GaussianCoulomb[x, y, sigx, sigy] returns the electromagnetic force $f_x + if_y$ at the coordinates (x, y), generate with sizes (sigx,sigy)= (σ_x, σ_y) . Its derivative at the origin is

$$\frac{\partial f_x}{\partial x} = -2 \frac{x}{\sigma_x (\sigma_x + \sigma_y)},$$
$$\frac{\partial f_y}{\partial y} = -2 \frac{y}{\sigma_y (\sigma_x + \sigma_y)}.$$

$$\frac{\partial f_y}{\partial y} = -2 \frac{y}{\sigma_y(\sigma_x + \sigma_y)}$$
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