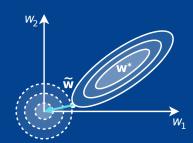




Lesson 8: Regularization, Optimization and Searching

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AUTUMN 2020





# L08: Agenda

ML Algorithm and Model Selection: k-fold Cross-Validation revisited, k-fold CV for Hyperparameter Tuning.

Regularization and Optimization: Regulizers, Exercise: L09/regulizers.ipynb Optimizers (no-exe).

Searching:

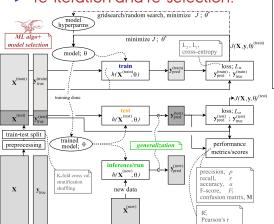
Gridsearch, Randomsearch,

Exercise: L09/gridsearch.ipynb

# ML Algorithm Selection and Model Selection

Manually Choosing an Algorithm and Tuning a Model..

- algorithm selection.
- model selection.
- model evaluation.
- re-iteration and re-selection!



Model Evaluation, Model Selection, and Algorithm Selection in Machine Learning Sebastian Raschka University of Wisconsin-Madison Abstract The correct use of model evaluation, model selection, and algorithm selection techniques is vital in academic machine learning research as well as in many of each technique with references to theoretical and empirical studies. Further, applications of machine learning. Common methods such as the holdout method for model evaluation and selection are covered, which are not recommended when working with small datasets. Different flavors of the bootstran technique are introduced for estimating the uncertainty of performance estimates, as an alternative to confidence intervals via normal approximation if bootstrapping is trade-off for choosing k is discussed, and practical tips for the optimal choice of it are given based on empirical evidence. Different statistical tests for algorithm comparisons are presented, and strategies for dealing with multiple comparisons alternative methods for algorithm selection, such as the combined F-test 5x2 crossvalidation and nested cross-validation, are recommended for comparing machine learning algorithms when datasets are small

"Model Evaluation, Model Selection, and Algorithm Selection in Machine Learning",

Sebastian Raschka, 2018.



# ML Algorithm Selection and Model Selection

Manually Choosing an Algorithm and Tuning a Model..

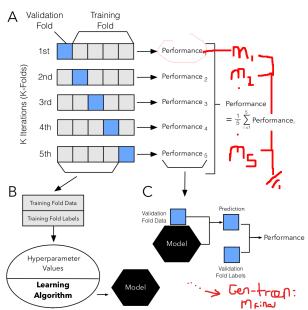
- algorithm selection:
  - choose an algo that 'fits' the problem, ...perhaps via searching??
- model selection:
  - looking for 'optimal' model capacity,
  - tuning model hyperparameters..
    - model weights regularizers..(for NN's)
    - gradient descent optimizers..(for NN's)
- model evaluation:
  - the performance metric score function,
  - how do you evaluate generalization performance?
  - holdout method (train-test split) and k-fold CV,
  - three-way split (train-validate-test split)...
- re-iteration and re-selection!

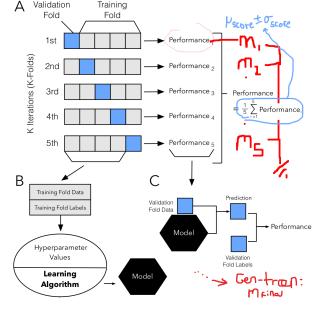
NOTE: Model selection:  $\sim$  selection the best capacity/hyperparameter for a given model—NOT choosing the ML algo/model itself!



## **Model Evaluation**

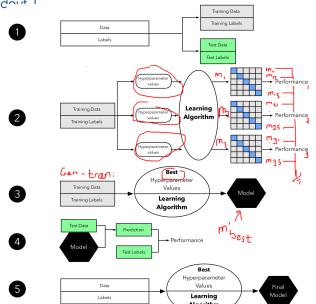
k-fold Cross-Validation Procedure, for k=5..





## Model Evaluation and Selection

k-fold Cross-Validation for Hyperparameter Tuning (Somewhat Similar to Treeway Holdaut )



# Regularization

### Adding a Penalty to the Cost Function

For a linear regressor, our cost function was

$$J(\mathbf{X}, \mathbf{y}; \mathbf{w}) = ||\mathbf{X}\mathbf{w} - \mathbf{y}||_2^2 \propto \mathsf{MSE}(\mathbf{X}, \mathbf{y}; \mathbf{w})$$

But now enters a **penalty factor**,  $\Omega$ , that scaled with  $\alpha$  adds extra cost to J,

$$\tilde{J}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = ||\mathbf{X}\mathbf{w} - \mathbf{y}||_2^2 + \alpha \Omega(\mathbf{w})$$

so this becomes **a-tug-of-war** between the two terms in  $\tilde{J}$ .

The effect of the added penalty is to:

- put a contraint on the norm of the weights, w, disallowing 'em to grow wildely,
- leading to reduced overfitting, disabling the model to learn the background noise in the data.

# $\mathcal{L}_2$ Regularization

### Ridge Penalization

Aka Weight Decay, aka Tikhonov regularization

$$\Omega(\mathbf{w}) = ||\mathbf{w}||_2^2 = \mathbf{w}^{\mathsf{T}}\mathbf{w}$$

$$\tilde{\textit{J}}_{\text{ridge}}(\mathbf{X},\mathbf{y};\mathbf{w}) \ = \textit{J}(\mathbf{X},\mathbf{y};\mathbf{w}) + \alpha \mathbf{w}^{\top} \mathbf{w}$$

with  $\mathbf{w} = [w_1 \ w_2 \ \cdots \ w_n]^{\top}$  without the bias element  $w_0$  in the regulizer term,  $\Omega$ , and recalling the Euclidean norm

$$\mathcal{L}_2^2: ||\mathbf{x}||_2^2 = \mathbf{x}^{\top}\mathbf{x}$$

NOTE: ..and give-or-take some additional 1/2 or 1/n constant, that we do not care about.

# $\mathcal{L}_2$ Regularization

Ridge Penalization A graphical view for a linear regressor 1D featurespace 3D: ideal convex loss in  $J - \mathbf{w}$  space. 2D: flat  $w_2 - w_1$  view with some feature scaling.

The tug-of-war: what happens with  $\tilde{\mathbf{w}}$ , if  $\mathbf{w}^*$  is far from the origin  $[w_1, w_2] = (0, 0)$ ?

# $\mathcal{L}_1$ Regularization

### Lasso penalization

Now, just replace the  $\mathcal{L}_2$  with  $\mathcal{L}_1$  and we have the Lasso regularizer

$$\Omega(\mathbf{w}) = ||\mathbf{w}||_1$$

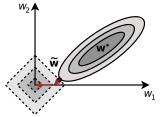
$$\tilde{J}_{\text{lasso}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha ||\mathbf{w}||_1$$

with the Manhattan norm

$$\mathcal{L}_1: ||\mathbf{x}||_1 = \sum_{i=1}^n \mathsf{abs}(x_i)$$

and the  $\mathcal{L}_1$  penalty tends to drive weights to zero:

- automatic feature selection.
- outputs a sparce model,
- i.e few nonzero w's.



# $\mathcal{L}_1$ and $\mathcal{L}_2$ Regularization

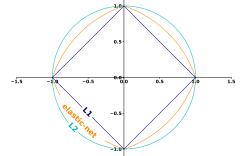
### **Elastic-net Penalization**

And finally a combination of the two: an Elastic-net regularizer

$$\Omega(\mathbf{w}) = \beta ||\mathbf{w}||_1 + (1 - \beta)||\mathbf{w}||_2^2$$

$$\tilde{J}_{\text{elastic}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha \left(\beta ||\mathbf{w}||_1 + (1 - \beta)||\mathbf{w}||_2^2\right)$$

Regularization selection: via searching..



## **Optimizers**

### **Momentum Optimization**

Normal GD algo

$$\mathbf{w} \leftarrow \mathbf{w} - \eta \nabla_{\mathbf{w}} \mathbf{J}$$

but now with added (physical) momentum

$$\begin{array}{c} \mathbf{m} \leftarrow \beta \mathbf{m} - \eta \nabla_{\mathbf{w}} J \\ \mathbf{w} \leftarrow \mathbf{w} + \mathbf{m} \end{array}$$

Optimizer selection: (perhaps) via searching...

# **Optimizers**

### Or solvers in Scikit-learn..



## sklearn.neural\_network.MLPRegressor

class sklearn.neural\_network. MLPRegressor(hidden\_layer\_sizes=(100, ), activation='relu', \*, solver='adam', alpha=0.0001, batch\_size='auto', learning\_rate='constant', learning\_rate\_init=0.001, power\_t=0.5, max\_iter=200, shuffle=True, random\_state=None, tol=0.0001, verbose=False, warm\_start=False, momentum=0.9, nesterovs\_momentum=True, early\_stopping=False, validation\_fraction=0.1, beta\_1=0.9, beta\_2=0.999, epsilon=1e-08, n\_iter\_no\_change=10, max\_fun=15000) [source

Multi-layer Perceptron regressor.

This model optimizes the squared-loss using LBFGS or stochastic gradient descent.

New in version 0.18.

#### Parameters:

hidden\_layer\_sizes : tuple, length = n\_layers - 2, default=(100,)

The ith element represents the number of neurons in the ith hidden layer.

solver : {'lbfgs', 'sgd', 'adam'}, default='adam'
The solver for weight optimization.

- . 'Ibfgs' is an optimizer in the family of quasi-Newton methods.
- 'sad' refers to stochastic gradient descent.
- 'adam' refers to a stochastic gradient-based optimizer proposed by Kingma, Diederik, and Jimmy Ba

Note: The default solver 'adam' works pretty well on relatively large datasets (with thousands of training samples or more) in terms of both training time and validation score. For small datasets, however, 'lbfgs' can converce faster and perform better.

activation: ("identity", "logistic", "tanh", "relu"), default="relu".
Activation function for the hidden laver.

## **Optimizers**

Or optimizers in Keras...



About Keras

Getting started

Models API

Lavers API

Callbacks API

Optimizers

Metrics

Losses Built-in small datasets

Utilities

Code examples

Why choose Keras?

Data preprocessing

Keras Applications

Developer guides

Keras API reference

» Keras API reference / Optimizers

### Available optimizers

- SGD
- RMSprop
- Adam
- Adadelta Adagrad
- Adamax
- Nadam
- Etrl .

## **Optimizers**

Usage with compile() & fit()

An optimizer is one of the two arguments required for compiling a Keras model:

```
from tensorflow import keras
from tensorflow.keras import layers
model = keras.Sequential()
```

model.add(layers.Dense(64, kernel initializer='uniform', input shape=(10,)))

model.add(layers.Activation('softmax'))

opt = keras.optimizers.Adam(learning rate=0.01)

model.compile(loss='categorical\_crossentropy', optimizer=opt)

You can either instantiate an optimizer before passing it to model.compile(), as in the above example, or you can pass it by its string identifier. In the latter case, the default parameters for the optimizer will be used.

# pass optimizer by name: default parameters will be used model.compile(loss='categorical crossentropy', optimizer='adam')



#### Optimizers □ Usage with compile

fit() Usage in a custom to

- ▶ Learning rate decay
- scheduling
- Available optimizers
- □ Core Optimizer API apply gradients m weights property get weights metho set\_weights metho

## 14/22

# ML Models (or ML algorithms)

### Models encountered so far

## Some classifiers and regressors..

sklearn.neighbors.KNeighborsRegressor sklearn.linear\_model.LinearRegression sklearn.linear\_model.SGDClassifier sklearn.linear\_model.SGDRegressor

### Perhaps..

sklearn.naive\_bayes.GaussianNB
sklearn.naive\_bayes.MultinomialNB
sklearn.svm.SVC
sklearn.svm.SVR

## and to some degree..

sklearn.linear\_model.LogisticRegression sklearn.linear\_model.Perceptron sklearn.neural\_network.MLPClassifier sklearn.neural\_network.MLPRegressor keras.Sequential

### Or even more exotic models like..

- superviced ensemble: AdaBoost, Bagging, DecisionTree, RandomForest,...
- semi-supervised: ??
- unsupervised: K-means, manifolds, restricted Boltzmann machines,...
- clustering: K-means





# ML Algorithm + Model Selection via Searching

What ML algorithm to choose?

- manual:
  - algorithm characteristics,  $\mathcal{O}$  complexity, etc. browsing through Scikit-learn documentation, ...and also based on data assumptions.
- semi-automatic:

brute-force model search, and fun with python!

```
models = {
  SVC(gamma="scale"),
  SGDClassifier(tol=1e-3, eta0=0.1),
  GaussianNB()
                                                prints..
                                                  Gaussian NB:
                                                                 p=1.00
for i in models:
                                                  SGDClassifier:
                                                                 p = 0.93
    i.fit(X_train, y_train)
                                                                 p = 0.98
                                                  SVC:
    y_pred_test = i.predict(X_test)
    p = precision_score(y_test, y_pred_test, average='micro')
    print(f'{type(i).__name__:13s}: precision={p:0.2f}')
NOTE: Python set = \{a, b\}
     Python dictionary= \{a:x, b:y\}
```

## Model Selection via Grid Search

## The hyperparamter-set for SGD linear regressor

```
class sklearn.linear_model.SGDRegressor(
 loss ='squared_loss', penalty
                                   ='12'.
 alpha =0.0001,
                        ll ratio
                                   =0.15,
 tol =None,
                        shuffle
                                   =True,
 verbose = 0.
                        epsilon
                                   =0.1.
                        power_t = 0.25,
 eta0 = 0.01.
 n_iter_no_change=5,
                        warm_start
                                   =False.
 fit_intercept =True,
                        max iter
                                   =None.
              =False, n_iter
                                   =None
 average
  random_state =None,
                        learning_rate='invscaling',
 early_stopping =False,
                        validation_fraction=0.1
```

## Search best hyperparameters in a (smaller) set, say

## Model Selection via Grid Search

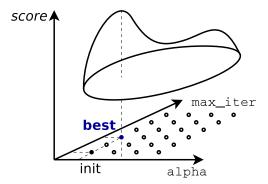
How to select 'best' set of hyperparameter—using bute force?

Gridsearch seen in 3D for the two hyperspace dimensions:

- ▶  $alpha \in [1, 2, 3, ..]$
- ► max\_iter  $\in [1, 2, 3, ...]$

(NOTE: linear range for this plot only,

should be 1, 10, 100 or similar.)



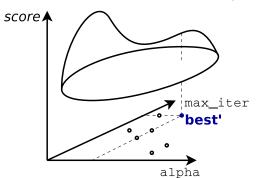
- $\triangleright$  why score and not J on z-axis?
- and what if there are many hyperparameters and many combinations? → Zzzzzzz!

## Model Selection via Randomized Search

How to select 'best' set of hyperparameters—faster than brute force?

Replace GridSearchCV() with

RandomizedSearchCV(n\_iter=100,...)



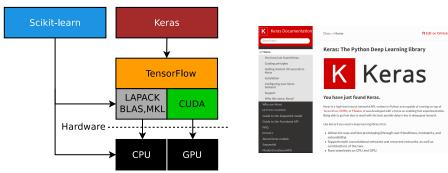
- faster, but will not yield the (sub) optimal score maximum.
- ...but does it matter in a huge hyperparameter search-space?

# Extra Slides..

## Keras and Tensorflow



## Using the Keras API instead of Scikit-learn or TensorFlow

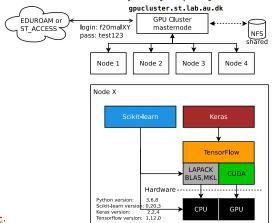


### NOTE:

- documentation: https://keras.io/
- keras provides a fit-predict-interface,
- many similiarities to Scikit-learn,
- but also many differences!

# High-Performace-Computing (HPC)

Running on the ASE GPU cluster, your group login=e20malXY



### NOTE:

manuel GPU hukommelses Garbage Collection...

For keras GPU kald:

StartupSequence\_EnableGPU(gpu\_mem\_fraction=0.1, gpus=1)

NOTE2: script found in /home/shared/00\_init.py that runs for all users!