# Second Assignment

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## 1 Very Busy Expressions

The search for very busy expressions can be useful for code hoisting, since very busy expressions can be moved from the place they are up to a joint point from which the flow departures.

#### 1.1 Problem formalization

Formally an expression is said to be **very busy** when it is computed along each path that part from the point p without any redefinition of its operands. This information can be used to move the expression to a point of the code in which is computation can be used by all the paths that use the expression.

	Very Busy Expressions
Domain	Sets of expressions
Direction	Backward
	$in[b] = f_b(out[b])$
	$out[b] = \wedge in[succ(b)]$
Transfer function	$f_b(x) = Gen_b \cup (x - Kill_b)$
Meet Operation $(\land)$	Π
Boundary Condition	$out[exit] = \varnothing$
Initial interior points	out[b] = U

Table 1: Very busy expressions summary table

#### 1.2 Example

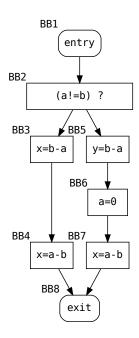


Figure 1: Very Busy Expression Example

	Iteration	n 1	Iteration 2						
	IN[B]	OUT[B]	IN[B]	OUT[B]					
BB1	$\{b-a\}$	$\{b-a\}$	$\{b-a\}$	$\{b-a\}$					
BB2	$\{b-a\}$	$\{b-a\}$	$\{b-a\}$	$\{b-a\}$					
BB3	$\{b-a\}, \{a-b\}$	$\{a-b\}$	$\{b-a\}, \{a-b\}$	$\{a-b\}$					
BB4	$\{a-b\}$	Ø	$\{a-b\}$	Ø					
BB5	$\{b-a\}$	Ø	$\{b-a\}$	Ø					
BB6	Ø	$\{a-b\}$	Ø	$\{a-b\}$					
BB7	$\{a-b\}$	Ø	$\{a-b\}$	Ø					
BB8	Ø	Ø	Ø	Ø					

Table 2: Very Busy Expression Algorithm Execution Table

# 2 Dominator Analysis

Dominator analysis is fundamental to create the single static assignment form.

#### 2.1 Problem formalization

A basic block  $B_1$  dominates another block  $B_2$  if it is encountered in every path from entry to  $B_2$ .

	Dominator Analysis
Domain	Sets of Basic Blocks
Direction	Forward
Transfer function	$f_b(x) = \{x\} \cup (\bigcap_{m \in preds(x)} f_b(m))$
Meet Operation $(\land)$	Λ
Boundary Condition	$Dom[entry] = \{entry\}$
Initial interior points	$Dom[b] = N  \forall b \neq entry, \text{ with } N$
	the number of basic blocks of the
	CFG

Table 3: Dataflow Problem X Properties

### 2.2 Example

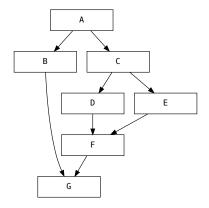


Figure 2: Dominance Analysis example

	DOM[B]
A	$\{A\}$
В	$\{A,B\}$
$\mathbf{C}$	$\{A,C\}$
D	$\{A, C, D\}$
$\mathbf{E}$	$\{A,C,E\}$
F	$\{A,C,F\}$
G	$\{A,G\}$

Table 4: Dominance analysis execution table

# 3 Constant Propagation

The constant propagation problem aims at finding what are the couples  $< variable, constant\ value >$  that are availables in a certain basic block, so that the variable constant value can be propagated across the blocks.

#### 3.1 Problem formalization

We say that a couple < variable, constant > is valid at block n if it is guaranteed that the variable x gets that constant value every time that the block is reached.

	Constant Propagation
Domain	Sets of variables and their con-
	stant values
Direction	Forward
	$in[b] = \land (out[pred(b)])$
	$out[b] = f_b(in[b])$
Transfer function	$f_b(x) = Gen_b \cup (x - Kill_b)$
Meet Operation $(\land)$	Λ
Boundary Condition	$out[entry] = \varnothing  in[entry] = \varnothing$
Initial interior points	$out[b] = \varnothing  in[b] = U$

Table 5: Constant Propagation Problem Summary Table

### 3.2 Example

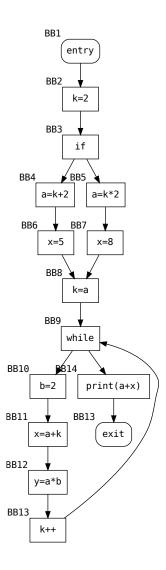


Figure 3: Constant Propagation example

	Iteration 1					
	IN[B]	$\mathrm{OUT}[\mathrm{B}]$				
BB1	Ø	< k, 2 >				
BB2	Ø	< k, 2 >				
BB3	< k, 2 >	< k, 2 >				
BB4	< k, 2 >	< k, 2 >, < a, 4 >				
BB5	< k, 2 >	< k, 2 >, < a, 4 >				
BB6	< k, 2 >, < a, 4 >	< k, 2 >, < a, 4 >, < x, 5 >				
BB7	< k, 2 >, < a, 4 >	< k, 2 >, < a, 4 >, < x, 8 >				
BB8	< k, 2 >, < a, 4 >	< k, 4 >, < a, 4 >				
BB9	< k, 2 >, < a, 4 >	< k, 2 >, < a, 4 >				
BB10	< k, 4 >, < a, 4 >	< k, 2 >, < a, 4 >, < b, 2 >				
BB11	< k, 4 >, < a, 4 >, < b, 2 >	< k, 4 >, < a, 4 >, < b, 2 >, < x, 8 >				
BB12	< k, 4 >, < a, 4 >,	< k, 2 >, < a, 4 >,				
DD12	< b, 2 >, < x, 8 >	< b, 2 >, < x, 8 >, < y, 8 >				
BB13	< k, 4>, < a, 4>,	< k, 5>, < a, 4>,				
1010	< b, 2 >, < x, 8 >, < y, 8 >	< b, 2 >, < x, 8 >, < y, 8 >				
BB14	< k, 4 >, < a, 4 >	< k, 4 >, < a, 4 >				

Table 6: Constant Propagation Algorithm Execution Table (Iteration 1)

	Iteration 2					
	IN[B]	OUT[B]				
BB1	Ø	< k, 2 >				
BB2	Ø	< k, 2 >				
BB3	< k, 2 >	< k, 2 >				
BB4	< k, 2 >	< k, 2 >, < a, 4 >				
BB5	< k, 2 >	< k, 2 >, < a, 4 >				
BB6	< k, 2 >, < a, 4 >	< k, 2 >, < a, 4 >, < x, 5 >				
BB7	< k, 2 >, < a, 4 >	< k, 2 >, < a, 4 >, < x, 8 >				
BB8	< k, 2 >, < a, 4 >	< k, 4 >, < a, 4 >				
BB9	< a, 4 >	< a, 4 >				
BB10	< a, 4 >	< a, 4 >, < b, 2 >				
BB11	< a, 4 >, < b, 2 >	< a, 4 >, < b, 2 >				
BB12	< a, 4 >, < b, 2 >	< a, 4>, < b, 2>, < y, 8>				
BB13	< a, 4 >, < b, 2 >, < y, 8 >	< a, 4 >, < b, 2 >, < y, 8 >				
BB14	< a, 4 >	< a, 4 >				

Table 7: Constant Propagation Algorithm Execution Table (Iteration 2)