University of Bayreuth

Institute for Computer Science

Bachelor Thesis

in Applied Computer Science

Topic:	The CYK-Algorithm, a CLI-Tool and different ways of filling the Parsing Table
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To my parents.

Abstract

The abstract of this thesis will be found here.

Zusammenfassung

Hier steht die Zusammenfassung dieser Bachelorarbeit.

Contents

1 Introduction

What has already been done in this area? Why are you doing this?

Let there be a grammar $G = (V, \ \Sigma, \ S, \ P)$ in Chomsky Normal Form (CNF).
V is a finite set of variables.
Σ is an alphabet.
S is the starting symbol and $S \in V$.
P is a finite set of rules: $P \subseteq V \times (V \cup \Sigma)^*$. G is in CNF and therefore, more specifically, it holds: $P \ \subseteq \ V \times (V^2 \cup \Sigma)$.

For simplification the default definitions hold:

- $V = \{A, B, ...\}$

- $(V^2 \cup \ \Sigma)^* = \{a, b, ...\} \cup \{AB, BS, AC, ...\}$

Let there be a word $w \in \Sigma^*$, a language $L(G)$ and a grammar G in CNF.

1.1 Forward Problem vs. Backward Problem

Forward Problem ($G \xrightarrow{derivation} w$):
Informal definition: "Forming a derivation from a root node to a final sentence." [Duda 8.6.3 page 426]
Input: Grammar G in CNF.
Output: Derivation d that shows implicitly $w \subseteq L$.

Backward Problem = Parsing ($w \overset{?}{\subseteq} L(G)$):
Informal definition: "Given a particular w, find a derivation in G that leads to w. This process, called parsing, is virtually always much more difficult than forming a derivation." [Duda 8.6.3 page 426]
Input: w and a grammar G in CNF.
Output: $w \subseteq L(G) \implies$ derivation d.

1.2 Parsing: Bottom-Up vs Top-Down

Bottom-Up: Bottom-Up parsing is "the general method used in the Cocke-Younger-Kasami(CYK) algorithm, which fills a parse table from the "bottom up"." (Bottom up means starting from the leaves.) [Duda 8.6.3 page 426]

Top-Down: "Top-Down parsing starts with the root node and successively applies productions from P, with the goal of finding a derivation of the test sentence w. Because it is rare indeed that the sentence is derived in the first production attempted, it is necessary to specify some criteria to guide the choice of which rewrite rule to apply. Such criteria could include beginning the parse at the first (left) character in the sentence (i.e., finding a small set of rewrite rules that yield the first character), then iteratively expanding the production to derive subsequent characters, or instead starting at the last (right) character in the sentence." [Duda 8.6.3 page 428]

1.3 Scope of this thesis

The starting point of this thesis was to get a command line interface (CLI) tool to automatically generate $exercises = (grammar,\ word,\ parse\ table,\ derivation\ tree)$, which are used to test if the students have understood the way of working of the CYK algorithm. A scoring model is used to evaluate the generated exercises regarding their usability in an exam.

This alone doesn't meet the requirements for being an adequate topic for a bachelor thesis. Therefore the task of finding a clever algorithm to get exercises with a high chance of being usable as an exam exercise was added.

2 Simple Scoring Model

Short preface to the rationale about the scoring model. Add diversity criteria = homogenity of the cells to the scoring matrix.

2.1 Elimination Criteria and Selection Criteria

Success rates: Producibility: $w \subseteq L(G)$

Grammar restricitons: $n = |w|$, maxNumberOfVarsPerCell; **Delete SuccessRates-GrammarRestrictions class. Move maxNumberOfVarsPerCell to exam restrictions class and use n only as parameter.**

Exam restrictions: rightCellCombinationsForcedCount, maxSumOfProductions, maxSumOfVarsInPyramid

Picture of used scoring model without weights here. Maybe one picture together with the next subsection.

2.2 Weighting of the criteria

Picture of the final used scoring model with weights here.

2.3 Direct Ranking vs. Preference Analysis vs. ...

What method is used to compare the results out of the scoring model.

Direct Ranking is the simplest way.

3 Algorithms

3.1 Help Data Structure Pyramid and Others

Define $[i, \ j]$:
$[i, \ j] := \{i, \ i+1, ..., j-1, \ j\} \subseteq \mathbb{N}_{\geq 0}$.

Define $Pyramid$:
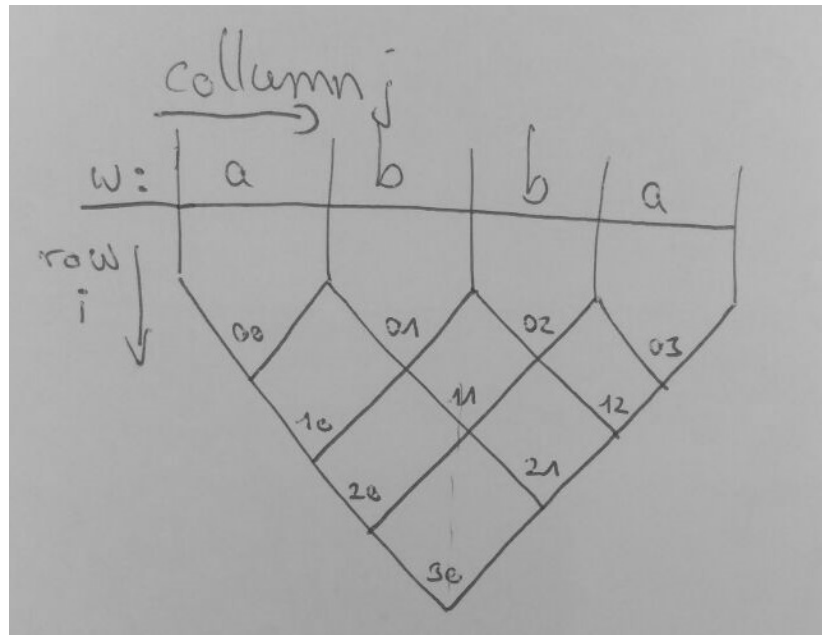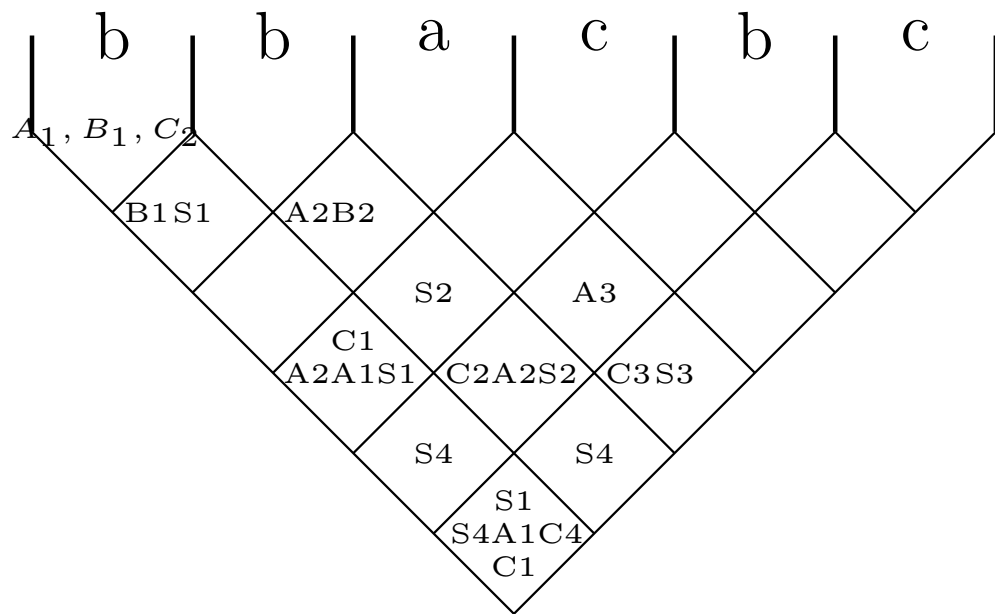$Pyramid := \{cell_{i,j} \mid i \in \mathbb{N}_{\geq 0}, \ j \in [0, \ j_{max} - i], \ i_{max} = j_{max} = |word| - 1\}$.
$cell_{i,j} = \{c \mid c \subseteq V\}$.
$EmptyPyramid \Leftrightarrow \forall i \ \forall j \ cell_{i,j} = \emptyset$.
Regarding one $cell_{i,j}$: $cell_{i,j} = cellDown$, $cell_{i-1,j} = cellUpperLeft$ and $cell_{i-1,j+1} = cellUpperRight$
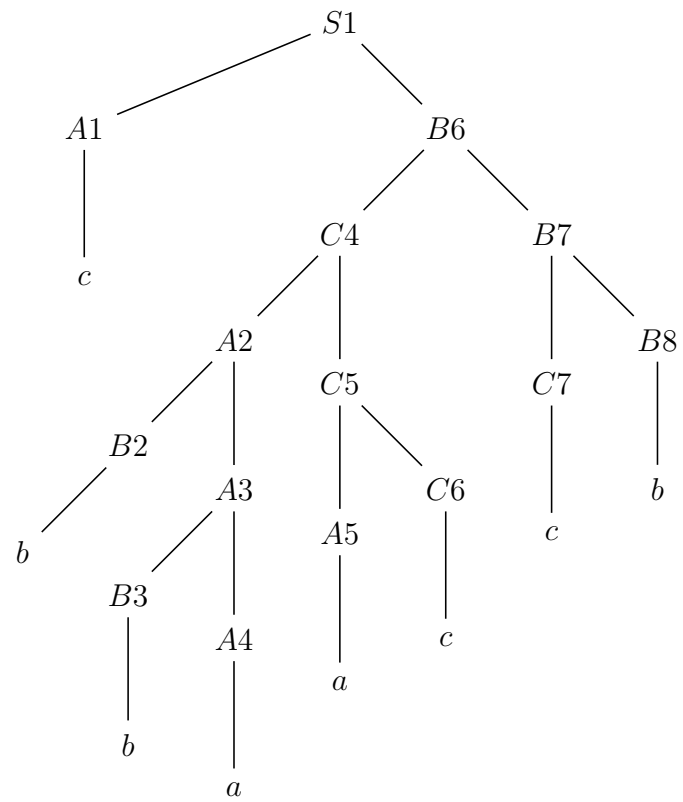
3.2 Exam Exercise Generating Algorithms
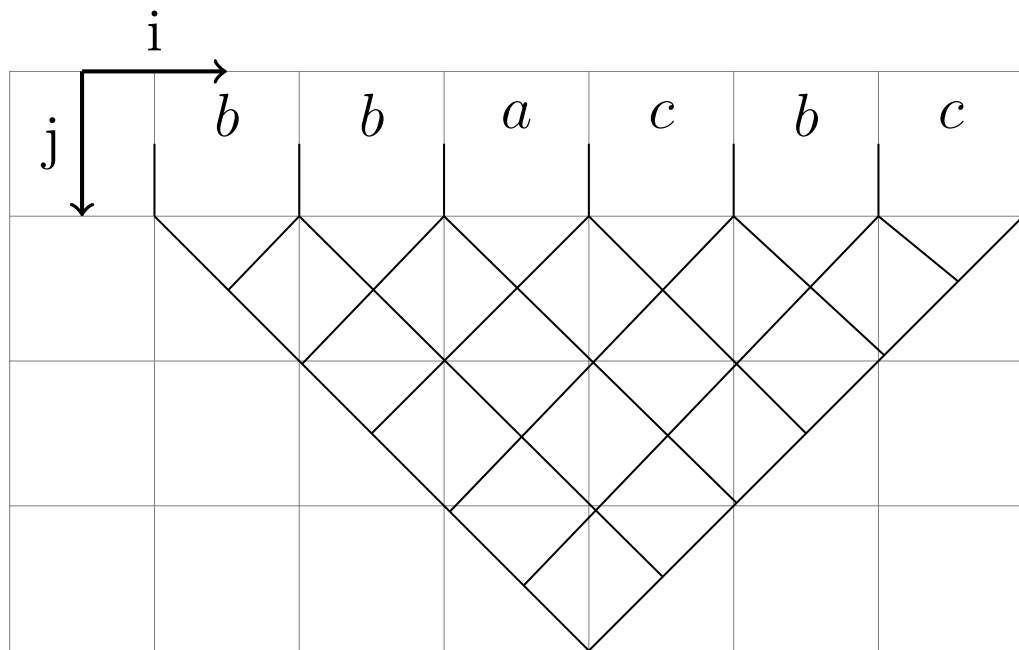
3.2.1 Algorithm: AlgorithmName

Things like the $G = (V, \Sigma, S, P)$ can be assumed as known.

$P = P \cup \{distribute\ \{\sigma \mid \sigma \in w\}\ uniform\ randomly\ over\ \{v \mid v \in V\}\}$ which equals the $distributeRhse$ module.

Bias is only allowed top vs down regarding the pyramid. No left or right bias intended yet.

(A), (B), ... represent exchangeable algorithm modules. Make hyperrefs für (A)

3.2.1.1 Basic Idea

3.2.1.2 Tweak Idea 1 for Algorithm

3.2.1.3 Tweak Idea 2 for Algorithm

3.2.1.4 Finished Algorithm   break

3.2.2 Algorithm: GeneratorGrammarDiceRollOnly

Very naive way of generating grammars. This is intended to be the starting point for our algorithms we find. Each found algorithm must have a higher score than this algorithm or otherwise it would be worse than simple dice rolling and then removing the useless productions.

Algorithm 1: GeneratorGrammarDiceRollOnly

   Input: $Word\ w \in \Sigma^*$
   Output: $P \subseteq V \times (V^2 \cup \Sigma)$
1 $P = \{distribute\ \Sigma\ over\ V\};$ (A)
2 $P = P \cup \{distribute\ V^2\ over\ V\};$ (B)
3 $P = P \setminus \{p \mid p \subseteq P,\ vc\ is\ right\ in\ p,\ \forall i\ \forall j\ vc \notin cell_{i,j}\ of\ the\ pyramid\};$
4 **return** P;

Line 3: Removes all useless production.

Does the output $P \subseteq V \times (V^2 \cup \Sigma)$ imply that G is in CNF? CNF does only have useful variables [TI script Def. 8.3 page 210] vs. $P \subseteq V \times (V^2 \cup \Sigma)$

Algorithm 2: GeneratorGrammarDiceRollOnlyBias

Input: $Word\ w \in \Sigma^*,\ P \subseteq V \times (V^2 \cup \Sigma) = \emptyset,$

Output: $Grammar\ G\ in\ CNF$

1 NOT FINISHED, MAYBE LATER.

2 *pick uniform randomly* $\{v \mid v \in V\}$*with...* ;

3 ...;

4 $P = P \cup \{distribute\ \{\sigma \mid \sigma \in w\}\ over\ \{v \mid v \in V\}\};$

5 $P = P \cup \{distribute\ \{vc \mid vc \in V^2\}\ over\ \{v \mid v \in V\}\};$

6 $P = P \setminus \{p \mid p \subseteq P,\ vc\ is\ right\ in\ p,\ \forall i\ \forall j\ vc \notin cell_{i,j}\ of\ the\ pyramid\};$

7 **return** G;

3.2.3 Algorithm: BottomUp GeneratorGrammarDiceRollMartens

Algorithm 3: GeneratorGrammarDiceRollMartens

Input: $Word\ w \in \Sigma^*$

Output: $P \subseteq V \times (V^2 \cup \Sigma)$

1   $P = \{distribute\ \Sigma\ over\ V\};$ (A)

2   $pyramid = CYK(G,\ w);$

3 **for** $i := 1$ **to** i_{max} **do**

4     $J \subseteq \mathbb{N};$

5     $cellSet \subseteq V^2;$

6   **while** $|J| < j_{max} - i$ **do**

7       $choose\ one\ j \notin J\ uniform\ randomly\ in\ [0, j_{max} - i]\ ;$

8       $J = J \cup j;$

9       $cellSet = calculateSubsetForCell(pyramid,\ i,\ j);$

10       $P = P \cup \{distribute\ cellSet \subseteq V^2\ over\ V\};$ (B)

11       $pyramid = CYK(G,\ w);$

12   **if** $stopping\ criteria\ met$ (C) **then**

13   **return** $P;$

14   **end**

15   **end**

16 **end**

17 **return** $P;$

Line 2: Fills the i=0 row of the pyramid.

Line 7: Instead of going from left to right, choose j uniform randomly with the restrictions that one cell is only visited one time.

Note: Maybe modify algorithm to also work with the threshold.

Stopping criteria regarding the entire pyramid.

Algorithm 4: GeneratorGrammarDiceRollMartens2

Input: $Word\ w \in \Sigma^*$

Output: $P \subseteq V \times (V^2 \cup \Sigma)$

1   $P = \{distribute\ \Sigma\ over\ V\};$ (A)

2   $pyramid = CYK(G,\ word)\ ;$

3   **for** $i := 1$ **to** i_{max} **do**

4   **for** $j := 0$ **to** $j_{max} - i$ **do**

5         $rowSet = rowSet \cup \{(XY, i) \mid X, Y \in V,$
        $XY \in calculateSubsetForCell(Pyramid,\ i,\ j)\};$

6   **end**

7   **while** $threshold_i$ *not reached* **do**

8   *choose one* $vc \subseteq V^2$ *out of rowSet with priority, depending on i,*
        uniform randomly; (D)

9         $P = P \cup \{distribute\ vc\ over\ V\};$ (B)

10        $pyramid = CYK(G,\ w);$

11   **if** *stopping criteria met* (C) **then**

12   **return** P;

13   **end**

14   **end**

15 **end**

16 **return** P;

Line 2: Fills the i=0 row of the pyramid.

Line 5: $(AB, 1), (AB, 2), (BC, 3)... \in sub \rightarrow$ multiple occurrences of AB are allowed. This considers "more important" compound variables.

Line 8: One vc can be chosen several times.

Note Line 8: Priority mechanism: In line $i + 1$ the $k = \{(A, l) \mid (A, l) \in sub,\ l = i\}$ are preferred over the $m = \{(A, n) \mid (A, n) \in sub,\ n < i\}$. In what way are they preferred? Using some kind of factor to weight the i of (A, i).

thresholdi is regarding a line. Threshold, Linear or log function $f(i)$?

   $P = P \cup \{distribute\ vc \in rowSet\ over\ V\};$ (B) vs.

$P = P \cup \{distribute\ rowSet \subseteq V^2 over\ V\};$ (B)

   (AB,3) and (AB,1) -> (AB,1)

   break

$\cdot$ Sub $\subseteq V \times V \times \mathbb{N}$

$\cdot$ new $\subseteq V \times V$

priority $\subseteq V \times V \times \mathbb{N}$

$\{(A,B,i) \mid (A,B) \in \text{new}, \nexists j. (A,B,j) \in A\}$

$\cup \{(A,B,j) \mid (A,B) \in \text{new}, (A,B,j) \in \text{Sub}\}$

Sub = Sub $\cup$ new

3.2.4 Algorithm: Idea 1, TopDown From node to leaves

Algorithm 5: Idea1Part1

Input: $Word\ w \in \Sigma^*,\ i, j \in \mathbb{N}$

Output: $(P \subseteq V \times (V^2 \cup \Sigma),\ cell_{i,j} \subseteq V)$

1 **if** $i = 0$ **then**

2 $\quad$ **return** $(P,\ cell_{i,j})$;

3 **end**

4 **if** *stopping criteria met* Ⓒ **then**

5 $\quad$ **return** $(P,\ cell)$;

6 **end**

7 *choose one m uniform randomly in* $[m_{min},\ m_{max}]$;

8 $(A,\ cell_a) = Idea1(w,\ m,\ j)$;

9 $(B,\ cell_b) = Idea1(w,\ (i - m),\ (m + j + 1))$;

10 $VC = uniform\ random\ subset\ from\ \{vc \mid v \in A\ \wedge\ c \in B\}$;

11 $P = P \cup \{distribute\ VC \subseteq V^2\ over\ V\}$; Ⓐ

12 **return** $(P,\ cell)$;

Line 7: $m_{min} = j$ equals the shift in the word and $m_{max} = j + i - 1$ [height of the triangle $h(i)$] that equals exactly the size of the following inspected sub string.
choose one m uniform randomly in $[j,\ j + i - 1]$;
Line 8: $(A,\ cell_a) = Idea1(w,\ m,\ j)$
Line 9: $(B,\ cell_b) = Idea1(w,\ (i - m),\ (m + j + 1))$
Line 9 $\longrightarrow$ *new cells* : $cell_{m,j}$ *and* $cell_{i-m,m+j+1}$ *See Alg. subSetCalc with* $k \in [i - 1; 0]$ $[Y \in V_{k,j},\ Z \in V_{i-k-1,k+j+1}]$

Algorithm 6: Idea1Part2

Input: $Word\ w \in \Sigma^*$

Output: $P \subseteq V \times (V^2 \cup \Sigma)$

1 $P = \{distribute\ \Sigma\ over\ V\}$; Ⓐ

2 $(P_t,\ cell) = Idea1Part1(w,\ i_{max},\ 0)$;

3 $P = P \cup P_t$;

4 **return** P;

The stopping criteria would be, that each marked $cell_{i,j} \neq \emptyset$ and it must be possible to get from $cell_{m,j}$ and $cell_{i-m,m+j+1}$ to $cell_{i,j}$ through applying one of the production rules.

Algorithm **??** Idea1 uniform randomly generates a predefined structure of the derivation tree. You always update the pyramid after adding one production to the grammar. Now there are two options to fill the parse table:

1. Bottom Up: The parse table is filled relatively evenly. All information regarding the upper cells are available and can be used. Similar to the CYK Algorithm approach.

2. Top Down: The parse table is filled quiet unevenly. You don't have all information available. Think about adding a production for the node cell: You can add a production so that its producing cells fill the node cell, but you don't know what actually would be the best to fill in these producing cells because they themselves aren't looked at yet. This problem is kept until the last depth of the recursion, where the cells in row $i = 0$ are taken into account. Only starting there you know what variables actually produce the terminals.

   Maybe solution: For the Top Down approach, don't assume that the terminals are already distributed over the V. Distribute the terminals over the variables in an ideal way that fits your already generated productions best.

3.2.5 Algorithm: Idea 2, How often cells are used for subset calculations

3.2.6 Tweaking Sub Procedures in more detail

Maybe don't keep this so that the Algorithms can be read without flipping pages.
$\text{(A)}, \text{(B)}, ...$

Algorithm 7: distributeRhse2

Input: $Rhse \subseteq (V^2 \cup \Sigma)$, $i \in \mathbb{N}$, $j \in \mathbb{N}$

Output: $Grammar\ G\ in\ CNF\ with\ uniform\ randomly\ distributed\ Rhse's.$

1 $choose\ n\ uniform\ randomly\ in\ [i,j];$

2 $choose\ V_{add} := uniform\ random\ subset\ of\ size\ n\ from\ V;$

3 $P = P \cup \{"v \longrightarrow rhse"\ |\ v \in V_{add},\ rhse \in Rhse\};$

4 **return** $G;$

Algorithm 7 isn't needed anymore for the descriptions of the basic idea of the algorithm. It will be a module later on while tweaking the algorithms.

Algorithm 8: calculateSubsetForCell

Input: $cell_{i,j} \in pyramid$

Output: $V_{i,j} \subseteq V^2$

1 $V_{i,j} = \emptyset;$

2 **for** $k := i - 1 \rightarrow 0$ **do**

3 $\quad \mid \quad V_{i,j} = V_{i,j} \cup \{X\ |\ X \longrightarrow YZ,\ Y \in V_{k,j},\ Z \in V_{i-k-1,k+j+1}\};$

4 **end**

5 **return** $V_{i,j};$

Algorithm 8 describes the magic of the CKY-algorithm. It shows what cells are taken into account while filling one cell of the parse table.

3.3 Criteria Checking Procedures

Description of the checks here.

All test of the GrammarValidityChecker class are based on the simple setV matrix.

isValid = isWordProducible && isExamConstraints && isGrammarRestrictions

isWordProducible = CYK.algorithmAdvanced()

isExamConstraints = isRightCellCombinationsForced && isMaxSumOfProductionsCount && isMaxSumOfVarsInPyramidCount && countRightCellCombinationsForced

isGrammarRestrictions = isSizeOfWordCount && isMaxNumberOfVarsPerCellCount

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Algorithm 9: checkForceCombinationPerCell

Input: $cell_{i,j} \subseteq V, \ cell_{i-1,j} \subseteq V, \ cell_{i-1,j+1} \subseteq V, \ P \subseteq V \times (V^2 \cup \Sigma)$

Output: $varsForcing \subseteq V$

1 $varsForcing \subseteq V$;

2 $varComp = \{XY \mid X \in cell_{i-1,j} \ \wedge \ Y \in cell_{i-1,j+1}\}$;

3 **foreach** $v \in cell_{i,j}$ **do**

4      $prods = \{p \mid p \subseteq P, \ v \ is \ left \ in \ p\}$;

5      $rhses = \{rhse \mid rhse \ is \ right \ in \ p \in prods\}$;

6   **if** $varComp \not\subseteq rhses$ **then**

7          $varsForcing = varsForcing \cup v$;

8   **end**

9 **end**

10 **return** $varsForcing$;

Input: $cell_{i,j} = cellDown, \ cell_{i-1,j} = cellUpperLeft$ and $cell_{i-1,j+1} = cellUpperRight$

Algorithm 9 is a check that needs to be explained.

Algorithm 10: checksumOfProductions

Input: $max \in \mathbb{N}_{\geq 0}$

Output: $true \iff sum \leq max$

1 **if** $|P| > max$ **then**

2   **return** $fales$;

3 **end**

4 **return** $true$;

Algorithm 10 can be explained via the Output of the algorithm alone.

Algorithm 11: checkMaxNumberOfVarsPerCell

Input: $max \in \mathbb{N}_{\geq 0}$

Output: $true \iff \forall cell_{i,j} \in pyramid, \; |cell_{i,j}| \leq max$

1 **for** $i := 1$ **to** i_{max} **do**
2   **for** $j := 0$ **to** $j_{max} - i$ **do**
3   **if** $|cell_{i,j}| > max$ **then**
4   **return** $false$;
5   **end**
6   **end**
7 **end**
8 **return** $true$;

Algorithm 11 can be explained via the Output of the algorithm alone.

Algorithm 12: checkMaxSumOfVarsInPyramid

Input: $max \in \mathbb{N}_{\geq 0}$

Output: $true \iff sum \leq max$

1 $sum = 0$;
2 **for** $i := 1$ **to** i_{max} **do**
3   **for** $j := 0$ **to** $j_{max} - i$ **do**
4       $sum = sum + |cell_{i,j}|$;
5   **if** $sum > max$ **then**
6   **return** $false$;
7   **end**
8   **end**
9 **end**
10 **return** $true$;

Algorithm 12 could possible be explained via a simple mathematical statement like the algorithms 10 and 11.

4 CLI Tool

4.1 Short Requirements Specification

Use Cases i $\longrightarrow$ "Lastenheft".

Input and Output parameter identification.

Here is described what the finished tool must and can do.

Generating the latex code and storing it in .tex-file. Then converting the .tex-file to .pdf-file via:

Runtime rt = Runtime.getRuntime();

Process pr = rt.exec("pdflatex mydoc.tex");

Process pr = rt.exec("pdflatex mydoc.tex");

Process pr = rt.exec("pdflatex mydoc.tex");

The triple invocation of LaTeX is to ensure that all references have been properly resolved and any page layout changes due to inserting the references have been accounted for. [http://www.arakhne.org/autolatex/]

4.1.1 Exam Exercises

An exam exercise consists out of a grammar, a word, a parsing table and a derivation tree. Creating a exam exercises must be possible. Therefore it is needed:

- Selection of a possible exam exercise out of high scoring samples $\longrightarrow$ calculate-Samples.jar [Input parameter: countOfNewSamples (better scoring samples in exchange for longer computation time)], which upon execution fills samples.txt with new high scoring samples, together with its actual scoring model parameters. Out of this samples one can be selected manually that is used for an exam exercise.

- Modifying of a exam exercise candidate: Changing the grammar and changing the word. [?changing the pyramid (I think no, because of the strong interconnection between the grammar and the parsing table it is already covered through being able to change the grammar)?] $\longrightarrow$ calculateExamExercise.jar [Input parameter: examExercise.txt], that updates pre defined information for one sample upon execution.

- Predefined Information: It is a printable version of the finished exam exercise like grammar.png, parsingTable.png and derivationTable.png together with its latex code, that was used for its creation - modification later one possible. Also it is examExerciseInfo.txt, that has the information about its actual scoring model parameters.

4.1.2 Fun With CNF's and CYK

Trying out stuff freestyle:

- Se

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4.2 Overview - UML

UML-Diagramm showing the general idea of the implementation.

List noteworthy used libraries here, too.

Maybe some information out of the statistics tool of IntelliJ.

4.2.1 UML: More Detail 1

4.2.2 UML: More Detail 2

4.3 User Interaction

Here the specific must can do's are explained with short examples.

4.3.1 Use Case 1

4.3.2 Use Case i

5 Notes

The informal goal is to find a suitable combination of a grammar and a word that meets the demands of an exam exercise. Also the CYK pyramid and one derivation tree of the word must be generated automatically as a "solution picture".
Firstly the exam exercise must have an upper limit of variables per cell while computing the CYK-pyramid.
Secondly the exam exercise must have one or more "special properties" so that it can be checked if the students have clearly understood the algorithm, e.g. "Excluding the possibility of luck."

The more formal goal is identify and determine parameters that in general can be used to define the properties of a grammar, so that the demanded restrictions are met. Also parameters could be identified for words, but "which is less likely to contribute, than the parameters of the grammar." [Second appointment with Martens]

Some introductory stuff:

Possible basic approaches for getting these parameters are the Rejection Sampling method and the "Tina+Wim" method.
Also backtracking plays some role, but right now I don't know where to put it. Backtracking is underapproach to Rejection Sampling.
Note: Starting with one half of a word and one half of a grammar.

Identify restrictions (=parameters) regarding the grammar.
Maybe find restrictions regarding the words, too.

Procedures for automated generation. Each generation procedure considers different restrictions and restriction combinations. The restrictions within one generation procedure can be optimized on its own. Up till now:
Generating grammars: DiceRolling, ...
Generating words: DiceRolling, ...

Parameter optimisation via theoretical and/or benchmarking approach.
Benchmarking = generate N grammars and test them, (N=100000).
Define a success rate and try to increase it.

The overall strategy is as following:

1.) Identify theoretically a restriction/parameter for the grammar. Think about the influence it will have. Think also about correlations between the restrictions.
2.) Validate the theoretical conclusion with the benchmark. Test out the influence of this parameter upon the success rate. Try different parameter settings.

The ordering of step 1 and step 2 can be changed.

Used software

Github

IntelliJ IDEA

Algorithms

This section contains all algorithms referenced in this thesis.

References

[1] JSR 220: Enterprise Java Beans 3.0 `https://jcp.org/en/jsr/detail?id=220`, 09/09/2015