

## Semester Project

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## Map Fusion for Collaborative UAV SLAM

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ETH zürich



Autonomous Systems Lab

## Map Fusion for Collaborative UAV SLAM

Andreas  
Ziegler

Acronyms

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Map merging

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Culling  
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**SLAM** Simultaneous Localisation and Mapping.

**UAV** Unmanned Aerial Vehicle.

**KF** KeyFrame.

**KFM** KeyFrame Match.

**BA** Bundle Adjustment.

**PGO** Pose Graph Optimization.

**LM** Levenberg-Marquardt.

**DL** Powell's dog leg.

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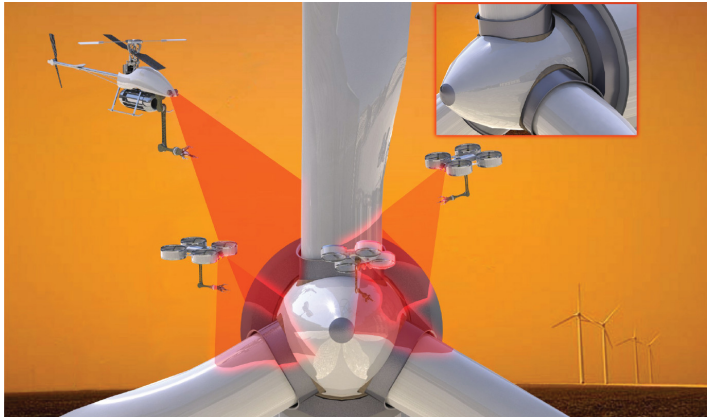
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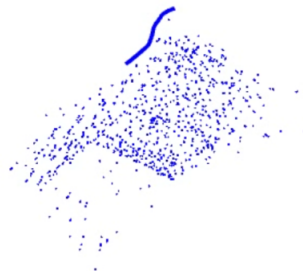
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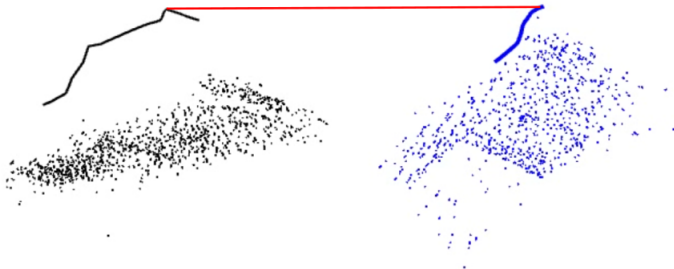
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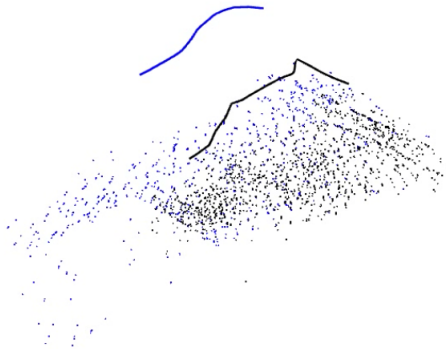
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KeyFrames (KFs): The most “representative” poses

# Introduction - What is a KeyFrame Match (KFM)?

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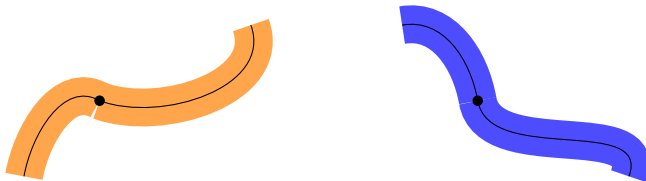
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KeyFrames (KFs): The most “representative” poses

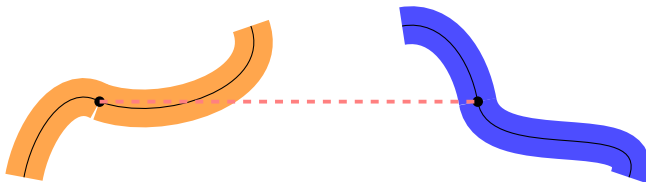
Two clients each with own landmarks and KeyFrames (KFs)



# Introduction - What is a KeyFrame Match (KFM)?

KeyFrames (KFs): The most “representative” poses

KeyFrame Match (KFM): Two KeyFrames (KFs) observing the same location



# Introduction - What is a KeyFrame Match (KFM)?

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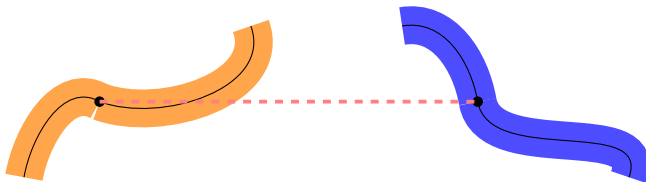
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KeyFrames (KFs): The most “representative” poses

KeyFrame Match (KFM): Two KeyFrames (KFs) observing the same location → Can obtain transformation

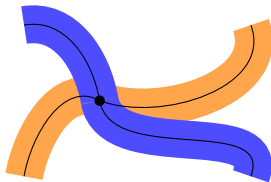


# Introduction - What is a KeyFrame Match (KFM)?

KeyFrames (KFs): The most “representative” poses

KeyFrame Match (KFM): Two KeyFrames (KFs) observing the same location

With the transformation  $\rightarrow$  maps can be aligned

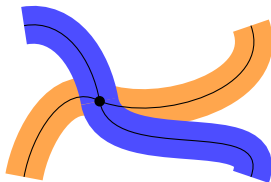


# Introduction - What is a KeyFrame Match (KFM)?

KeyFrames (KFs): The most “representative” poses

A KeyFrame Match (KFM) contains:

- Two KeyFrames (KFs) (One per map)
- The transformation ( $T \in \text{Sim}(3)$ ) between them



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- A multi agent SLAM system based on ORB-SLAM2 should be extended

[Mur-Artal and Tardos, 2016]



- A multi agent SLAM system based on ORB-SLAM2 should be extended
- So far, as soon as a KeyFrame Match (KFM) was detected, maps were merged

[Mur-Artal and Tardos, 2016]

- A multi agent SLAM system based on ORB-SLAM2 should be extended
- So far, as soon as a KeyFrame Match (KFM) was detected, maps were merged
- Using multiple KFMs to guarantee no false map merging

[Mur-Artal and Tardos, 2016]

- A multi agent SLAM system based on ORB-SLAM2 should be extended
- So far, as soon as a KeyFrame Match (KFM) was detected, maps were merged
- Using multiple KFMs to guarantee no false map merging
- Using multiple KFMs to obtain an optimal map alignment

[Mur-Artal and Tardos, 2016]

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Old approach:

- As soon as a KFM was detected, maps were merged

# Map merging - New approach

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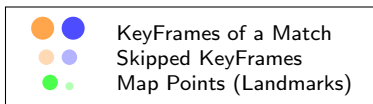
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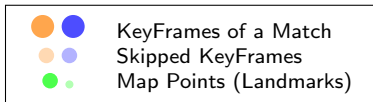
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Find  $n(= 3)$  KeyFrame Matches (KFMs)



# Map merging - New approach

Find  $n(= 3)$  KeyFrame Matches (KFMs),  
Skip  $m(= 5)$  KeyFrames (KFs)



# Map merging - New approach

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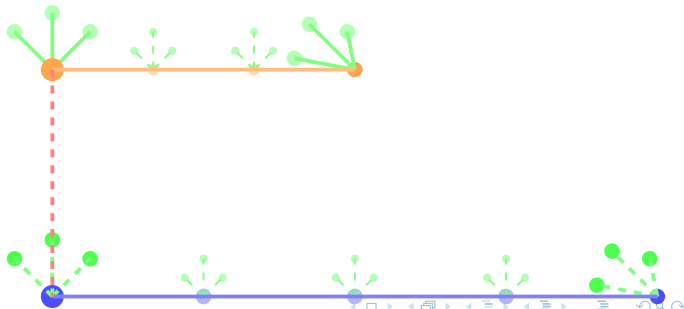
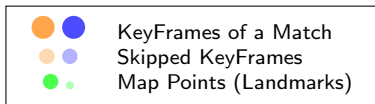
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Find  $n(= 3)$  KeyFrame Matches (KFMs),  
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# Map merging - New approach

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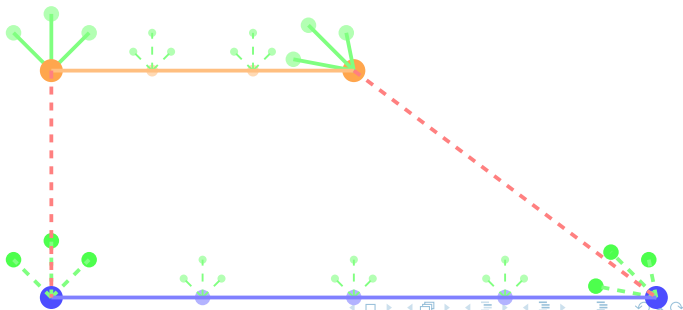
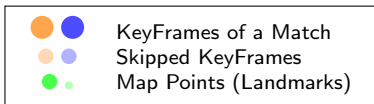
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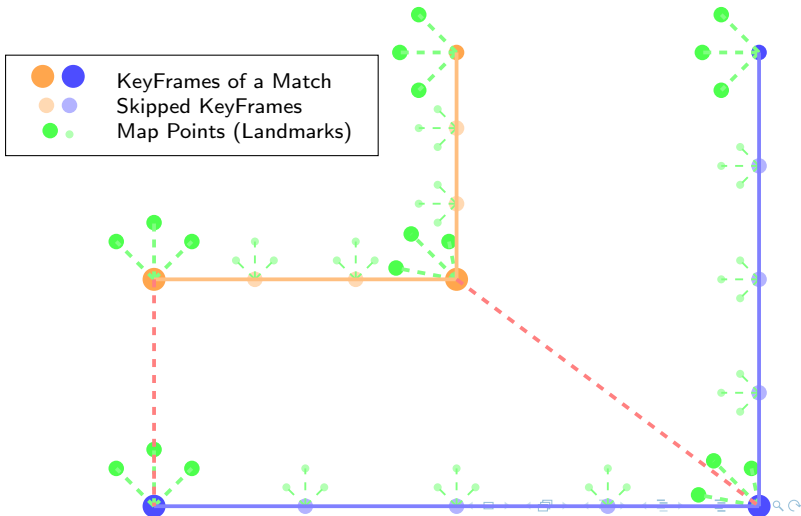
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Find  $n(= 3)$  KeyFrame Matches (KFMs),  
Skip  $m(= 5)$  KeyFrames (KFs)



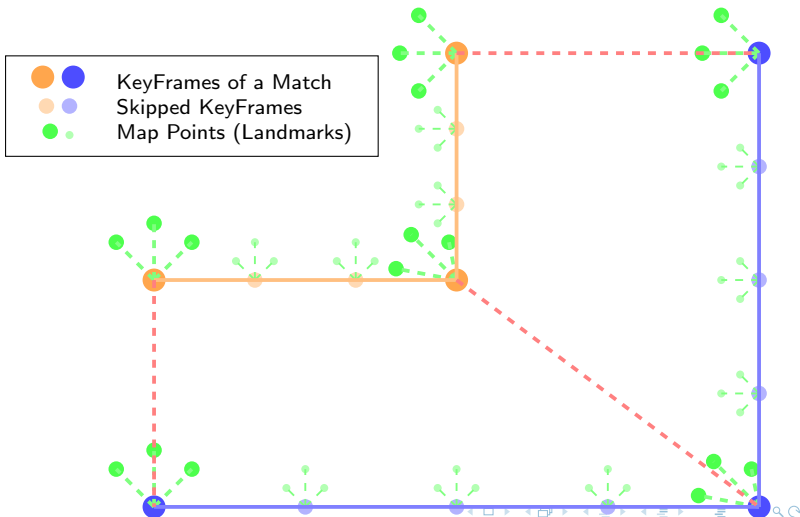
# Map merging - New approach

Find  $n(= 3)$  KeyFrame Matches (KFM), Skip  $m(= 5)$  KFs

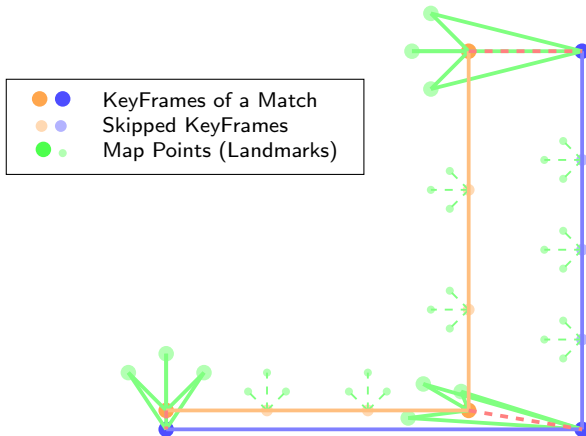


# Map merging - New approach

Find  $n(= 3)$  KeyFrame Matches (KFMs)



## Merge the two maps and fuse map points



# Map merging - Results - skipping of KeyFrame (KF)

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### Co-visibility graph

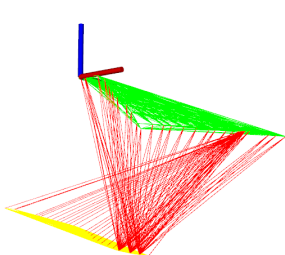
Connections/Edges between KeyFrames (KFs) which observe the same map points (landmarks)

# Map merging - Results - skipping of KF

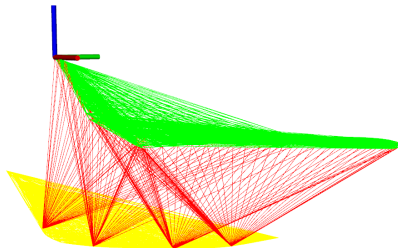
green: Covisibility graph of first map

yellow: Covisibility graph of second map

red: Covisibility between the KFM



(a) 1 KF skipped after a KFM was found



(b) 10 KF skipped after a KFM was found

# Map merging - Results - Reduction of drift

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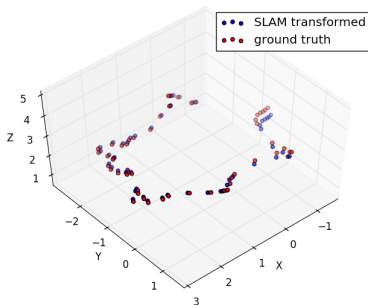
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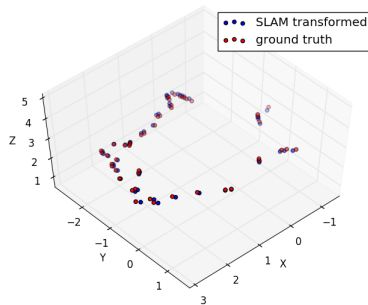
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Ground truth and SLAM transformed Map 1



(a) original approach

Ground truth and SLAM transformed Map 1



(b) new approach

Reduction of the error from  $\text{rmse} = 0.13\text{m}$  to  $\text{rmse} = 0.10\text{m}$

| # KFMs | # KFs skip | rmse   |
|--------|------------|--------|
| 1      | 0          | 0.1311 |
| 5      | 20         | 0.0912 |
| 10     | 5          | 0.1236 |
| 10     | 10         | 0.0961 |

Table: Error (rmse) of different settings (KFMs and KF skips).



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## Motivation

Perform KeyFrame (KF) culling to remove redundant information as bundle adjustment complexity grows with the number of KFs

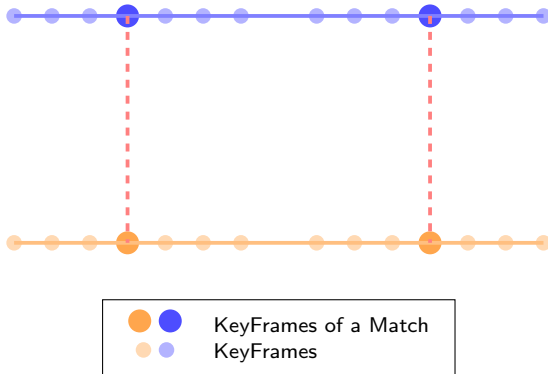
[Mur-Artal et al., 2015]

- Remove redundant KFs before map merging

- Remove redundant KFs before map merging
- Performs culling for every KFM separately

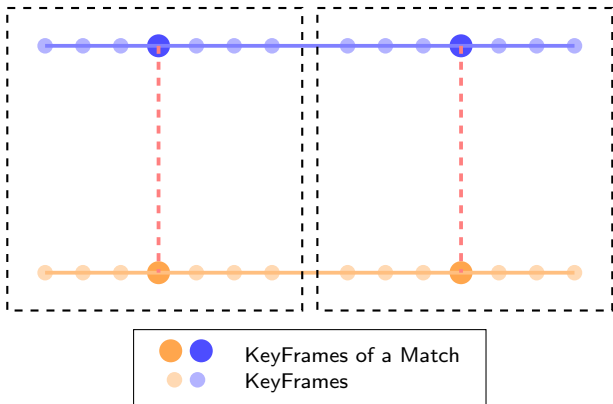
# Culling - Remove redundant KF

- Remove redundant KFs before map merging
- Performs culling for every KFM separately



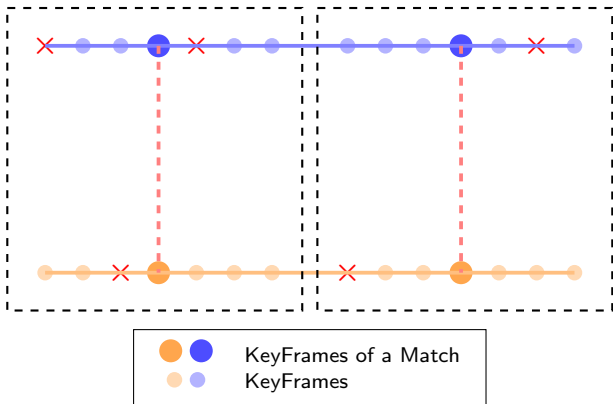
# Culling - Remove redundant KF

- Remove redundant KFs before map merging
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# Culling - Remove redundant KF

- Remove redundant KFs before map merging
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## Pose Graph Optimization (PGO)

## Bundle Adjustment (BA)

$v$  /  $e$ : numbers of **vertices** / **edges** of the graph to optimize

| Culling | # KFM | # KFs skip | PGO $v$ / $e$ | BA $v$ / $e$ |
|---------|-------|------------|---------------|--------------|
| No      | 1     | 0          | 59 / 754      | 2308 / 22193 |
| Yes     | 1     | 0          | 36 / 283      | 1893 / 13222 |
| No      | 10    | 10         | 150 / 1949    | 4806 / 49765 |
| Yes     | 10    | 10         | 93 / 657      | 4165 / 30453 |

**Table:** Time measurements of Pose Graph Optimization (PGO) and Bundle Adjustment (BA) without and with culling.



Culling removes  $\approx 13\%$  of the KeyFrames (KFs)

Pose Graph Optimization (PGO)  
Bundle Adjustment (BA)

Culling removes  $\approx 13\%$  of the KeyFrames (KFs)

| Culling | # KFM | # KFs skipped | PGO [ms] | BA [ms] |
|---------|-------|---------------|----------|---------|
| No      | 10    | 10            | 532.28   | 3659.48 |
| Yes     | 10    | 10            | 178.83   | 1098.37 |

**Table:** Time measurements of PGO and BA without and with culling.

Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

Culling removes  $\approx 13\%$  of the KeyFrames (KFs)

| Culling | # KFM | # KFs skipped | PGO [ms] | BA [ms] |
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| No      | 10    | 10            | 532.28   | 3659.48 |
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**Table:** Time measurements of PGO and BA without and with culling.

Performance increases significantly when culling is enabled

Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

| Culling | # KFMs | # KFs skipped | <i>rmse</i> [m] |
|---------|--------|---------------|-----------------|
| No      | 1      | 0             | 0.1311          |
| Yes     | 1      | 0             | 0.2187          |
| No      | 10     | 10            | 0.0961          |
| Yes     | 10     | 10            | 0.0965          |

Table: *rmse* without and with culling.

| Culling | # KFMs | # KFs skipped | <i>rmse</i> [m] |
|---------|--------|---------------|-----------------|
| No      | 1      | 0             | 0.1311          |
| Yes     | 1      | 0             | 0.2187          |
| No      | 10     | 10            | 0.0961          |
| Yes     | 10     | 10            | 0.0965          |

Table: *rmse* without and with culling.

Accuracy gets worse if not enough information is available.  
No problem with multiple KeyFrame Matches (KFMs).

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Considerable computational benefits can be gained by substituting the Levenberg-Marquardt (LM) algorithm in the implementation of Bundle Adjustment (BA) with a variant of Powell's dog leg (DL) non-linear least squares technique [Lourakis and Argyros, 2005]

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DL optimizer handles trust region differently



The Levenberg-Marquardt (LM) solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

The LM solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

- With a small  $\lambda$  LM becomes a Gauss-Newton method

The LM solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

- With a small  $\lambda$  LM becomes a Gauss-Newton method
- With a big  $\lambda$  LM behaves like a Gradient-descent method

The LM solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

- With a small  $\lambda$  LM becomes a Gauss-Newton method
- With a big  $\lambda$  LM behaves like a Gradient-descent method
- If an update doesn't reduce the error,  $\lambda$  will be increased and the equation must be solved again

The Powell's dog leg (DL) solves iteratively

$$\min_{\delta} 2\left(\frac{1}{2}\epsilon^T \epsilon - (\mathbf{J}\epsilon)^T \delta + \frac{1}{2}\delta^T \mathbf{J}^T \mathbf{J} \delta\right), \text{ subjected to } \|\delta\| \leq \Delta$$

For  $\kappa \in [0, 2]$ , the dog leg trajectory is defined as

$$\delta(\kappa) = \begin{cases} \kappa \delta_{gd} & 0 \leq \kappa \leq 1 \\ \delta_{gd} + (\kappa - 1)(\delta_{gn} - \delta_{gd}) & 1 \leq \kappa \leq 2 \end{cases}$$

With

$$\delta_{gd} = \frac{\mathbf{g}^T \mathbf{g}}{\mathbf{g}^T \mathbf{J}^T \mathbf{J} \mathbf{g}} \mathbf{g}$$

and  $\delta_{gn}$  the solution of

$$\mathbf{J}^T \mathbf{J} \delta_{gn} = \mathbf{g}$$

the dog leg trajectory looks like

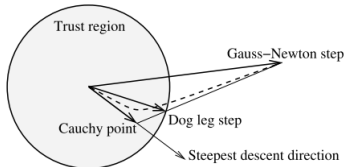


Figure from [Lourakis and Argyros, 2005]

- Once the Gauss-Newton step has been determined, the DL algorithm can solve the subproblem for various  $\Delta$  without resolving an equation

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- Reducing the number of times the Gauss-Newton step has to be determined is crucial for the overall performance of the minimization process



- Once the Gauss-Newton step has been determined, the DL algorithm can solve the subproblem for various  $\Delta$  without resolving an equation
- Reducing the number of times the Gauss-Newton step has to be determined is crucial for the overall performance of the minimization process
- For the mentioned reasons the DL algorithm requires less computational effort compared to the LM algorithm

- Tried Pose Graph Optimization (PGO) and Bundle Adjustment (BA) with the Powell's dog leg (DL) optimizer

- Tried Pose Graph Optimization (PGO) and Bundle Adjustment (BA) with the Powell's dog leg (DL) optimizer
- PGO: Slightly worse timing using the DL optimizer

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## Conclusion

LM optimizer for PGO and DL optimizer for BA

| Opt.  | # KFMs | # KFs skipped | PGO [ms] | BA [ms] |
|-------|--------|---------------|----------|---------|
| LM/LM | 10     | 10            | 178.83   | 1098.37 |
| LM/DL | 10     | 10            | 178.70   | 383.54  |

**Table:** Time measurements of LM and DL optimizer.

Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

| Opt.  | # KFMs | # KFs skipped | PGO [ms] | BA [ms] |
|-------|--------|---------------|----------|---------|
| LM/LM | 10     | 10            | 178.83   | 1098.37 |
| LM/DL | 10     | 10            | 178.70   | 383.54  |

**Table:** Time measurements of LM and DL optimizer.

Accuracy stays the same while the performance is increased

Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

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- Multiple KFMs approach increases accuracy

- Multiple KFMs approach increases accuracy
- Skipping of KFs spreads KFMs over a bigger area

## Higher accuracy

The use of KFMs from a bigger area serves PGO and BA with more information → higher accuracy

## Higher accuracy

The use of KFM from a bigger area serves PGO and BA with more information → higher accuracy

- Culling removes redundant KFs → improved timing

## Higher accuracy

The use of KFM from a bigger area serves PGO and BA with more information → higher accuracy

- Culling removes redundant KFs → improved timing
- Using DL optimizer for the BA also improves timing

## Higher accuracy

The use of KFMs from a bigger area serves PGO and BA with more information → higher accuracy

## Better timing

Culling and the use of the DL optimizer improves timing

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## Outlook:

- Heuristic for best map alignment
- Extend area for KF culling

## Limitation:

- # of KFMs and # of skips depends on data set



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Lourakis, M. I. A. and Argyros, A. A. (2005).

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