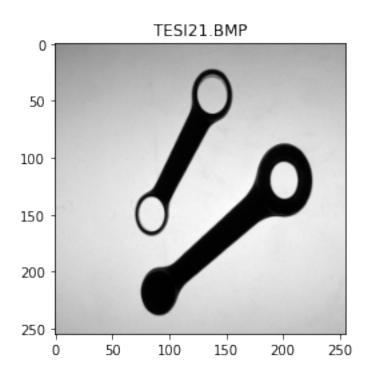
- 1. Images contain only connecting rods, which can be of both types and feature significantly diverse dimensions.
- 2. Connecting rods have been carefully placed within the inspection area so to appear well separated in images (i.e. they do not have any contact point).
- 3. Images have been taken by the backlighting technique so to render rods easily distinguishable (i.e. much darker) from background. However, for flexibility reasons the system should not require any change to work properly with lighting sources of different power.

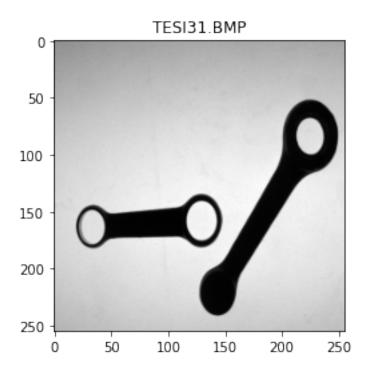
```
[4]: plot_figure_dict(first_task_img)
```

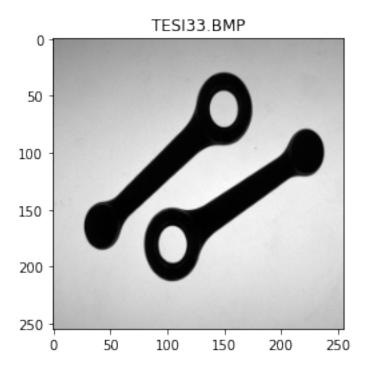












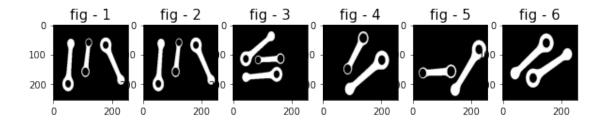
The following cell shows a function that separate the elements in a binary image. It returns a set of images, where in each of them there is only one element.

To achieve this result, it uses a built in OpenCV function called "connectedComponentsWith-Stats". This function computes the connected components of a binary image and produces a statistic output for each label.

```
[5]: def separate_rods(bin_image, connectivity = 4):
       Returns:
         - A set of image of each found element
         - A set of centroid of each found element
       _, label_image, stats, centroids = cv2.connectedComponentsWithStats(bin_image,_
      →connectivity, cv2.CV_32S)
       rod_idxs= np.unique(label_image)
       background_label = np.argmax(stats[:, 4]) # The background has the largest_
      \hookrightarrow label
       rod_labels = rod_idxs[rod_idxs != background_label] # remove the background
       rod_images = []
       rod_centroids = []
       for label in rod_labels:
         rod = label_image.copy()
         rod[label_image == label] = 255
         rod[label_image != label] = 0
         rod_images.append(rod)
         rod_centroids.append(centroids[label])
       return [rod_images, rod_centroids]
```

Image binarization is performed through **OTSU's algorithm**.

The idea behind this algorithm is to segment the image into two maximally homogeneous regions. From this situation, find the optimal threshold that minimizes the gray-level range. This process finds the within-group Variance, which measures the spread of the region intensities after the binarization.

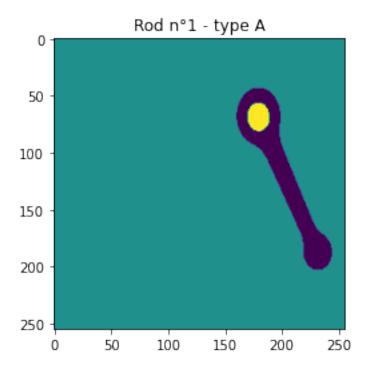


### 4.1 1.1. Type of rod

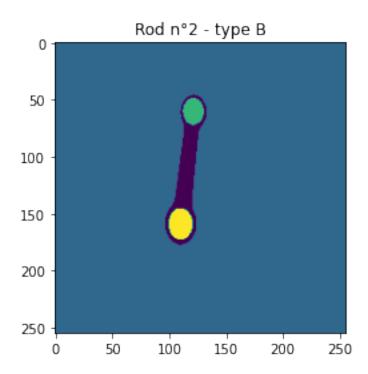
The type of rod represents the number of holes. A rod is typed A if it has 1 hole, type B if it has 2 holes. To compute the number of rods it is possible to perform **second labelling** for each rod image. From the resulting labelling, it is possible to remove the background and the rod itself. From this, we can count the remaining labels. If one label is left, then the rod is type A, if two labels are left, then the rod is type B.

```
[7]: def get_type_from_list(rod_list, connectivity = 4, plot_rod_type = True,_
      →print_rod_type = True):
       n n n
       Input:
        - list of binary images having just one rod each
       Output:
        - Dictionary with {"rod number" : "rod type"}
       type_dict = {}
       for n, rod in enumerate(rod_list):
         holes_rod = np.array(255-rod, dtype=np.uint8)
         _, holes_rod_labelled, _, _ = cv2.connectedComponentsWithStats(holes_rod,_
      ⇒connectivity, cv2.CV_32S)
         n_holes = len(np.unique(holes_rod_labelled)) - 2 # remove background and the_
      \rightarrow rod\ itself
         final_type = "A" if n_holes == 1 else "B" if n_holes == 2 else "NA"
         if plot_rod_type:
           plt.figure()
           plt.title(f"Rod n°{n+1} - type {final_type}")
           plt.imshow(holes_rod_labelled)
           plt.show()
         if print_rod_type:
           print(f"Rod n°{n+1} - type {final_type}")
         type_dict[n+1] = final_type
```

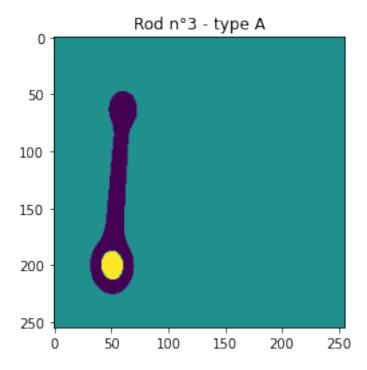
return type\_dict



Rod n°1 - type A



Rod n°2 - type B



```
Rod n°3 - type A
[8]: {1: 'A', 2: 'B', 3: 'A'}
```

#### 4.2 1.2. Position and orientation (module $\pi$ )

The position of the rod is given by its centroid. The centroid can be easily found using the default OpenCV function "connectedComponentsWithStats".

To compute the rod orientation, it is necessary to use the covariance matrix of the image. To derivate the covariance matrix, it is required to use the central moment: - The central moment is given by:

$$\mu_{pq} = \sum_{x} \sum_{y} (x - \bar{x})^{p} (y - \bar{y})^{q} f(x, y)$$

Where  $\bar{x}$ ,  $\bar{y}$  are the centroids, f(x, y) the digital image.

• The covariance matrix of the image I(x, y) is given by:

$$cov[I(x,y)] = \begin{pmatrix} \sigma_{ii} & \sigma_{ij} \\ \sigma_{ij} & \sigma_{ii} \end{pmatrix}$$

• Where  $\sigma^2$  is given by:

$$\sigma_{ii} = \mu_{2,0}/A$$

$$\sigma_{ij} = \mu_{1,1}/A$$

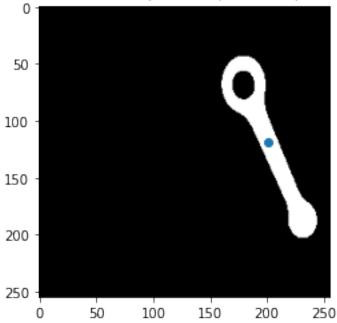
$$\sigma_{ij} = \mu_{0,2}/A$$

```
returns:
          - Return a couple of dictionaries
             - pos_dict = {"rod number" : rod's centroid}
             - ori_dict = {"rod number" : rod's orientation}
        pos_dict = {}
        ori_dict = {}
        for n, (rod, centroid) in enumerate(zip(rod_list, centroid_list)):
          # compute the orientation of the rod
          cov_matrix = covariance_matrix(rod, centroid)
          theta = -0.5 * math.atan2((2 * cov_matrix[0, 1]), (cov_matrix[0, 0] - 0))
       \rightarrowcov_matrix[1, 1]))
          orient = math.degrees(theta)
          # prepare the dictionary to retrun
          pos_dict[n+1] = centroid # passed in input
          ori dict[n+1] = orient
        if is_plot :
          for n, rod in enumerate(rod_list):
            plt.figure()
            plt.title(f"Rod n°{n+1}\n - orientation: {round(ori_dict[n+1],5)}°\n -___
       \rightarrowcenter: ({round(pos_dict[n+1][0], 3)}, {round(pos_dict[n+1][1], 3)})")
            position = pos_dict[n+1]
            plt.plot(position[0], position[1], 'o')
            plt.imshow(rod, cmap='gray')
            plt.show()
        return [pos_dict, ori_dict]
[11]: rod_imgs, centroids = separate_rods(bin_images[0])
      pos_dict, ori_dict = position_and_orientation(rod_imgs, centroids) # compute_u
       \rightarrow position and orientation
      # for n, rod in enumerate(rod_imgs):
            plt.figure()
            plt.title(f"Rod n°{n+1}\n - orientation: {round(ori_dict[n+1],5)})^{\circ}n - 
       \rightarrowcenter: (\{round(pos\_dict[n+1][0], 3)\}, \{round(pos\_dict[n+1][1], 3)\})")
```

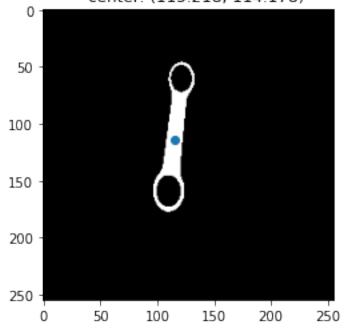
plt.imshow(rod, cmap='gray')
position = pos\_dict[n+1]

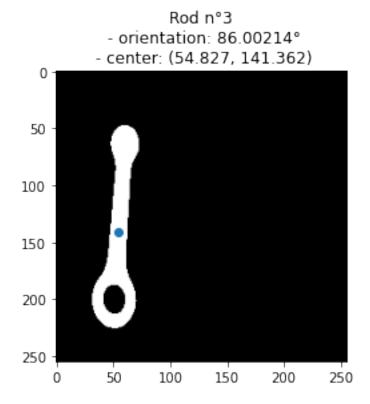
plt.plot(position[0], position[1], 'o')

Rod n°1 - orientation: -66.8066° - center: (201.386, 119.119)



Rod n°2 - orientation: 83.50936° - center: (115.218, 114.178)





### **4.3 1.3.** Length (*L*), Width (*W*), Width at the barycenter ( $W_B$ ).

Using the **covariance matrix** from the previous section, we can compute the major and th minor axes of each rod. Indeed, the largest and the smallest eigenvalue of the covariance matrix define the major and minor axes respectively. Using the equation of the major and minor axes, it is possible to compute the **Minimum Enclosing Rectanagle** (MER) of each rod.

Two axes intersect at the barycenter of the rod. It is possible to use one of them to determine the other one and viceversa. The axes are defined as follows:

$$major\_axis: \alpha x - \beta y - \alpha c_0 + \beta c_1$$

$$minor\_axis: \beta x - \alpha y - \beta c_0 - \alpha c_1$$

Where  $\alpha$  and  $\beta$  are the eigenvalues of the major and minor axes,  $c_0$  and  $c_1$  are the rod centroids.

The algorithm consists of computing the MER by finding the intersection between the lines parallel to the major and minor axes. Hence, for each pixel that composes the single rod, we compute the distance from the major and minor axis. In this way we can find the point where the parallel axis should pass by. Once the four axis are found, the vertexes of the MER are the intersection of these lines.

The **width at the barycenter** is found by computing the distance of the point close to the minor axes, hence to the barycenter

```
[12]: def contact_points(img_bin, major_equation, minor_equation):
          Inputs:
              - imq_bin: binary image
              - major_equation: numpy array 3x1 representing the major axis equation
              - minor_equation: numpy array 3x1 representing the minor axis equation
          Outputs:
          Returns the contact points between major and minor axes and the contour of ...
       \hookrightarrow the object
          and measure the width at the barycenter
              - maj_a1: on major axis, negative maximum
              - maj_a2: on major axis, positive maximum
              - min_a1: on minor axis, negative maximum
              - min_a2: on minor axis, positive maximum
              barycenter - the width at the barycenter (along the minor axis)
           111
          # initialize variables
          min_major_distance = math.inf
          max_major_distance = -math.inf
          min_minor_distance = math.inf
          max_minor_distance = -math.inf
          maj_a1 = None
          mai_a2 = None
          min_a1 = None
          min_a2 = None
          min_barycenter_distance = math.inf
          max_barycenter_distance = -math.inf
          # for each point in the image,
          # if the columns move --> change in the horizontal coordinate and vice versa
          for y in range(img_bin.shape[0]):
              for x in range(img_bin.shape[1]):
                  if img_bin[y,x] == 255:
                       # distance from the major axis as distance of a point to a line
                      major_distance = (major_equation[1] * y + major_equation[0] * x__
       → + major_equation[2]) / math.sqrt((major_equation[0] ** 2) + (major_equation[1]
       →** 2))
                      # distance from the minor axis as distance of a point to a line
                      minor_distance = (minor_equation[1] * y + minor_equation[0] * x_{\sqcup})
       → minor_equation[2]) / math.sqrt((minor_equation[0] ** 2) + (minor_equation[1]
       →** 2))
                       # update contact points searching for extreme in both horizontal
       \rightarrowand vertical axes
```

```
if major_distance < min_major_distance:</pre>
                   min_major_distance = major_distance
                   maj_a1 = [x, y]
                if major_distance > max_major_distance:
                   max_major_distance = major_distance
                   maj_a2 = [x, y]
                if minor_distance < min_minor_distance:</pre>
                   min_minor_distance = minor_distance
                   min_a1 = [x, y]
                if minor_distance > max_minor_distance:
                   max_minor_distance = minor_distance
                   min_a2 = [x, y]
                # if the point is close to the minor axes then it is considered.
 →in computing the width at the barycenter
               if abs(minor_distance) < 0.75:
                    # the distances are computed on both directions and summed,
 →to obtain the final value
                   if major_distance < min_barycenter_distance:</pre>
                       min_barycenter_distance = major_distance
                    if major_distance > max_barycenter_distance:
                       max_barycenter_distance = major_distance
   return maj_a1, maj_a2, min_a1, min_a2, abs(min_barycenter_distance) +u
 →abs(max_barycenter_distance)
def line_intersection(p1, p2, m1, m2):
    ''' Intersect 2 lines given 2 points and the associated slopes
   Input:
        - p1: (x,y) first line's first point
        - p2: (x,y) second line's first point
       - m1: slope of first line
        - m2: slope of second line
   Output:
       - res: an array containing the intersection point of the two lines if_{\sqcup}
 \rightarrow exists, np.nan otherwise
    111
   if p1 is None or p2 is None or m1 is None or m2 is None:
       raise ValueError("Argument error")
    \rightarrow intersection if there is
   a = np.array([[-m1, 1], [-m2, 1]])
   b = np.array([p1[1] - m1 * p1[0], p2[1] - m2 * p2[0]])
   try:
       res = np.linalg.solve(a, b)
   except:
       res = np.array([np.nan, np.nan])
```

```
return res
```

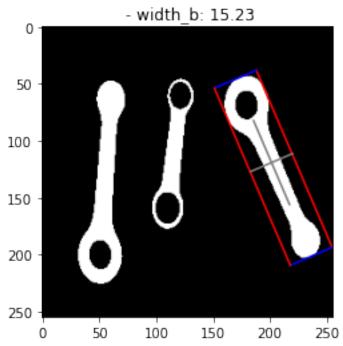
```
[13]: def get_sizes(img_bin, rod_list, centroid_list, sizes_round = 2, scale = 20, __
       →is_plot = True) :
        111
        Input:
         - img_bin: binary image used to plot the result
         - rod_list: list of binary images having just one rod each
         - sizes_round: result precision
         - scale: dimension of the axis in the plot
        Output:
         - sizes: A dictionary of the requested sizes for each rod
                  {rod's number : (Length, Width, Width_b)}
        sizes = {} # {label : (Length, Width, Width_b)}
        for n, (rod, centroid) in enumerate(zip(rod_list, centroid_list), start=1):
          # use covariance matrix to find major and minor axes
          cov_matrix = covariance_matrix(rod, centroid)
          # cov = covariance_matrix(rod_image, rods[-1]["centroid"])
          eigenvalues, eigenvectors = np.linalg.eig(cov_matrix)
          sort_indices = np.argsort(eigenvalues)[::-1]
          major_axes = eigenvectors[:, sort_indices[0]]
          minor_axes = eigenvectors[:, sort_indices[1]]
          alpha = major_axes[1]
          beta = major_axes[0]
          # store major and minor equations
          major_equation = [alpha, - beta, beta * centroid[1] - alpha * centroid[0]]
          minor_equation = [beta, alpha, - beta * centroid[0] - alpha * centroid[1]]
          # find contact points and width at the barycenter
          maj_a1, maj_a2, min_a1, min_a2, barycenter_width = contact_points(rod, __
       →major_equation, minor_equation)
          width_b = round(barycenter_width, sizes_round)
          # compute MER vertices
          v1 = line_intersection(maj_a1, min_a1, -major_equation[0] /__
       →major_equation[1], -minor_equation[0] / minor_equation[1])
          v2 = line_intersection(maj_a1, min_a2, -major_equation[0] /___
       →major_equation[1], -minor_equation[0] / minor_equation[1])
          v3 = line_intersection(maj_a2, min_a1, -major_equation[0] /__
       →major_equation[1], -minor_equation[0] / minor_equation[1])
          v4 = line_intersection(maj_a2, min_a2, -major_equation[0] /_
       →major_equation[1], -minor_equation[0] / minor_equation[1])
```

```
# measure length and width
  length = round(math.sqrt(((v1[0] - v2[0])**2) + ((v1[1] - v2[1])**2)),
→sizes_round)
  width = round(math.sqrt(((v1[0] - v3[0])**2) + ((v1[1] - v3[1])**2)),
→sizes_round)
  # result
  sizes[n] = (length, width, width_b)
  if is_plot :
    # MER
    plt.plot([v1[0], v2[0]], [v1[1], v2[1]], color="red")
    plt.plot([v2[0], v4[0]], [v2[1], v4[1]], color="blue")
    plt.plot([v3[0], v1[0]], [v3[1], v1[1]], color="blue")
    plt.plot([v4[0], v3[0]], [v4[1], v3[1]], color="red")
    # Major and minor axes
    plt.plot([major_axes[0] * - scale * 2 + centroid[0], major_axes[0] * scale_
\rightarrow* 2 + centroid[0]],
     [major_axes[1] * - scale * 2 + centroid[1], major_axes[1] * scale * 2 + _{\sqcup}
plt.plot([minor_axes[0] * - scale + centroid[0], minor_axes[0] * scale +

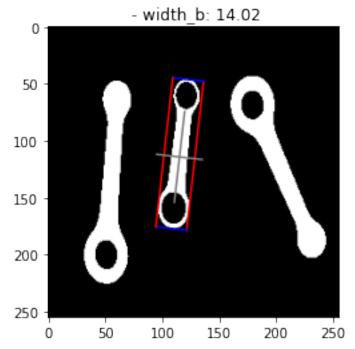
→centroid[0]],
     [minor_axes[1] * - scale + centroid[1], minor_axes[1] * scale +__
→centroid[1]], color='gray')
    plt.title(f"Rod {n} - MER\n - length: {sizes[n][0]}\n - width:
\rightarrow{sizes[n][1]}\n - width_b: {sizes[n][2]}")
    plt.imshow(img_bin, cmap='gray')
    plt.show()
return sizes
```

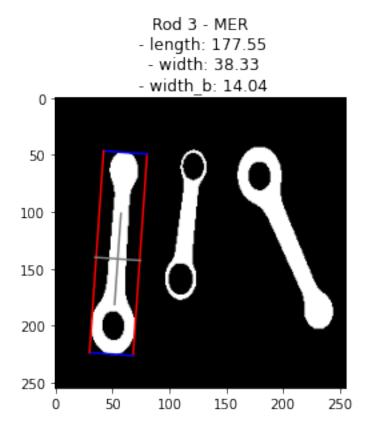
```
[14]: rod_imgs, centroids = separate_rods(bin_images[0])
sizes = get_sizes(bin_images[0], rod_imgs, centroids)
```

Rod 1 - MER - length: 169.25 - width: 40.05



Rod 2 - MER - length: 131.74 - width: 27.19





### 4.4 1.4. For each hole, position of the centre and diameter size

The "connectedComponentsWithStats" function gives all the items to obtain the information we need. Starting from the information generated by the function we exclude those related to the background and the rods them selfes.

```
[15]: def get_holes_centre_diam(rod_list, connectivity = 4, is_plot = True):

'''

Input:

- rod_list: a list binary images of each single rod

Output:

- dict_centres_diameters: a dictionary that stores the information of the rods as follow

{rod number : [[hole centres coord (x, y)], the dict_centres_diameters = {} # {label : [(x,y), (stats)]}

for n, rod in enumerate(rod_list, start = 1):

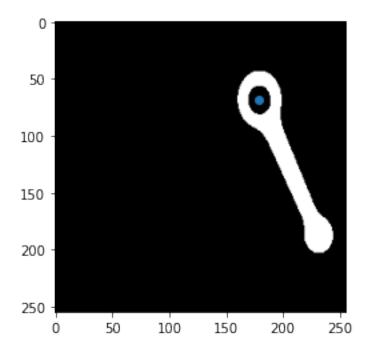
holes_image = np.array(255 - rod, dtype = np.uint8)

_, holes_labelled, holes_stats, holes_centroid = \
```

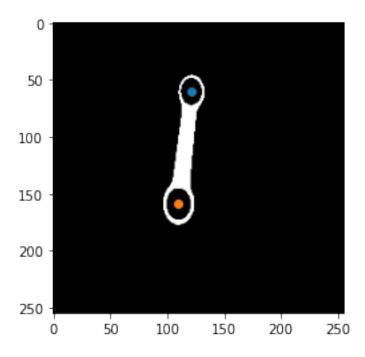
```
cv2.connectedComponentsWithStats(holes_image, cv2.CV_32S,_
→connectivity) # obtain the label of the holes for each rod
       background_rods = (
           np.argsort(
               holes_stats[:, 4]
           )[::-1]
       )[0:2]
       final_holes = set(np.unique(holes_labelled)) - set(background_rods) #__
→remove the background and rod from the labelled image
       centres = []
       diamenters = []
       for hole_label in final_holes:
           # compute center and diameter for each hole in rod n
           center = holes_centroid[hole_label]
           radius = holes_stats[hole_label, 4] / math.pi
           diameter = math.sqrt(radius * 2)
           centres.append(center)
           diamenters.append(diameter)
       dict_centres_diameters[n] = [centres, diamenters]
       if is_plot :
           plt.figure()
           title = f"Rod n°{n}\n"
           for k in range(len(dict_centres_diameters[n][1])):
               cntr_x = round(dict_centres_diameters[n][0][k][0], 3)
               cntr_y = round(dict_centres_diameters[n][0][k][1], 3)
                    = round(dict_centres_diameters[n][1][k],5)
               title += f'' - hole \{k+1\} diameter: \{dia\}\setminus n - hole \{k+1\} center:
\rightarrow ({cntr_x}, {cntr_y})\n"
               plt.plot(cntr_x, cntr_y, 'o')
           plt.title(title)
           plt.imshow(rod, cmap='gray')
   return dict_centres_diameters
```

```
[16]: centers_diameter = get_holes_centre_diam(rod_imgs)
```

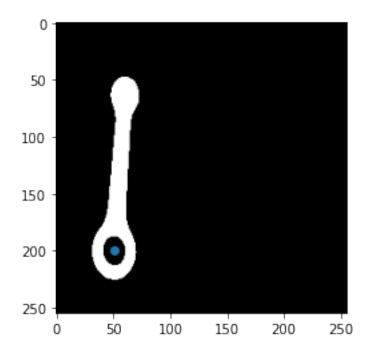
Rod n°1 - hole 1 diameter: 15.67594 - hole 1 center: (179.008, 68.756)



Rod n°2
- hole 1 diameter: 14.75547
- hole 1 center: (121.143, 60.351)
- hole 2 diameter: 17.14988
- hole 2 center: (109.957, 158.972)



Rod n°3 - hole 1 diameter: 15.67594 - hole 1 center: (50.966, 199.933)



#### 4.4.1 Conclusion task 1

The cells below show how the functions explained above are used all at once. For each binary image, the functions computes the algorithms in the following order: - separate\_rods to obtain the rods that compose the image - get\_type\_from\_list to get the type of each rod - position\_and\_orientation to find the center and orientation of each rod - get\_sizes to get the size of each rod - get\_holes\_centre\_diam to get the info regarding the holes in the rod

```
[17]: def compile_all(bin_image):
    print("____" * 20)
    rod_imgs, centroids = separate_rods(bin_image)
    get_type_from_list(rod_imgs, plot_rod_type = False)
    position_and_orientation(rod_imgs, centroids)

    get_sizes(bin_image, rod_imgs, centroids)
    get_holes_centre_diam(rod_imgs)
```

```
[18]: bin_images = []
for k in first_task_img:
```

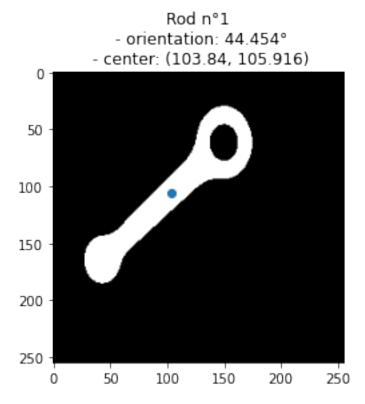
```
_, bin_image = cv2.threshold(first_task_img[k], 0, 255, cv2.THRESH_BINARY_INV_

\( \text{st} + cv2.THRESH_OTSU) \)
bin_images.append(bin_image)

compile_all(bin_images[5])
```

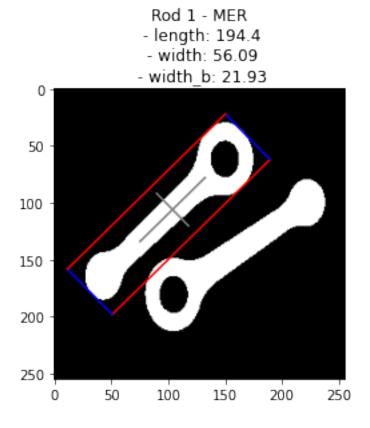
-----

Rod n°1 - type A Rod n°2 - type A

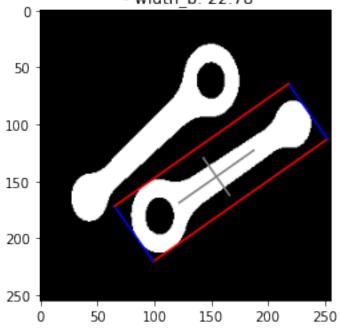


Rod n°2
- orientation: 35.09298°
- center: (154.696, 145.909)

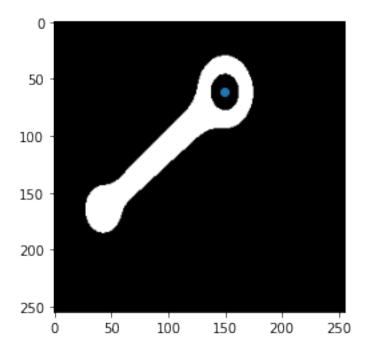
50 
100 
250 
50 
100 
250 
50 
100 150 200 250



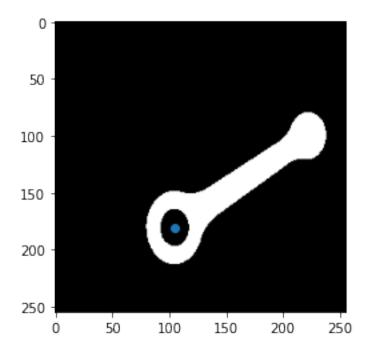
Rod 2 - MER - length: 186.97 - width: 59.37 - width\_b: 22.78



Rod n°1 - hole 1 diameter: 19.81904 - hole 1 center: (149.575, 61.737)



Rod n°2 - hole 1 diameter: 20.12188 - hole 1 center: (104.761, 180.445)



### 5 2. Second Task

While still meeting the requirement of the First Task, students should modify the system in order to deal with one (or more) of the following three changes in the characteristics of the working images:

The following function perform a mean filter over an image. It is used by both sub-task solutions.

```
[19]: def mean_filter_preprocessing(image, size=3, iterations=5):
    prepr_image = image.copy()
    for i in range(0, iterations):
        prepr_image = cv2.medianBlur(prepr_image, size)
    return prepr_image
```

#### 5.1 2.1

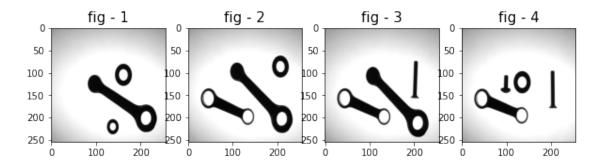
1. Images may contain other objects (i.e. screws and washers) that need not to be analysed by the system (such kind of objects are often referred to in computer vision as "distractors").

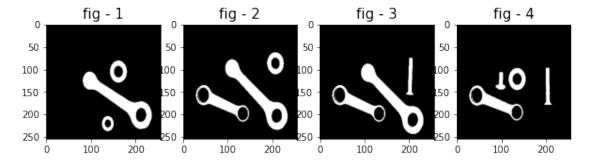
This task could be solved using the get\_type\_from\_list function explained in the first task. Indeed, this function finds if an element has one or two rods; hence, if it has **zero holes**, that element could be classified as a **screw**. Eventually, the washers may result in rods of type A since they have

one hole. We can overcome this problem by considering a washer as a **circle**. Hence, computing the difference between the element **width** and\*\* width at the barycenter\*\* they result to be similar. This characteristic may be considered to remove the element.

Another technique is to use Haralick's circularity.

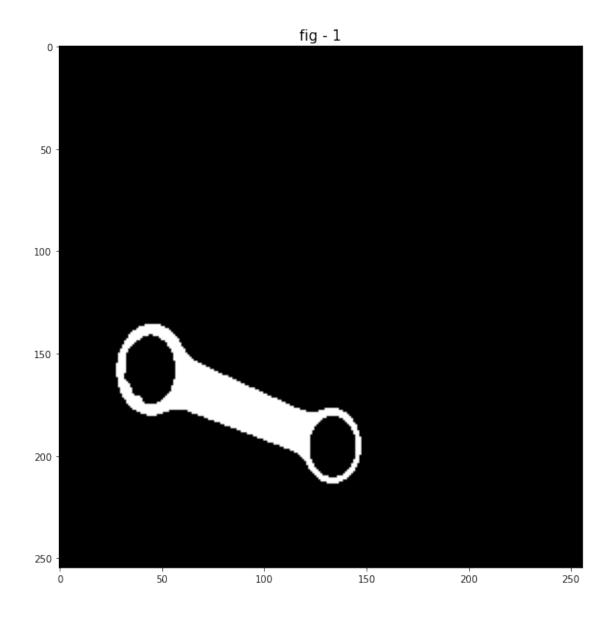
```
[20]: plot_figures(second_task_1_img.values(), cmap='gray')
```





```
[23]: filtered_img = separate_rods_by_type(mean_filter_preprocessing(bin_images[3]))

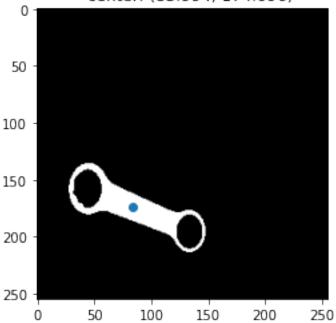
plot_figures([filtered_img], cmap='gray')
```



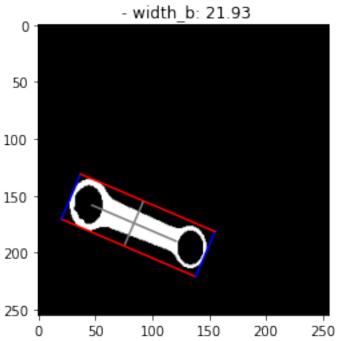


Rod n°1 - type B

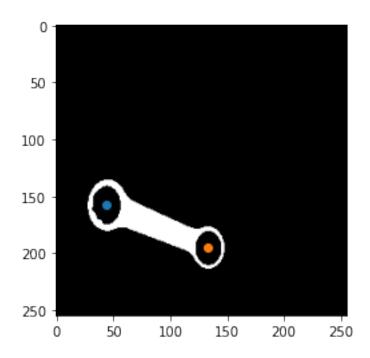
Rod n°1 - orientation: -23.17512° - center: (83.994, 174.096)



Rod 1 - MER - length: 128.42 - width: 43.07



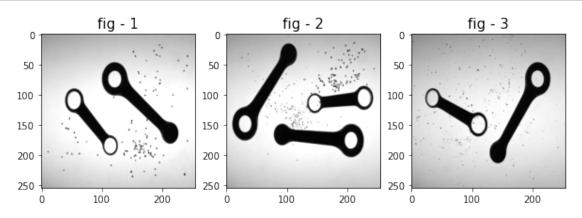
Rod n°1
- hole 1 diameter: 20.09022
- hole 1 center: (44.377, 157.55)
- hole 2 diameter: 18.36868
- hole 2 center: (133.5, 195.445)



# 5.2 2.3.

3. The inspection area may be dirty due to the presence of scattered iron powder.

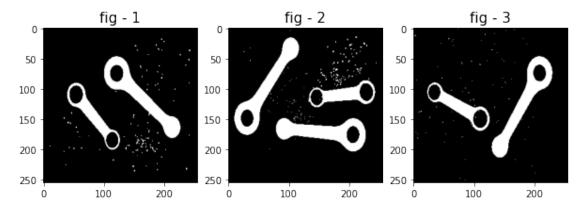




```
[26]: bin_images = []

for k in second_task_3_img:
    _, bin_image = cv2.threshold(second_task_3_img[k], 0, 255, cv2.
    _THRESH_BINARY_INV + cv2.THRESH_OTSU)
    bin_images.append(bin_image)

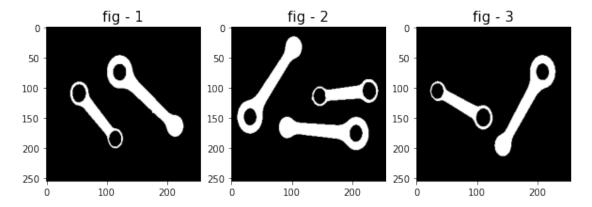
plot_figures(bin_images, cmap='gray')
```



A **mean filter** on the image is a robust technique to solve the problem. below are shown the results of this method that are effective

```
[27]: t2_filtered_imgs = []
for bin_img in bin_images:
    filtered_img = mean_filter_preprocessing(bin_img)
    t2_filtered_imgs.append(filtered_img)

plot_figures(t2_filtered_imgs, cmap='gray')
```



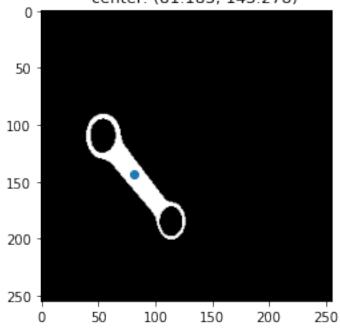
# [28]: compile\_all(t2\_filtered\_imgs[0])

Rod n°1 - type A Rod n°2 - type B

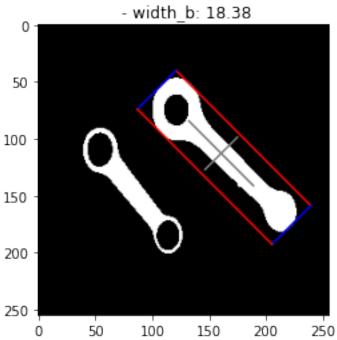
Rod n°1 - orientation: -45.08588° - center: (160.649, 112.791) 0 50 -100 -150 -200 -250 150 200 50 100

250

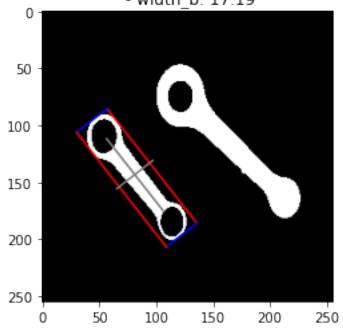
Rod n°2 - orientation: -51.90511° - center: (81.183, 143.278)



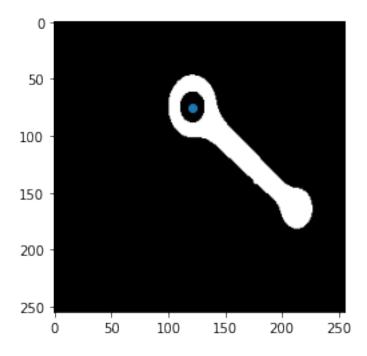
Rod 1 - MER - length: 167.6 - width: 48.08



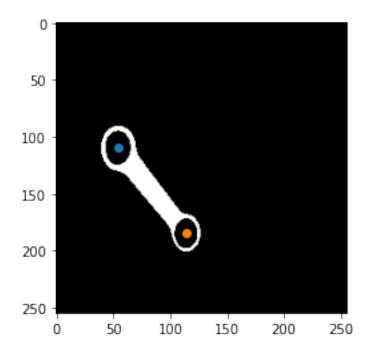
Rod 2 - MER - length: 127.84 - width: 33.97 - width\_b: 17.19



Rod n°1 - hole 1 diameter: 17.22396 - hole 1 center: (121.105, 74.858)



Rod n°2
- hole 1 diameter: 18.15954
- hole 1 center: (54.197, 109.674)
- hole 2 diameter: 16.15593
- hole 2 center: (113.793, 184.676)



### 5.3 2.2.

# 2. Rods can have contact points but do not overlap one to another.

no effective solution has been found for problem number 2.2. Some morphological operations have been tried, but none allowed to separate the rods without ruining their integrity.