

# Second Assignment

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# 1 Very Busy Expressions

The search for very busy expressions can be useful for code hoisting, since very busy expressions can be moved from the place they are up to a joint point from which the flow departs.

## 1.1 Problem formalization

Formally an expression is said to be **very busy** when it is computed along each path that part from the point  $p$  without any redefinition of its operands. This information can be used to move the expression to a point of the code in which its computation can be used by all the paths that use the expression.

	<b>Very Busy Expressions</b>
Domain	Sets of expressions
Direction	Backward $in[b] = f_b(out[b])$ $out[b] = \wedge in[succ(b)]$
Transfer function	$f_b(x) = Gen_b \cup (x - Kill_b)$
Meet Operation ( $\wedge$ )	$\cap$
Boundary Condition	$out[exit] = \emptyset$
Initial interior points	$out[b] = U$

Table 1: Very busy expressions summary table

## 1.2 Example

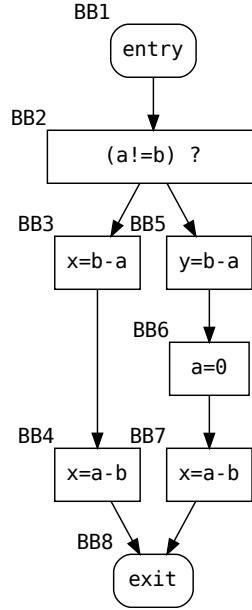


Figure 1: Very Busy Expression Example

	Iteration 1		Iteration 2	
	IN[B]	OUT[B]	IN[B]	OUT[B]
<b>BB1</b>	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$
<b>BB2</b>	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$	$\{b - a\}$
<b>BB3</b>	$\{b - a\}, \{a - b\}$	$\{a - b\}$	$\{b - a\}, \{a - b\}$	$\{a - b\}$
<b>BB4</b>	$\{a - b\}$	$\emptyset$	$\{a - b\}$	$\emptyset$
<b>BB5</b>	$\{b - a\}$	$\emptyset$	$\{b - a\}$	$\emptyset$
<b>BB6</b>	$\emptyset$	$\{a - b\}$	$\emptyset$	$\{a - b\}$
<b>BB7</b>	$\{a - b\}$	$\emptyset$	$\{a - b\}$	$\emptyset$
<b>BB8</b>	$\emptyset$	$\emptyset$	$\emptyset$	$\emptyset$

Table 2: Very Busy Expression Algorithm Execution Table

## 2 Dominator Analysis

Dominator analysis is fundamental to create the single static assignment form.

## 2.1 Problem formalization

A basic block  $B_1$  **dominates** another block  $B_2$  if it is encountered in every path from entry to  $B_2$ .

	<b>Dominator Analysis</b>
Domain	Sets of Basic Blocks
Direction	Forward
Transfer function	$f_b(x) = \{x\} \cup (\bigcap_{m \in \text{preds}(x)} f_b(m))$
Meet Operation ( $\wedge$ )	$\cap$
Boundary Condition	$\text{Dom}[\text{entry}] = \{\text{entry}\}$
Initial interior points	$\text{Dom}[b] = N \quad \forall b \neq \text{entry}$ , with $N$ the number of basic blocks of the CFG

Table 3: Dataflow Problem X Properties

## 2.2 Example

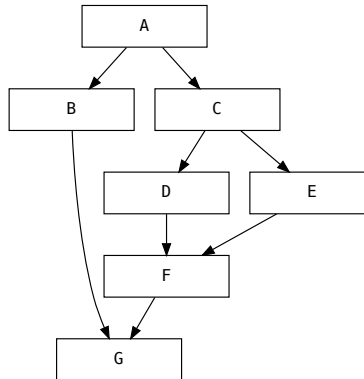


Figure 2: Dominance Analysis example

	<b>DOM[B]</b>
<b>A</b>	$\{A\}$
<b>B</b>	$\{A, B\}$
<b>C</b>	$\{A, C\}$
<b>D</b>	$\{A, C, D\}$
<b>E</b>	$\{A, C, E\}$
<b>F</b>	$\{A, C, F\}$
<b>G</b>	$\{A, G\}$

Table 4: Dominance analysis execution table

### 3 Constant Propagation

The constant propagation problem aims at finding what are the couples  $\langle \text{variable}, \text{constant value} \rangle$  that are available in a certain basic block, so that the variable constant value can be propagated across the blocks.

#### 3.1 Problem formalization

We say that a couple  $\langle \text{variable}, \text{constant} \rangle$  is valid at block  $n$  if it is guaranteed that the variable  $x$  gets that constant value every time that the block is reached.

	<b>Constant Propagation</b>
Domain	Sets of variables and their constant values
Direction	Forward $in[b] = \wedge(out[pred(b)])$ $out[b] = f_b(in[b])$
Transfer function	$f_b(x) = Gen_b \cup (x - Kill_b)$
Meet Operation ( $\wedge$ )	$\cap$
Boundary Condition	$out[entry] = \emptyset \quad in[entry] = \emptyset$
Initial interior points	$out[b] = \emptyset \quad in[b] = U$

Table 5: Constant Propagation Problem Summary Table

### 3.2 Example

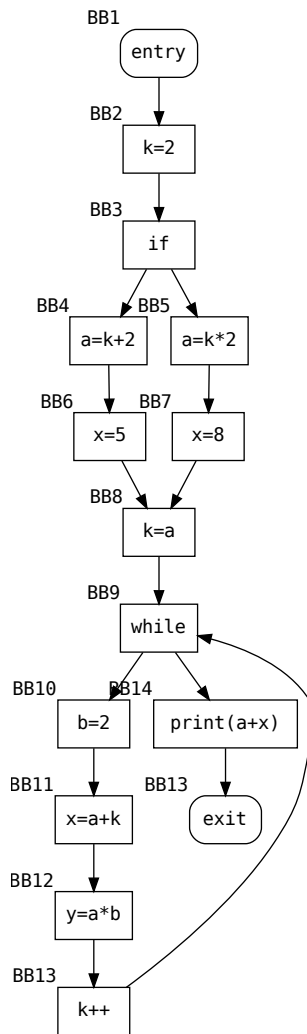


Figure 3: Constant Propagation example

	<b>Iteration 1</b>	
	<b>IN[B]</b>	<b>OUT[B]</b>
<b>BB1</b>	$\emptyset$	$\langle k, 2 \rangle$
<b>BB2</b>	$\emptyset$	$\langle k, 2 \rangle$
<b>BB3</b>	$\langle k, 2 \rangle$	$\langle k, 2 \rangle$
<b>BB4</b>	$\langle k, 2 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle$
<b>BB5</b>	$\langle k, 2 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle$
<b>BB6</b>	$\langle k, 2 \rangle, \langle a, 4 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle, \langle x, 5 \rangle$
<b>BB7</b>	$\langle k, 2 \rangle, \langle a, 4 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle, \langle x, 8 \rangle$
<b>BB8</b>	$\langle k, 2 \rangle, \langle a, 4 \rangle$	$\langle k, 4 \rangle, \langle a, 4 \rangle$
<b>BB9</b>	$\langle k, 2 \rangle, \langle a, 4 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle$
<b>BB10</b>	$\langle k, 4 \rangle, \langle a, 4 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle, \langle b, 2 \rangle$
<b>BB11</b>	$\langle k, 4 \rangle, \langle a, 4 \rangle, \langle b, 2 \rangle$	$\langle k, 4 \rangle, \langle a, 4 \rangle, \langle b, 2 \rangle, \langle x, 8 \rangle$
<b>BB12</b>	$\langle k, 4 \rangle, \langle a, 4 \rangle,$ $\langle b, 2 \rangle, \langle x, 8 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle,$ $\langle b, 2 \rangle, \langle x, 8 \rangle, \langle y, 8 \rangle$
<b>BB13</b>	$\langle k, 4 \rangle, \langle a, 4 \rangle,$ $\langle b, 2 \rangle, \langle x, 8 \rangle, \langle y, 8 \rangle$	$\langle k, 5 \rangle, \langle a, 4 \rangle,$ $\langle b, 2 \rangle, \langle x, 8 \rangle, \langle y, 8 \rangle$
<b>BB14</b>	$\langle k, 4 \rangle, \langle a, 4 \rangle$	$\langle k, 4 \rangle, \langle a, 4 \rangle$
<b>BB15</b>	$\langle k, 4 \rangle, \langle a, 4 \rangle$	$\langle k, 4 \rangle, \langle a, 4 \rangle$

Table 6: Constant Propagation Algorithm Execution Table (Iteration 1)

	<b>Iteration 2</b>	
	<b>IN[B]</b>	<b>OUT[B]</b>
<b>BB1</b>	$\emptyset$	$\langle k, 2 \rangle$
<b>BB2</b>	$\emptyset$	$\langle k, 2 \rangle$
<b>BB3</b>	$\langle k, 2 \rangle$	$\langle k, 2 \rangle$
<b>BB4</b>	$\langle k, 2 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle$
<b>BB5</b>	$\langle k, 2 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle$
<b>BB6</b>	$\langle k, 2 \rangle, \langle a, 4 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle, \langle x, 5 \rangle$
<b>BB7</b>	$\langle k, 2 \rangle, \langle a, 4 \rangle$	$\langle k, 2 \rangle, \langle a, 4 \rangle, \langle x, 8 \rangle$
<b>BB8</b>	$\langle k, 2 \rangle, \langle a, 4 \rangle$	$\langle k, 4 \rangle, \langle a, 4 \rangle$
<b>BB9</b>	$\langle a, 4 \rangle$	$\langle a, 4 \rangle$
<b>BB10</b>	$\langle a, 4 \rangle$	$\langle a, 4 \rangle, \langle b, 2 \rangle$
<b>BB11</b>	$\langle a, 4 \rangle, \langle b, 2 \rangle$	$\langle k, 8 \rangle, \langle a, 4 \rangle, \langle b, 2 \rangle$
<b>BB12</b>	$\langle a, 4 \rangle, \langle b, 2 \rangle$	$\langle a, 4 \rangle, \langle b, 2 \rangle, \langle y, 8 \rangle$
<b>BB13</b>	$\langle a, 4 \rangle, \langle b, 2 \rangle, \langle y, 8 \rangle$	$\langle k, 5 \rangle, \langle a, 4 \rangle, \langle b, 2 \rangle, \langle y, 8 \rangle$
<b>BB14</b>	$\langle a, 4 \rangle$	$\langle a, 4 \rangle$
<b>BB15</b>	$\langle a, 4 \rangle$	$\langle a, 4 \rangle$

Table 7: Constant Propagation Algorithm Execution Table (Iteration 2)