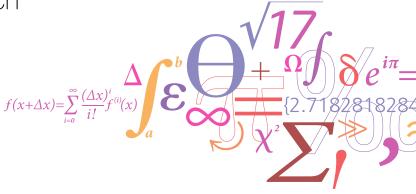


University Timetabling

Curriculum-based Course Timetabling using ALNS and Tabu Search



DTU Compute

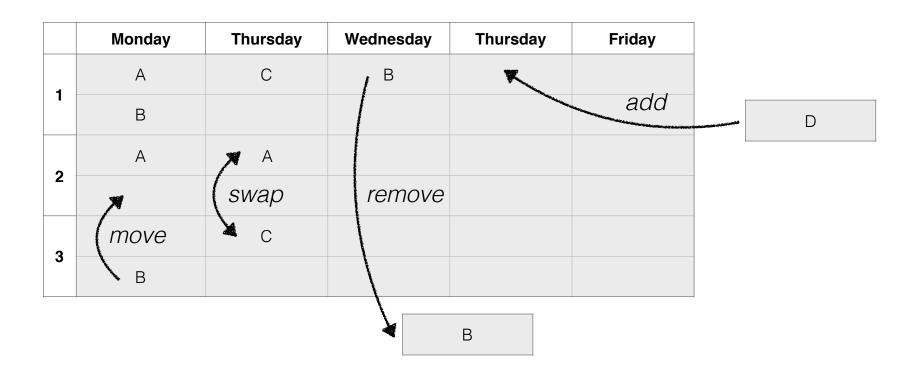
Department of Applied Mathematics and Computer Science

The Meta Heuristics

• Tabu Search: good for large neighborhood

• ALNS: good for highly constrained problem

Operations



Initialization

all missing courses in random order

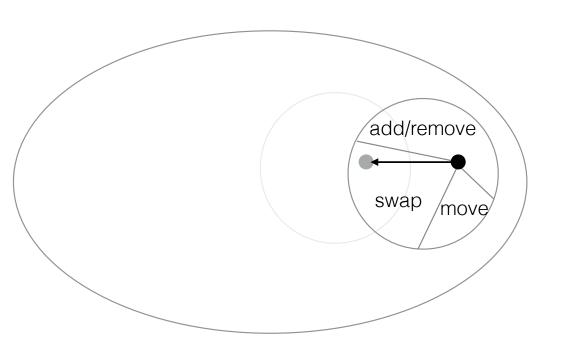


all available slots in random order

| Mon | Tue | Mon | Wen | Fri | Mon | Tue |
|-----|-----|-----|-----|-----|-----|-----|
| 1 | 2 | 2 | 2 | 1 | 2 | 1 |
| R1 | R2 | R2 | R2 | R2 | R1 | R1 |



```
\begin{aligned} & \textbf{for all } c \text{ in courses } \textbf{do} \\ & \textbf{for } i \text{ from 1 to Length}(slots) \textbf{ do} \\ & (t,r) \leftarrow \text{PopRight}(slots) \end{aligned} \\ & \triangleright \text{ add } (c,t,r) \text{ to solution if it improves the objective} \\ & \Delta \leftarrow \text{SimulateAdd}(c,t,r) \\ & \textbf{ if } \Delta < 0 \textbf{ then} \\ & \text{MutateAdd}(c,t,r) \\ & \textbf{ break} \end{aligned} \\ & \textbf{ else} \\ & \text{PushLeft}((t,r) \text{ on } slots) \\ & \triangleright \text{ The slot is still avaliable} \end{aligned}
```



Algorithm 4 Generalization of the Tabu search algorithm

```
1 function TabuSearch(solution<sub>init</sub>)
                                                                       ▷ Globally best solution
        s_{qlobal} \leftarrow solution_{init}
        s_{local} \leftarrow solution_{init}
                                                                              ▷ Current solution
        tabu \leftarrow \text{LimitedSet}()
                                                                     ▶ May have infinite space
 6
        repeat
             \Delta, move \leftarrow \text{LocalSearch}(s_{local}, tabu)
                                                                      \triangleright Find best move \notin tabu
             if \Delta < 0 then
                 s_{local} \leftarrow \text{Apply}(move \text{ on } s_{local})
                 Add(Opposite(move) \text{ on } tabu)
10
11
                 if s_{qlobal} hasn't been updated for awhile then
12
                      s_{local} \leftarrow \text{Intensify}(s_{qlobal})
                                                                   ▶ Intensification is optional
13
                 s_{local} \leftarrow \text{Divserify}(s_{local})
                                                                  ▷ Diversification is optional
14
             if Cost(s_{local}) < Cost(s_{global}) then
15
                 s_{global} \leftarrow s_{local}
16
        until no more time
17
        return s_{global}
18
```

| name | type | description |
|-----------------|-------------|--|
| diversification | integer | How many $(course, time, room)$ combi- |
| | | nations should be removed. May be |
| | | zero to disable diversification. |
| intensification | integer | Same as in the generalized tabu search. |
| tabu limit | integer | This parameter controls the tabu limit |
| | | of all the tabu lists. |
| allow swap | $\{always,$ | If always the swap neighborhood is al- |
| | dynamic, | ways checked. If $never$ the swap neigh- |
| | never | borhood is never checked. Additionally |
| | | if dynamic, the swap neighborhood is |
| | | only checked if none of the other oper- |
| | | ations could reduce the objective. |

Table 3: Parameters for specialized Tabu search

| name | type | description | |
|-----------------|----------|---|--|
| diversification | integer | How many $(course, time, room)$ combi- | |
| | | nations should be removed. May be | |
| | | zero to disable diversification. | |
| intensification | integer | Same as in the generalized tabu search. | |
| tabu limit | integer | This parameter controls the tabu limit | |
| | | of all the tabu lists. | |
| allow swap | {always, | If always the swap neighborhood is al- | |
| | dynamic, | ways checked. If never the swap neigh- | |
| | never} | borhood is never checked. Additionally | |
| | | if dynamic, the swap neighborhood is | |
| | | only checked if none of the other oper- | |
| | | ations could reduce the objective. | |

Table 3: Parameters for specialized Tabu search

| | parameter | search space | value |
|---|-----------------|--------------------------|---------|
| - | allow swap | {never, always, dynamic} | dynamic |
| | tabu limit | $\{10, 20, 40, \infty\}$ | 40 |
| | intensification | $\{2, 10, \infty\}$ | 10 |
| | diversification | $\{0, 1, 5\}$ | 5 |

Table 9: Best Tabu search parameters with $\mu = 4.139$ and $\sigma = 0.122$

| | | intensification | | |
|-----------------|---|-----------------|--------------|--------------|
| | | 2 | 10 | ∞ |
| | | (4.90, 0.52) | (5.36, 0.37) | (5.53, 0.71) |
| diversification | 1 | (5.07, 0.97) | (5.34, 0.17) | (5.29, 0.63) |
| | 5 | (5.19, 0.41) | (4.14, 0.12) | (5.06, 0.77) |

Table 7: Shows (μ, σ) with allow_swap=dynamic and tabu_limit=40 fixed

| | | tabu_limit | | | |
|------------|---------|--------------|--------------|--------------|--------------|
| | | 10 | 20 | 40 | ∞ |
| | never | (5.53, 0.70) | (5.91, 0.89) | (6.52, 0.60) | (5.93, 0.43) |
| allow_swap | always | (9.12, 0.18) | (8.77, 0.26) | (9.16, 0.87) | (8.82, 0.44) |
| | dynamic | (5.52, 0.69) | (5.10, 0.59) | (4.14, 0.12) | (5.45, 0.27) |

Table 8: Shows (μ, σ) with diversification=5 and intensification=10 fixed

Destroy

- Fully Random Remove random combinations
- Curriculum Only sample from a random curriculum
- Day Only sample from a random day
- Course Only sample from a random course

Repair

- Very Greedy Insert missing courses at the first placement with Λ < 0.
- Best Placement For each course sort placement by Δ, then add the requested amount.

In this case there are no invalid destroy or repair methods.

```
\Psi = \max\{w_{global}, w_{current}\}
```

Algorithm 6 Generalization of the ALNS search algorithm

```
1 function ALNSSEARCH(solution<sub>init</sub>)
                                                                                   ▷ Globally best solution
          s_{qlobal} \leftarrow solution_{init}
          s_{local} \leftarrow solution_{init}
                                                                                            ▷ Current solution
         p^+, p^- \leftarrow \text{vector of 1s}
 6
          repeat
               d \leftarrow \text{SampleFunction}(p^{-})
               r \leftarrow \text{SAMPLEFUNCTION}(p^+)
               s_{local} \leftarrow \text{Repair}(\text{Destroy}(s_{local}, d), r)
10
               \Psi \leftarrow \max\{w_{global}, w_{current}, w_{accept}, w_{reject}\}
11
              p_d^- \leftarrow \lambda p_d^- + (1 - \lambda)\Psi
p_d^+ \leftarrow \lambda p_d^+ + (1 - \lambda)\Psi
12
13
14
               if Cost(s_{local}) < Cost(s_{qlobal}) then
15
                    s_{global} \leftarrow s_{local}
16
          until no more time
17
          return s_{global}
```

| name | type | description |
|-------------------------------------|--|--|
| λ | $ratio \in [0, 1]$ | remember parameter used in the mov- |
| $w_{global} \ w_{current} \ remove$ | positive integer positive integer positive integer | ing average update of the probabilities. reward for a globally better solution reword for a locally better solution number of courses removed in each de- stroy function |

Table 5: Parameters for generalized ALNS search

| parameter | search space | value |
|---------------|-----------------------|-------|
| λ | $\{0.9, 0.95, 0.99\}$ | 0.99 |
| w_{global} | $\{5, 10, 20\}$ | 10 |
| $w_{current}$ | $\{1, 3, 4, 10\}$ | 10 |
| remove | $\{1, 3, 5\}$ | 1 |

Table 12: Best ALNS parameters with $\mu = 0.3502$ and $\sigma = 0.0594$

| | | | remove | |
|---------------|------|--------------|--------------|--------------|
| | | 1 | 3 | 5 |
| | 0.9 | (0.62, 0.04) | (0.58, 0.02) | (0.99, 0.04) |
| update_lambda | 0.95 | (0.46, 0.13) | (1.09, 0.05) | (1.22, 0.05) |
| | 0.99 | (0.35, 0.06) | (1.86, 0.04) | (1.72, 0.15) |

Table 10: Shows (μ, σ) with w_global=10 and w_current=10 fixed

| | | w_current | | | |
|----------|----|--------------|--------------|--------------|--------------|
| | | 1 | 3 | 5 | 10 |
| | 5 | (0.45, 0.15) | (0.55, 0.14) | (0.67, 0.04) | (0.39, 0.09) |
| w_global | 10 | (0.42, 0.12) | (0.58, 0.01) | (0.55, 0.06) | (0.35, 0.06) |
| | 20 | (0.52, 0.18) | (0.40, 0.11) | (0.43, 0.11) | (0.58, 0.10) |

Table 11: Shows (μ, σ) with update_lambda=0.99 and remove=1 fixed

Compareing

| | | Tabu | ALNS |
|------------------------|----|---------------|--------------|
| | 1 | (3.00, 0.84) | (0.22, 0.18) |
| | 3 | (3.07, 0.08) | (0.23, 0.15) |
| | 5 | (0.14, 0.04) | (0.07, 0.05) |
| train | 7 | (6.33, 0.22) | (0.20, 0.11) |
| | 9 | (3.19, 0.24) | (0.13, 0.09) |
| | 11 | (12.80, 2.45) | (0.80, 0.81) |
| | 13 | (3.90, 0.17) | (0.11, 0.11) |
| | 2 | (3.17, 0.27) | (0.09, 0.11) |
| | 4 | (4.88, 0.35) | (0.09, 0.08) |
| test | 6 | (5.06, 0.35) | (0.05, 0.05) |
| test | 8 | (5.19, 0.43) | (0.12, 0.07) |
| | 10 | (6.22, 0.39) | (0.14, 0.07) |
| | 12 | (0.92, 0.10) | (0.06, 0.06) |
| all train | | (4.63, 0.46) | (0.25, 0.14) |
| all test | | (4.24, 0.15) | (0.09, 0.04) |

Table 13: Test and train results over 5 runs using best parameters

Conclusion

- Dynamic neighborhood is a good strategy.
- The ALNS sub functions should have approximately same speed.
- It is a long line of good choices, that makes a good solution.
- It was more important to search wide and suboptimal than narrow and optimal.