

Semester Project

-

Map Fusion for Collaborative UAV SLAM

-



Autonomous Systems Lab

Map Fusion for Collaborative UAV SLAM

Andreas
Ziegler

Acronyms

Introduction

Motivation

Map merging

Approaches
Results

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Optimization
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- ➌ Map merging
- ➍ Culling
- ➎ Optimization
- ➏ Conclusion
- ➐ Outlook

SLAM Simultaneous Localisation and Mapping.

UAV Unmanned Aerial Vehicle.

KF KeyFrame.

KFM KeyFrame Match.

BA Bundle Adjustment.

PGO Pose Graph Optimization.

LM Levenberg-Marquardt.

DL Powell's dog leg.

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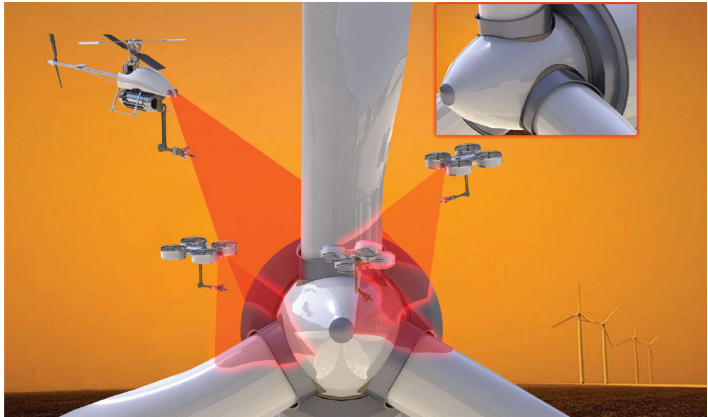
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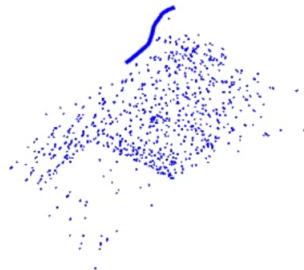
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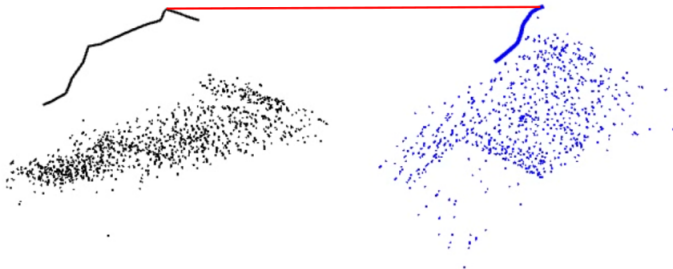
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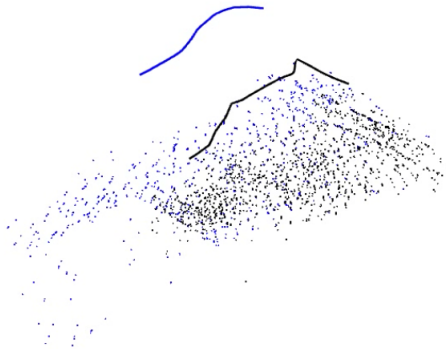
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KeyFrames (KFs): The most “representative” poses

Introduction - What is a KeyFrame Match (KFM)?

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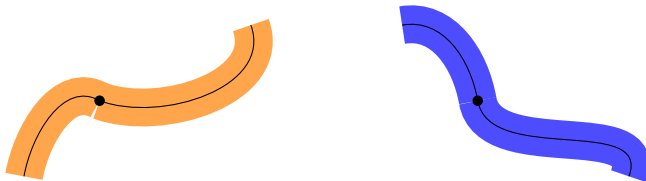
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KeyFrames (KFs): The most “representative” poses

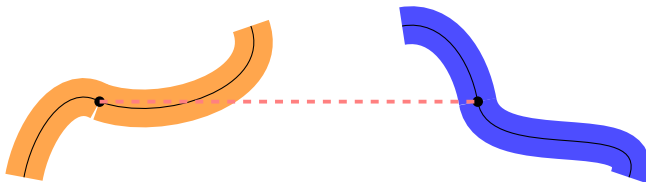
Two clients each with own landmarks and KeyFrames (KFs)



Introduction - What is a KeyFrame Match (KFM)?

KeyFrames (KFs): The most “representative” poses

KeyFrame Match (KFM): Two KeyFrames (KFs) observing the same location



Introduction - What is a KeyFrame Match (KFM)?

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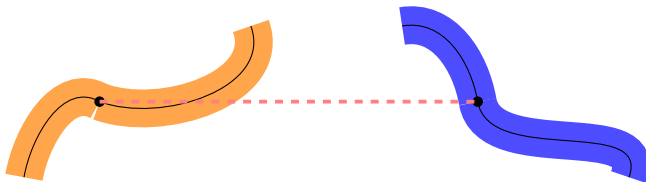
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KeyFrames (KFs): The most “representative” poses

KeyFrame Match (KFM): Two KeyFrames (KFs) observing the same location → Can obtain transformation

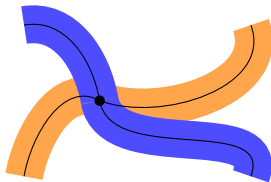


Introduction - What is a KeyFrame Match (KFM)?

KeyFrames (KFs): The most “representative” poses

KeyFrame Match (KFM): Two KeyFrames (KFs) observing the same location

With the transformation \rightarrow maps can be aligned

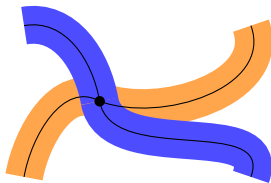


Introduction - What is a KeyFrame Match (KFM)?

KeyFrames (KFs): The most “representative” poses

A KeyFrame Match (KFM) contains:

- Two KeyFrames (KFs) (One per map)
- The transformation ($T \in \text{Sim}(3)$) between them



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- A multi agent SLAM system based on ORB-SLAM2 should be extended

[Mur-Artal and Tardos, 2016]

- A multi agent SLAM system based on ORB-SLAM2 should be extended
- So far, as soon as a KeyFrame Match (KFM) was detected, maps were merged

[Mur-Artal and Tardos, 2016]

- A multi agent SLAM system based on ORB-SLAM2 should be extended
- So far, as soon as a KeyFrame Match (KFM) was detected, maps were merged
- Using multiple KFMs to guarantee no false map merging

[Mur-Artal and Tardos, 2016]

- A multi agent SLAM system based on ORB-SLAM2 should be extended
- So far, as soon as a KeyFrame Match (KFM) was detected, maps were merged
- Using multiple KFMs to guarantee no false map merging
- Using multiple KFMs to obtain an optimal map alignment

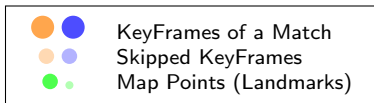
[Mur-Artal and Tardos, 2016]

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Old approach:

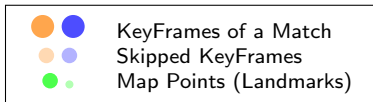
- As soon as a KFM was detected, maps were merged

Find $n(= 3)$ KeyFrame Matches (KFMs)



Map merging - New approach

Find $n(= 3)$ KeyFrame Matches (KFMs),
Skip $m(= 5)$ KeyFrames (KFs)



Map merging - New approach

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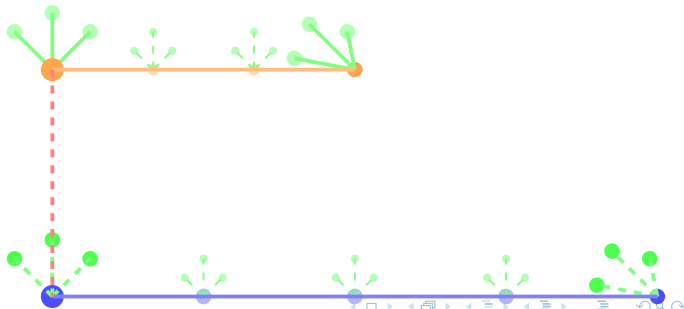
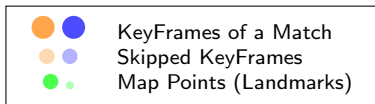
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Find $n(= 3)$ KeyFrame Matches (KFMs),
Skip $m(= 5)$ KeyFrames (KFs)



Map merging - New approach

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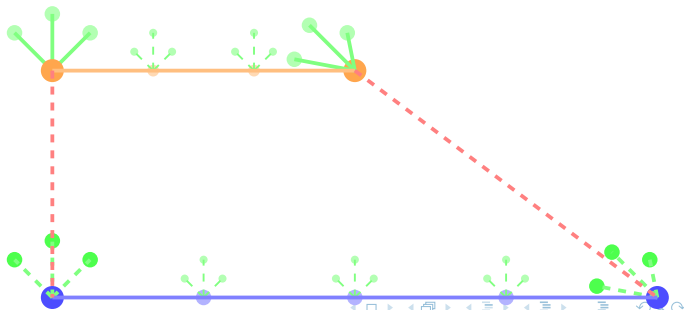
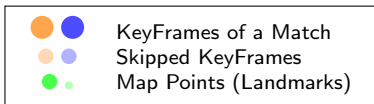
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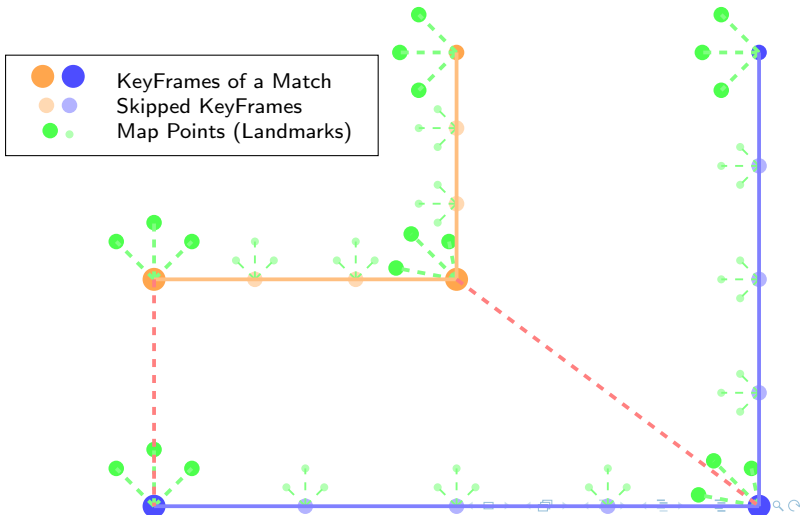
Outlook

Find $n(= 3)$ KeyFrame Matches (KFMs),
Skip $m(= 5)$ KeyFrames (KFs)



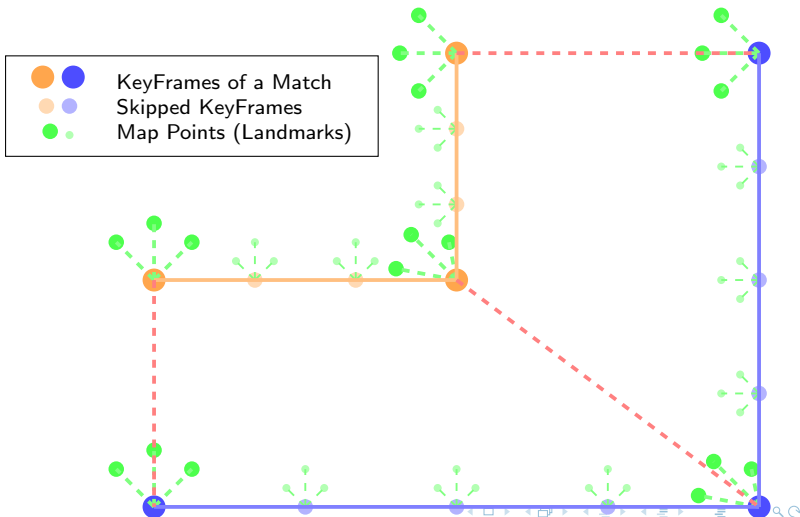
Map merging - New approach

Find $n(= 3)$ KeyFrame Matches (KFM), Skip $m(= 5)$ KFs

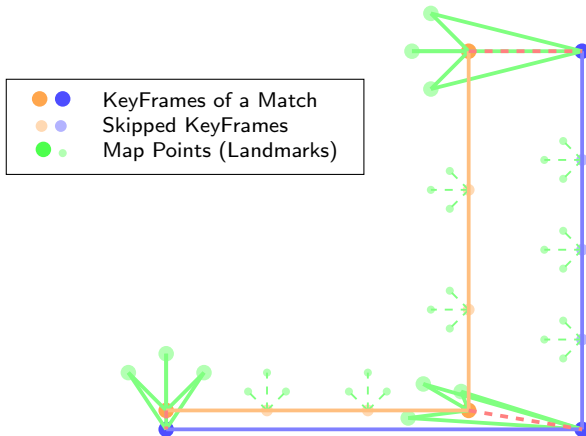


Map merging - New approach

Find $n(= 3)$ KeyFrame Matches (KFMs)



Merge the two maps and fuse map points



Map merging - Results - skipping of KeyFrame (KF)

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Co-visibility graph

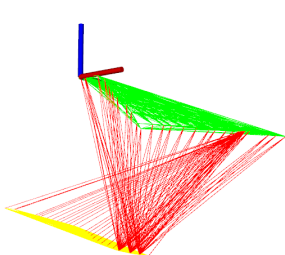
Connections/Edges between KeyFrames (KFs) which observe the same map points (landmarks)

Map merging - Results - skipping of KF

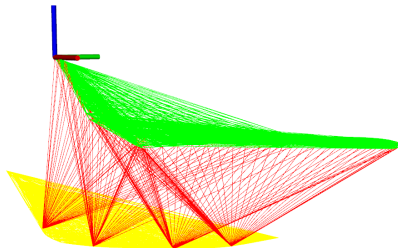
green: Covisibility graph of first map

yellow: Covisibility graph of second map

red: Covisibility between the KFM



(a) 1 KF skipped after a KFM was found



(b) 10 KF skipped after a KFM was found

Map merging - Results - Reduction of drift

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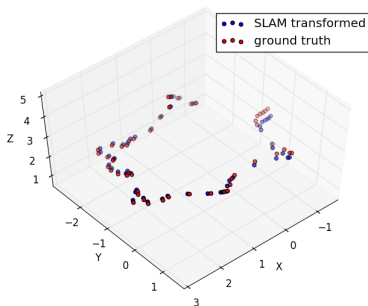
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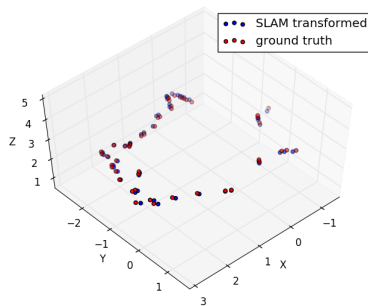
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Ground truth and SLAM transformed Map 1



(a) original approach

Ground truth and SLAM transformed Map 1



(b) new approach

Reduction of the error from $\text{rmse} = 0.13\text{m}$ to $\text{rmse} = 0.10\text{m}$

# KFMs	# KFs skip	rmse
1	0	0.1311
5	20	0.0912
10	5	0.1236
10	10	0.0961

Table: Error (rmse) of different settings (KFMs and KF skips).

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Motivation

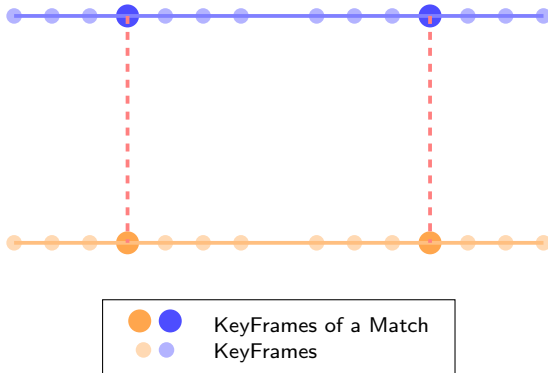
Perform KeyFrame (KF) culling to remove redundant information as bundle adjustment complexity grows with the number of KFs

- Remove redundant KFs before map merging

- Remove redundant KFs before map merging
- Performs culling for every KFM separately

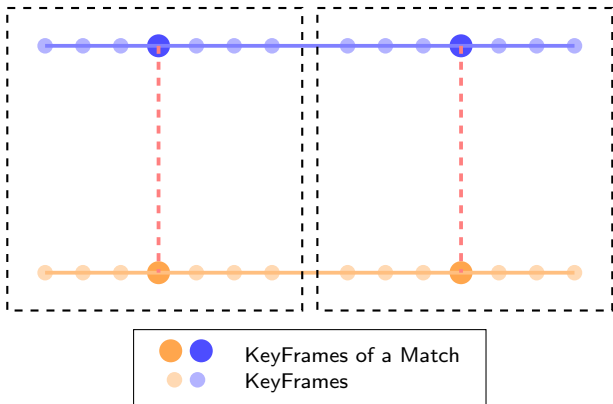
Culling - Remove redundant KF

- Remove redundant KFs before map merging
- Performs culling for every KFM separately



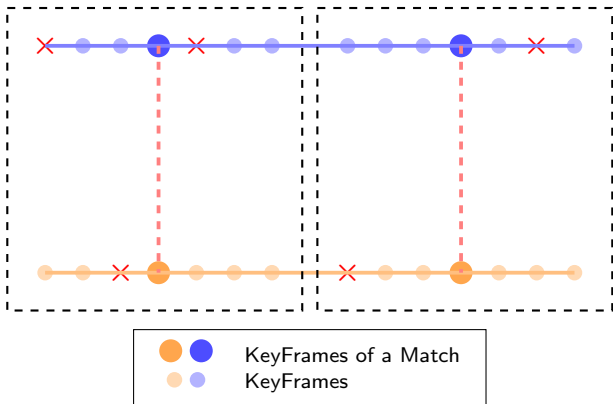
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Culling - Remove redundant KF

- Remove redundant KFs before map merging
- Performs culling for every KFM separately



Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

v / e : numbers of **vertices** / **edges** of the graph to optimize

Culling	# KFM	# KFs skip	PGO v / e	BA v / e
No	1	0	59 / 754	2308 / 22193
Yes	1	0	36 / 283	1893 / 13222
No	10	10	150 / 1949	4806 / 49765
Yes	10	10	93 / 657	4165 / 30453

Table: Time measurements of Pose Graph Optimization (PGO) and Bundle Adjustment (BA) without and with culling.

Culling removes $\approx 13\%$ of the KeyFrames (KFs)

Pose Graph Optimization (PGO)
Bundle Adjustment (BA)

Culling removes $\approx 13\%$ of the KeyFrames (KFs)

Culling	# KFM	# KFs skipped	PGO [ms]	BA [ms]
No	10	10	532.28	3659.48
Yes	10	10	178.83	1098.37

Table: Time measurements of PGO and BA without and with culling.

Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

Culling removes $\approx 13\%$ of the KeyFrames (KFs)

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No	10	10	532.28	3659.48
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Table: Time measurements of PGO and BA without and with culling.

Performance increases significantly when culling is enabled

Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

Culling	# KFMs	# KFs skipped	<i>rmse</i> [m]
No	1	0	0.1311
Yes	1	0	0.2187
No	10	10	0.0961
Yes	10	10	0.0965

Table: *rmse* without and with culling.

Culling	# KFMs	# KFs skipped	<i>rmse</i> [m]
No	1	0	0.1311
Yes	1	0	0.2187
No	10	10	0.0961
Yes	10	10	0.0965

Table: *rmse* without and with culling.

Accuracy gets worse if not enough information is available.
No problem with multiple KeyFrame Matches (KFMs).

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Considerable computational benefits can be gained by substituting the Levenberg-Marquardt (LM) algorithm in the implementation of Bundle Adjustment (BA) with a variant of Powell's dog leg (DL) non-linear least squares technique [Lourakis and Argyros, 2005]

Considerable computational benefits can be gained by substituting the Levenberg-Marquardt (LM) algorithm in the implementation of Bundle Adjustment (BA) with a variant of Powell's dog leg (DL) non-linear least squares technique [Lourakis and Argyros, 2005]

DL optimizer handles trust region differently

The Levenberg-Marquardt (LM) solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

The LM solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

- With a small λ LM becomes a Gauss-Newton method

The LM solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

- With a small λ LM becomes a Gauss-Newton method
- With a big λ LM behaves like a Gradient-descent method

The LM solves iteratively

$$(\mathbf{J}^T \mathbf{J} + \lambda \mathbf{I}) \delta = \mathbf{J}^T \epsilon, \text{ where } \epsilon = [\mathbf{y} - \mathbf{f}(\beta)]$$

- With a small λ LM becomes a Gauss-Newton method
- With a big λ LM behaves like a Gradient-descent method
- If an update doesn't reduce the error, λ will be increased and the equation must be solved again

The Powell's dog leg (DL) solves iteratively

$$\min_{\delta} 2\left(\frac{1}{2}\epsilon^T \epsilon - (\mathbf{J}\epsilon)^T \delta + \frac{1}{2}\delta^T \mathbf{J}^T \mathbf{J} \delta\right), \text{ subjected to } \|\delta\| \leq \Delta$$

For $\kappa \in [0, 2]$, the dog leg trajectory is defined as

$$\delta(\kappa) = \begin{cases} \kappa \delta_{gd} & 0 \leq \kappa \leq 1 \\ \delta_{gd} + (\kappa - 1)(\delta_{gn} - \delta_{gd}) & 1 \leq \kappa \leq 2 \end{cases}$$

With

$$\delta_{gd} = \frac{\mathbf{g}^T \mathbf{g}}{\mathbf{g}^T \mathbf{J}^T \mathbf{J} \mathbf{g}} \mathbf{g}$$

and δ_{gn} the solution of

$$\mathbf{J}^T \mathbf{J} \delta_{gn} = \mathbf{g}$$

the dog leg trajectory looks like

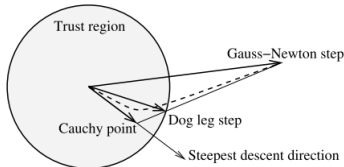


Figure from [Lourakis and Argyros, 2005]

- Once the Gauss-Newton step has been determined, the DL algorithm can solve the subproblem for various Δ without resolving an equation

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- Reducing the number of times the Gauss-Newton step has to be determined is crucial for the overall performance of the minimization process

- Once the Gauss-Newton step has been determined, the DL algorithm can solve the subproblem for various Δ without resolving an equation
- Reducing the number of times the Gauss-Newton step has to be determined is crucial for the overall performance of the minimization process
- For the mentioned reasons the DL algorithm requires less computational effort compared to the LM algorithm

- Tried Pose Graph Optimization (PGO) and Bundle Adjustment (BA) with the Powell's dog leg (DL) optimizer.

- Tried Pose Graph Optimization (PGO) and Bundle Adjustment (BA) with the Powell's dog leg (DL) optimizer.
- PGO: Slightly worse timing using the DL optimizer

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Conclusion

LM optimizer for PGO and DL optimizer for BA

Opt.	# KFMs	# KFs skipped	PGO [ms]	BA [ms]
LM/LM	10	10	178.83	1098.37
LM/DL	10	10	178.70	383.54

Table: Time measurements of LM and DL optimizer.

Pose Graph Optimization (PGO)

Bundle Adjustment (BA)

Opt.	# KFMs	# KFs skipped	PGO [ms]	BA [ms]
LM/LM	10	10	178.83	1098.37
LM/DL	10	10	178.70	383.54

Table: Time measurements of LM and DL optimizer.

Accuracy stays the same while the performance is increased

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Bundle Adjustment (BA)

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- Multiple KFMs approach increases accuracy

- Multiple KFMs approach increases accuracy
- Skipping of KFs spreads KFMs over a bigger area

Higher accuracy

The use of KFMs from a bigger area serves PGO and BA with more information → higher accuracy

Higher accuracy

The use of KFM from a bigger area serves PGO and BA with more information → higher accuracy

- Culling removes redundant KFs → improved timing

Higher accuracy

The use of KFM from a bigger area serves PGO and BA with more information → higher accuracy

- Culling removes redundant KFs → improved timing
- Using DL optimizer for the BA also improves timing

Higher accuracy

The use of KFMs from a bigger area serves PGO and BA with more information → higher accuracy

Better timing

Culling and the use of the DL optimizer improves timing

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Outlook:

- Heuristic for best map alignment
- Extend area for KF culling

Limitation:

- # of KFMs and # of skips depends on data set

Outlook:

- Heuristic for best map alignment
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Lourakis, M. I. A. and Argyros, A. A. (2005).

Is Levenberg-Marquardt the most efficient optimization algorithm for implementing bundle adjustment?

In Proceedings of the IEEE International Conference on Computer Vision, volume II, pages 1526–1531.



Mur-Artal, R. and Tardos, J. D. (2016).

ORB-SLAM2: an Open-Source SLAM System for Monocular, Stereo and RGB-D Cameras.