$\mathbf{R} = \begin{pmatrix} \mu \mathbf{I} & \mathbf{J} \mathbf{r}^T \mathbf{J} \\ \mathbf{r} & \mu \mathbf{I} \end{pmatrix} = \begin{pmatrix} \mu & . & -\mathbf{R}\mathbf{T} & \mathbf{R}\mathbf{Z} \\ . & \mu & \mathbf{R}\mathbf{3} & -\mathbf{R}\mathbf{1} \\ \mathbf{R}\mathbf{1} & \mathbf{R}\mathbf{2} & \mu & . \\ \mathbf{R}\mathbf{2} & \mathbf{R}\mathbf{4} & . \end{pmatrix}$ with a submatrix $r = \begin{pmatrix} R1 & R2 \\ R3 & R4 \end{pmatrix},$

The transformation matrix from the physical coordinate (x, p_x, y, p_y) to the x-y decoupled coordinate (X, P_X, Y, P_Y) is

$$\mu^{2} + \det(\mathbf{r}) = 1,$$

$$\mathbf{I} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix},$$

$$\mathbf{J} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}.$$

as

where

The inverse of R is obtained by reversing the sign of r:

$$R^{-1} = \begin{pmatrix} \mu I & -Jr^{T}J \\ -r & \mu I \end{pmatrix} = \begin{pmatrix} \mu & . & R4 & -R2 \\ . & \mu & -R3 & R1 \\ -R1 & -R2 & \mu & . \\ -R3 & -R4 & . & \mu \end{pmatrix}$$

The value of the function DETR is equal to det(r) in this case.

 $R_2TR_1^{-1} = \begin{pmatrix} T_X & 0 \\ 0 & T_Y \end{pmatrix}$.

The Twiss parameters are defined for the 2 by 2 matrices T_X and T_Y .

If $det(r) \ge 1$, the above condition for μ is violated. In such a case, an alternative form of R is used:

 $R = \begin{pmatrix} Jr^T J & \mu I \\ \mu I & r \end{pmatrix},$ where $\mu^2 + \det(\mathbf{r}) = 1$. The function DETR shows a number $a - \det(\mathbf{r})$, where a = 1.375. thus the alternative form is used

Let T stand for the physical transfer matrix from location 1 to location 2, then the transformation in the decoupled coor